

Αλγοριθμική Επιχειρησιακή Έρευνα Δεύτερη Εργασία

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1. Find a differentiable function $f : \mathbb{R} \rightarrow \mathbb{R}$ such that f does not have an extremum at its critical point.

2. Given a positive integer S , which decompositions $a_1 + \dots + a_n = S$ with the a_i positive integers have the largest product $a_1 \dots a_n$?

3. Find the optimal solution to the Diet Problem when the cost function is $\text{Cost}(x_1, x_2) = x_1 + x_2$.

4. Let $A, B \in \mathbb{R}^{n \times n}$. Show that the traditional way of computing their product AB requires a total of $(2n - 1)n^2$ arithmetic operations.

5. Consider the problem of solving a system of n linear equations in n unknowns. Show that the Gaussian elimination method requires $O(n^3)$ arithmetic operations in order to either compute a solution or to decide that no solution exist.

6. Suppose that we are given a set of vectors in \mathbb{R}^n that form a basis and let y be an arbitrary vector in \mathbb{R}^n . We wish to express y as a linear combination of the basis vectors. How can this be accomplished?

7. Study the paper with title: Do dogs know Calculus? found in the Readings folder.