Lab 4: Asymmetric (Public) Key

Objective: The key objective of this lab is to provide a practical introduction to public key encryption, and with a focus on RSA and Elliptic Curve methods. This includes the creation of key pairs and in the signing process.

Web link (Weekly activities): https://asecuritysite.com/esecurity/unit04

Demo: https://youtu.be/3n2TMpHqE18

A RSA Encryption

A.1 We will follow a basic RSA process. If you are struggling here, have a look at the following page:

https://asecuritysite.com/encryption/rsa

First, pick two prime numbers:

```
p=
q=
```

Now calculate N (p.q) and PHI [(p-1).(q-1)]:

```
N=
PHI =
```

Now pick a value of e which does not share a factor with PHI [gcd(PHI,e)=1]:

```
e=
```

Now select a value of d, so that (e.d) (mod PHI) = 1:

```
d=
```

Now for a message of M=5, calculate the cipher as:

```
C = M^e \pmod{N} =
```

Now decrypt your ciphertext with:

```
M = C^{d} \pmod{N} =
```

Did you get the value of your message back (M=5)? If not, you have made a mistake, so go back and check.

A.2 The following defines a public key:

```
----BEGIN PGP PUBLIC KEY BLOCK----
```

Version: GnuPG v2

mQENBFTzi1ABCADIEwchOyqRQmU4AyQAMj2Pn68Sqo9lTPdPcItwo9LbTdv1YCFz w3qLlp2RORMP+Kpdi92CIhduYHDmZfHZ3IWTBqo9+y/Np9UJ6tNGocrqsq4xWz15 4vX4jJRddC7QySSh9UxDpRwf9sgqEv1pah136r95zuyjC1EXnoNxdLJtx8PliCXchV/v4+Kf0yzYh+HDJ4xP2bt1S07dkasYZ6cA7BHYi9k4xgEwxVvYtNjSPjTsQY5R cTayXveGafuxmhSauZKiB/2TFErjEt49Y+p07tPTLX7bhMBVbUvojtt/JeUKv6vK R82dmOd8seUvhwOHYB0JL+3S7PgFFsLo1NV5ABEBAAG0LkJpbGwgQnVjaGFuYW4g KE5vbmUpIDx3LmJ1Y2hhbmFuQG5hcG1lci5hYy51az6JATkEEwECACMFA1Tzi1AC GwMHCwkiBwMCAQYVCAIJCgsEfgIDAQIeAQIXgAAKCRDsAFZRGtdPQi13B/9KHeFbl1AxqbafFGRDEvx8ufPnEww4FFqwhcr8RLwyE8/ColupB/5As2yvojmbNFMGzURb LGf/u1LVH0a+NHQu57u8Sv+g3bBthEPh4bKaEzBYRS/dYHOx3APFyIayfm78JVRF zdeTOOf6PaXUTRx7iscCTkN8DUD31g/465ZX5aH3HWFFX500JSPSt0/udqjoQuArWA5JqB//g2GfzZe1UzH5Dz3PBbJky8GiIfLm0OXSEIgAmpvc/9NjzAgjOW56n3MusjVkibc+11jw+r0o97CfJMppmtcOvehvQv+KG0LZnpibiwVmM3vT7E6kRy4gEbDu enHPDqhsvcqTDqaduQENBFTzi1ABCACzpJgZLK/sge2rMLURUQQ6102Urs/Gi1GC ofq3WPnDt5hEjarwMMwN65Pb0Dj0i7vnorhL+fdb/J8b8QTiyp7i03dZVhDahcQ5 8afvCjQtQsty8+K6kZFzQOBgyOS5rHAKHNSPFq45MlnPo5aaDvP7s9mdMILITv1b CFhcLoC60qy+JoaHupJqHBgGc48/5NU4qbt6fBAQ/H4M+6og4OzohgkQb80Hox YbJV4sv4vYMULd+FK0q2RdGeNMM/awdqYo90qb/W2aHCCvXmhGHEEuok9ibc8cr/ xrWL0gDw1Wpad8RfQwyVU/VZ3Eg3OseL4SedEmwOO

