

# Blockchain Privacy Bloom Filter & SPV

# Enable mobile Bitcoin clients

Bloom filter

0	0	0	0	0	0	0
---	---	---	---	---	---	---

# Enable mobile Bitcoin clients

Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

Bloom filter

0	0	0	0	0	0	0
---	---	---	---	---	---	---

# Enable mobile Bitcoin clients

Insertion

Bloom filter

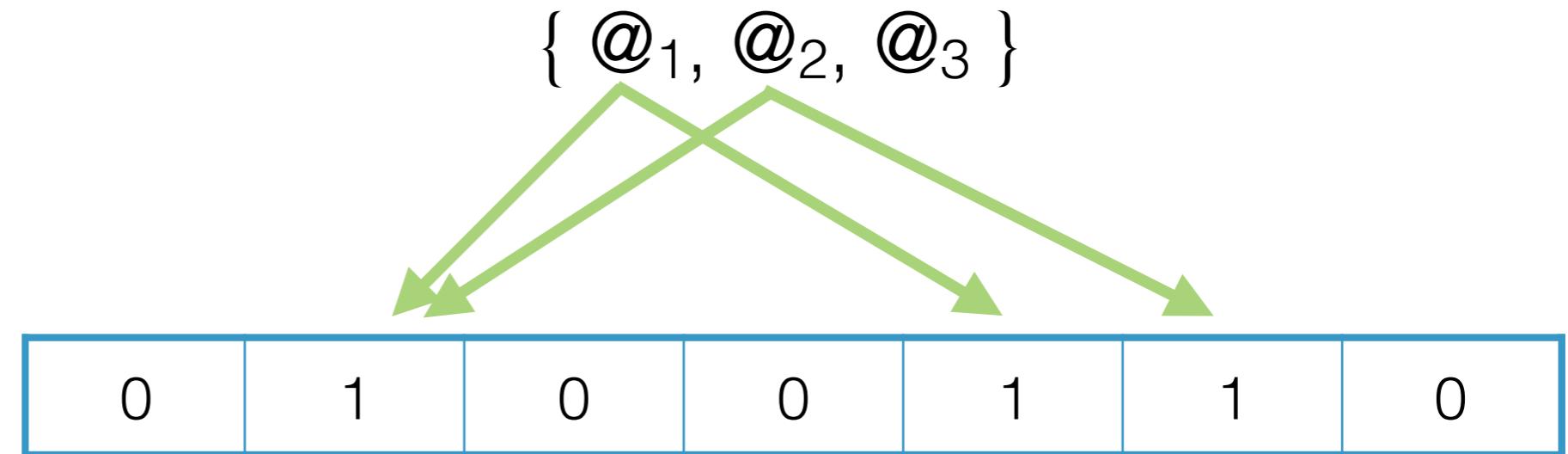
$\{ @_1, @_2, @_3 \}$



# Enable mobile Bitcoin clients

Insertion

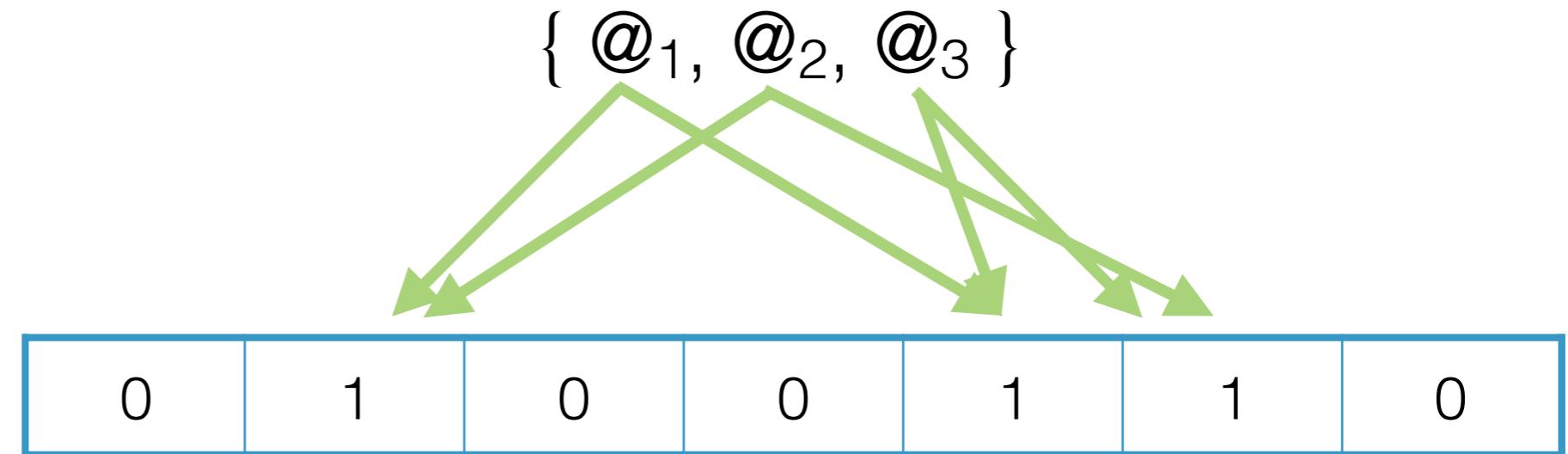
Bloom filter



# Enable mobile Bitcoin clients

Insertion

Bloom filter



# Enable mobile Bitcoin clients

Insertion

$\{ @_1, @_2, @_3 \}$



Bloom filter

0	1	0	0	1	1	0
---	---	---	---	---	---	---

Membership test

$\{ @_1, @_4, @_5 \}$

# Enable mobile Bitcoin clients

Insertion

$\{ @_1, @_2, @_3 \}$

Bloom filter



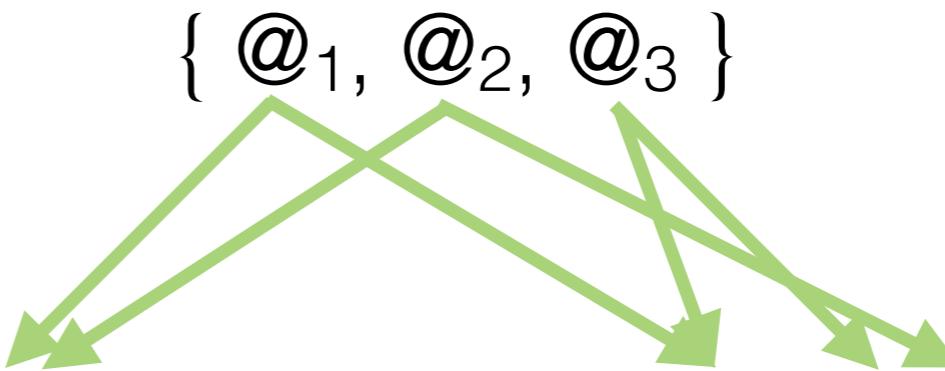
Membership test

$\{ @_1, @_4, @_5 \}$



# Enable mobile Bitcoin clients

Insertion

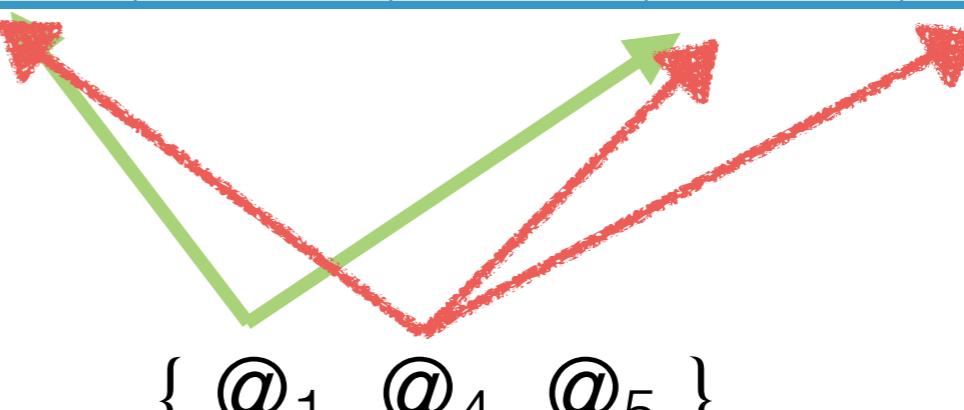


Bloom filter



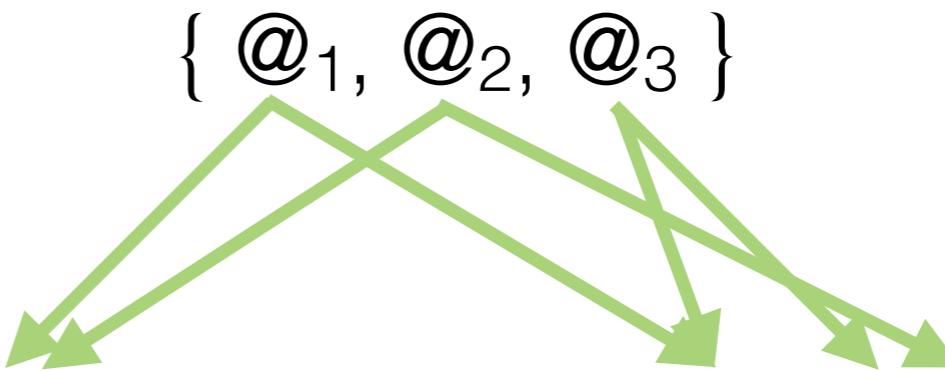
Membership test

$\{ @_1, @_4, @_5 \}$



# Enable mobile Bitcoin clients

Insertion

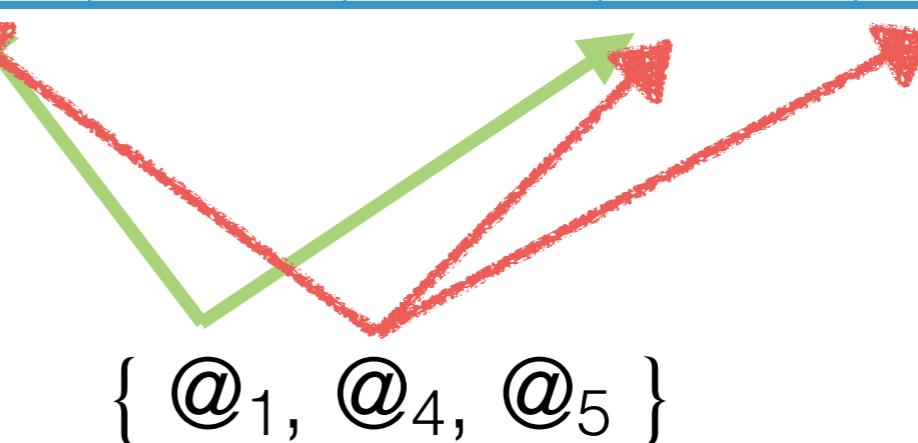


Bloom filter

0	1	0	0	0	1	1	0
---	---	---	---	---	---	---	---

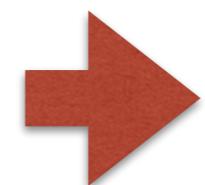
Membership test

$\{ @_1, @_4, @_5 \}$



!

$@_4$  False positive



target False Positive Rate (FPR)

# Enable mobile Bitcoin clients

Insertion

$\{ @_1, @_2, @_3 \}$



Bloom filter

0	1	0	0	0	1	1	0
---	---	---	---	---	---	---	---

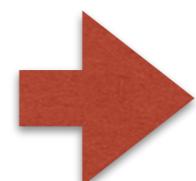
Membership test

$\{ @_1, @_4, @_5 \}$



!

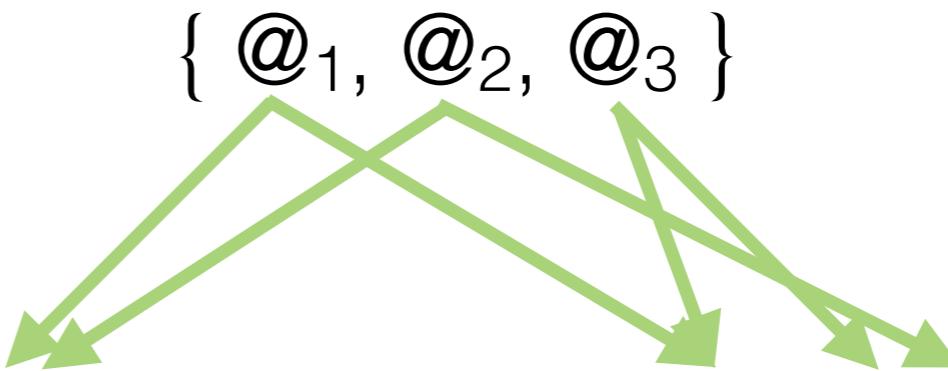
@<sub>4</sub> False positive



**target False Positive Rate (FPR)**

# Enable mobile Bitcoin clients

Insertion



Bloom filter

0	1	0	0	0	1	1	0
---	---	---	---	---	---	---	---

Membership test

$\{ @_1, @_4, @_5 \}$



!

$@_4$  False positive



**target False Positive Rate (FPR)**

$@_5$  True negative

# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user

SPV client



Full Bitcoin node



Full Bitcoin node

# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user

SPV client



$\begin{matrix} @_1 \\ @_2 \\ @_3 \end{matrix}$



Bloom filter

Full Bitcoin node



Full Bitcoin node

# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user

SPV client



$\begin{matrix} @_1 \\ @_2 \\ @_3 \end{matrix}$



Bloom filter

Full Bitcoin node



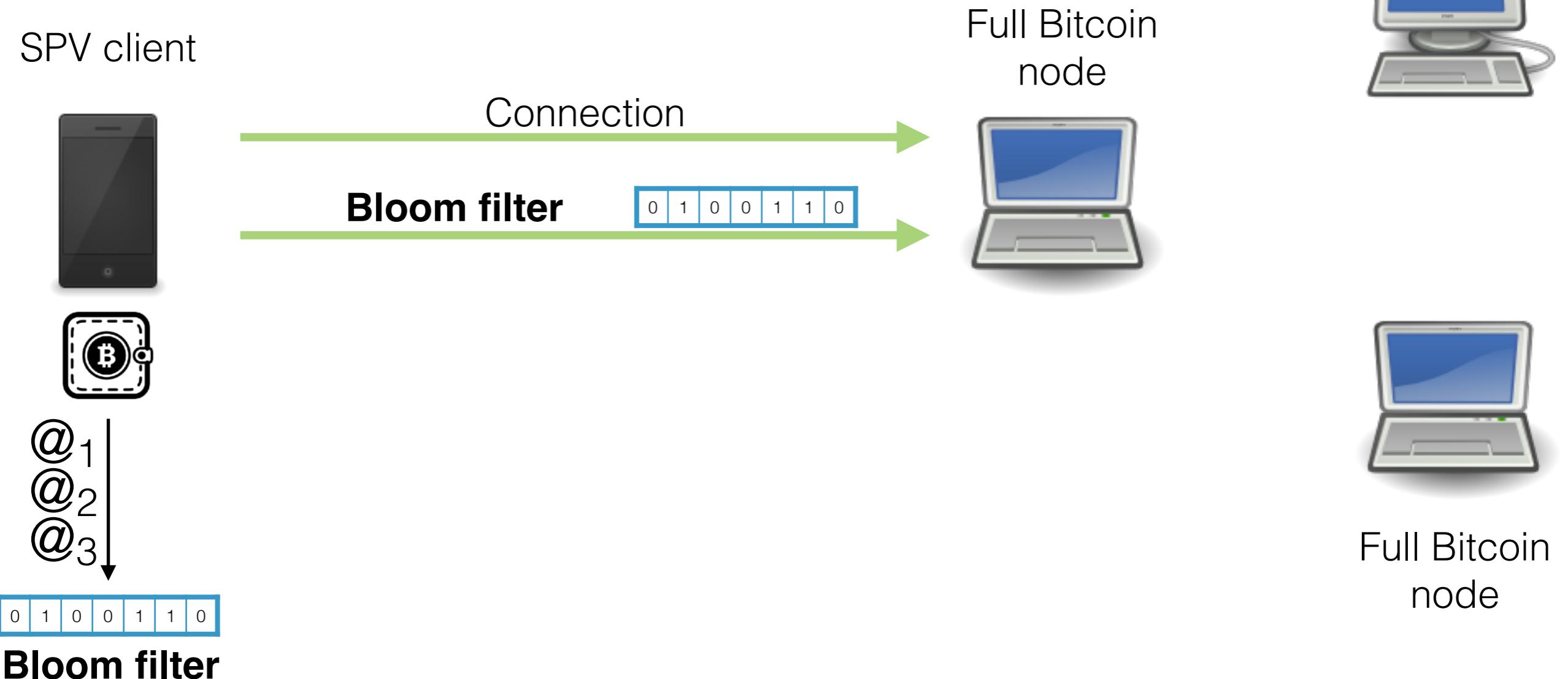
Full Bitcoin node

Connection



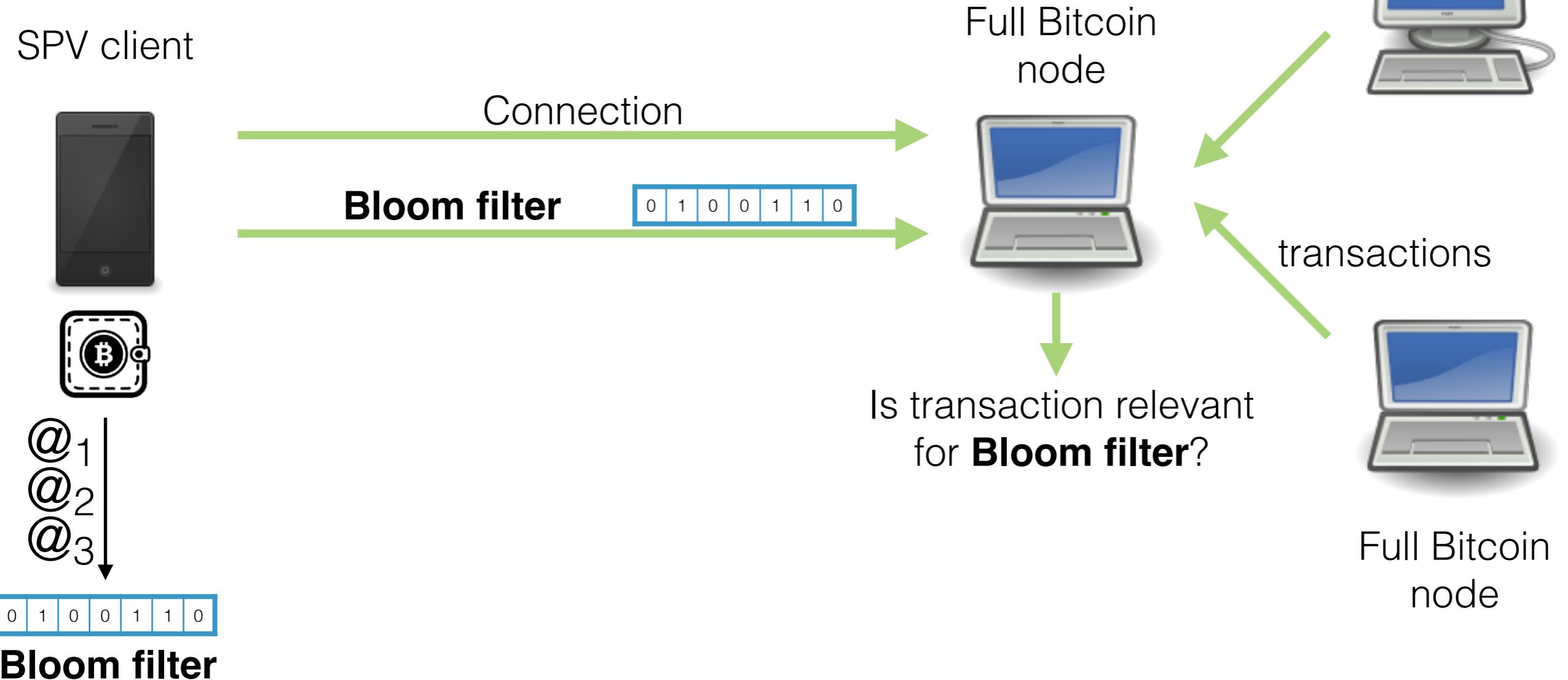
# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user



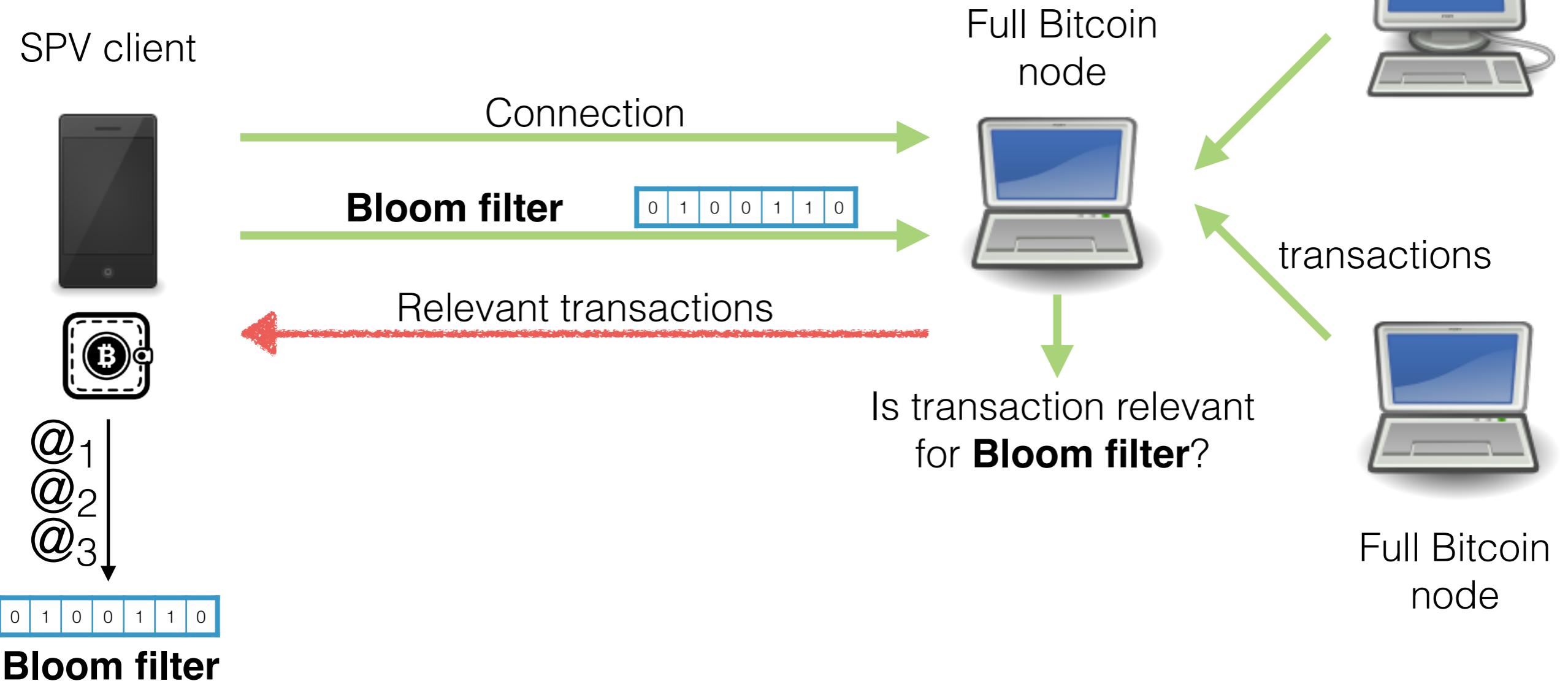
# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user



