

EPSRC

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Research Council

Epidemics & Errors: Finding the Silver Lining

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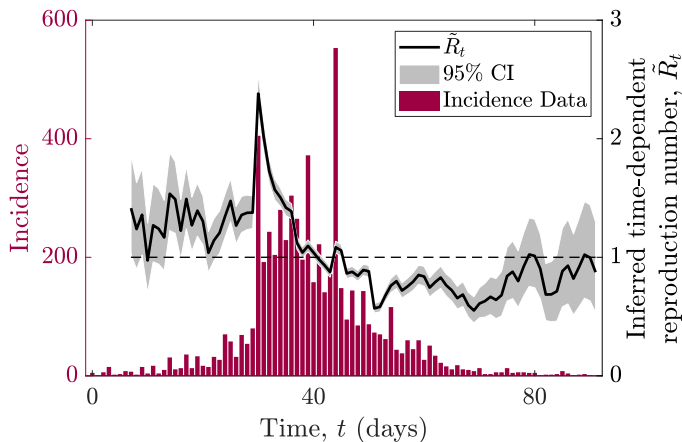
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September 27, 2021

Imperfect data collection may introduce systematic bias into parameter inference

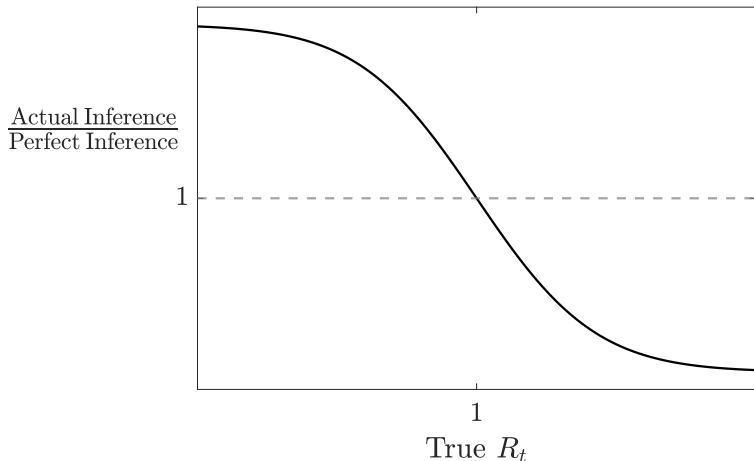


During epidemics, the reproduction number, R_t , is an important parameter to infer

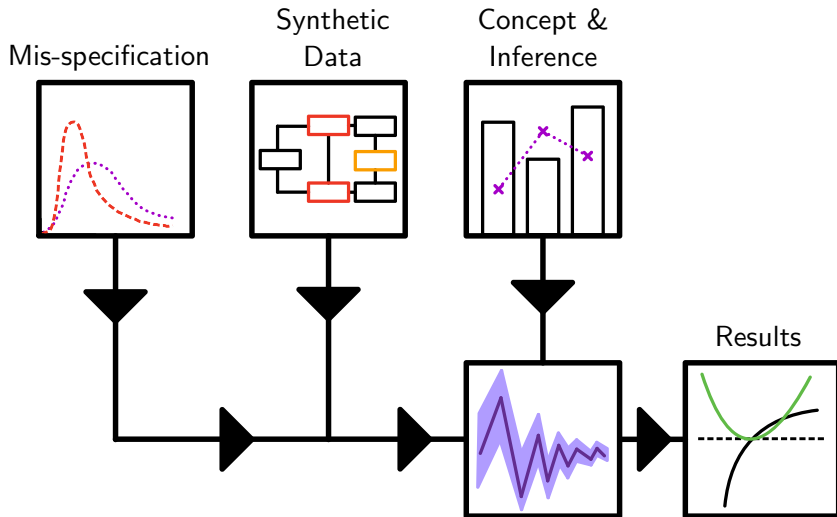


Data source: [Cori et. al, AJE 2013](#)

R_t inference may be improved with extra information about systematic inference bias



Talk Outline



Definitions

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- R_t : The average number of people someone infected at time t could expect to infect (should conditions remain unchanged).