cr15XDIs6dpABEBAAGJAR8E

GAECAAKFAlTzi1ACGwwACgkQ7ABwURrXT0KZTgf9FUpkh3wv7aC5M2wwdEjt0rDx nj9kxH99hhuTX2EHXuNLH+SwLGHBq502sq3jfP+owEhs8/Ez0j1/fSKIqAdlz3mB dbqwPjzPTY/m0It+wv3epOM75uwjD35PFOrKxxZmEf6SrjZD1sk0B9bRy2v9iwN9 9ZkuvcfH4vT++PognQLTUqNx0FGpD1agrG01XSCtJWQXCXPfWdtbIdThBgzH4f1Z ssAIbCaBlQkzfbPvrMzdTIP+AXg6++K9SnO9N/FRPYzjUSEmpRp+ox31WymvczcU RmyUquF+/zNnSBVgtY1rzwaYi05XfuxG0wHVHPTtRyJ5pF4HSqiuvk6Z/4z3bw== =ZrP+

----END PGP PUBLIC KEY BLOCK----

Using the following Web page, determine the owner of the key, and the ID on the key:

https://asecuritysite.com/encryption/pgp1

A.3 Bob has a private RSA key of:

MIICXAIBAAKBqQCwqjkeoyCXm9v6VBnUi5ihQ2knkdxGDL3GXLIUU43/froeqk7q9mtxT4AnPA aDX3f2r4STZYYiqXGSHCUBZcI90dvZf6YiEM5OY2jqsmqBjf2Xkp/8HqN/XDw/wD2+zebYGLLY td2u3GXx9edqJ8kQcU9LaMH+ficFQyfq9UwTjQIDAQABAOGAD7L1a6Ess+9b6G70gTANWkKJpshVZDGb63mxKRepaJEX8sRJEqLqOYDNsC+pkK08IsfHreh4vrp9bsZuECrB1OHSjwDB0S/fm3KEwbsaaxDUAu0dqg/JBMXAKzeATreoIYJItYgwzrJ++fuquKabAZumvOnWJyBIs2z103kDz2ECQQDnn3JpHirmgVdf81yBbAJaxBXNIPZOCCth1zwFAs4EvrE35n2HvUQuRhy3ahUKXsKX/bGvWzmC 206kbLTFEygVAkEAwxXZnPkaAY2vuoUCN5NbLZgegrAtmU+U2woa5A0fx6uXmShqxo1iDxEC71 FbNIgHBg5srsUyDj3OsloLmDVjmQJAIy7qLyOA+sCc6BtMavBgLx+bxCwFmsoZHOSX3179smTR AJ/HY64RREIsLIQ1q/yW7IWBzxQ5WTHg1iNZFjKBvQJBAL3t/vCJwRz0Ebs5FaB/8UwhhsrbtXlGdnkOjIGsmV0vHSf6poHqUiay/DV88pvhN11ZG8zHpeUhnaQccJ9ekzkCQDHHG9LYCOqTgsyY ms//cw4sv2nu0E1UezTjUFeqo1sq0+WN96b/M5qnv45/Z3xZxzJ4HOCJ/NRwxNOtEUkw+zY=

And receives a ciphertext message of:

Pob7AQZZSm1618nMwTpx3V74N45x/rTimUQeT10yHq8F0dsekZgOT385J1s1HUZWCx6ZRFPFMJ1RNYR2Yh7AkQtFLVx91YDfb/Q+SkinBIBX59ER3/fDhrVKxIN4S6h2QmMSRb1h4KdVhyY6coxu +g48Jh7TkQ2Ig93/nCpAnYQ=