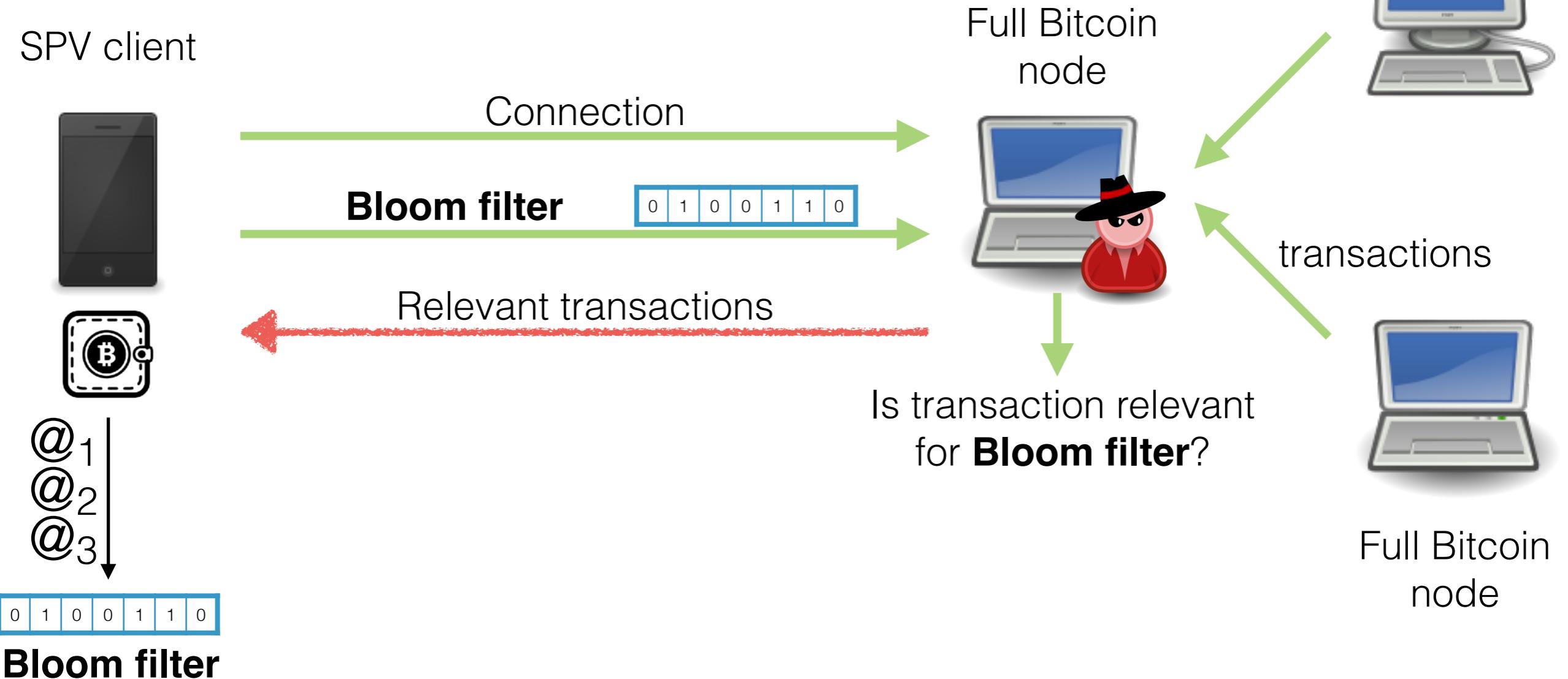
# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user



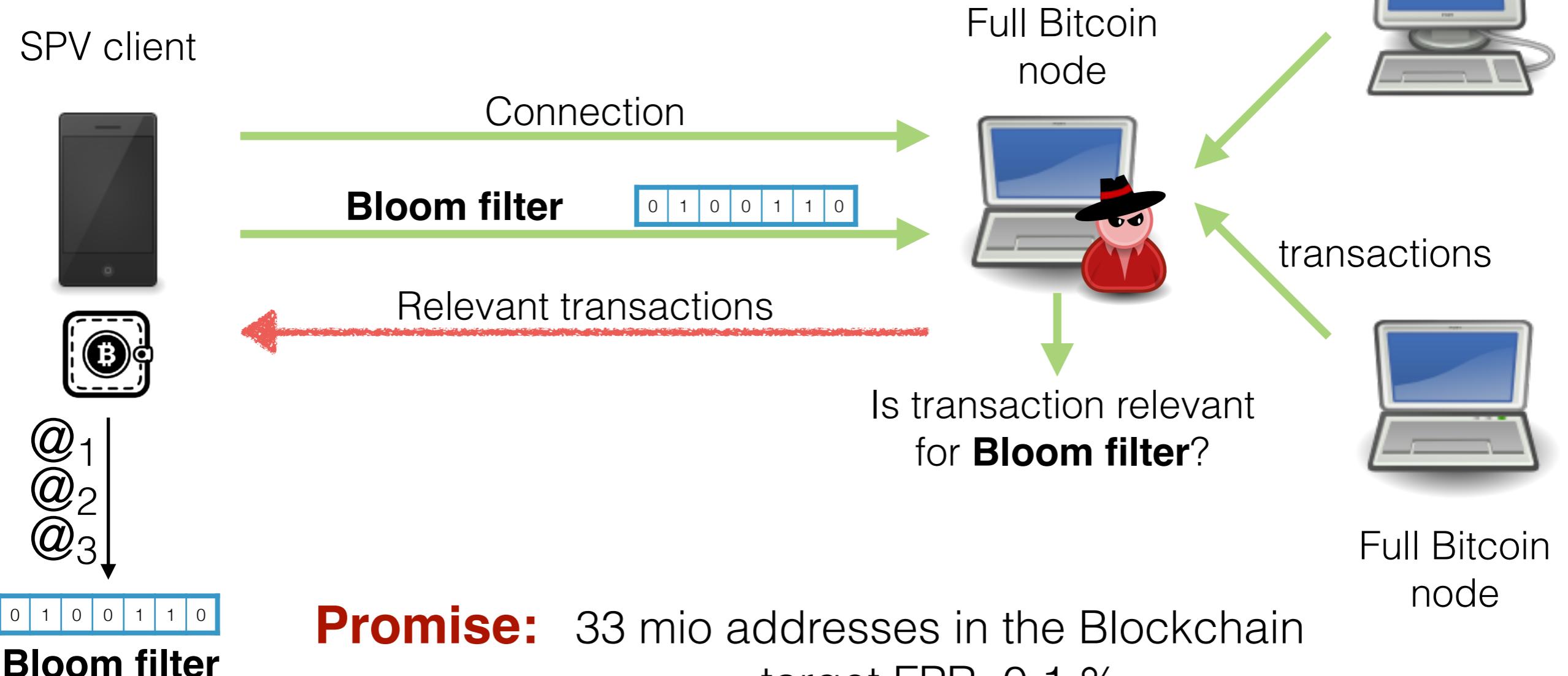
# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user