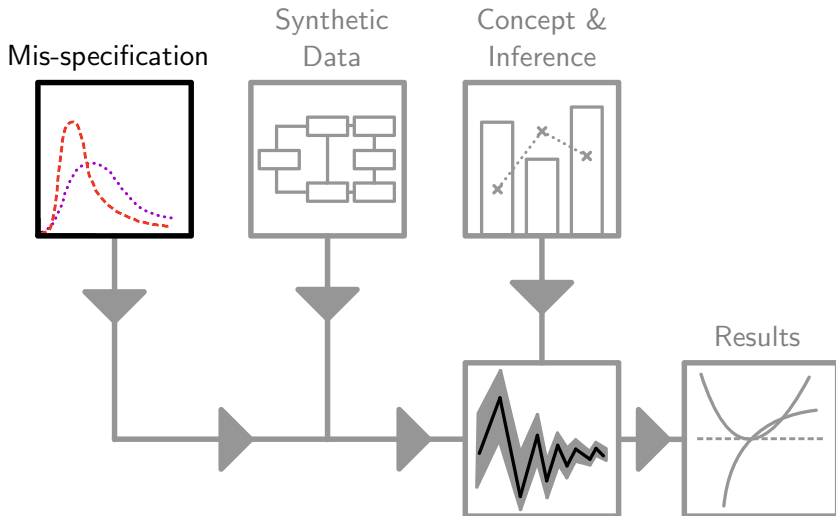
Definitions

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- Generation interval (GI): The interval between the time when an individual is infected by an infector and the time when this infector was infected.

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- Generation interval (GI): The interval between the time when an individual is infected by an infector and the time when this infector was infected.
- Incidence: The number of individuals who develop a specific disease during a particular time period (we assume days).

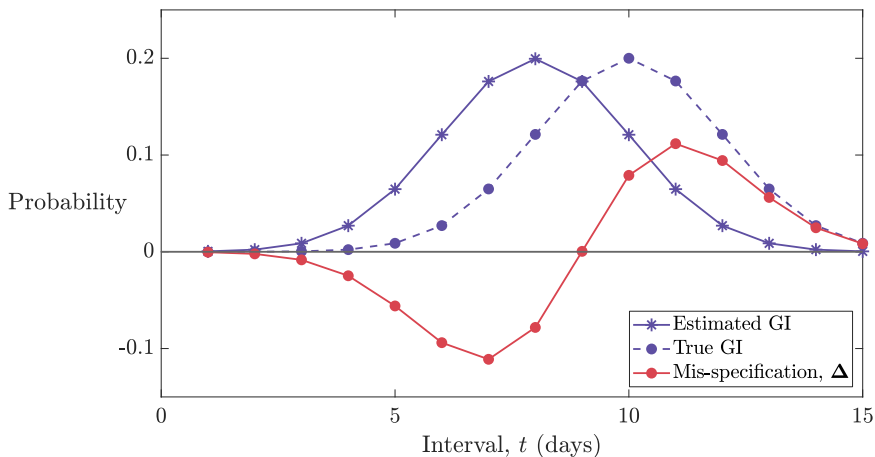
Mis-specification of generation intervals



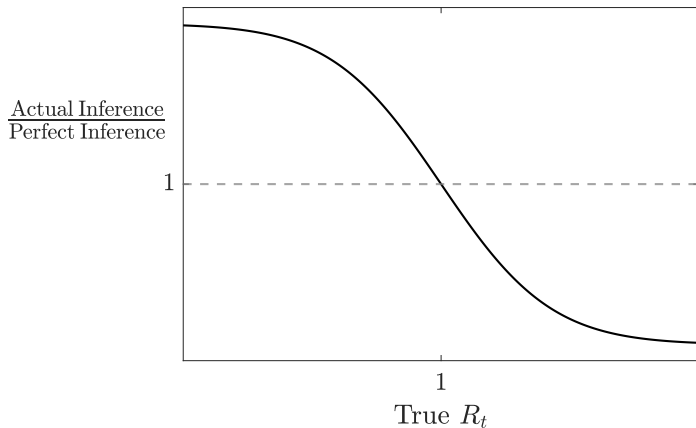
Generation intervals (GIs) can change during the course of an epidemic

One example cause: Public health measure e.g. enforced isolation if tested positive for disease.