Using the following code:

from Crypto.PublicKey import RSA from Crypto Util import asn1

from base64 import b64decode

 $\label{eq:msg} $$msg="Pob7aQZZSm1618nMwTpx3V74N45x/rTimUQeT10yHq8F0dsekZgOT385J1s1HUzwCx6ZRFPFMJ1RNYR2Yh7akQtFLVx91YDfb/Q+SkinBIBX59ER3/fDhrVKxIN4S6h2QmMSRb1h4KdVhyY6cOxu+g48Jh7TkQ2Ig93/nCpAnYQ="$

privatekey =

'MIICXAIBAAKBgQCwgjkeoyCXm9v6VBnUi5ihQ2knkdxGDL3GXLIUU43/froeqk7q9mtxT4AnPAaDX3f2r4STZYYiqXGSHCUBZcI90dvZf6YiEM5OY2jgsmqBjf2Xkp/8HgN/XDw/wD2+zebYGLLYtd2u3GXx9edqJ8kQcU9LaMH+ficFQyfq9UwTjQIDAQABAoGAD7L1a6Ess+9b6G70gTANWkKJpshVZDGb63mxKRepaJEX8SRJEqLqOYDNSC+pkKO8IsfHreh4vrp9bsZuECrB1OHSjwDBOS/fm3KEWbsaaXDUAu0dQg/JBMXAKzeATreoIYJItYgwzrJ++fuquKabAZumvOnWJyBIs2z103kDz2ECQQDnn3JpHirmgVdf81yBbAJaXBXNIPZOCCth1zwFAs4EvrE35n2HvUQuRhy3ahUKXsKX/bGvwzmC2O6kbLTFEygVAkEAwxXZnPkaAY2vuoUCN5NbLZgegrAtmU+U2woa5A0fx6uXmShqxo1iDxEC71FbNIgHBg5srsUyDj3OsloLmDVjmQJAIy7qLyOA+sCc6BtMavBgLx+bxCwFmsoZHOSX3179smTRAJ/HY64RREISLIQ1q/yw7IWBzxQ5wTHgliNZFjKBvQJBAL3t/vCJwRz0Ebs5FaB/8UwhhsrbtXlGdnkOjIGsmVOvHsf6poHqUiay/DV88pvhN11ZG8zHpeUhnaQccJ9ekzkCQDHHG9LYCOqTgsyYms//cW4sv2nuOE1UezTjUFeqOlsgO+WN96b/M5gnv45/Z3xZxzJ4HOCJ/NRwxNOtEUkw+zY='

keyDER = b64decode(privatekey)
keys = RSA.importKey(keyDER)

dmsg = keys.decrypt(b64decode(msg))
print dmsg

What is the plaintext message that Bob has been sent?

B OpenSSL (RSA)

We will using OpenSSL to perform the following:

No	Description	Result
B.1	First we need to generate a key pair with: openssl genrsa -out private.pem 1024	What is the type of public key method used:
		How long is the default key:
	This file contains both the public and the private key.	How long did it take to generate a 1,024 bit key?
		Use the following command to view the keys:
		type private.pem(or cat private.pem in Linux)
B.2	Use following command to view the output file: cat private.pem	What can be observed at the start and end of the file:

B.3	Next we view the RSA key pair:	Which are the attributes of the key shown:
	openssl rsa -in private.pem -text	
		Which number format is used to display the information on the attributes:
B.4	Let's now secure the encrypted key with 3-DES:	
	openssl rsa -in private.pem -des3 -out key3des.pem	
B.5	Next we will export the public key:	View the output key. What does the header and footer of the file identify?
	openssl rsa -in private.pem -out public.pem -outform PEM -pubout	
B.6	Now we will encrypt with our public key:	
	openssl rsautl -encrypt -inkey public.pem -pubin -in myfile.txt -out file.bin	
B.7	And then decrypt with our private key:	What are the contents of decrypted.txt
	openssl rsautl -decrypt -inkey private.pem -in file.bin -out decrypted.txt	

C OpenSSL (ECC)

Elliptic Curve Cryptography (ECC) is now used extensively within public key encryption, including with Bitcoin, Ethereum, Tor, and many IoT applications. In this part of the lab we will use OpenSSL to create a key pair. For this we generate a random 256-bit private key (*priv*), and then generate a public key point (*priv* multiplied by G), using a generator (G), and which is a generator point on the selected elliptic curve.