# Simple Payment Verification (SPV)

**Filter** transactions not relevant for user



**Promise:** 33 mio addresses in the Blockchain  
target FPR: 0.1 %

"User addresses hidden amongst  
33 000" false positives

# Model and Privacy measure

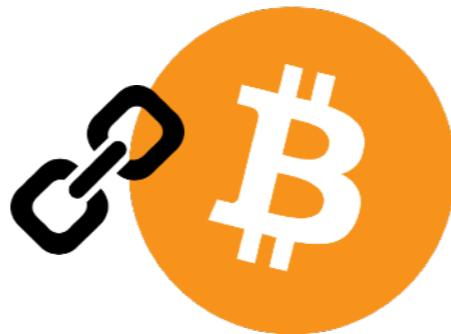


Blockchain



SPV client

# Model and Privacy measure



Blockchain

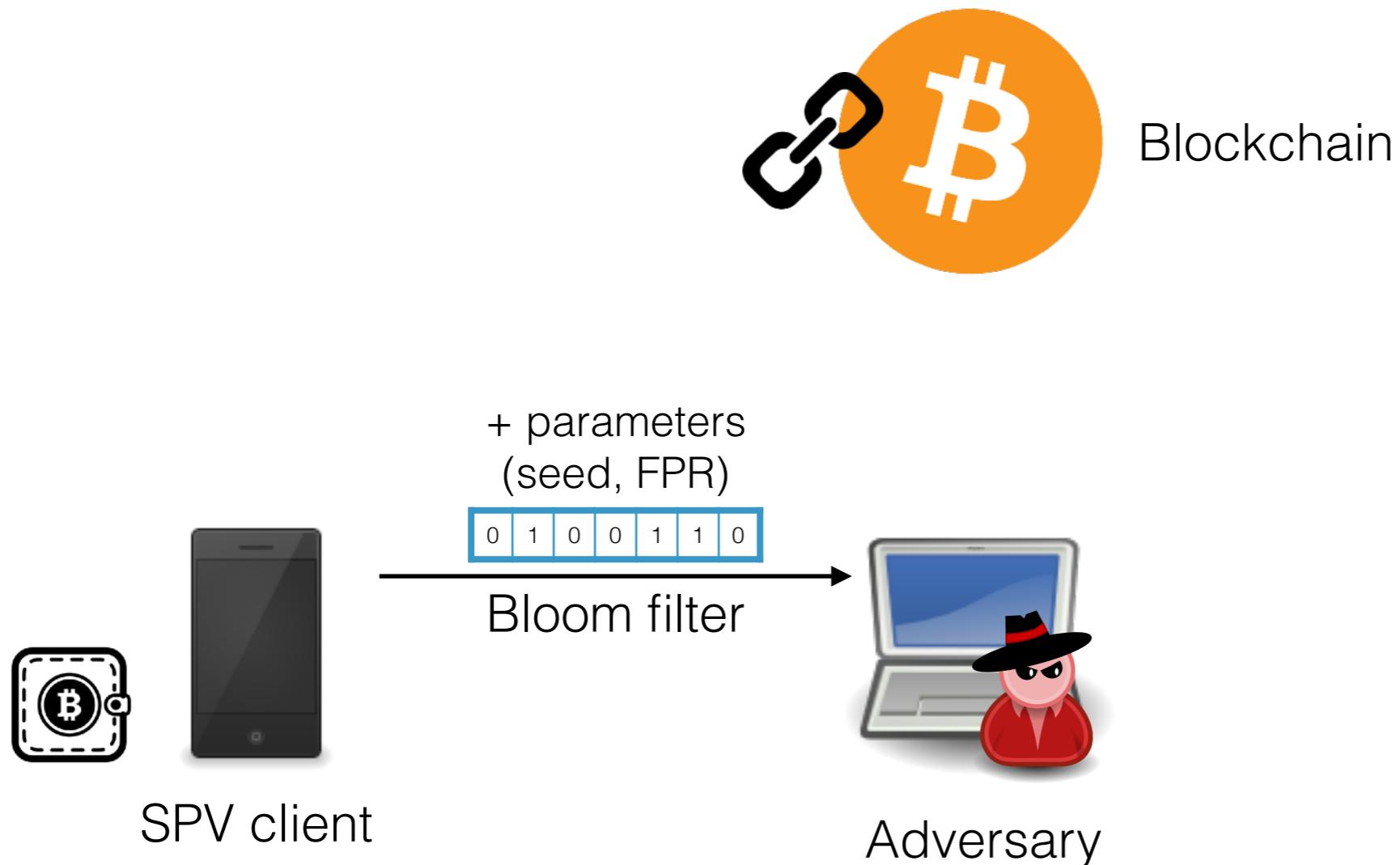


SPV client

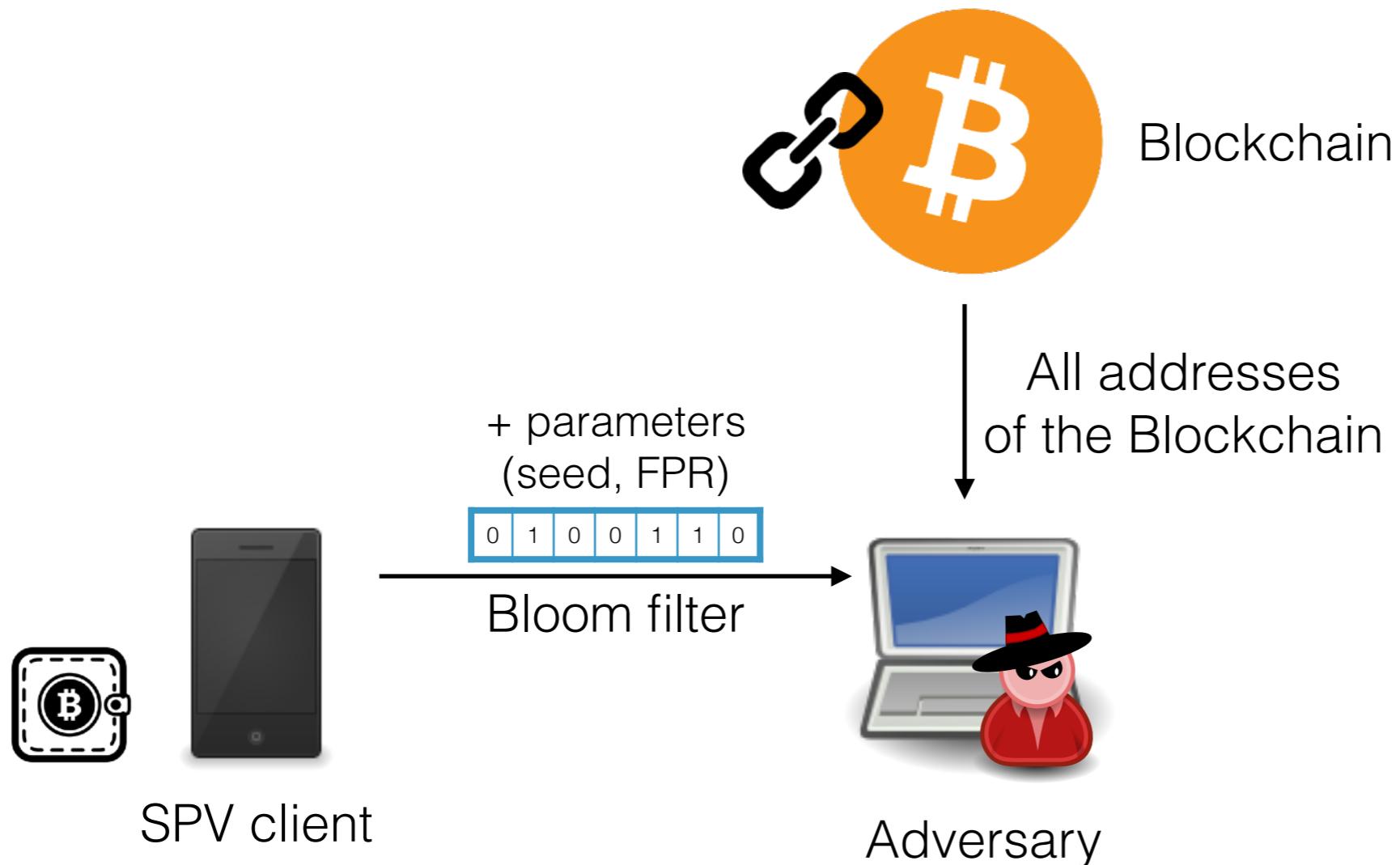


Adversary

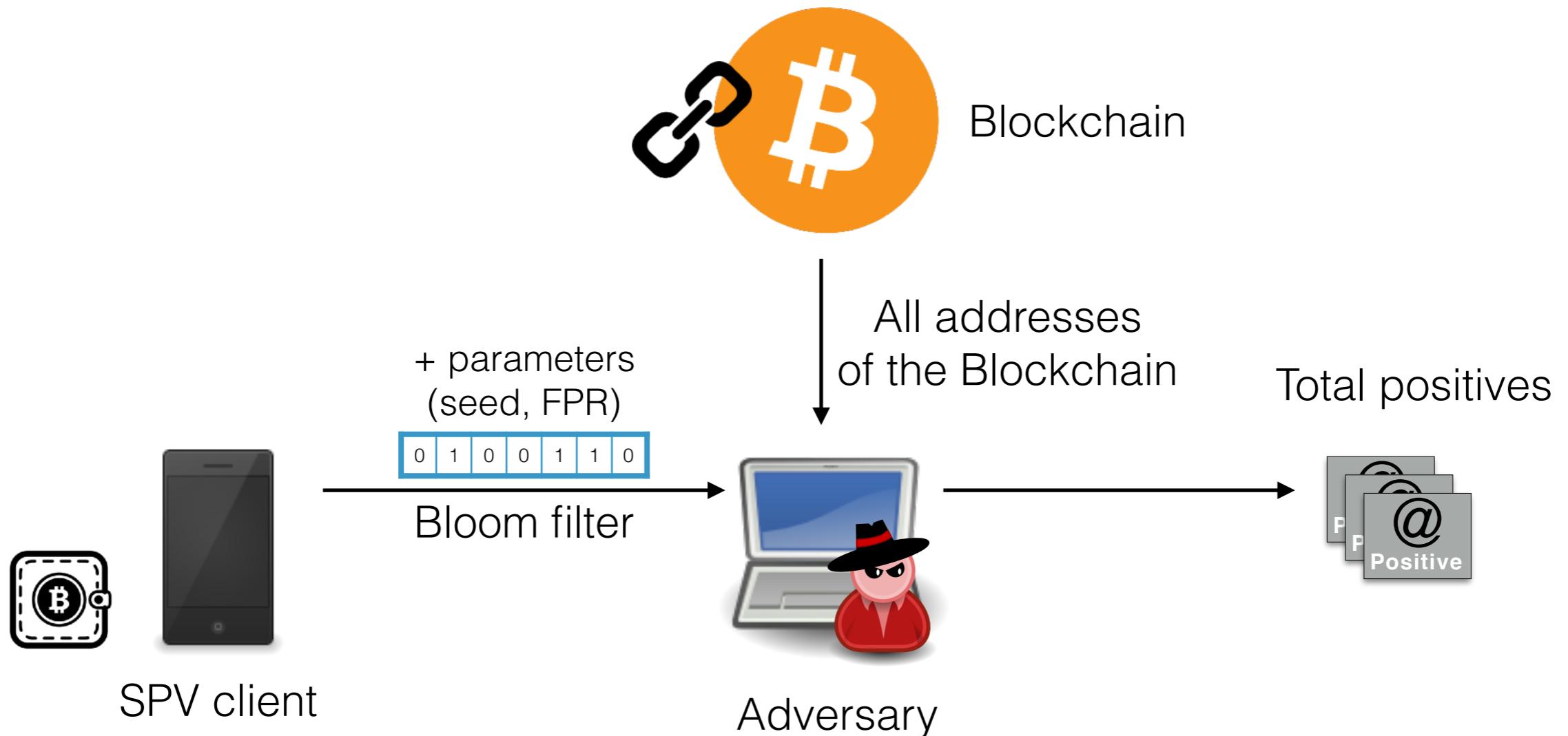
# Model and Privacy measure



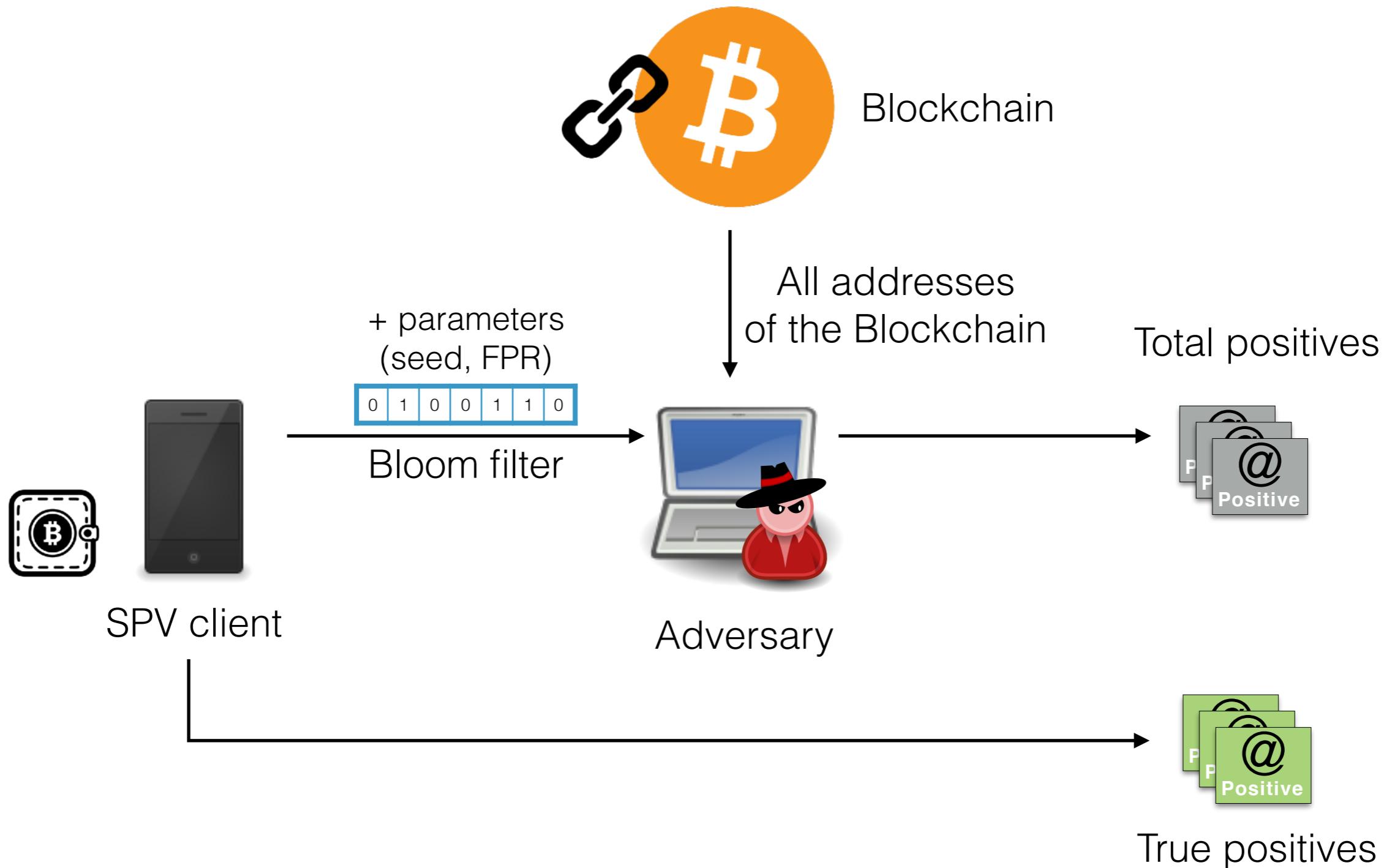
# Model and Privacy measure



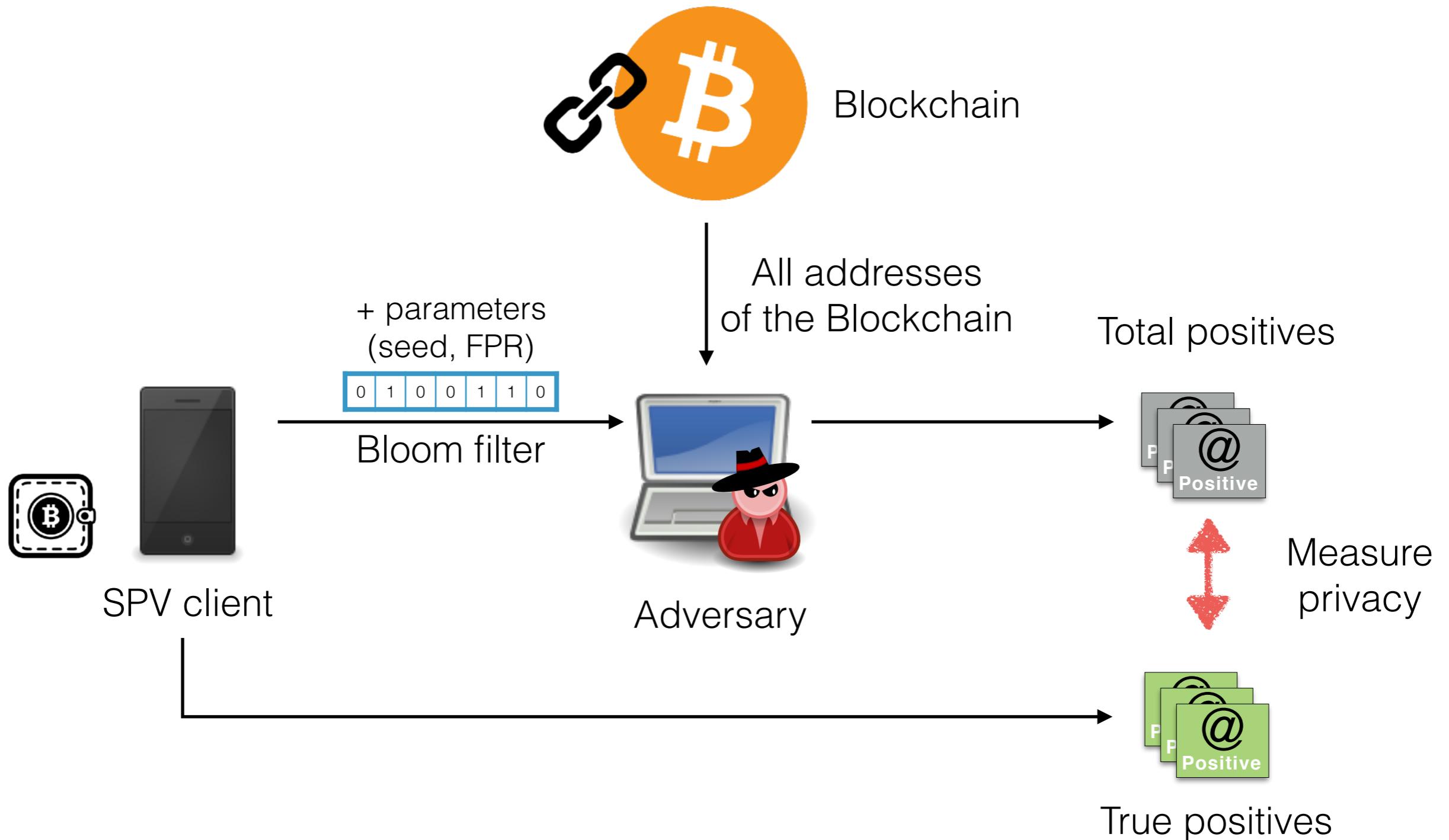
# Model and Privacy measure



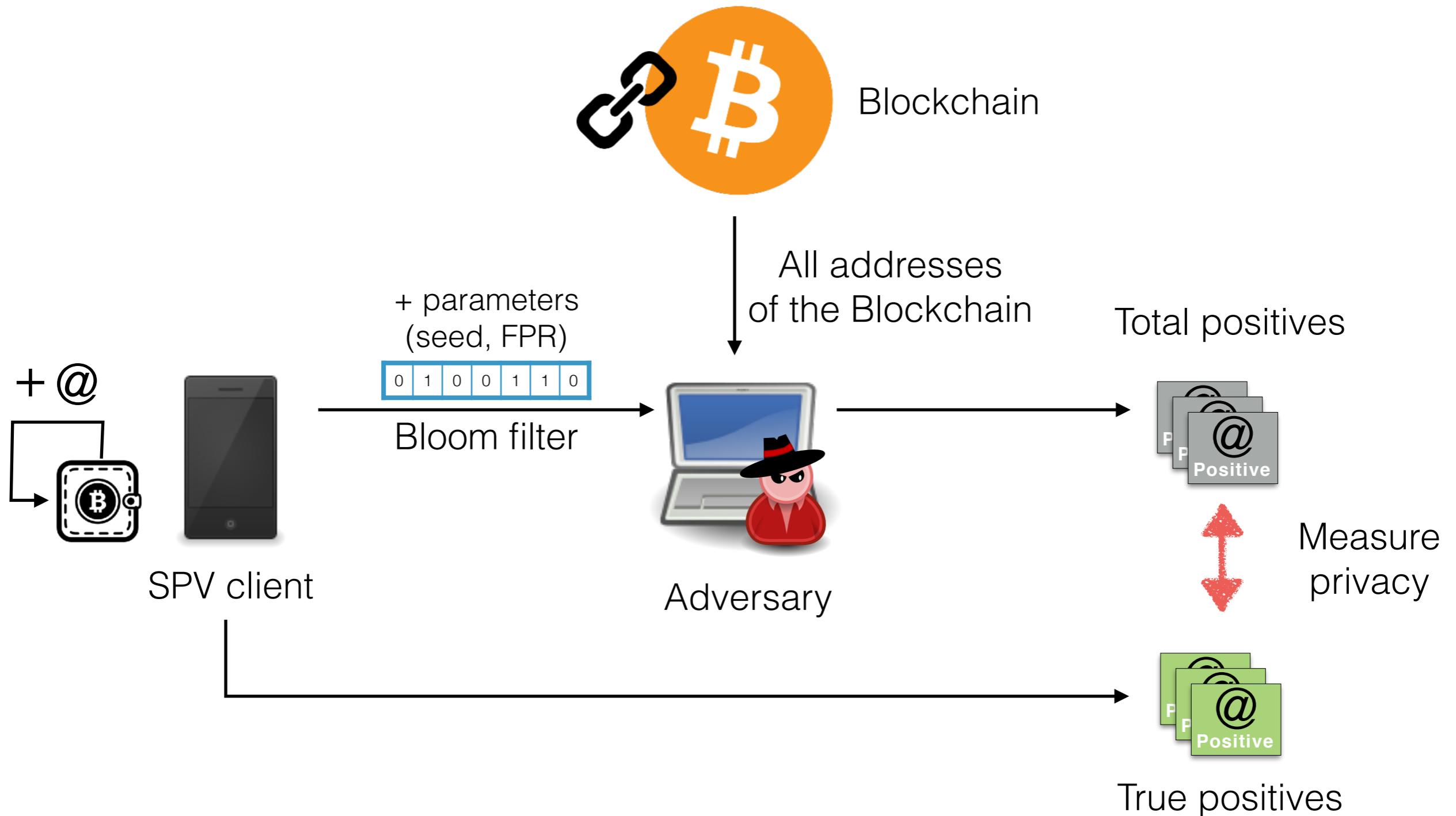
# Model and Privacy measure



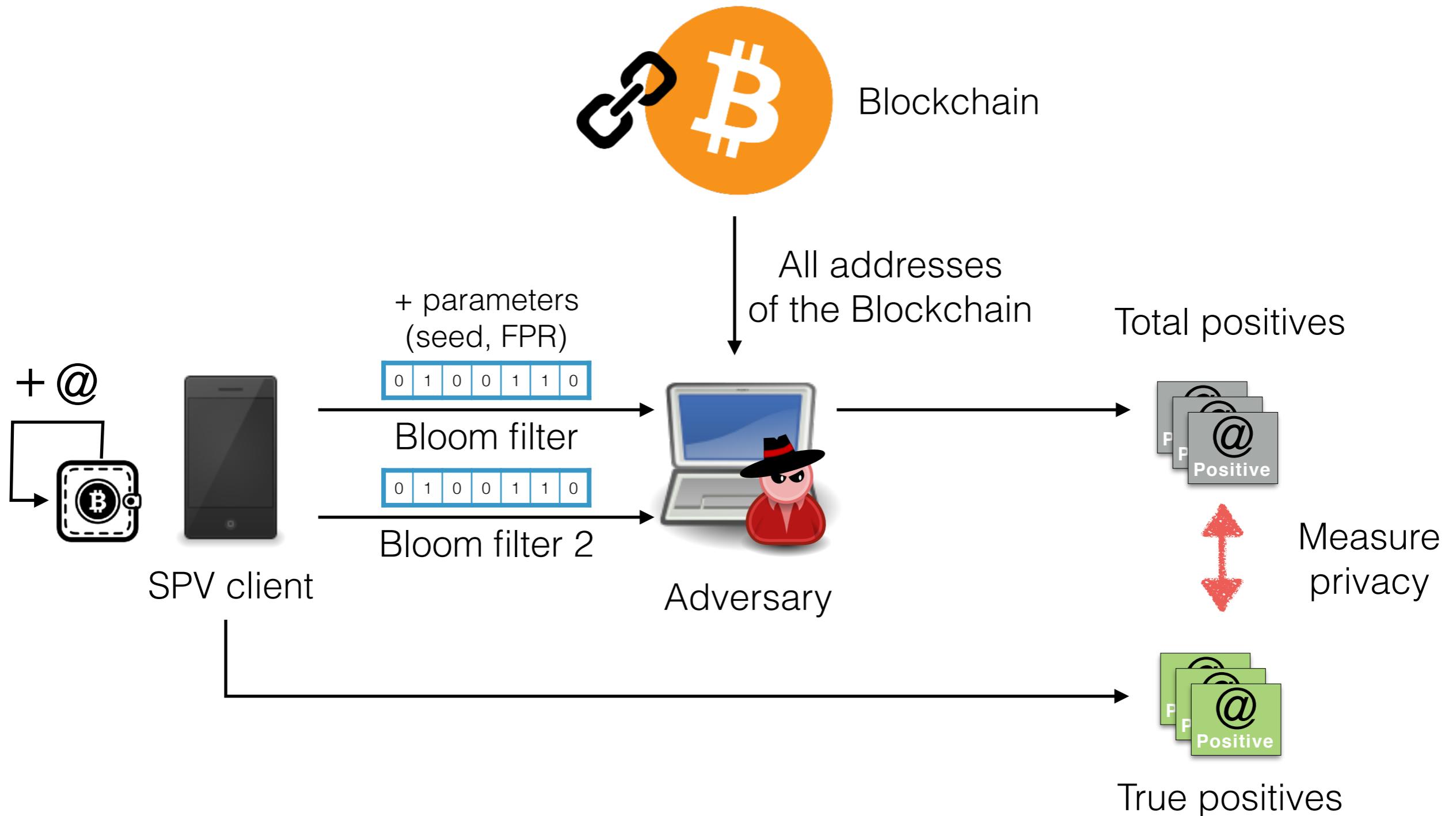
# Model and Privacy measure



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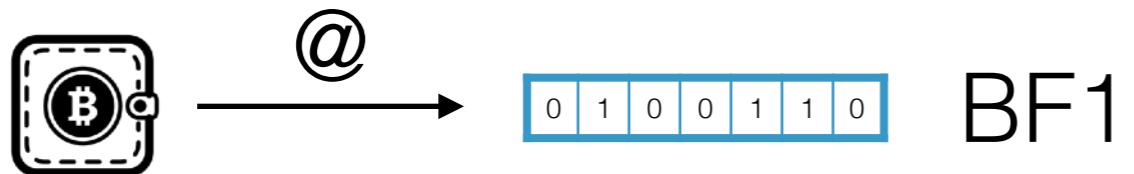
# Model and Privacy measure



## Stair stepping

Bloom filter designed for

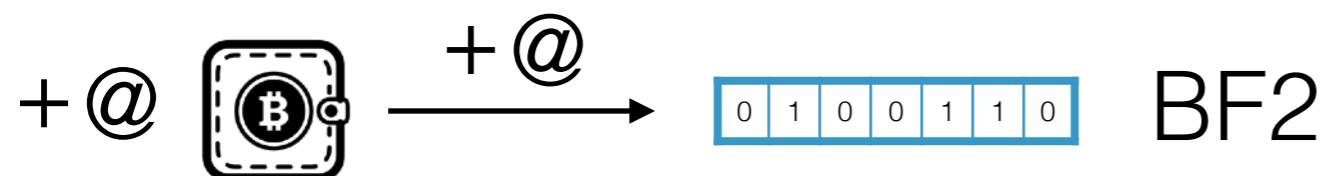
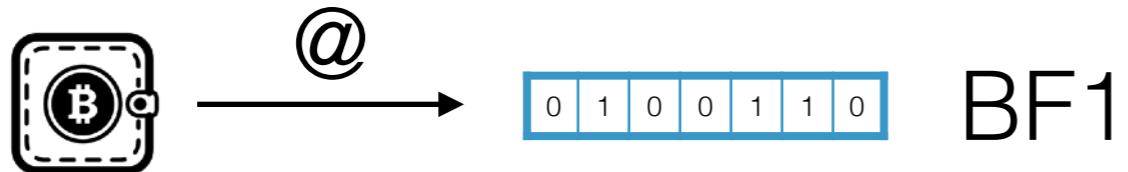
- max number of **addresses**
- **target FPR** when max addresses inserted



## Stair stepping

Bloom filter designed for

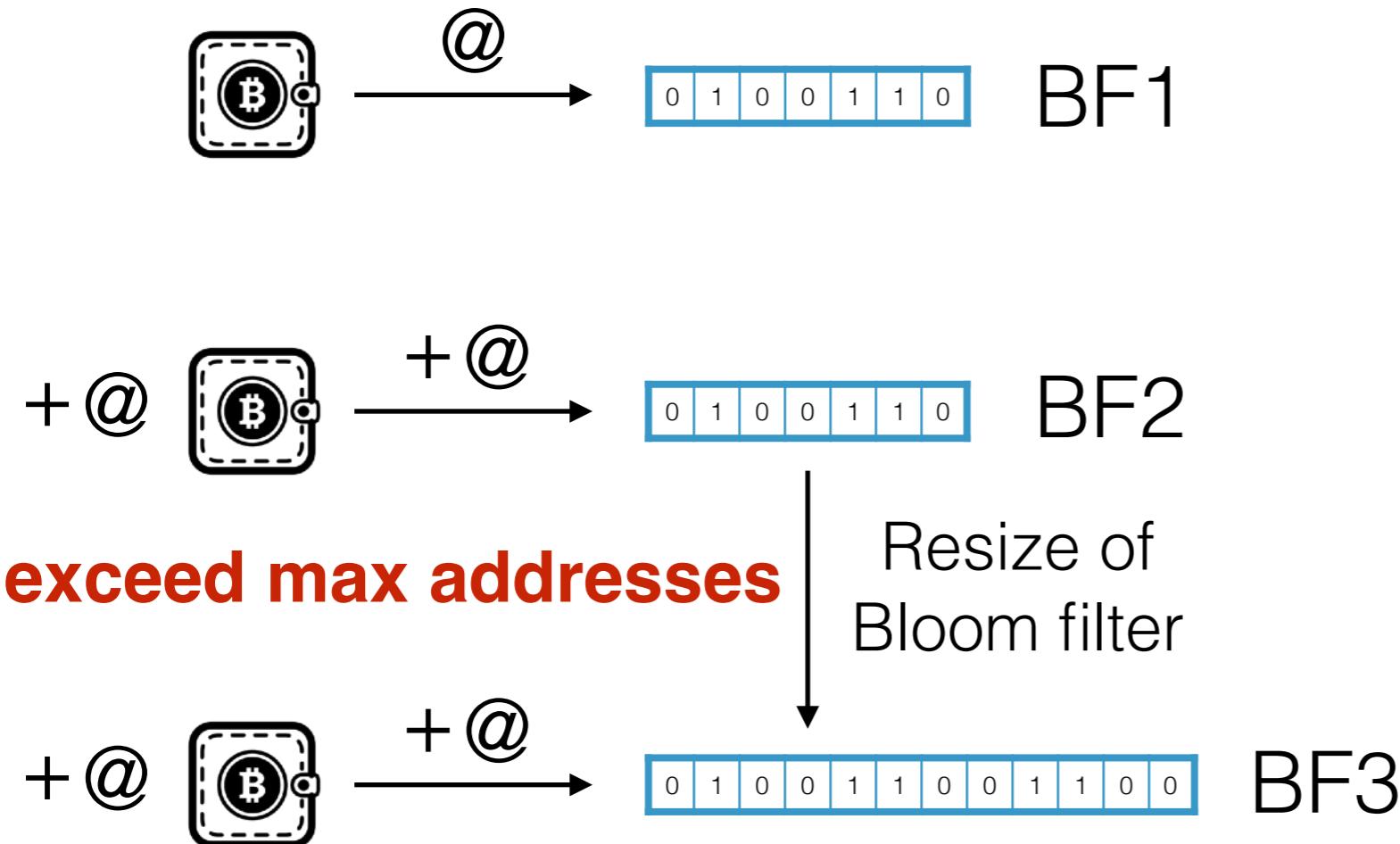
- max number of **addresses**
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# Stair stepping

Bloom filter designed for

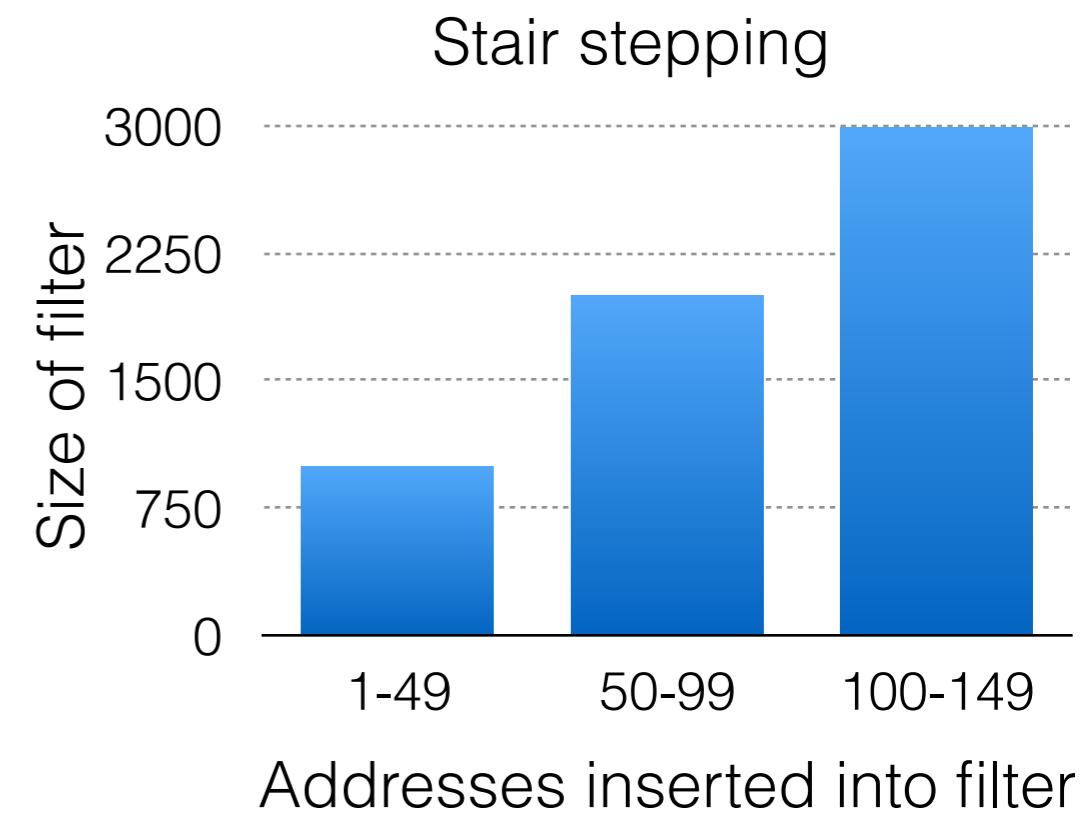
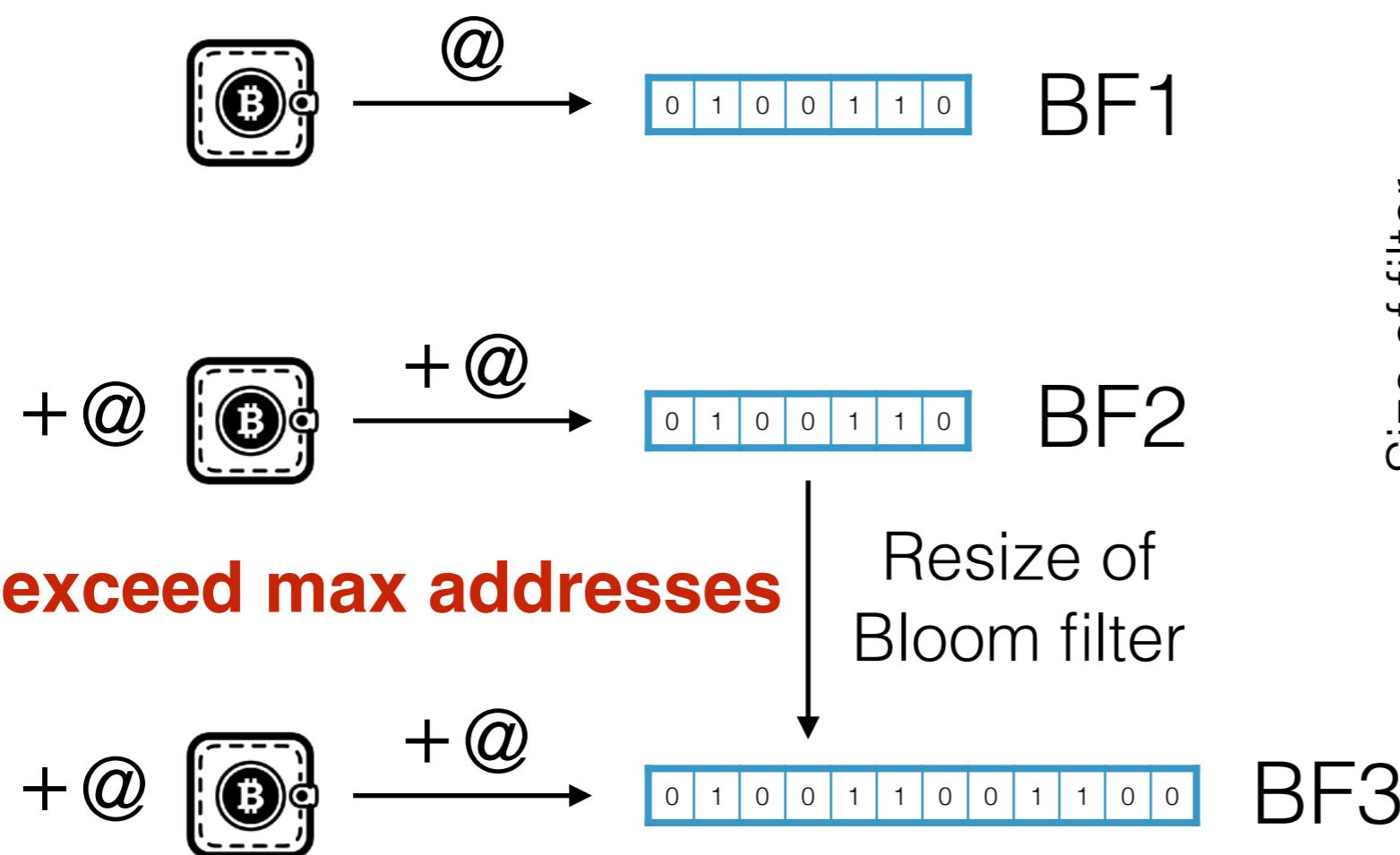
- max number of **addresses**
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# Stair stepping