The mis-specification, Δ , is the difference between the recorded & true generation intervals

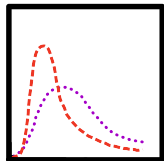


Certain mis-specification characteristics are significant in systematic R_t inference bias

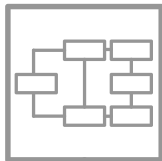


Mis-specification of generation intervals

Mis-specification



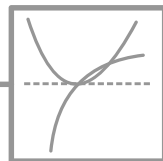
Synthetic
Data



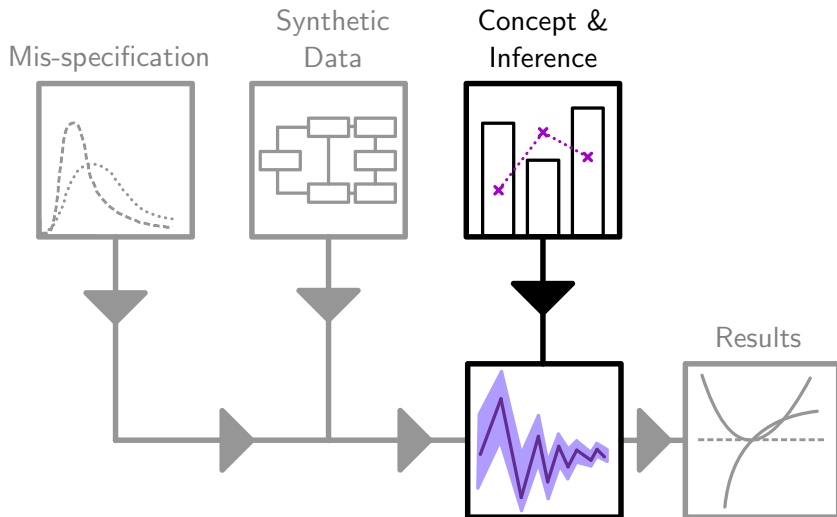
Concept &
Inference



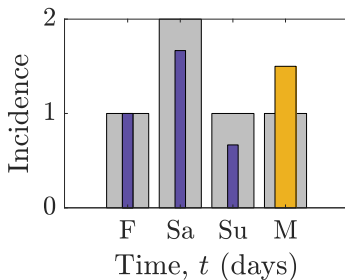
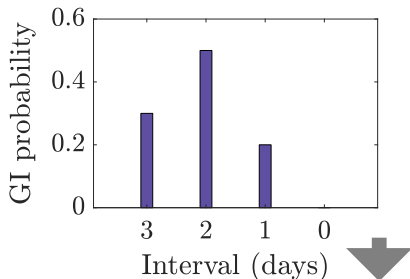
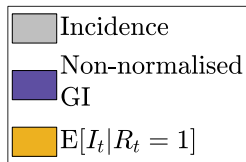
Results



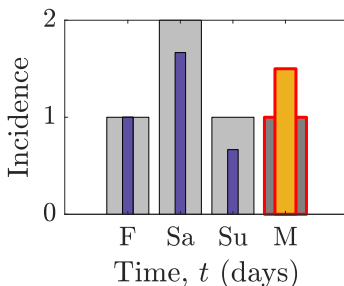
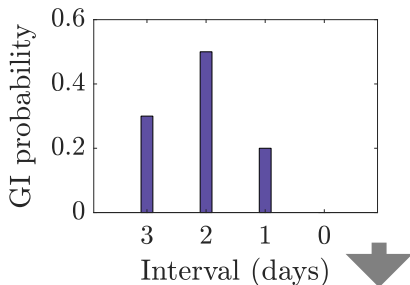
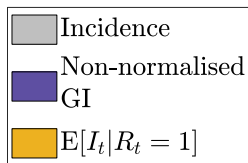
Concept for R_t inference