Ī	No	Description	Result
	C.1	First we need to generate a private key with:	Can you view your key?
		openssl ecparam -name secp256k1 -genkey -out priv.pem	

	The file will only contain the private key (and should have 256 bits).	
	Now use "cat priv.pem" to view your key.	
C.2	We can view the details of the ECC parameters used with:	Outline these values:
	openssl ecparam -in priv.pem -text -	Prime (last two bytes):
	param_enc explicit -noout	A:
		B:
		Generator (last two bytes):
		Order (last two bytes):
C.3	Now generate your public key based on your private key with:	How many bits and bytes does your private key have:
	openssl ec -in priv.pem -text -noout	
		How many bit and bytes does your public key have (Note the 04 is not part of the elliptic curve point):
		What is the ECC method that you have used?

If you want to see an example of ECC, try here: https://asecuritysite.com/encryption/ecc

D Elliptic Curve Encryption

D.1 In the following Bob and Alice create elliptic curve key pairs. Bob can encrypt a message for Alice with her public key, and she can decrypt with her private key. Copy and paste the program from here:

https://asecuritysite.com/encryption/elc

Code used:

import OpenSSL import pyelliptic

```
secretkey="password"
test="Test123"
alice = pyelliptic.ECC()
bob = pyelliptic.ECC()
print "++++Keys++++"
print "Bob's private key: "+bob.get_privkey().encode('hex')
print "Bob's public key: "+bob.get_pubkey().encode('hex')
print "Alice's private key: "+alice.get_privkey().encode('hex')
print "Alice's public key: "+alice.get_pubkey().encode('hex')
ciphertext = alice.encrypt(test, bob.get_pubkey().encode('hex')

print "\n++++Encryption++++"
print "Cipher: "+ciphertext.encode('hex')
print "Decrypt: "+bob.decrypt(ciphertext)
signature = bob.sign("Alice")
print "Bob verified: "+ str(pyelliptic.ECC(pubkey=bob.get_pubkey()).verify(signature, "Alice"))
```

For a message of "Hello. Alice", what is the ciphertext sent (just include the first four characters):

How is the signature used in this example?

D.2 Let's say we create an elliptic curve with $y^2 = x^3 + 7$, and with a prime number of 89, generate the first five (x,y) points for the finite field elliptic curve. You can use the Python code at the following to generate them:

https://asecuritysite.com/encryption/ecc points

First five points:

D.3 Elliptic curve methods are often used to sign messages, and where Bob will sign a message with his private key, and where Alice can prove that he has signed it by using his public key. With ECC, we can use ECDSA, and which was used in the first version of Bitcoin. Enter the following code:

```
from ecdsa import
SigningKey,NIST192p,NIST224p,NIST256p,NIST384p,NIST521p,SECP256k1
import base64
import sys
```

What are the signatures (you only need to note the first four characters) for a message of "Bob", for the curves of NIST192p, NIST512p and SECP256k1:

NIST192p:

NIST512p:

SECP256k1:

By searching on the Internet, can you find where SECP256k1 is used?

What do you observe from the different hash signatures from the elliptic curve methods?

E Inverse of a value mod N

E.1 In the RSA method, we have a value of e, and then determine d from (d.e) (mod PHI)=1. But how do we use code to determine d? Well we can use the Euclidean algorithm. The code for this is given at:

https://asecuritysite.com/encryption/inversemod

Using the code, can you determine the following:

Inverse of 53 (mod 120) =

1111/ELSE 01 0555 / (1110u 1054 / /005105 /41042001440011575514000) -	Inverse of 65537	(mod 1034776851837418226012406113933120080) =
---	------------------	---

F Reflective statements

1. In ECC, we use a 256-bit private key. This is used to generate the key for signing Bitcoin transactions. Do you think that a 256-bit key is largest enough? If we use a cracker what performs 1 Tera keys per second, will someone be able to determine our private key?

2. If someone takes our elliptic curve public key, how might they determine our public key?

G What I should have learnt from this lab?

The key things learnt:

- The basics of the RSA method.
- The process of generating RSA and Elliptic Curve key pairs.
- To illustrate how the private key is used to sign data, and then using the public key to verify the signature.

Notes

To setup your Python to run Python 2.7:

sudo update-alternatives --set python /usr/bin/python2.7

To install a Python library use:

easy_install libname

or:

pip install libname