Bloom filter designed for

- max number of **addresses**
- **target FPR** when max addresses inserted

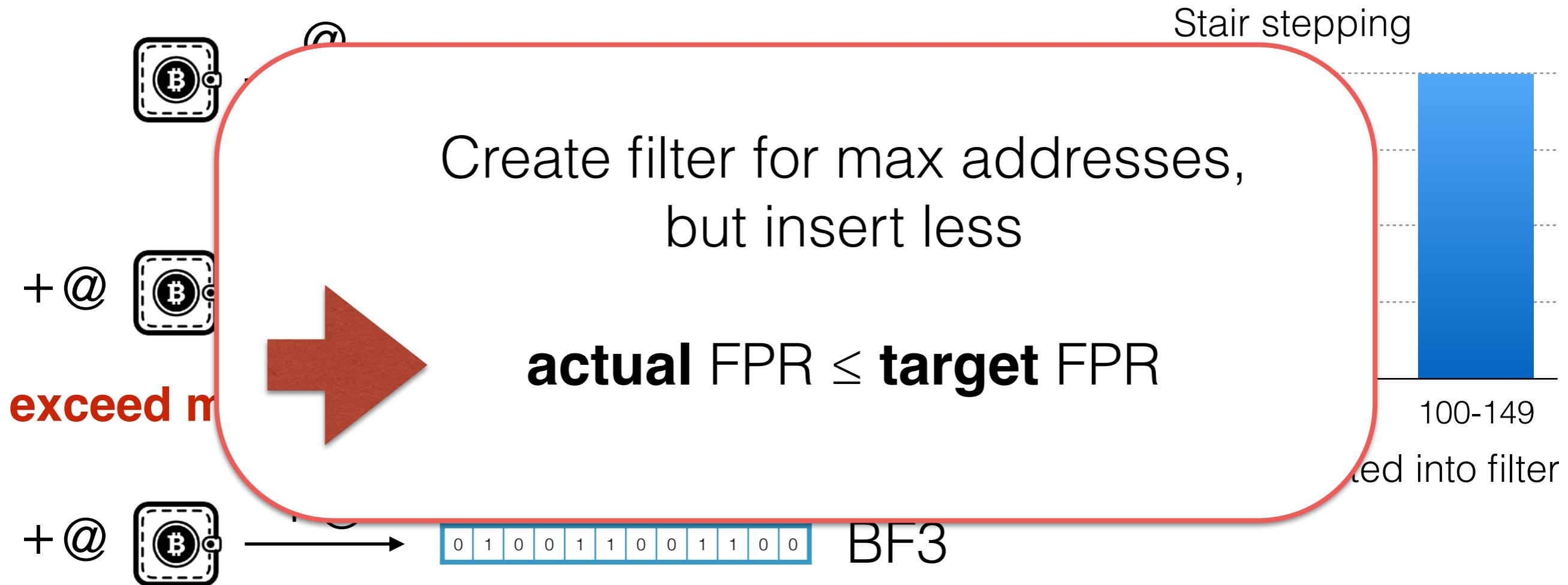


Rationale: **avoid** filters with different sizes

## Stair stepping

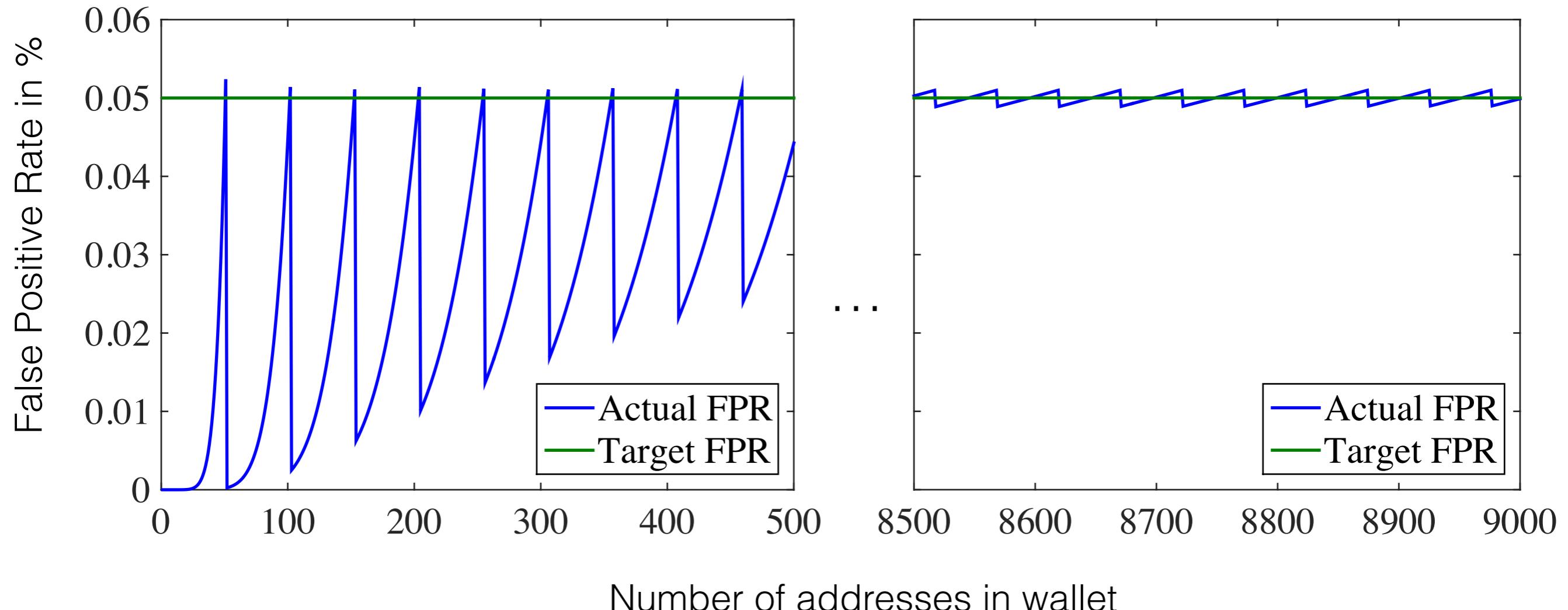
Bloom filter designed for

- max number of **addresses**
- **target FPR** when max addresses inserted

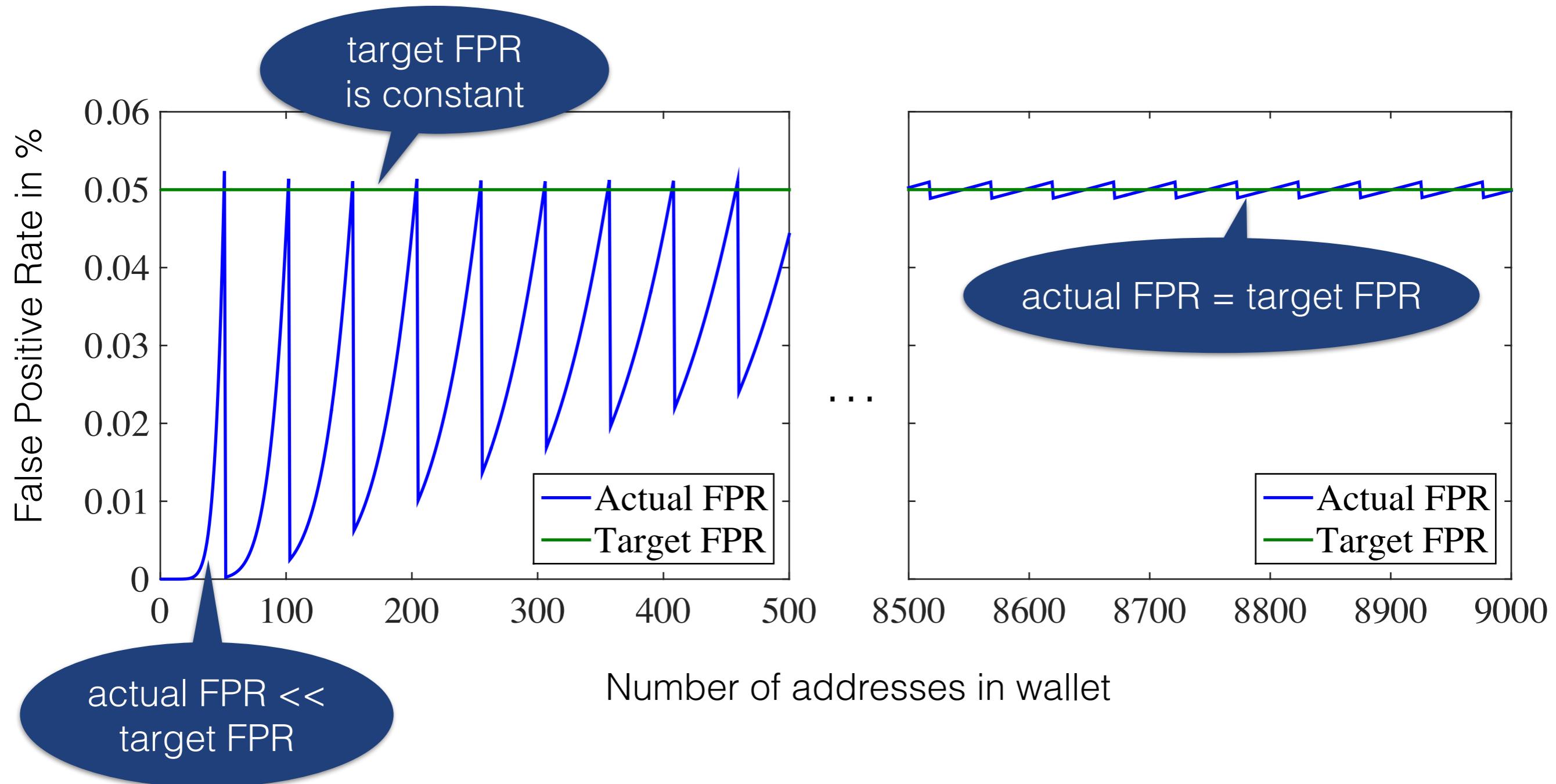


Rationale: **avoid** filters with different sizes

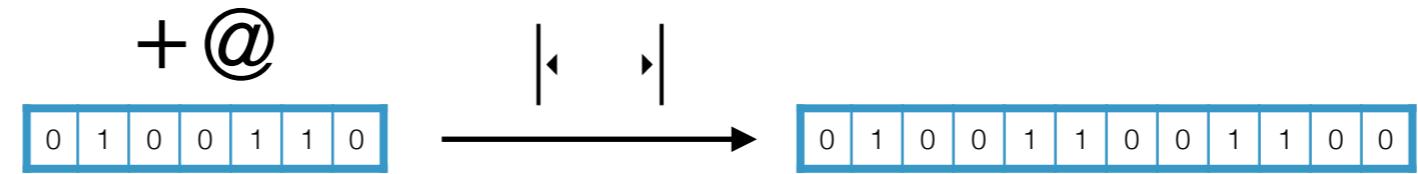
## Analytical results - Actual FPR vs. Target FPR



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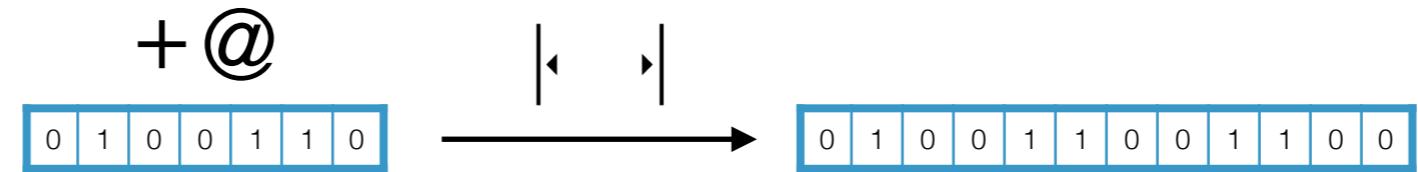
## Resizing



Once max addresses inserted —> bigger filter

- Hash functions adapted to fill space of new filter
- **Consequence:** New filter yields **different** false positives

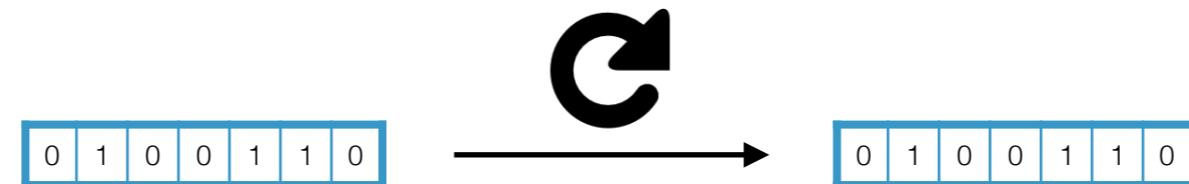
## Resizing



Once max addresses inserted → bigger filter

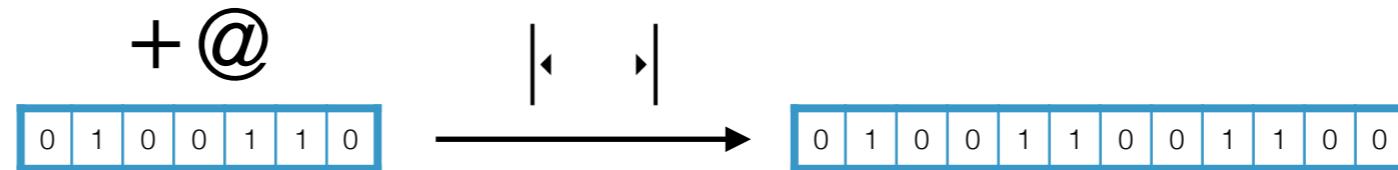
- Hash functions adapted to fill space of new filter
- **Consequence:** New filter yields **different** false positives

## Restarting



- Fresh seed value for hash functions of Bloom filter
- **Consequence:** New filter yields **different** false positives

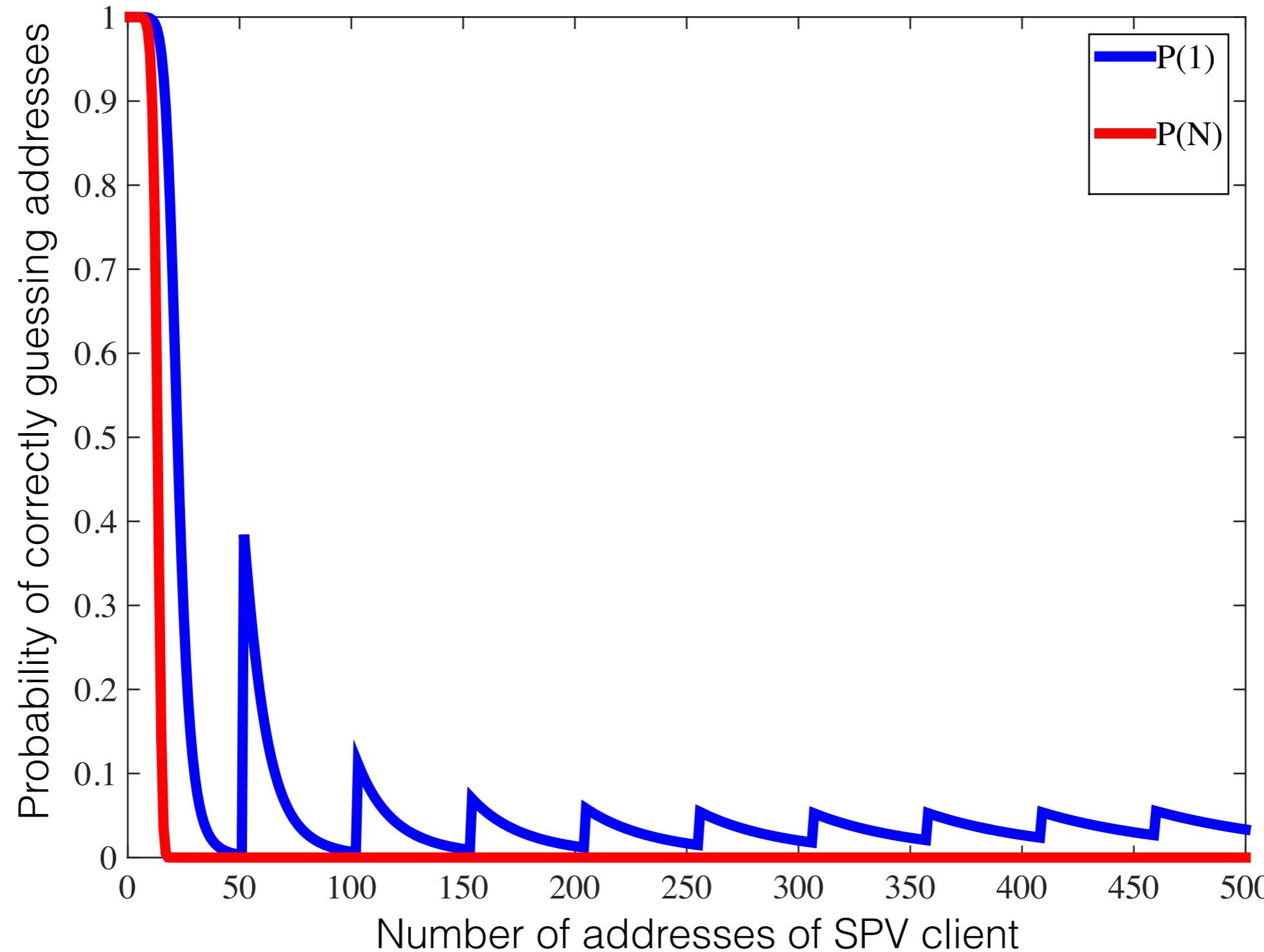
## Resizing



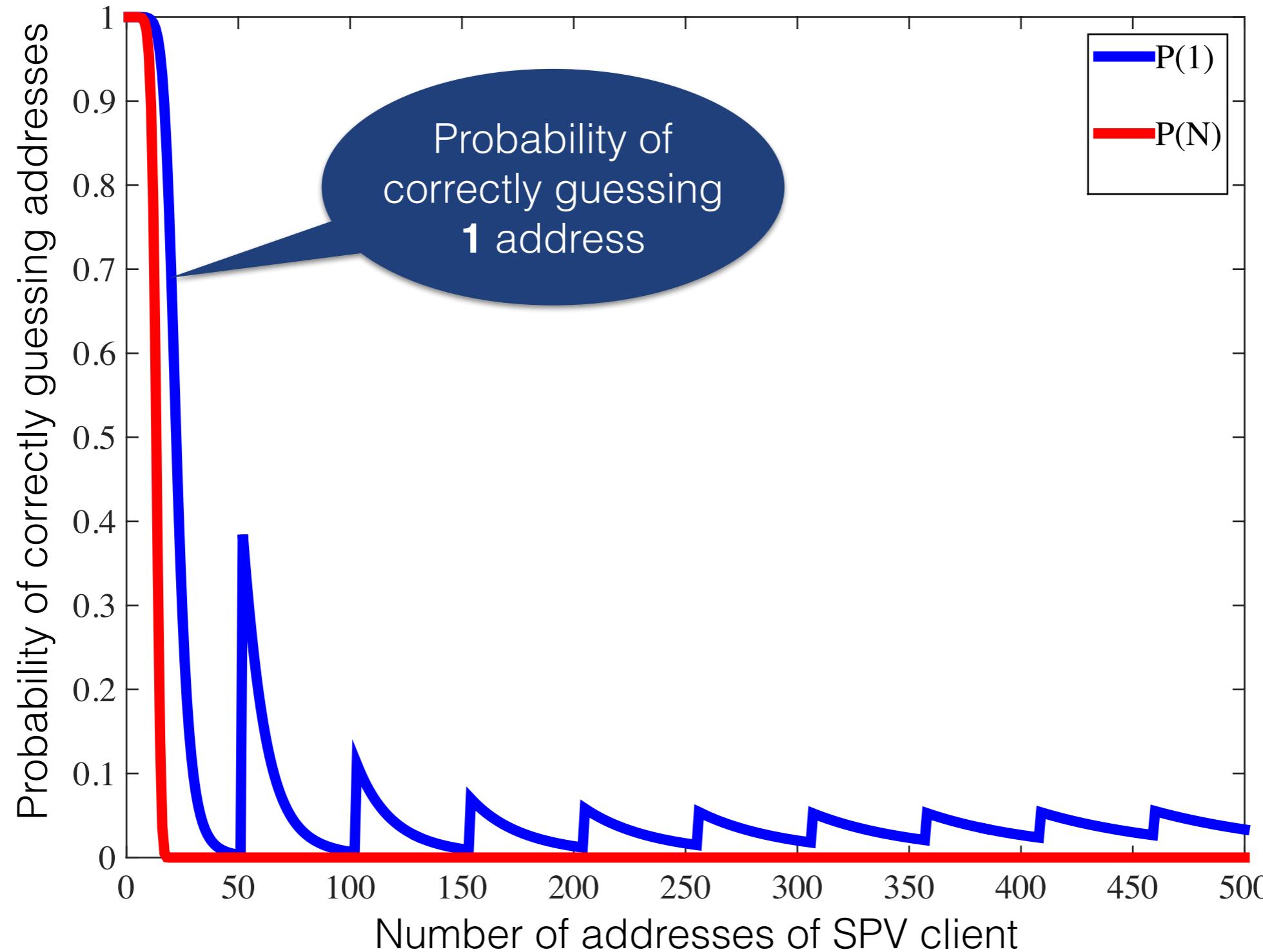
Once max addresses inserted → bigger filter

- Summary of current SPV design choices
- - 1. Stair stepping → actual FPR  $\leq$  target FPR
  - 2. Resizing → different False Positives
  - 3. Restarting → different False Positives
- **Consequence.** New filter yields **different** false positives

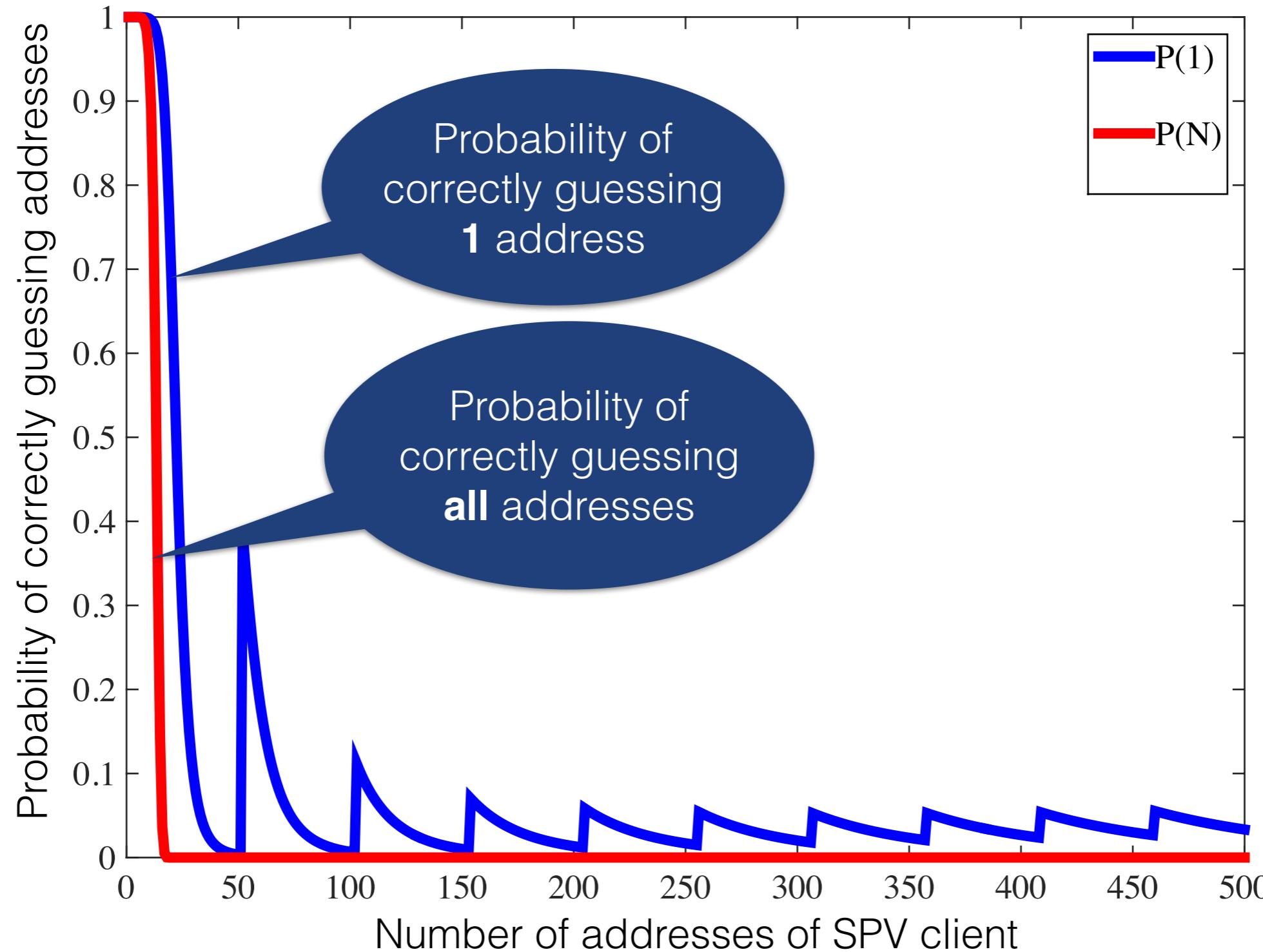
## One Bloom filter



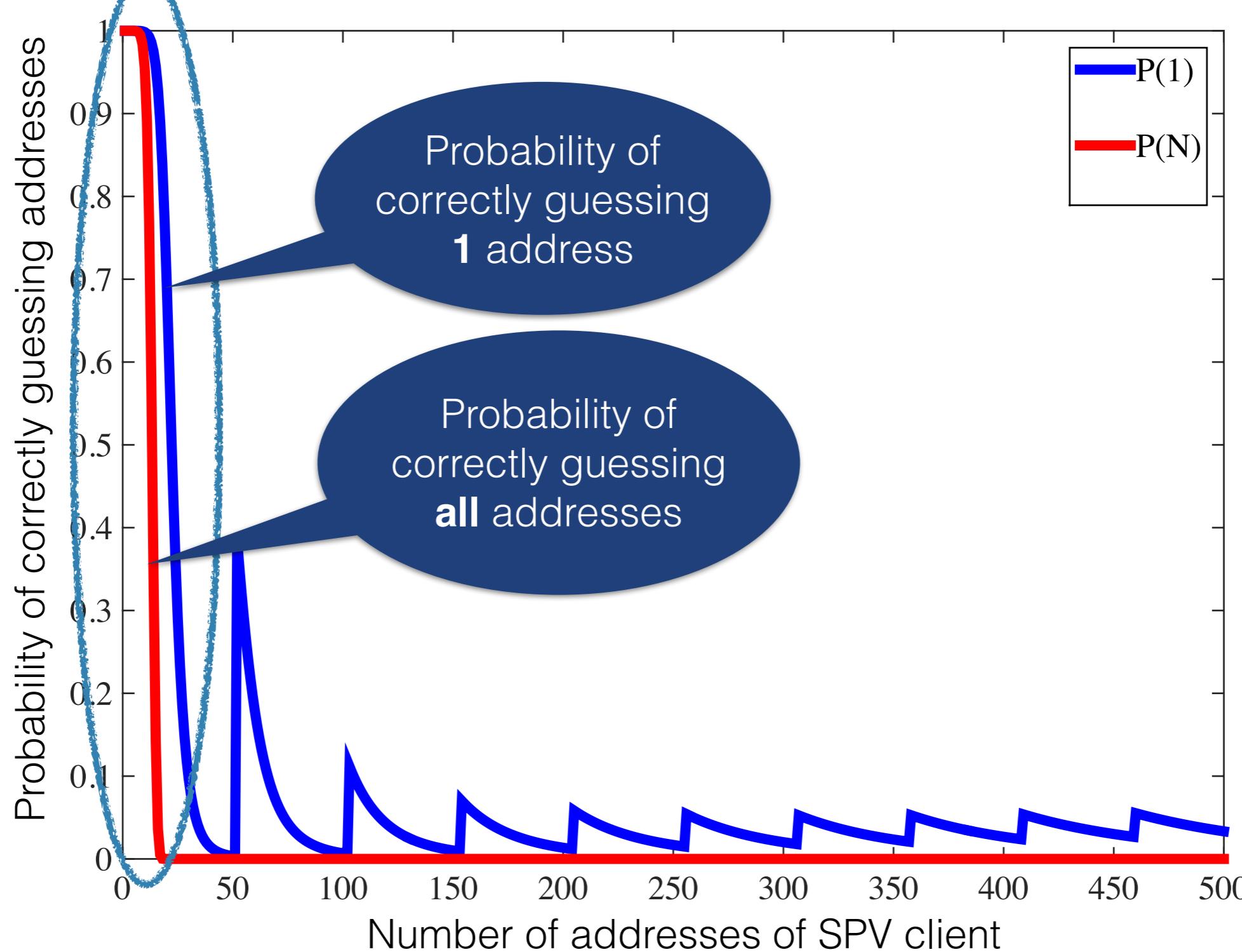
# One Bloom filter



# One Bloom filter



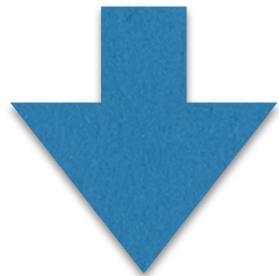
# One Bloom filter



# Multiple Bloom filters

Filter 1

0	1	0	0	1	1	0
---	---	---	---	---	---	---

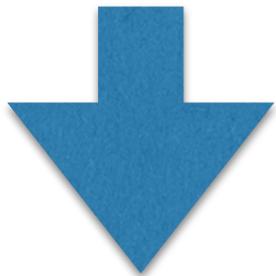


$\text{@}_1 \text{@}_2 \text{@}_3$

# Multiple Bloom filters

Filter 1

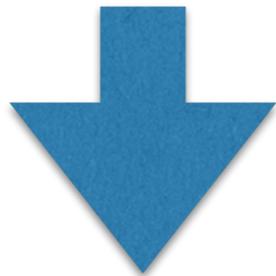
0	1	0	0	1	1	0
---	---	---	---	---	---	---