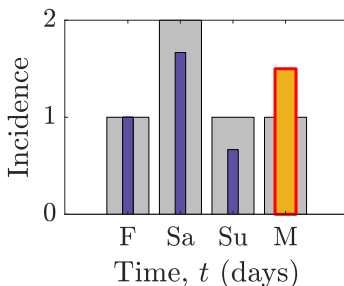
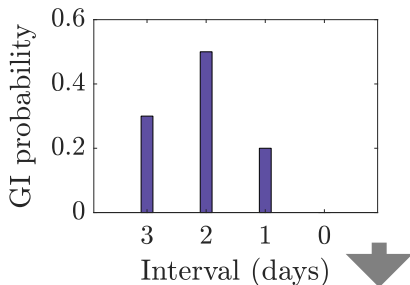
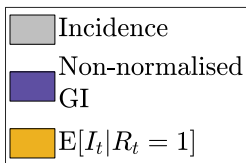
R_t can be estimated using estimated GIs & incidence data



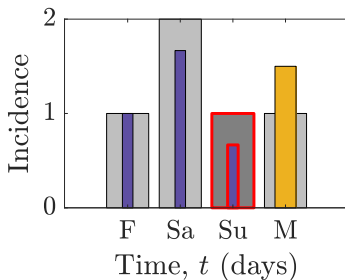
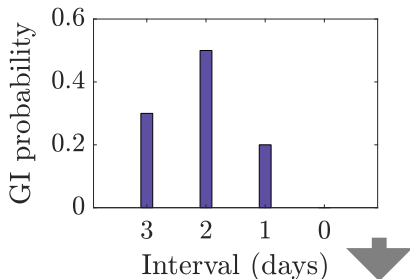
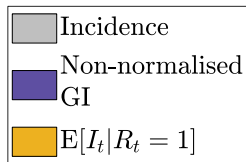
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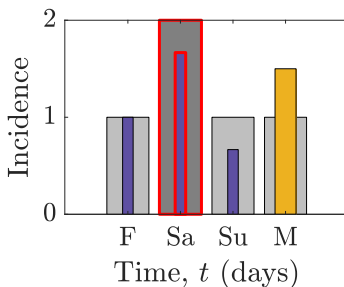
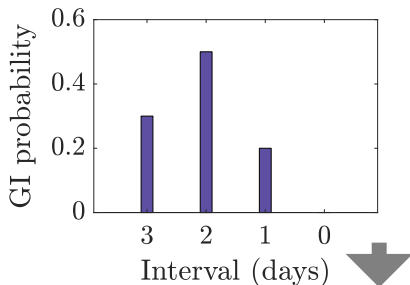
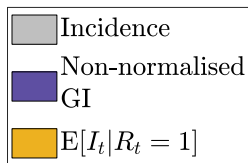
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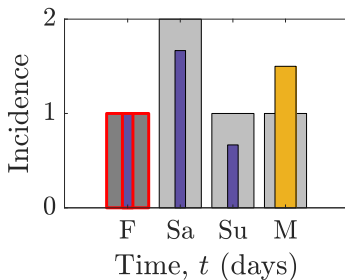
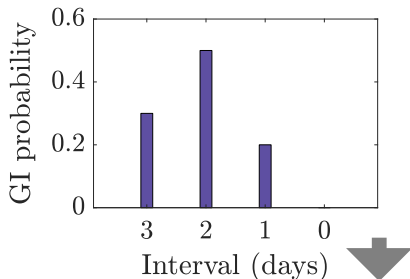
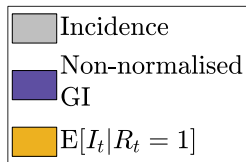
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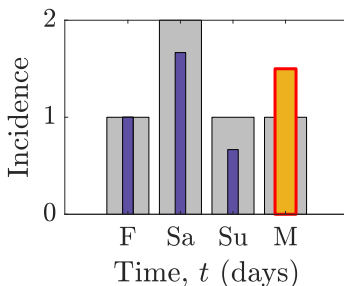
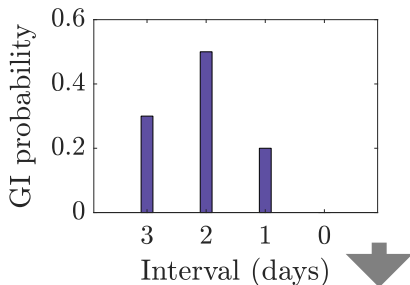
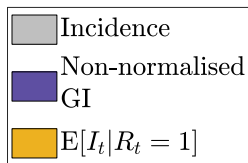
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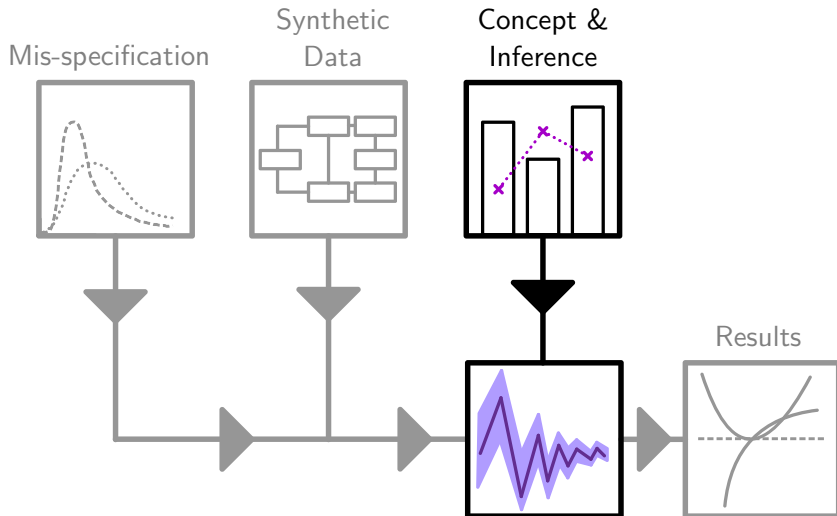


