



Cryptographic Hash Functions

Merkle Trees



# Cryptographic Hash Functions

SHA256
 RIPEMD160
 Arbitrarily long data

Fixed sized hash/digest

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## **Cryptographic Hash Function**

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- Cryptographic Hash Functions
  - Takes any byte sequence as input
  - Fixed size output
  - Efficiently computable
- Security Properties:
  - Collision-resistance
  - Second pre-image resistance
  - Pre-image resistance
  - Hiding
  - Puzzle-friendly

Example: <a href="https://www.pelock.com/products/hash-calculator">https://www.pelock.com/products/hash-calculator</a>

#### **Pre-image Resistance**

 For any given h in the output space of the hash function, it is hard to find x, s.t. H(x)=h



## **Second Pre-image Resistance**

 For a given message x, it is hard to find y s.t. x ≠ y and H(x) = H(y)

#### **Collision Resistance**

It is hard to find a pair of values,
 x ≠ y and H(x) = H(y)

#### **Hiding**

 A hash function H is hiding when a secret value r is chosen from a high min-entropy probability distribution, then given H(r || x), it is hard to find x.



## **Puzzle-friendly**

• A hash function H is puzzle friendly if for every possible n-bit output value h, if k is chosen from a distribution with high min-entropy, then it is infeasible to find x such that H(k || x) = h in time significantly less than  $2^n$ .

#### Search puzzle

- A hash function H
- A value, id, chosen from a high min-entropy distribution
- A target set Y

A solution to the puzzle is a value x, s.t.