$\text{@}_1 \text{@}_2 \text{@}_3$

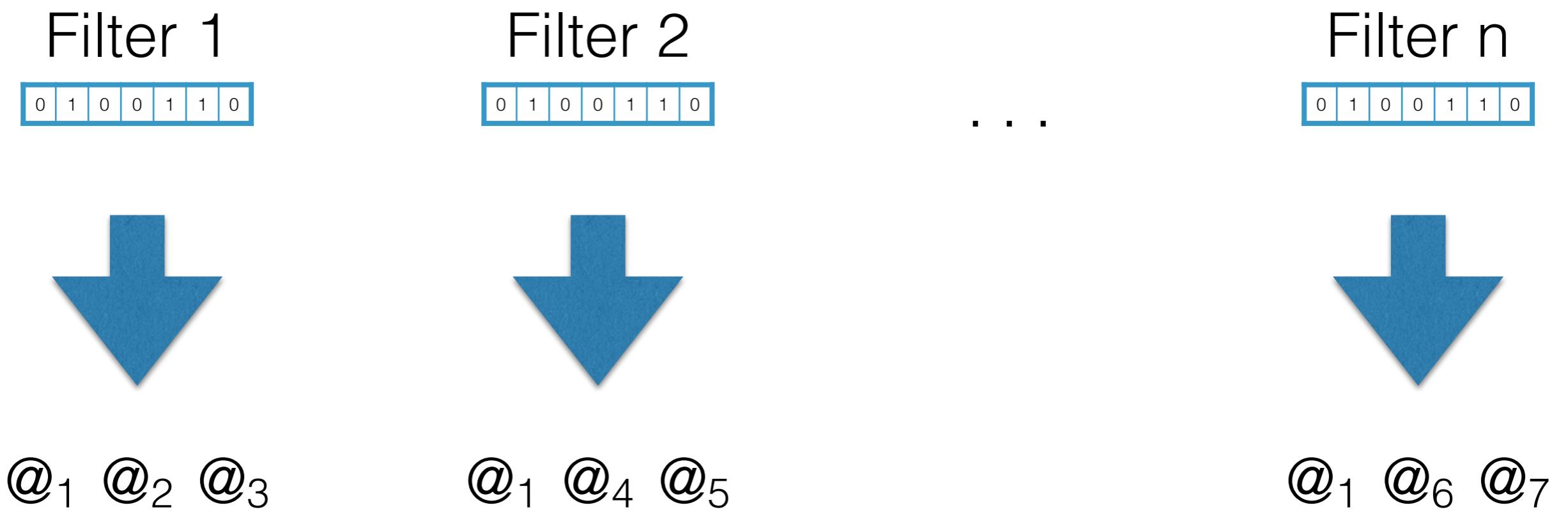
Filter 2

0	1	0	0	1	1	0
---	---	---	---	---	---	---

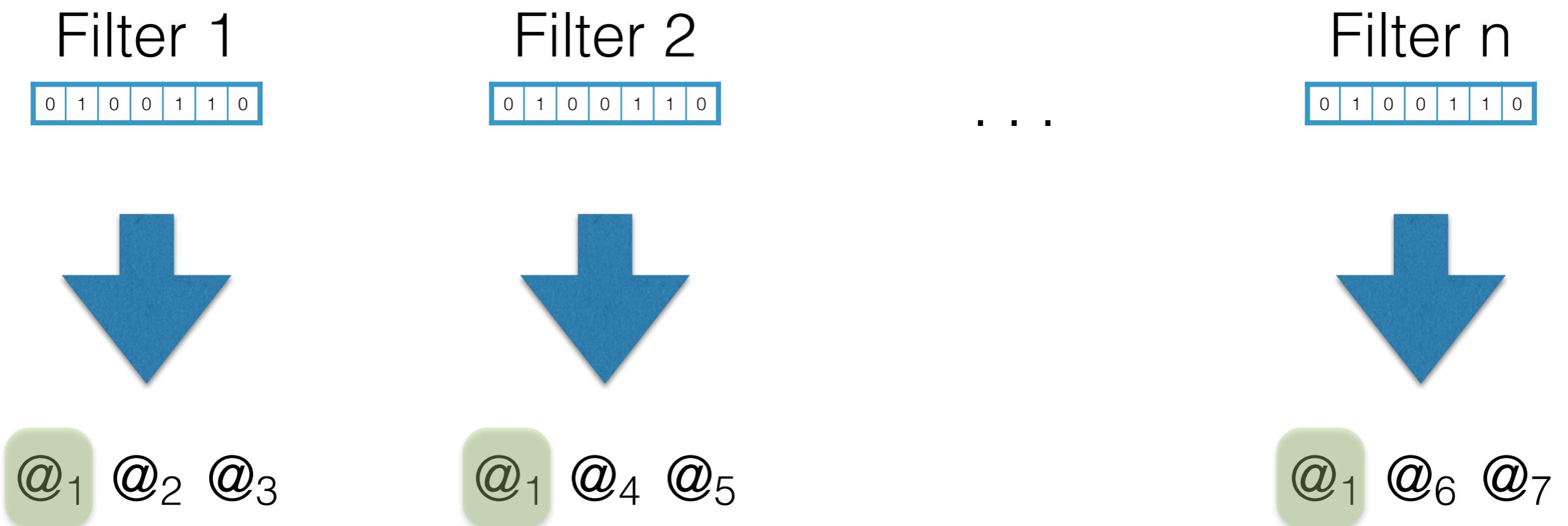


$\text{@}_1 \text{@}_4 \text{@}_5$

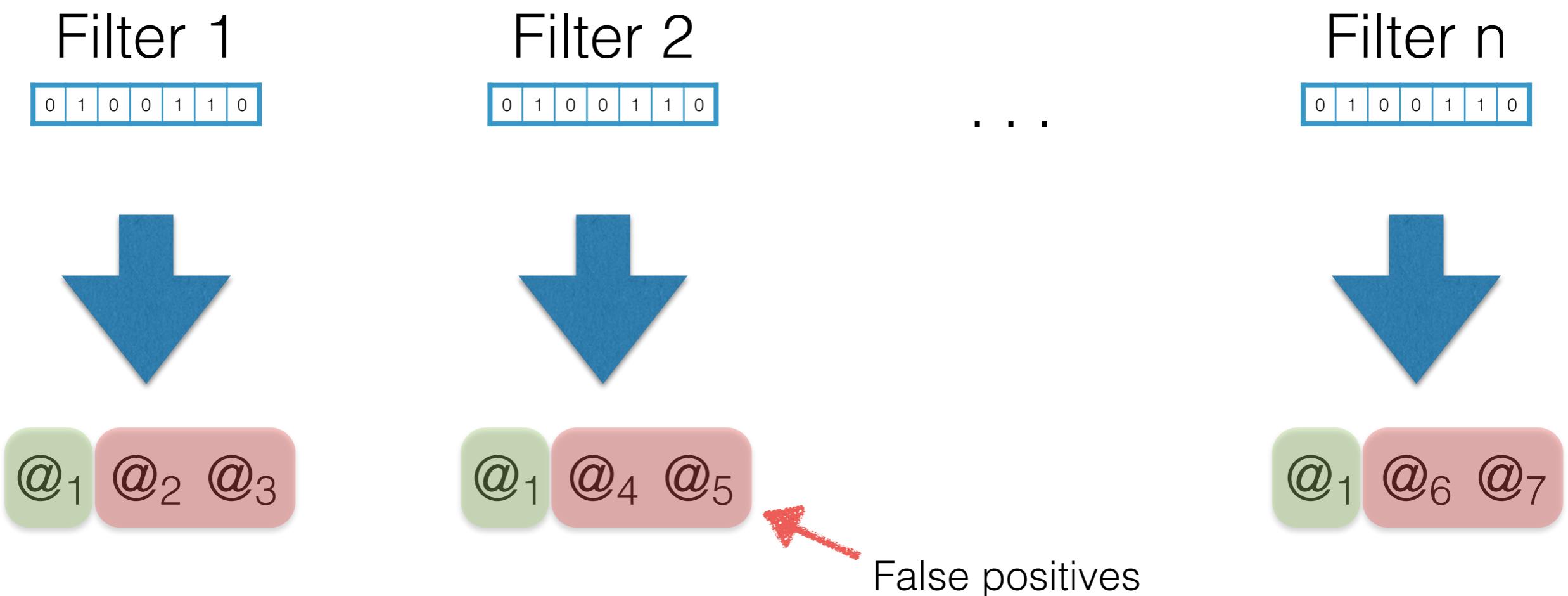
# Multiple Bloom filters



# Multiple Bloom filters



# Multiple Bloom filters



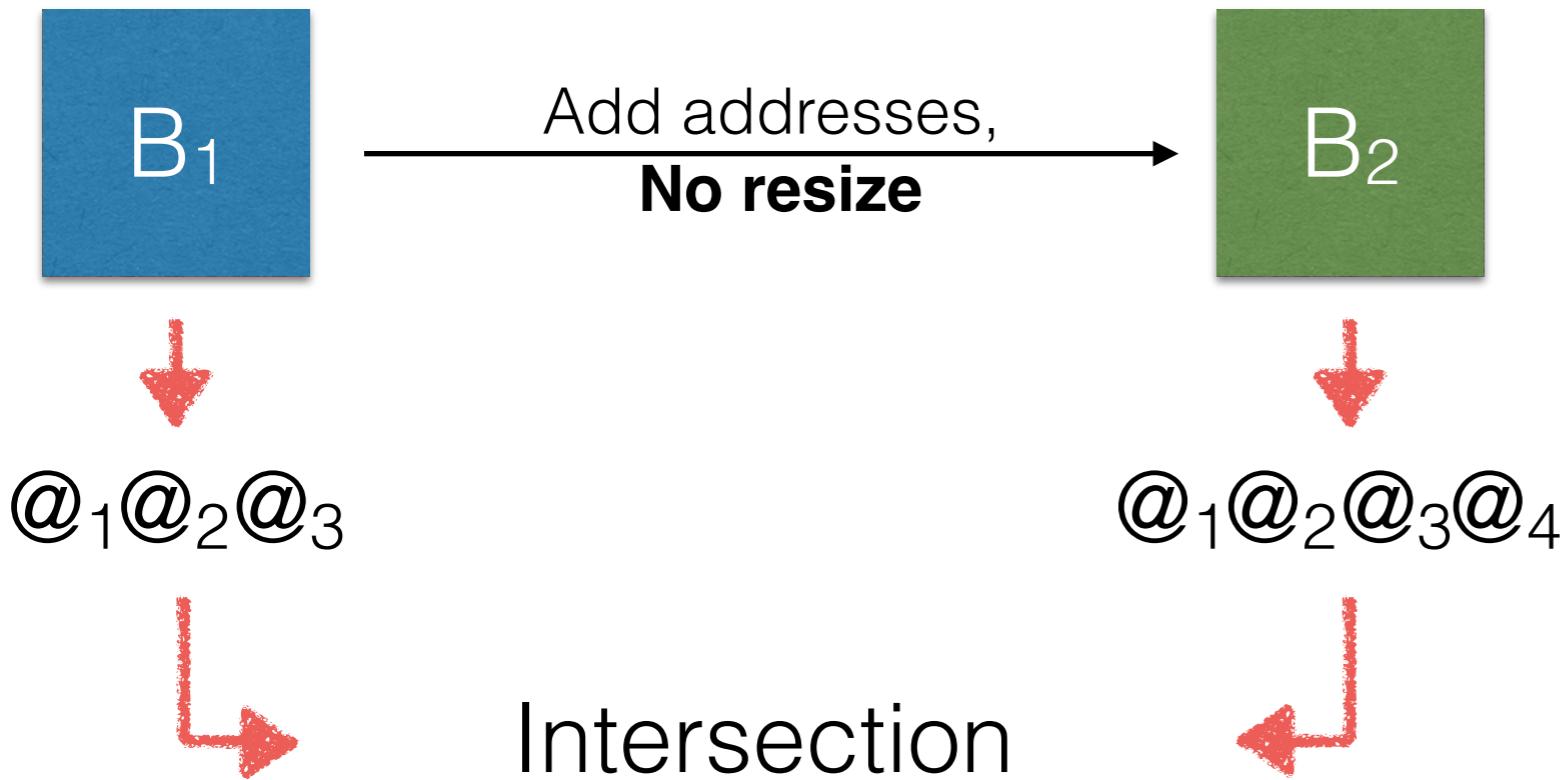
## Experiment 1 - No resize ~~1~~

Exp.	Client	Seed	Size
<b>No resize</b>	<b>Same</b>	<b>Same</b>	<b>Same</b>
<b>Resize</b>	Same	Same	Different
<b>Restart</b>	Same	Different	Same
<b>&gt; 2 filter</b>	Same	Different	Different

## Experiment 1 - No resize ~~↓↓~~

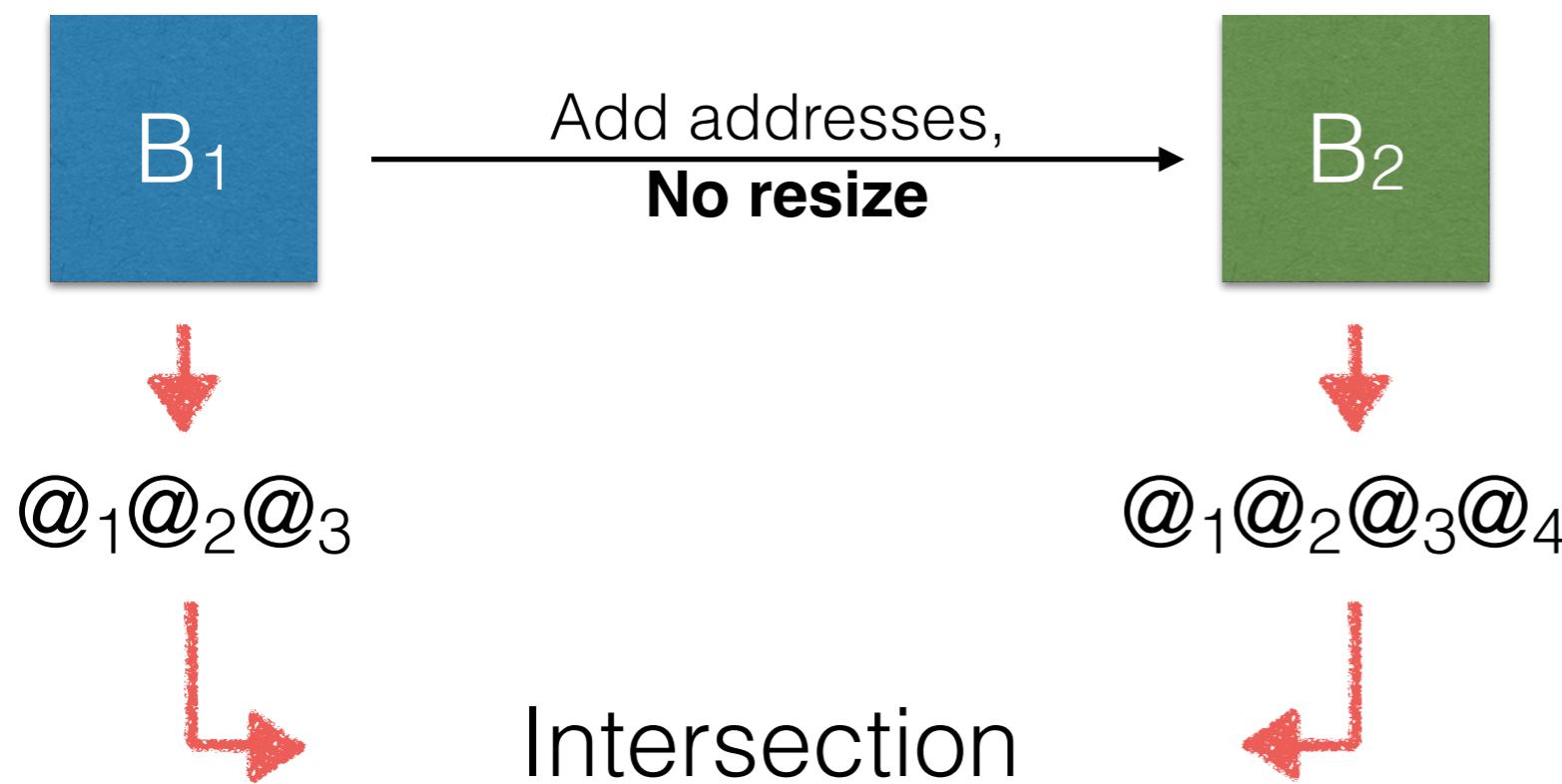
Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

## Experiment 1 - No resize ~~1~~



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<b>No resize</b>	<b>Same</b>	<b>Same</b>	<b>Same</b>
<b>Resize</b>	Same	Same	Different
<b>Restart</b>	Same	Different	Same
<b>&gt; 2 filter</b>	Same	Different	Different

## Experiment 1 - No resize

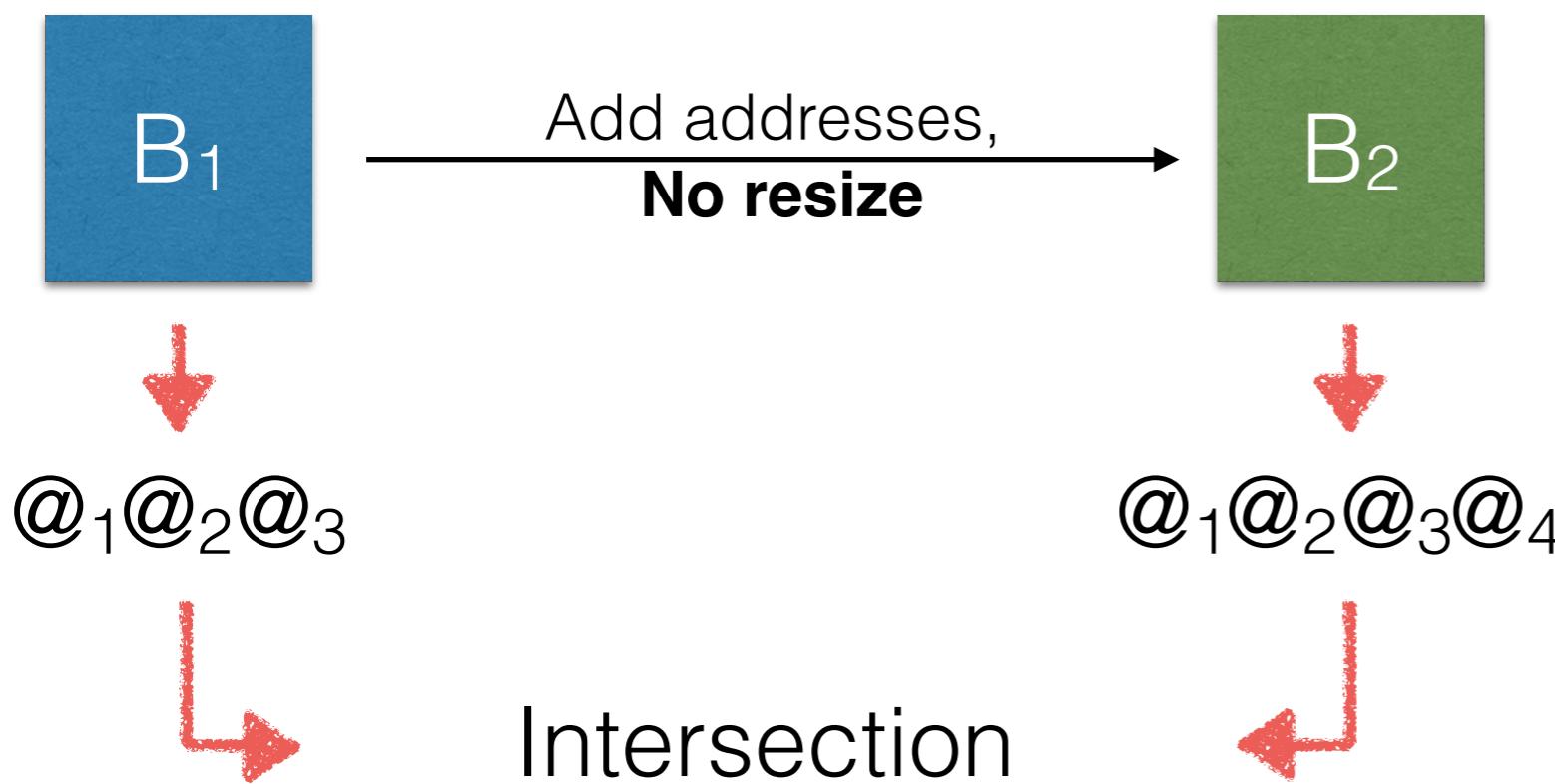


## Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.05	0.2990	0.2910
0.1	0.1020	0.1070
0.5	0.0078	0.0075