R_t can be estimated using estimated GIs & incidence data

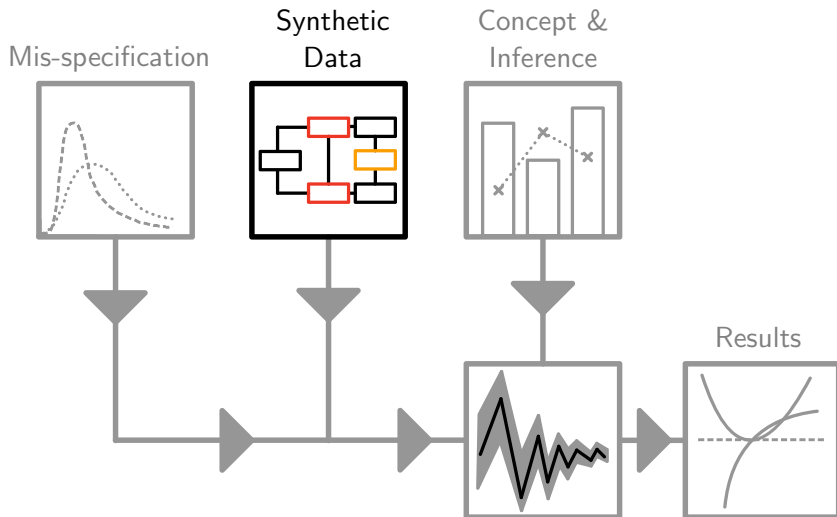
$$\begin{aligned}\mathbb{E}[I_{\text{Mon}} | R_{\text{Mon}} = 1] &= \mathbb{P}[\text{GI} = 1] \cdot I_{\text{Sun}} \\ &\quad + \mathbb{P}[\text{GI} = 2] \cdot I_{\text{Sat}} \\ &\quad + \mathbb{P}[\text{GI} = 3] \cdot I_{\text{Fri}}\end{aligned}$$

$$\tilde{R}_{\text{Mon}} = \frac{I_{\text{Mon}}}{\mathbb{E}[I_{\text{Mon}} | R_{\text{Mon}} = 1]}$$