$$H(id||x) \in Y$$

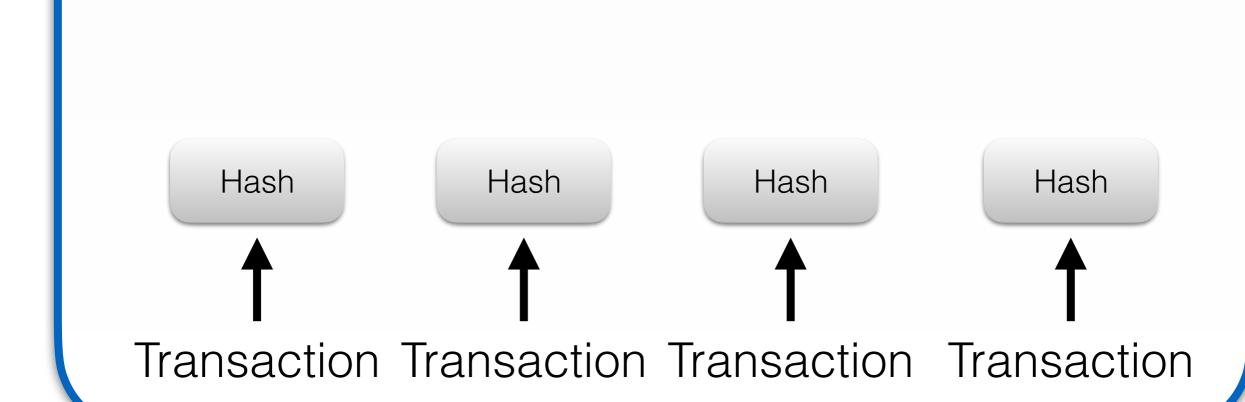




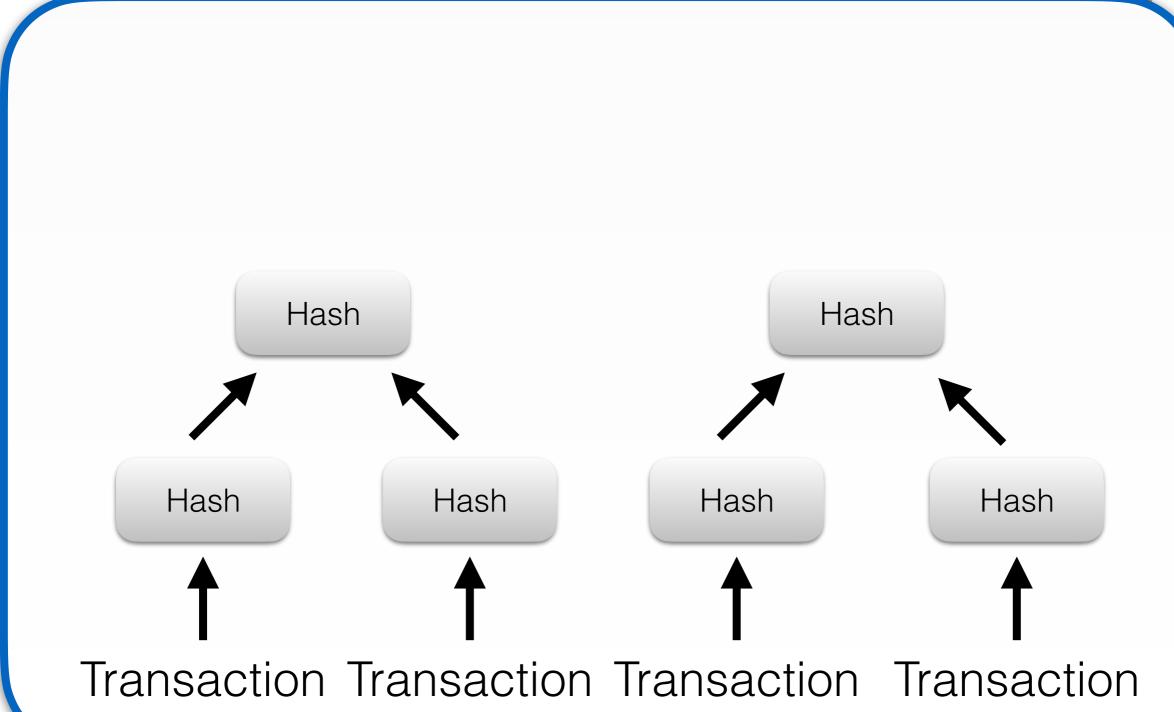
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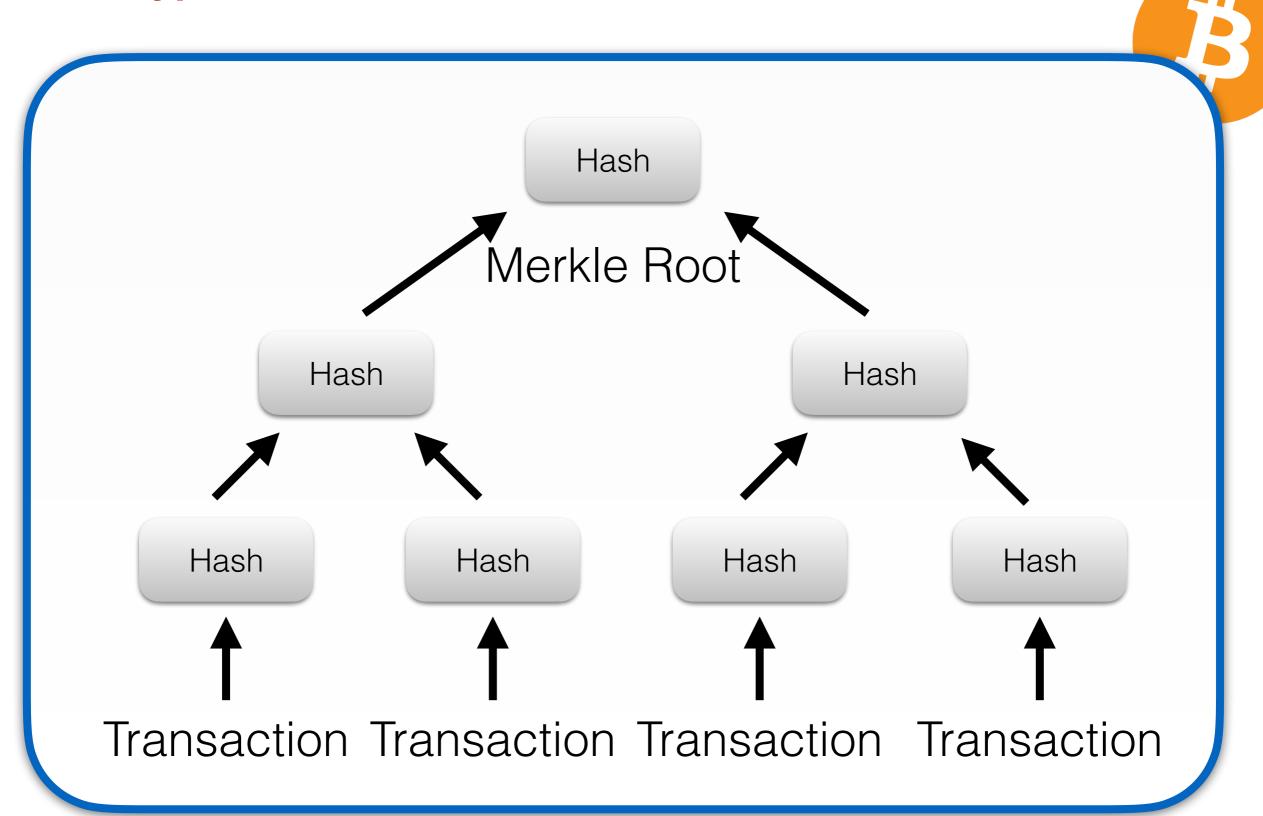
Merkle Trees













Cryptographic Hash Functions

Merkle Trees



- ECDSA (secp256k1 curve) is used to
  - Sign transactions
  - Verify the signature of transactions
- Nothing in Bitcoin is encrypted