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

# Experiment 1 - No resize

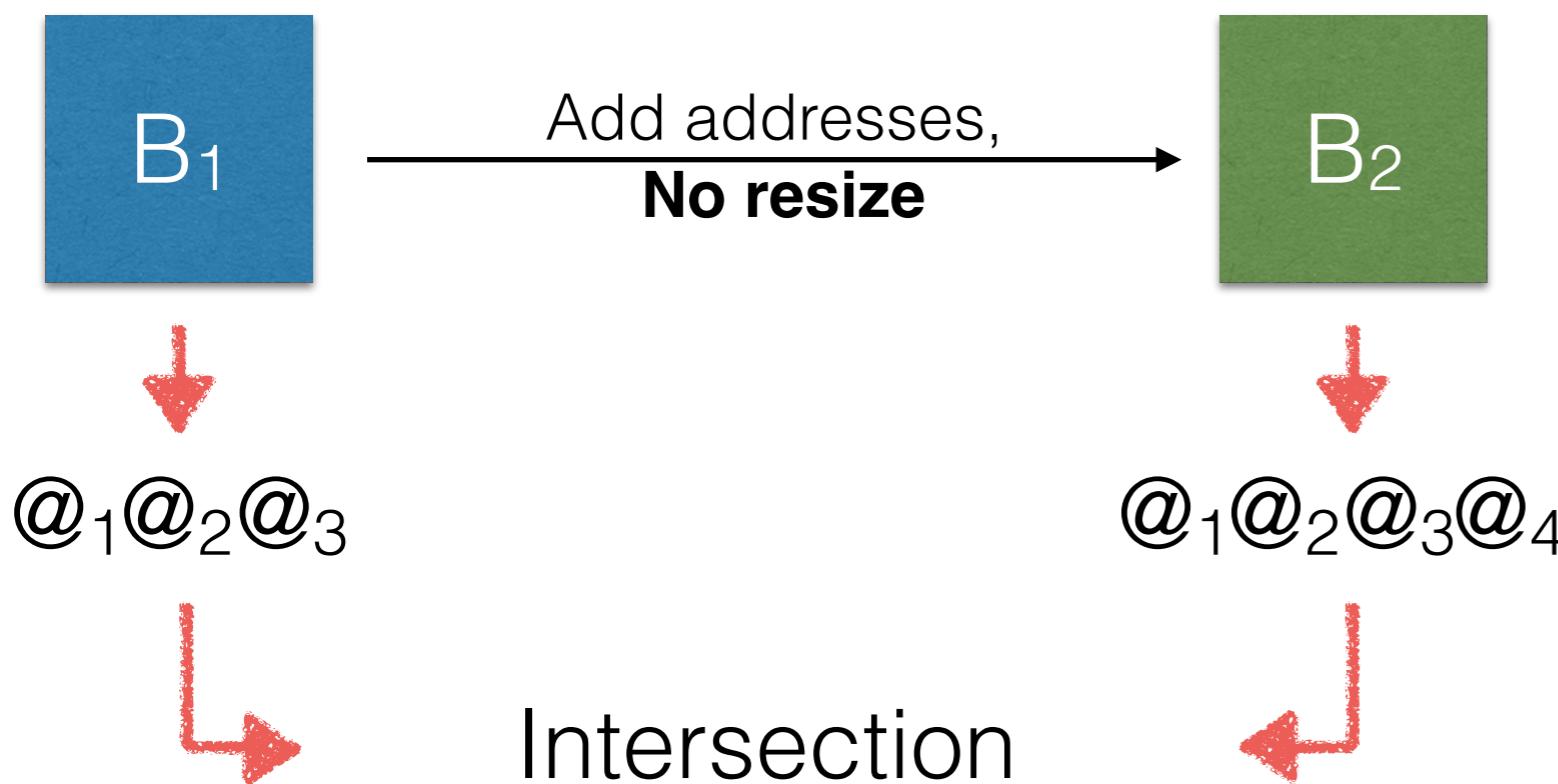


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<b>Resize</b>	Same	Same	Different
<b>Restart</b>	Same	Different	Same
<b>&gt; 2 filter</b>	Same	Different	Different

# Experiment 1 - No resize

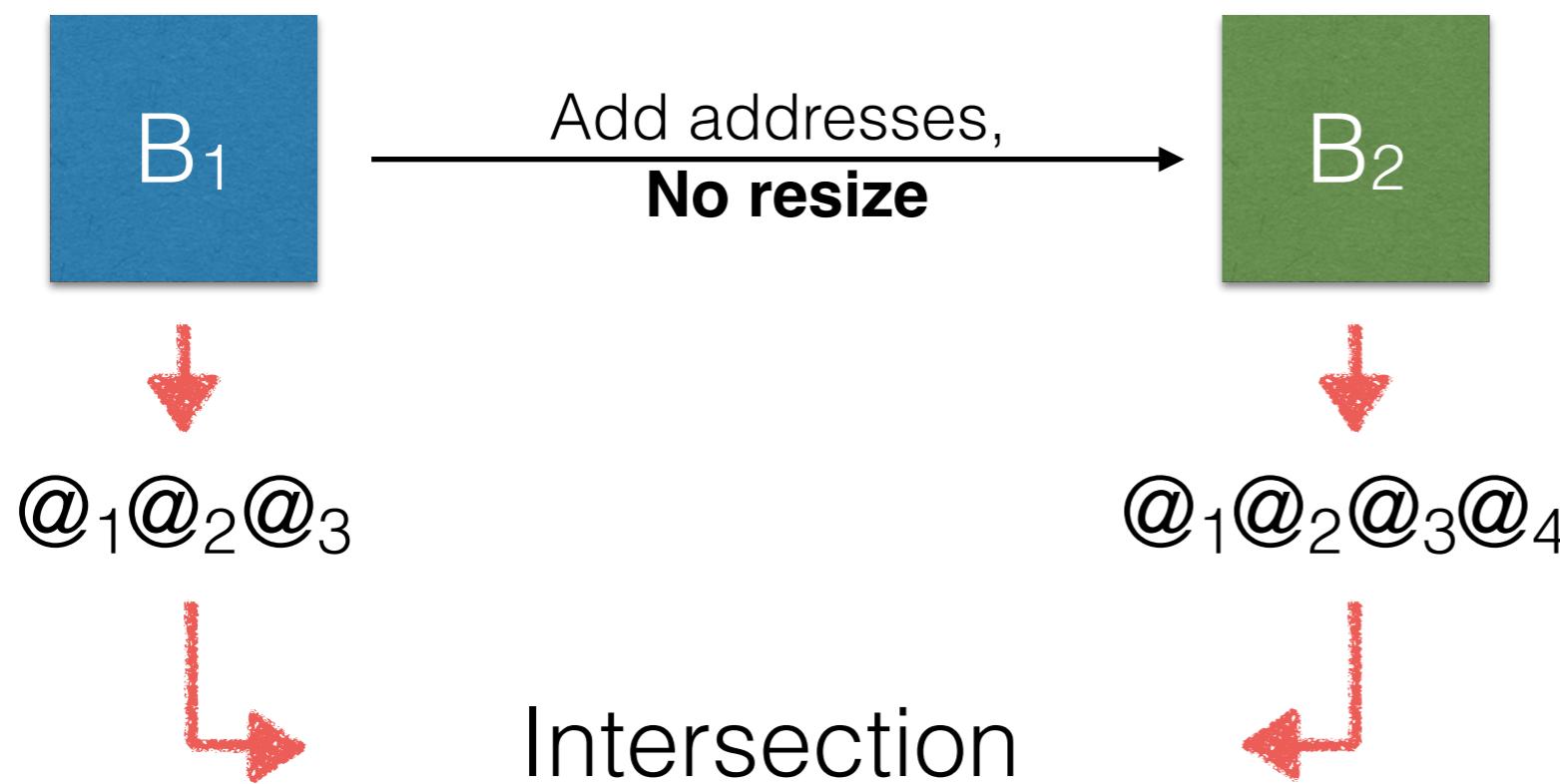


## Results

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Exp.	Client	Seed	Size
<b>No resize</b>	<b>Same</b>	<b>Same</b>	<b>Same</b>
<b>Resize</b>	Same	Same	Different
<b>Restart</b>	Same	Different	Same
<b>&gt; 2 filter</b>	Same	Different	Different

# Experiment 1 - No resize



## Results

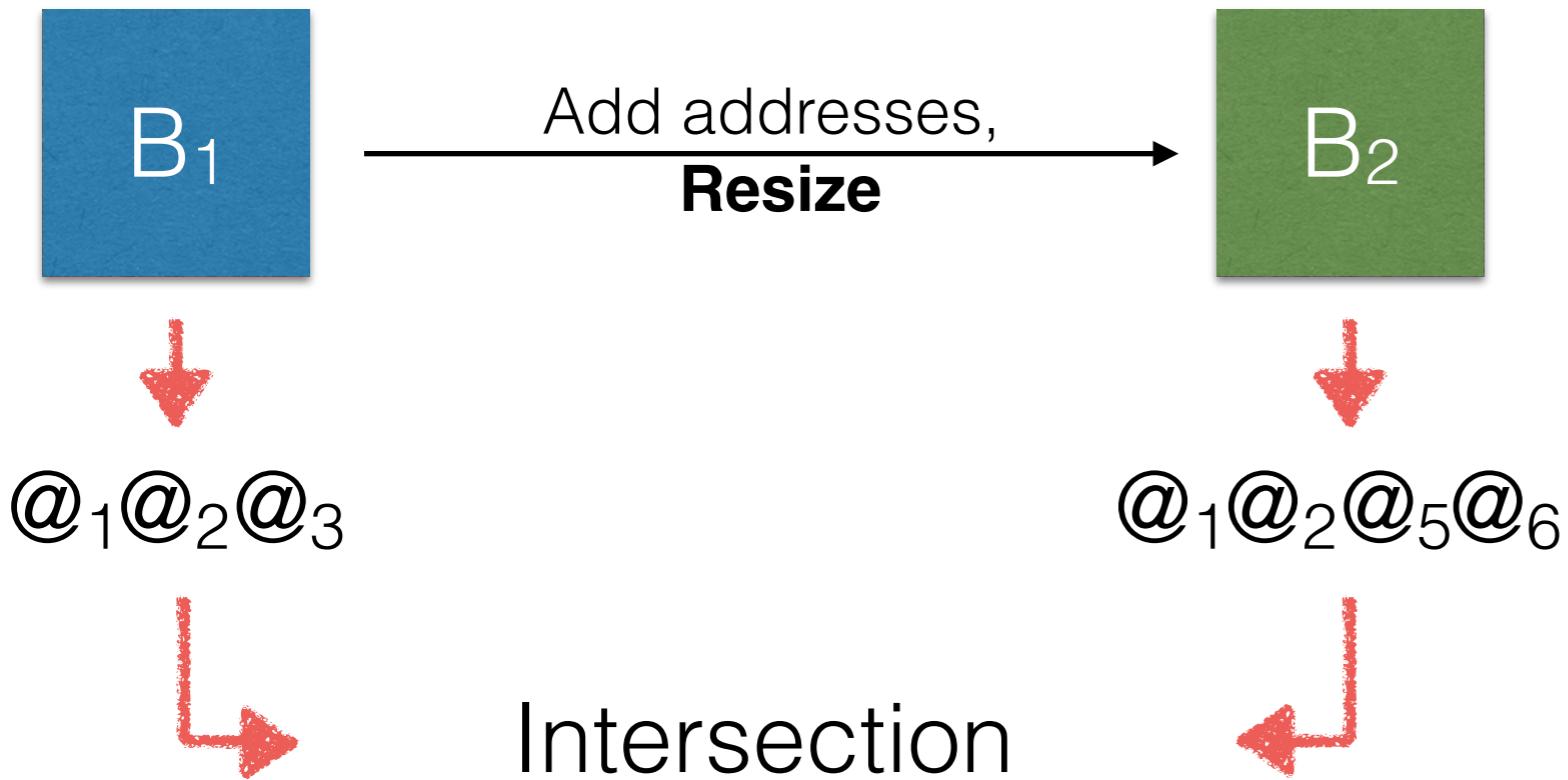
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0.05	0.2990	0.2910
0.1	0.1020	0.1070
0.5	0.0078	0.0075

no change of privacy

Exp.	Client	Seed	Size
<b>No resize</b>	<b>Same</b>	<b>Same</b>	<b>Same</b>
<b>Resize</b>	Same	Same	Different
<b>Restart</b>	Same	Different	Same
<b>&gt; 2 filter</b>	Same	Different	Different

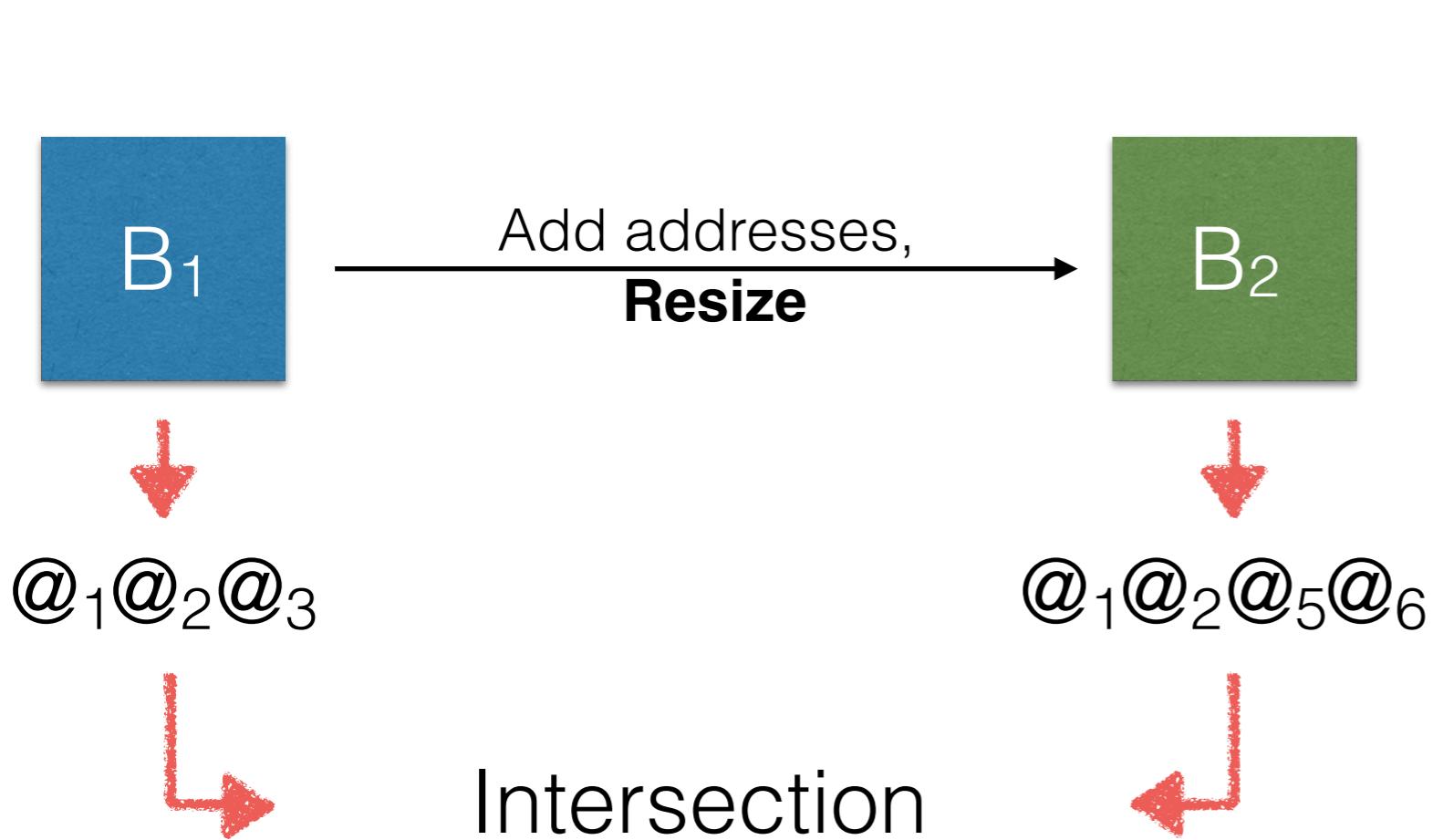
- Yield the same positives
- The adversary does not learn a lot

## Experiment 2 - Resize ↪ ↪



Exp.	Client	Seed	Size
No resize	Same	Same	Same
<b>Resize</b>	<b>Same</b>	<b>Same</b>	<b>Different</b>
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

# Experiment 2 - Resize ↶ ↷

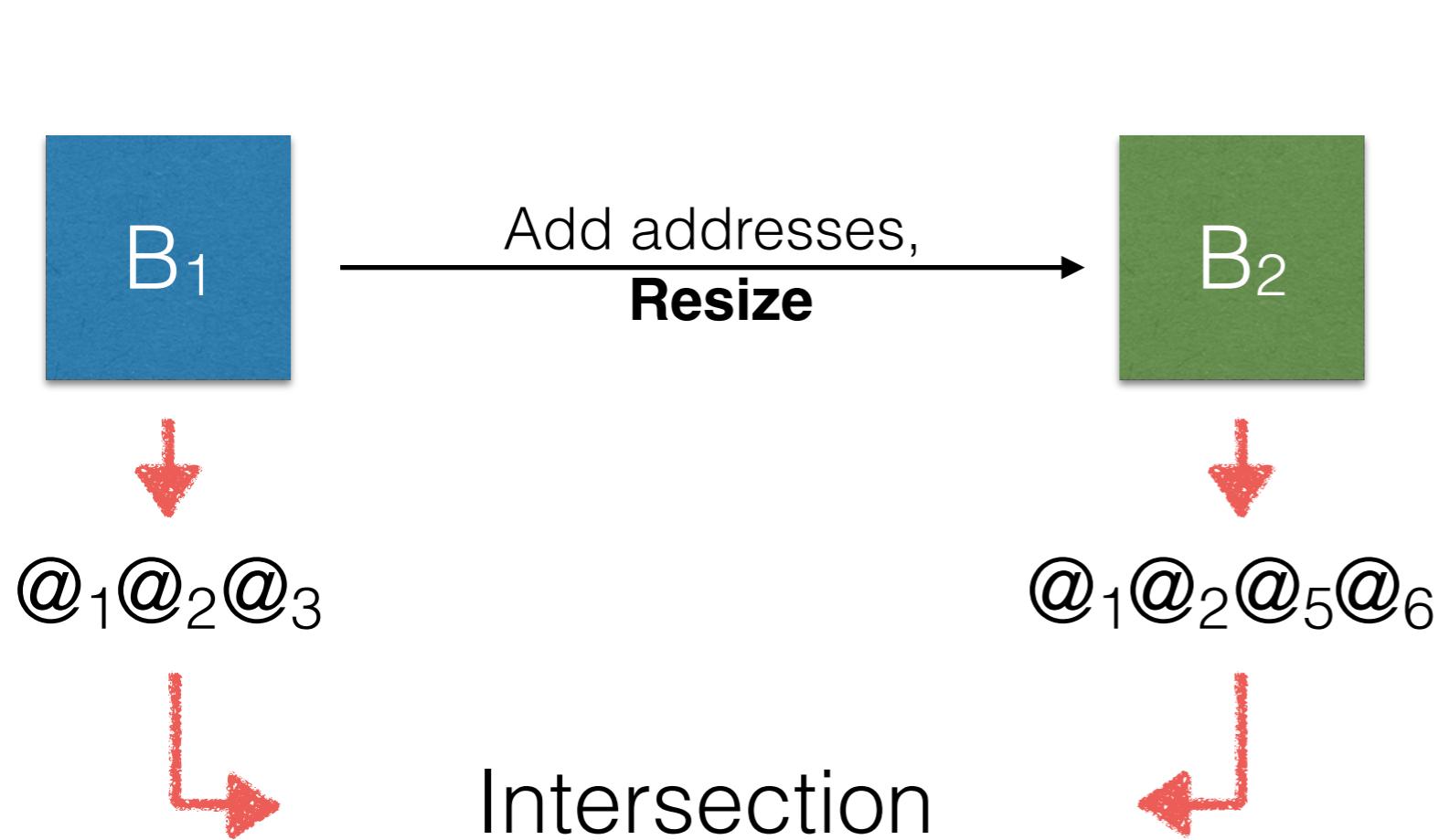


Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.98	0.03

Exp.	Client	Seed	Size
No resize	Same	Same	Same
<b><u>Resize</u></b>	<b>Same</b>	<b>Same</b>	<b>Different</b>
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

# Experiment 2 - Resize ↶ ◻

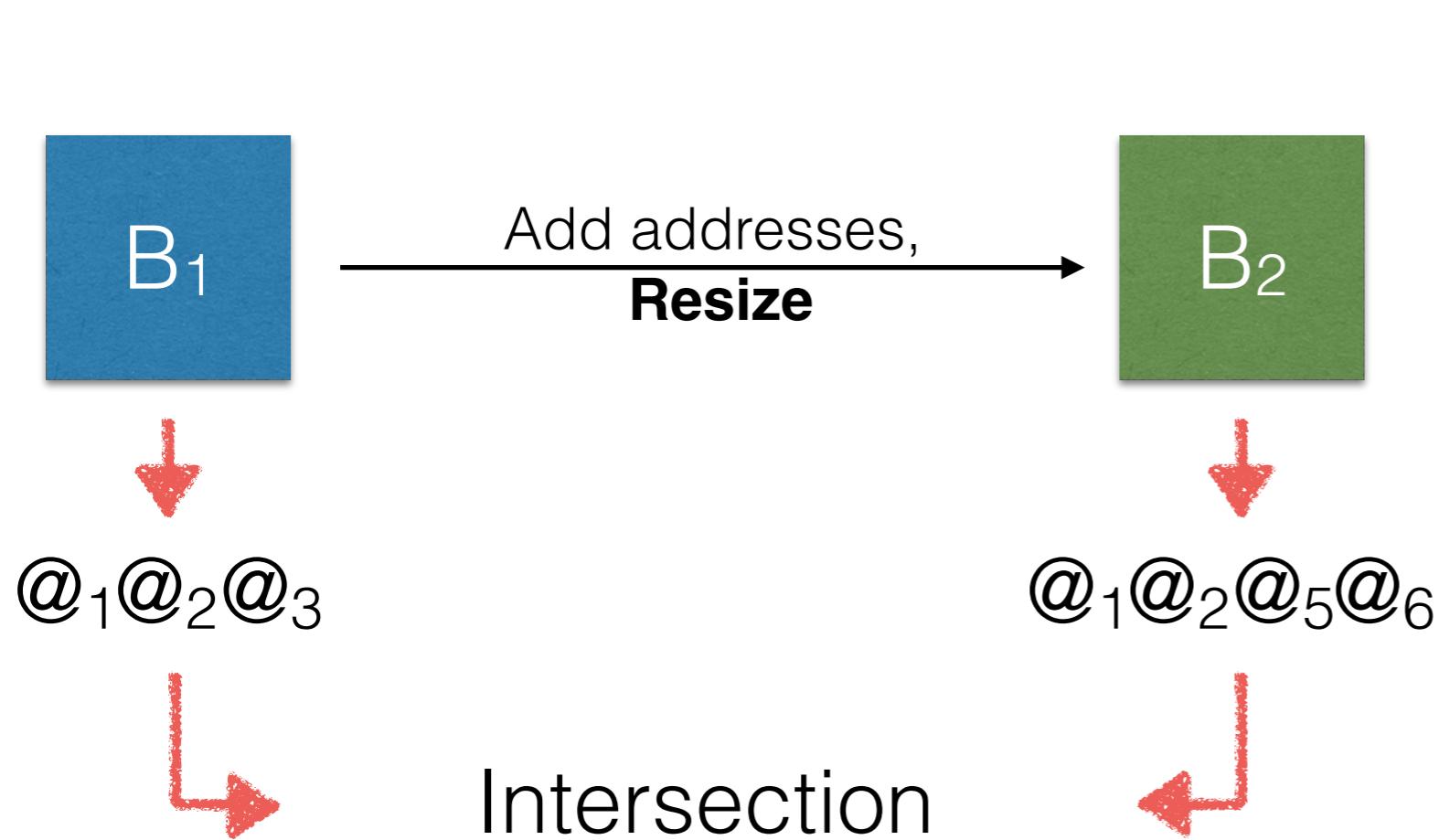


Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.98	0.03

Exp.	Client	Seed	Size
No resize	Same	Same	Same
<u>Resize</u>	<b>Same</b>	<b>Same</b>	<b>Different</b>
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

# Experiment 2 - Resize | ↻ ↺

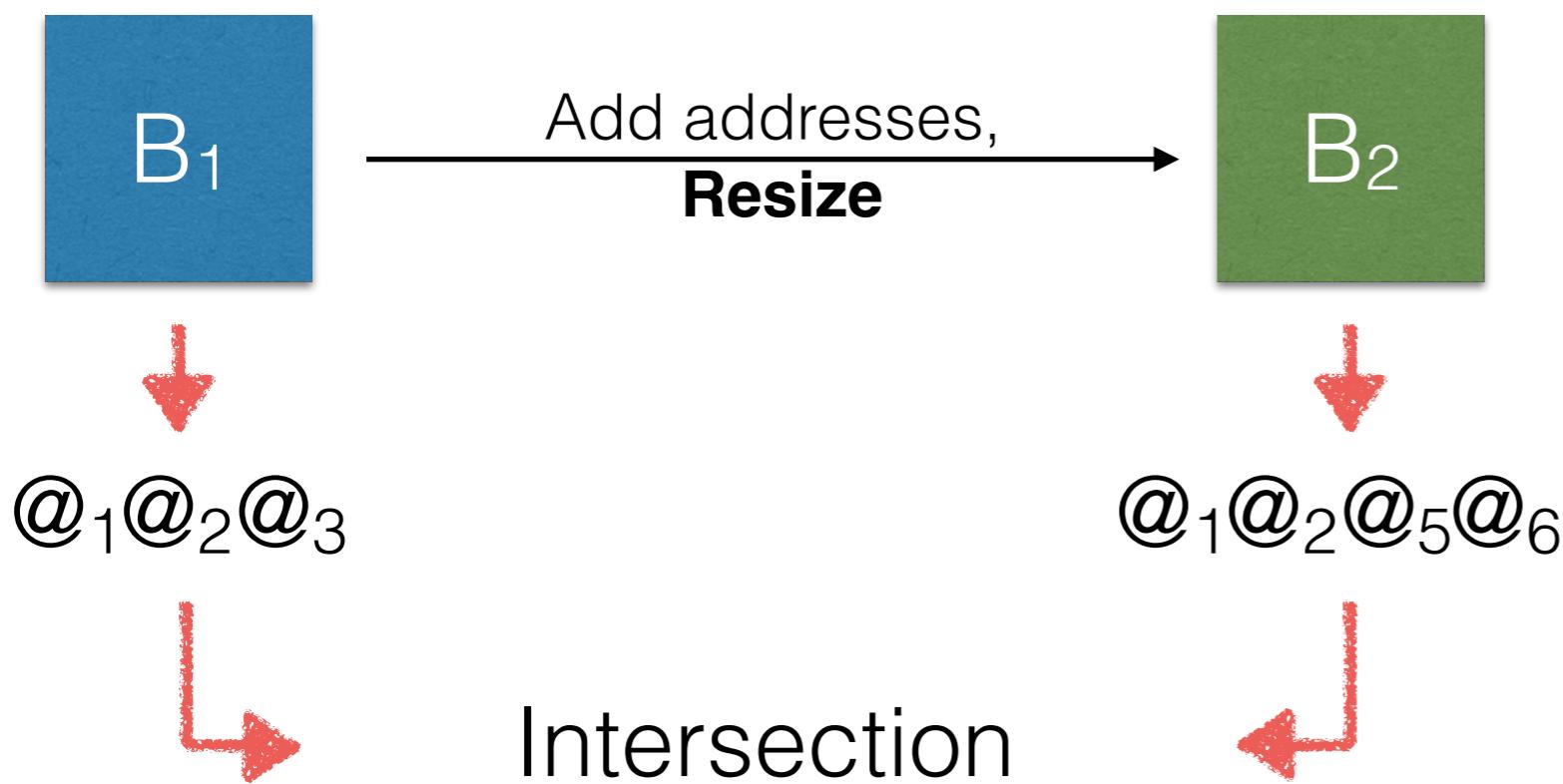


Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.98	0.03

Exp.	Client	Seed	Size
No resize	Same	Same	Same
<u>Resize</u>	<b>Same</b>	<b>Same</b>	<b>Different</b>
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