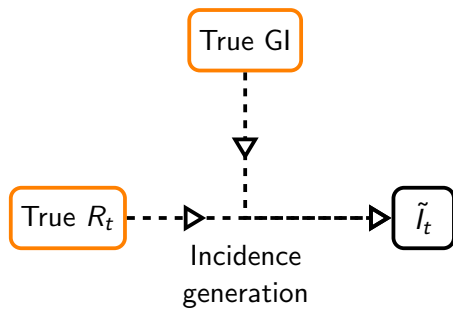
Concept for R_t inference



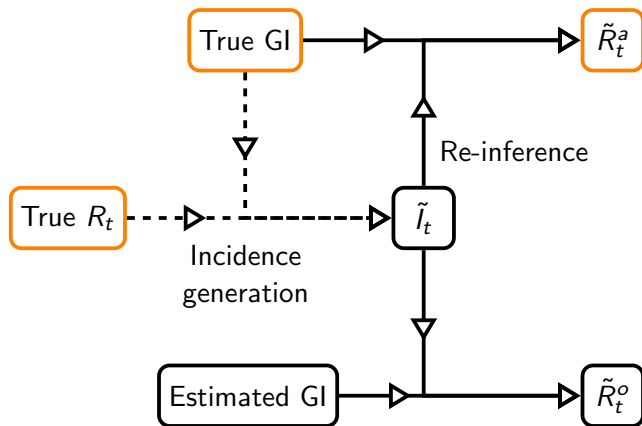
Comparing perfect & realistic inferences via synthetic data



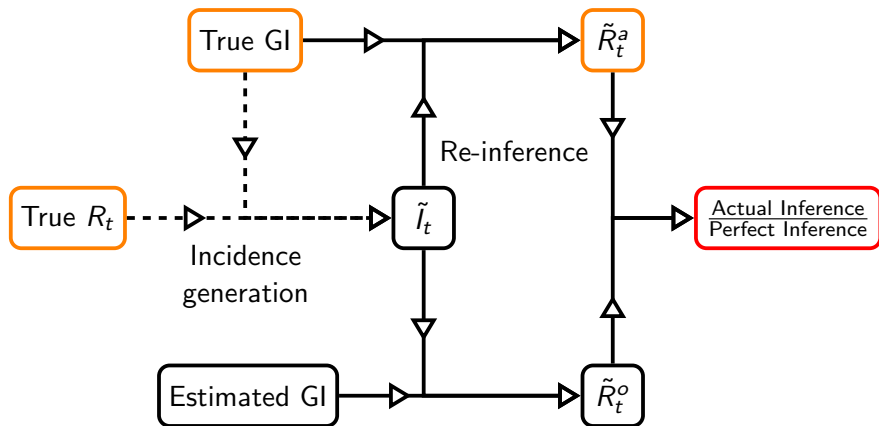
Synthetic outbreaks can be generated using the true R_t and the true GI



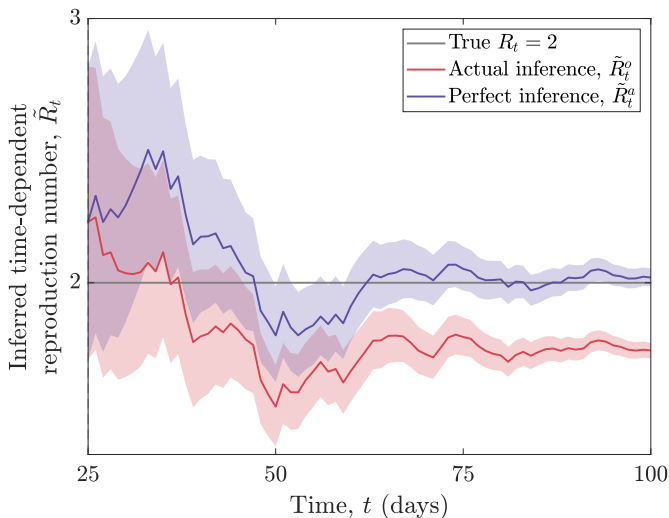
Best-case and realistic R_t estimates may be inferred using the true and recorded generation intervals respectively.



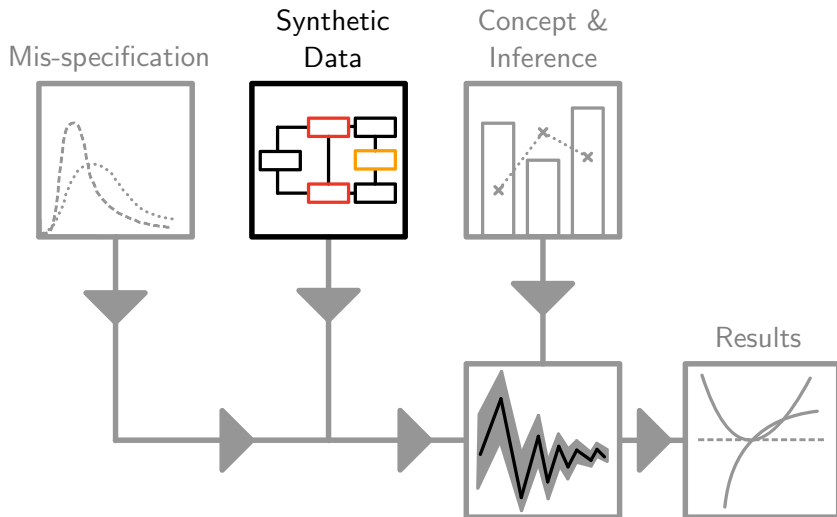
The ratio of these two inferences can be made, $\tilde{R}_t^o / \tilde{R}_t^a$



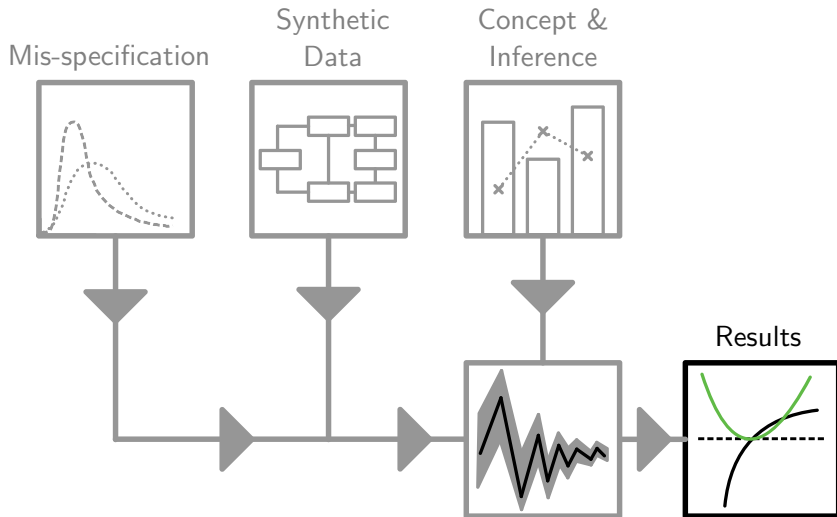
Systematic over/under estimation bias does not imply over/under R_t estimation



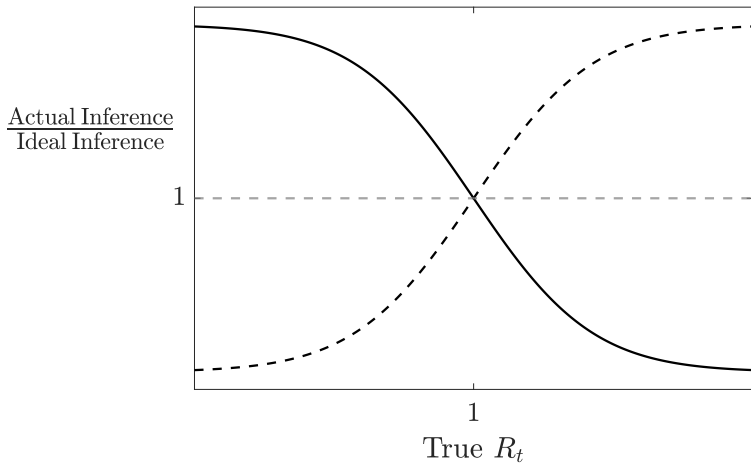
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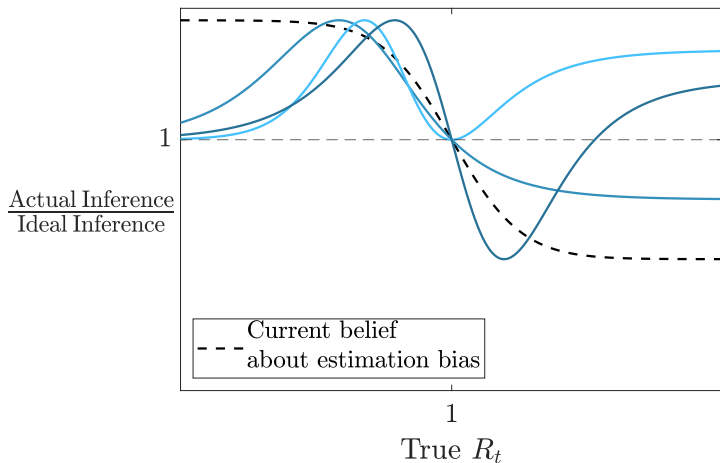
Results