## Experiment 2 - Resize ↪ ↪



## Results

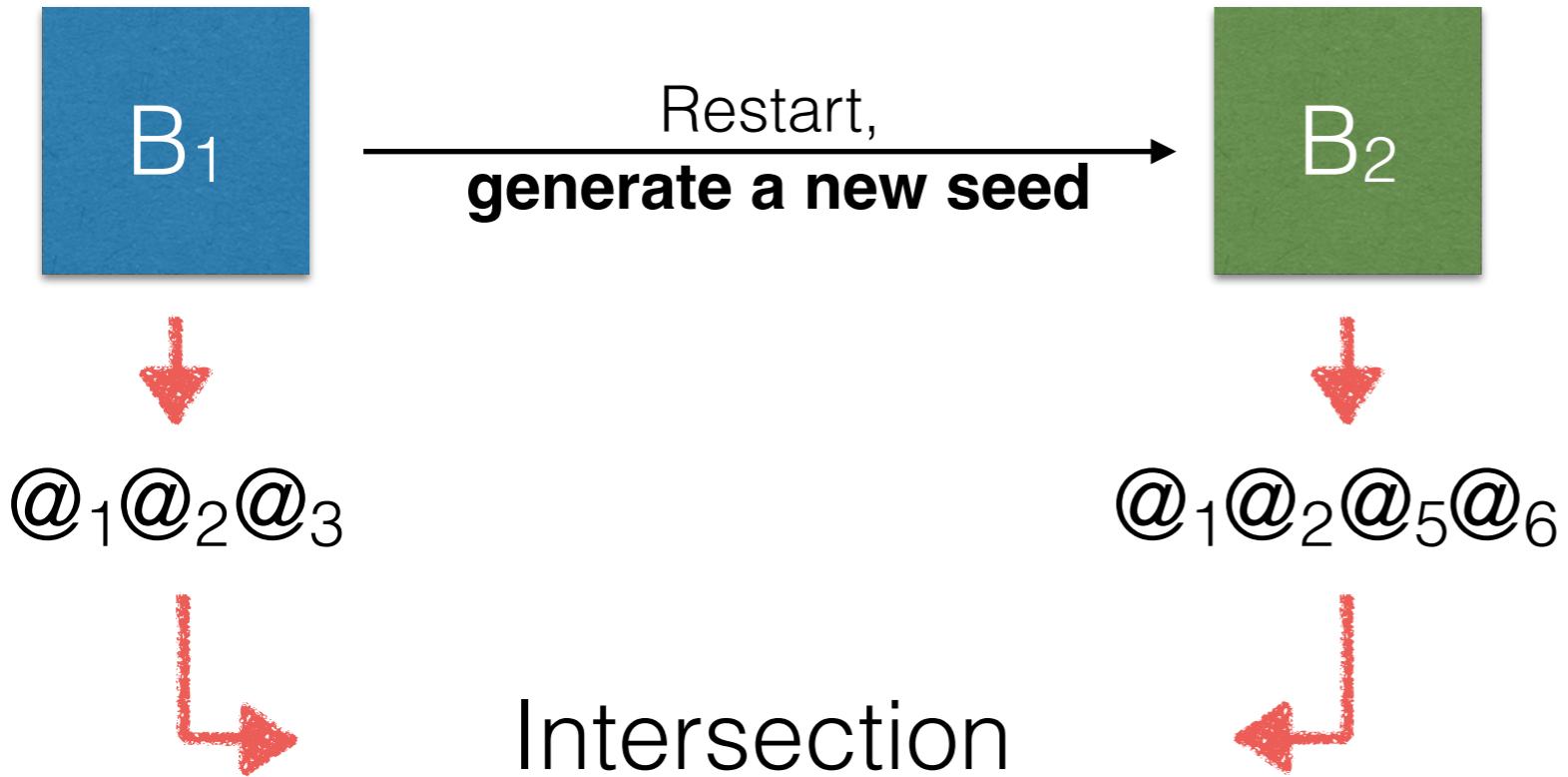
Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.98	0.03

significant change

Exp.	Client	Seed	Size
No resize	Same	Same	Same
<b>Resize</b>	<b>Same</b>	<b>Same</b>	<b>Different</b>
Restart	Same	Different	Same
> 2 filter	Same	Different	Different

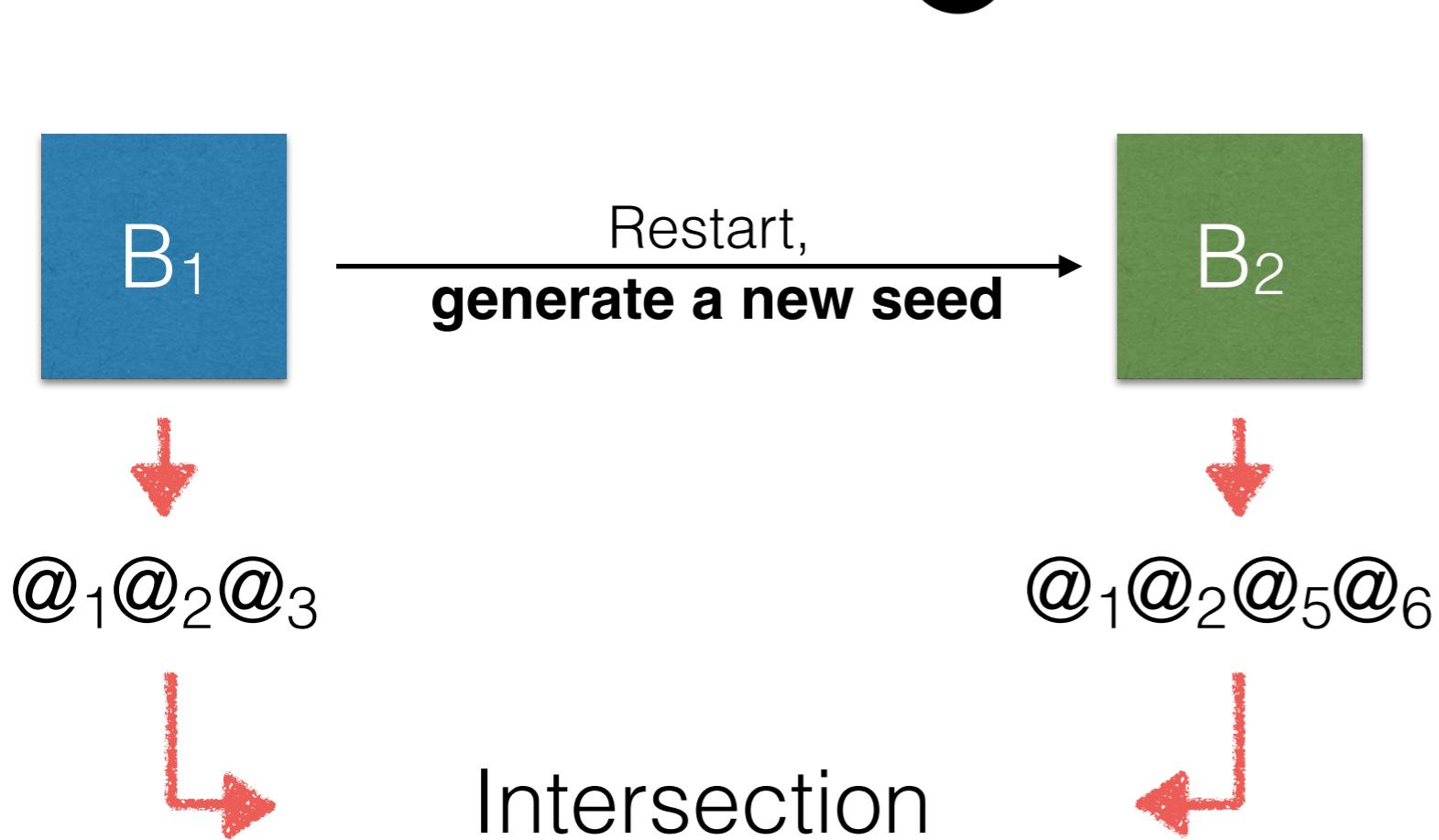
- Different BF sizes improve the attack

## Experiment 3 - restart



Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
<b>Restart</b>	<b>Same</b>	<b>Different</b>	<b>Same</b>
> 2 filter	Same	Different	Different

## Experiment 3 - restart

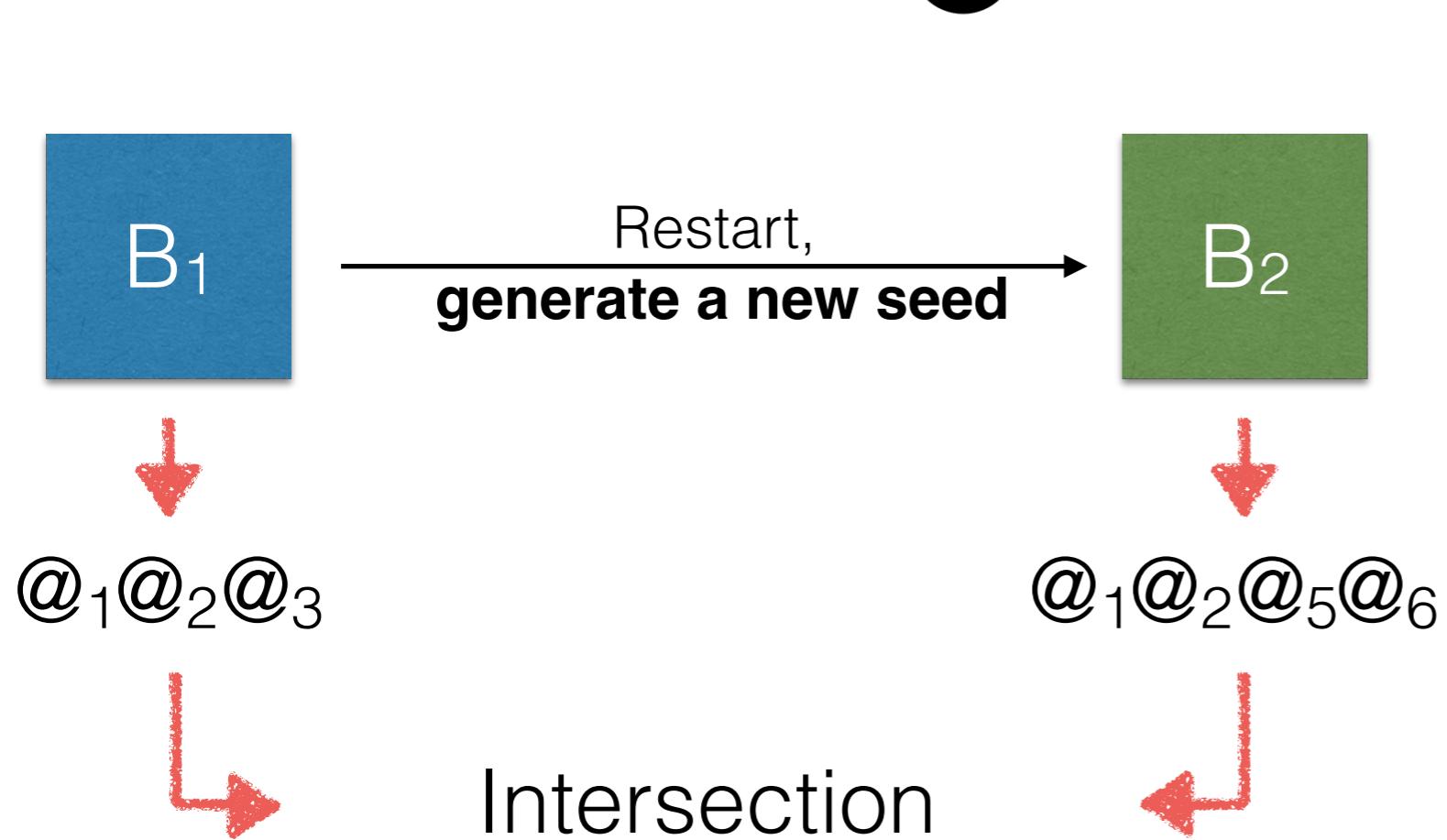


## Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.99	0.04

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
<b>Restart</b>	<b>Same</b>	<b>Different</b>	<b>Same</b>
> 2 filter	Same	Different	Different

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## Results

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Exp.	Client	Seed	Size
No resize	Same	Same	Same
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<b>Restart</b>	<b>Same</b>	<b>Different</b>	<b>Same</b>
> 2 filter	Same	Different	Different

# Experiment 3 - restart

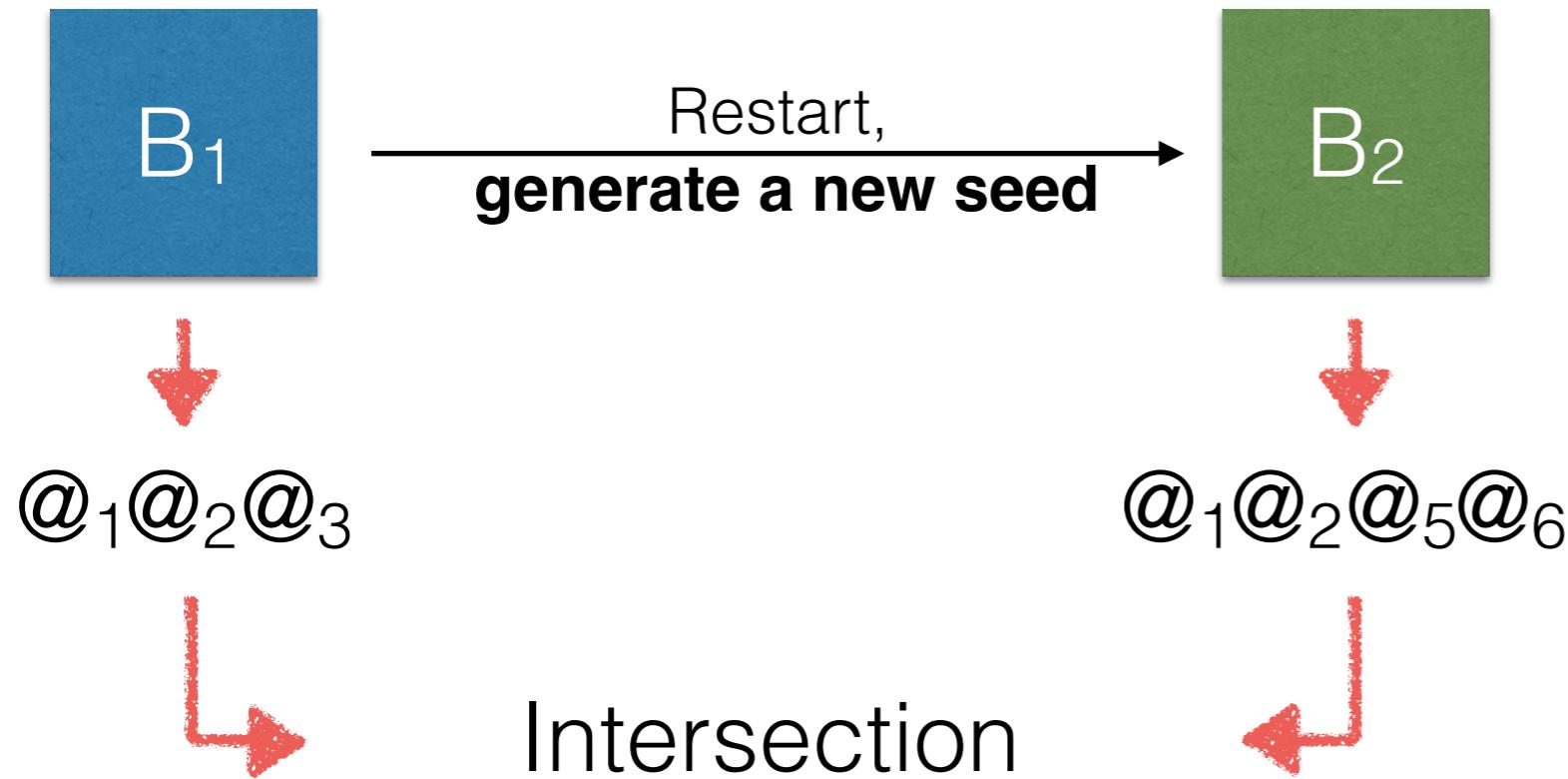
The diagram illustrates a state transition between two states,  $B_1$  and  $B_2$ . State  $B_1$  is represented by a blue square containing the text  $@_1 @_2 @_3$ . State  $B_2$  is represented by a green square containing the text  $@_1 @_2 @_5 @_6$ . A horizontal arrow points from  $B_1$  to  $B_2$ , labeled "Restart,  
**generate a new seed**". Below the arrows, red hand-drawn style arrows indicate an "Intersection". One red arrow originates from the bottom left of  $B_1$  and points towards the bottom center. Another red arrow originates from the bottom right of  $B_2$  and points towards the bottom center. The word "Intersection" is written in large black font at the bottom center.

## Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.99	0.04

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
<u>Restart</u>	<b>Same</b>	<b>Different</b>	<b>Same</b>
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# Experiment 3 - restart



Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	<b>Same</b>	<b>Different</b>	<b>Same</b>
> 2 filter	Same	Different	Different

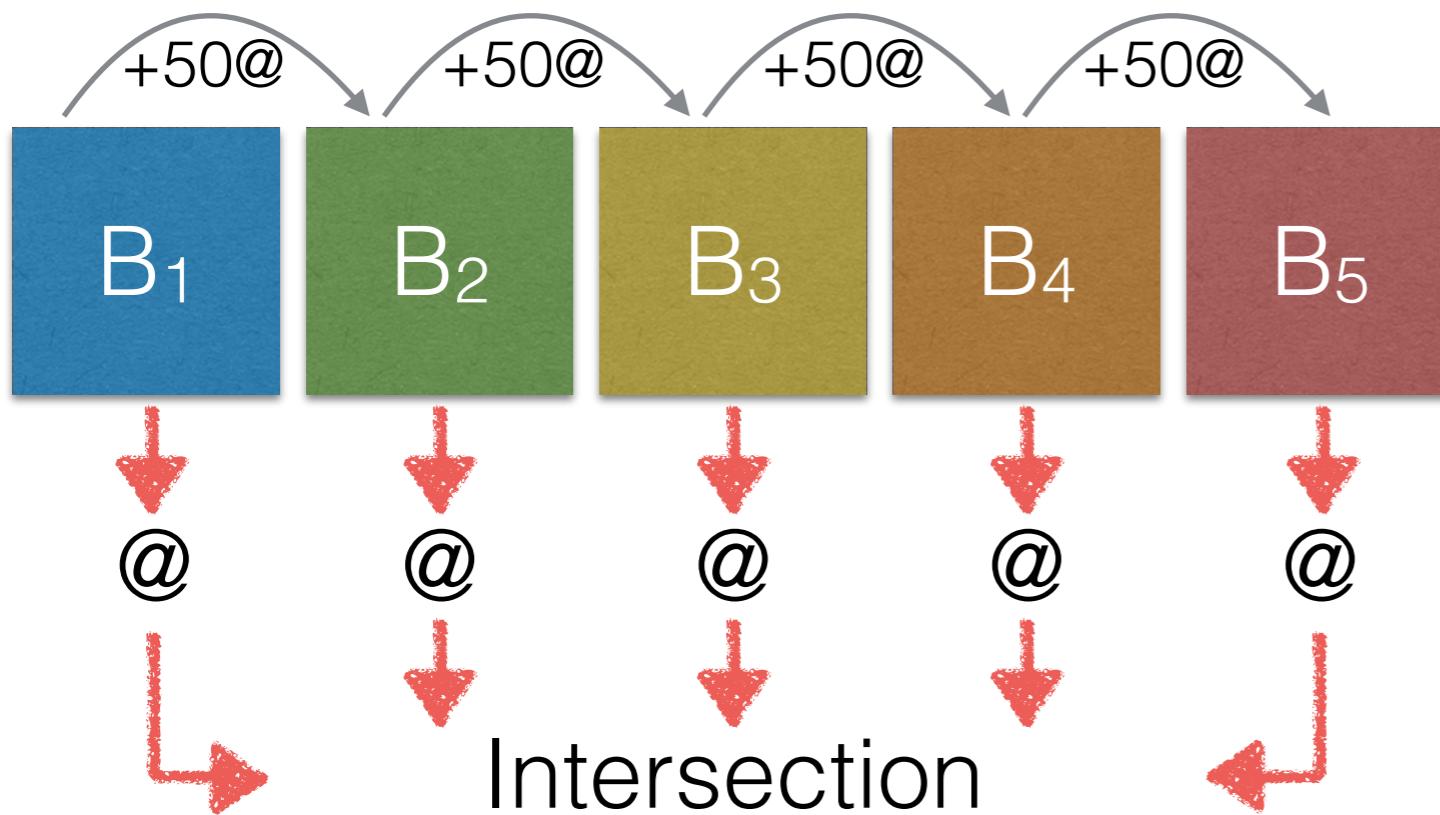
## Results

Target FPR (%)	P(1) with 2 BF	P(1) with 1 BF
0.1	0.99	0.04

# significant change

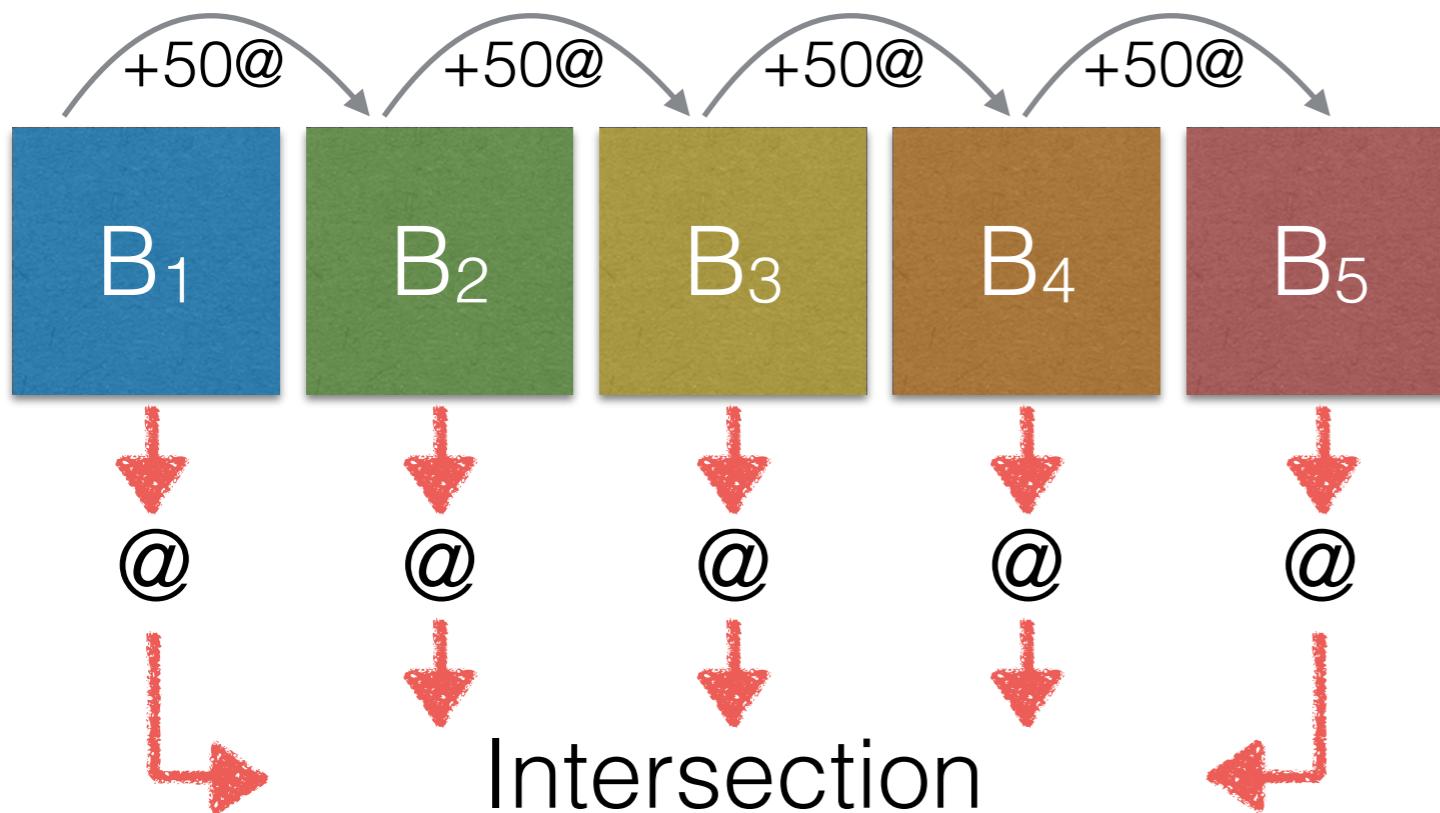
- Different BF seeds improve the attack

## Experiment 4 - More than 2 filter



Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
<b>&gt; 2 filter</b>	<b>Same</b>	<b>Different</b>	<b>Different</b>