The consensus view is that R_t inference is more bias, the greater R_t is from 1



Our results show that this view is false: Estimation bias is more complex



Using a limited knowledge of issues in data collection, we can comment on what type of bias may be present

Latest R and growth rate for England

Latest R range for England

0.8 to 1.0

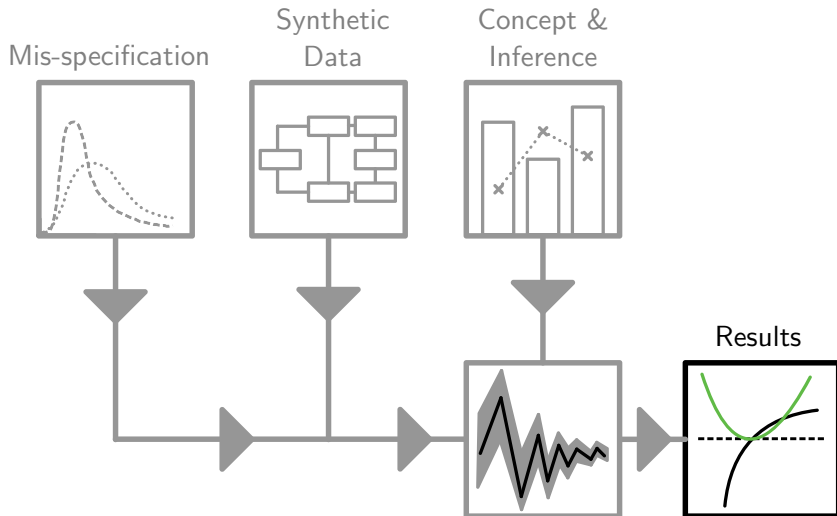
Latest growth rate range for England

-3% to -1%

per day

Source: <https://www.gov.uk/guidance/the-r-value-and-growth-rate>, 25/09/21

Results



The team!



Zak Ogi-Gittins

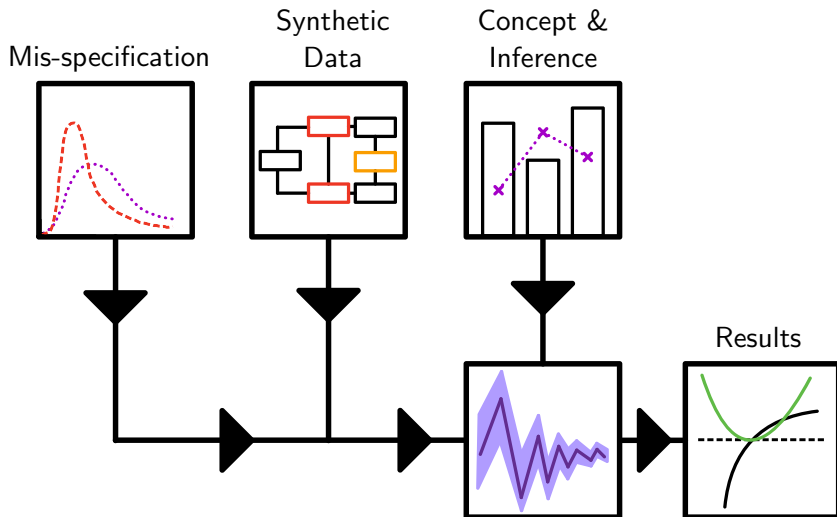


Robin Thompson

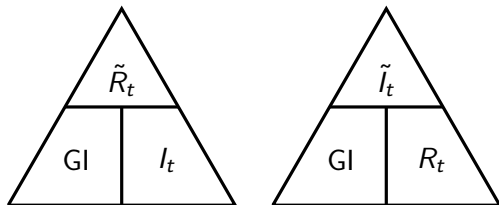


Ed Hill

Thank you for listening, any questions are welcome!



Incidence time-series can be synthetically generated using the same method reversed



The \tilde{X} notation indicates that X is either estimated or synthetically generated.

main