## Experiment 4 - More than 2 filter

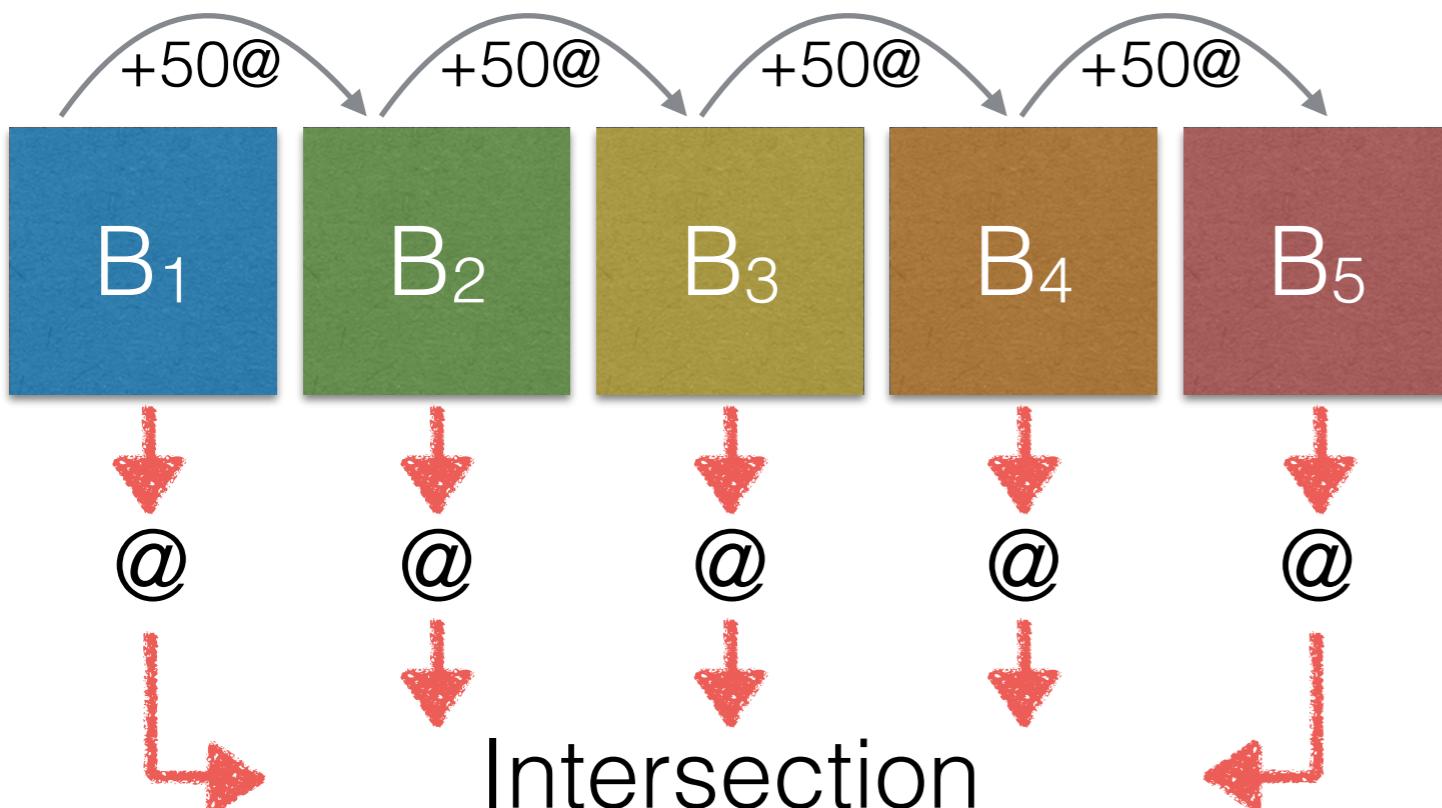


### Results

Target FPR (%)	$P(N)$ given 3 or more BF
0.05	~1
0.1	~1

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
<b>&gt; 2 filter</b>	<b>Same</b>	<b>Different</b>	<b>Different</b>

## Experiment 4 - More than 2 filter



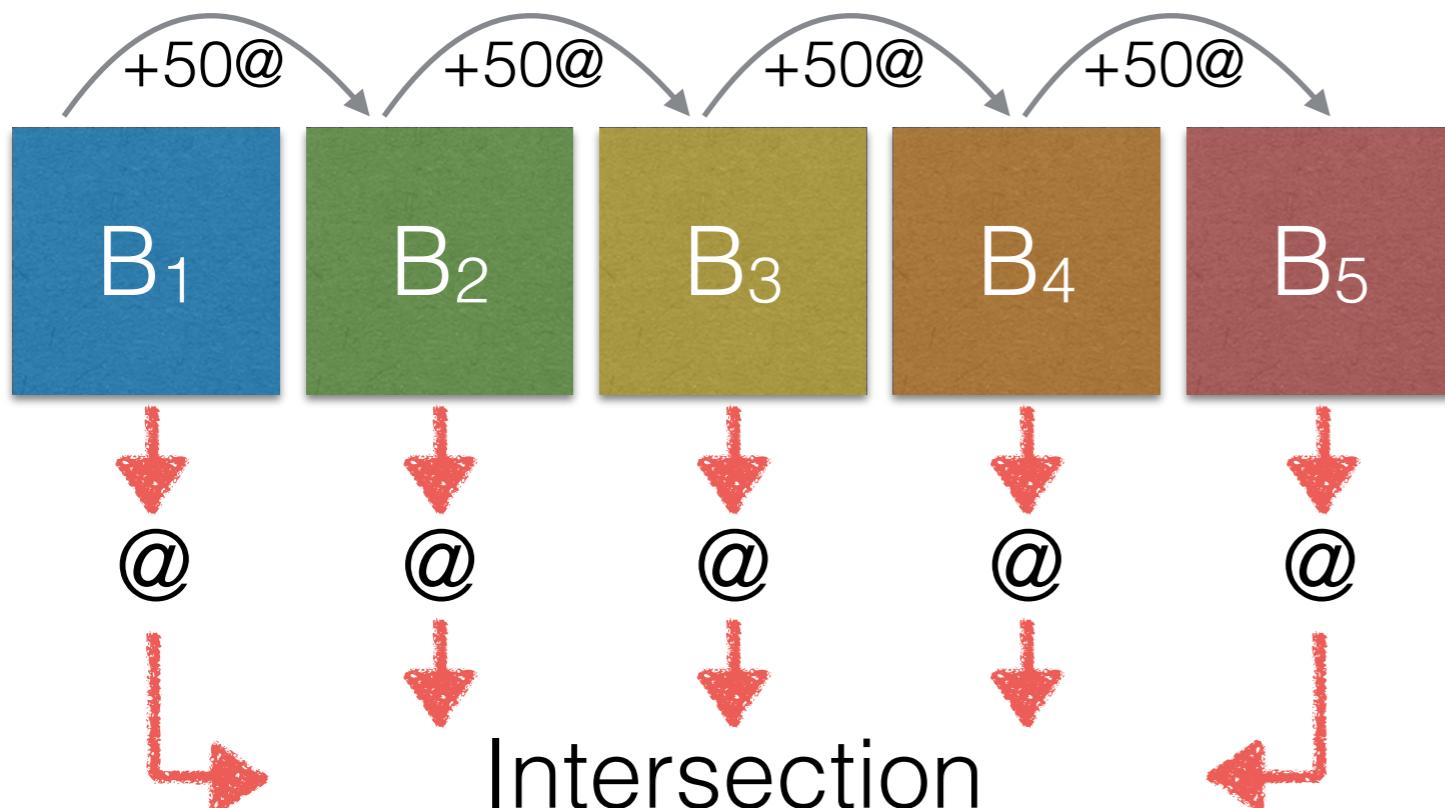
## Results

Target FPR (%)	$P(N)$ given 3 or more BF
0.05	~1
0.1	~1

Guessing all addresses

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
<b>&gt; 2 filter</b>	<b>Same</b>	<b>Different</b>	<b>Different</b>

## Experiment 4 - More than 2 filter



## Results

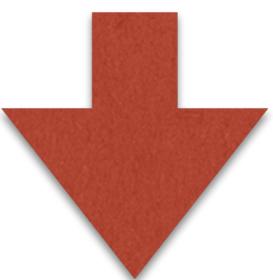
Target FPR (%)	P(N) given 3 or more BF
0.05	~1
0.1	~1

Guessing all addresses

3 Bloom filter

Exp.	Client	Seed	Size
No resize	Same	Same	Same
Resize	Same	Same	Different
Restart	Same	Different	Same
> 2 filter	<b>Same</b>	<b>Different</b>	<b>Different</b>

All addresses yielded by B<sub>1</sub> are leaked

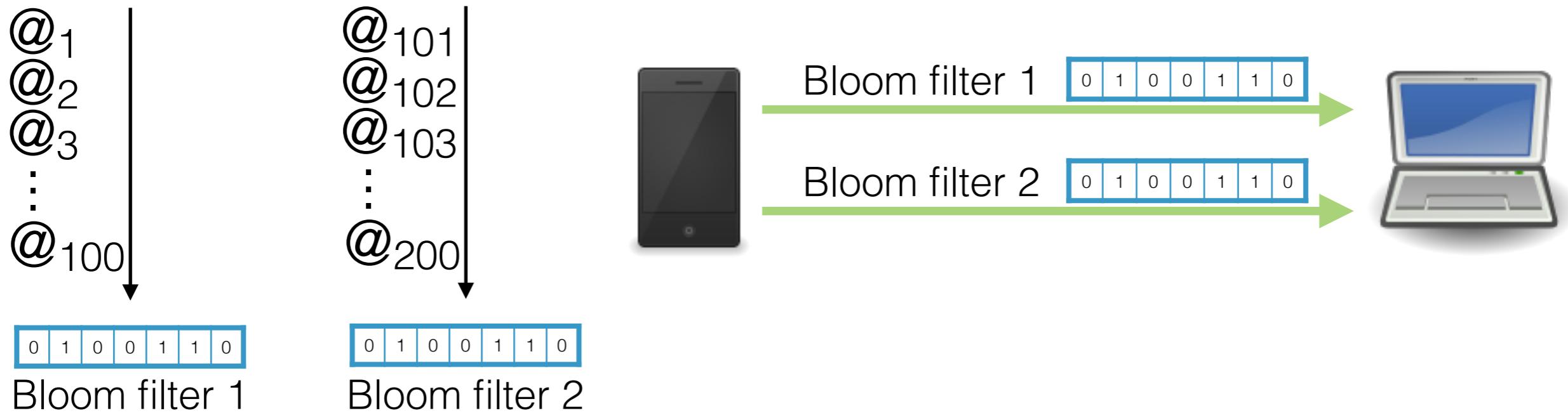


## Observations

1. Need constant FPR
2. Multiple Bloom filter with different parameters
3. SPV clients should keep state (e.g., about seed)

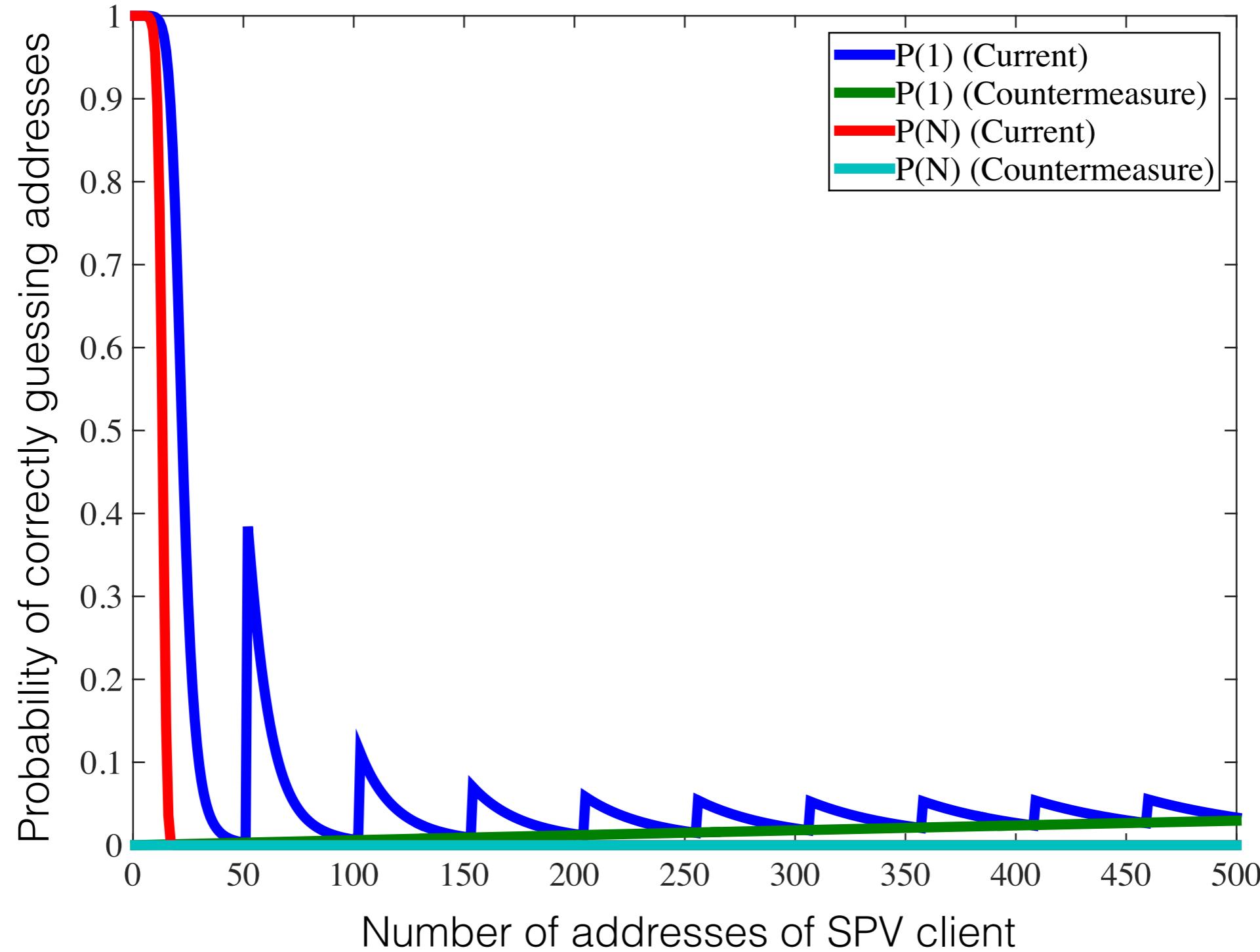


## Proposed solution

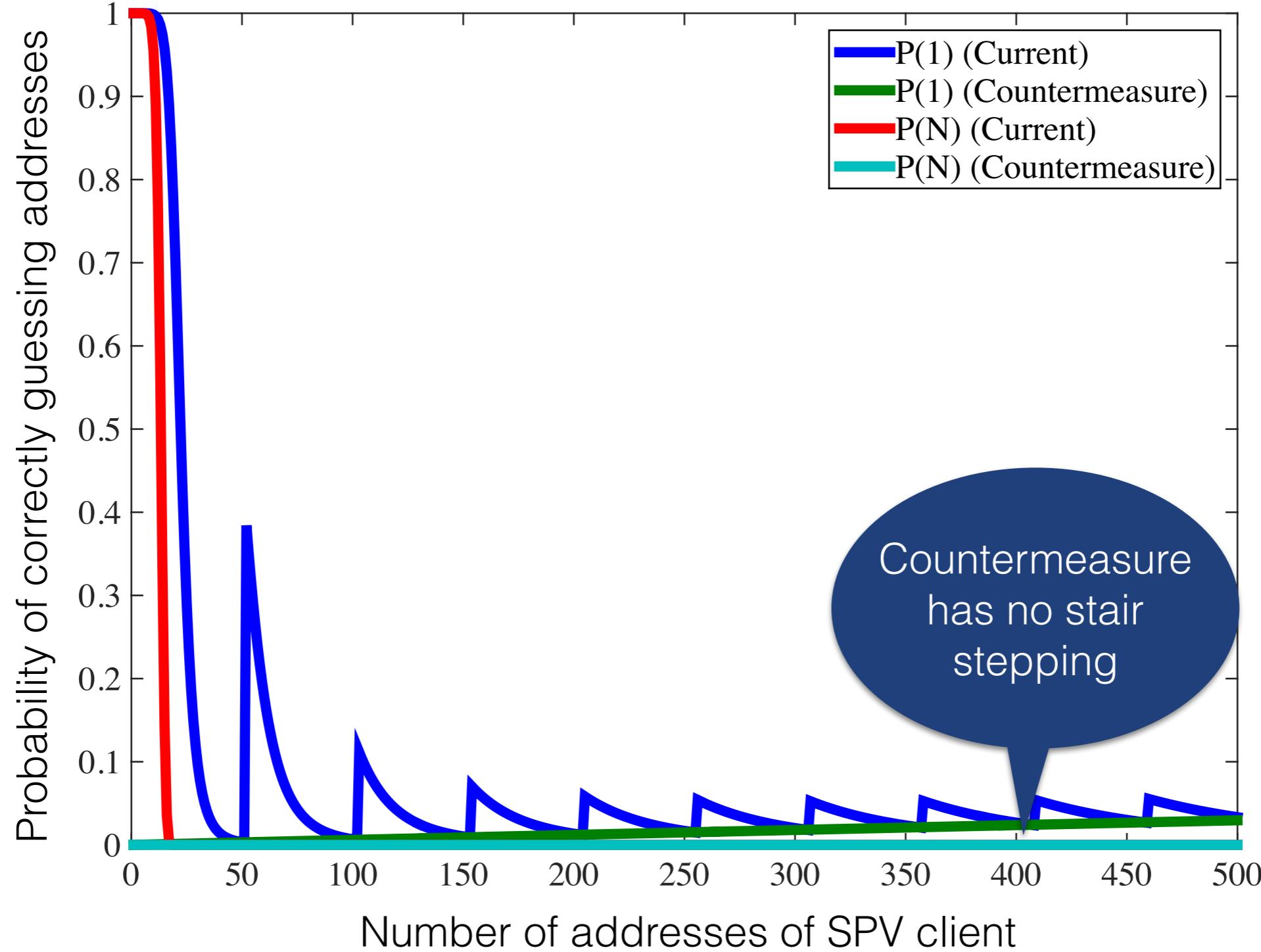


- Pre-generate Bitcoin addresses and insert into filter
- Keep state about outsourced Bloom filter 
- Overhead: For 100 addresses, < 1 kb

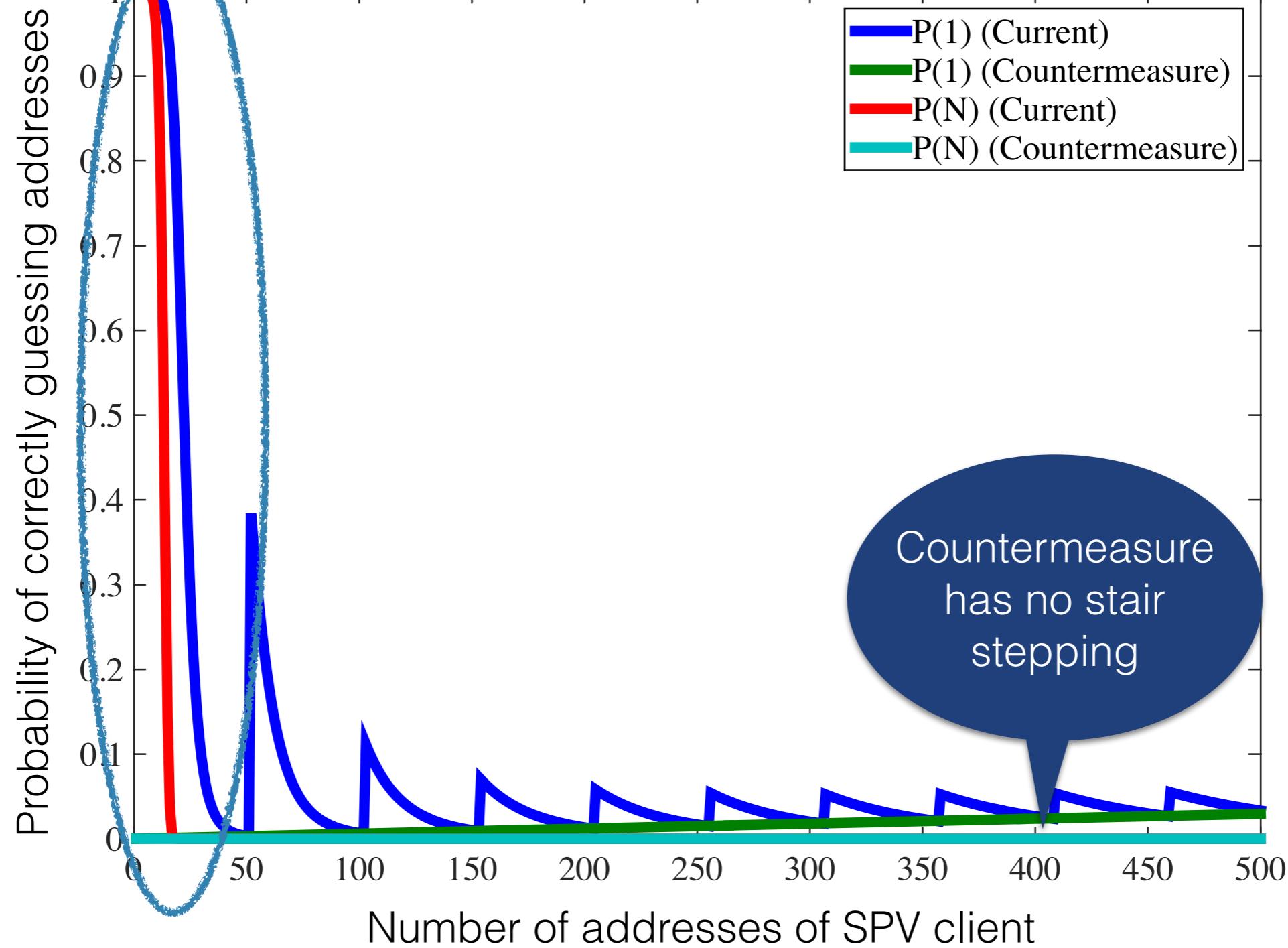
## Proposed solution



## Proposed solution



## Proposed solution



# Information leakage through Bloom Filters in SPV clients

## Analytical and Empirical evaluation

- ◆ 1 Bloom filter critical if < 20 Bitcoin addresses 
- ◆ 3+ Bloom filter intersection attack particularly strong 

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## Lightweight countermeasure

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- ◆ Intersection attack **not effective**
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Thank you!