

# Υλοποίηση σε Python

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# 1 The Python equivalents of the Linear Programming Formulations of Sudoku Variations

## 1.1 Classic Sudoku

```
self.matrix = matrix 1
self.n = len(matrix) 2
self.m = int(sqrt(self.n)) 3

super().__init__( 4
    name=f"{type(self).__name__}_solver_{self.n}_x_{self.n}".lower(), 5
    sense=LpMinimize) 6
7
```

Listing 1: TODO

```
self.x = [ 1
    [ 2
        [ 3
            LpVariable( 4
                f"x_{i + 1:02d}_{j + 1:02d}_{k + 1:02d}", cat=LpBinary) 5
            for k in range(self.n) 6
        ] for j in range(self.n) 7
    ] for i in range(self.n) 8
] 9
```

Listing 2: TODO

```
self += 0 1
```

Listing 3: TODO

```
for j in range(self.n): 1
    for k in range(self.n): 2
        self += lpSum([self.x[i][j][k] 3
            for i in range(self.n)]) == 1, f"in column {j + 4
1:02d} only one {k + 1:02d}"
```

Listing 4: TODO

```
for i in range(self.n): 1
    for k in range(self.n): 2
        self += lpSum([self.x[i][j][k] 3
```

```

                                for j in range(self.n)]] == 1, f"in row {i +
1:02d} only one {k + 1:02d}"

```

Listing 5: TODO

```

for k in range(self.n):
    for p in range(self.m):
        for q in range(self.m):
            self += lpSum([
                [
                    lpSum([
                        self.x[i][j][k]
                        for i in range(self.m * p, self.m * (p + 1))
                    ])
                ]
                for j in range(self.m * q, self.m * (q + 1))
            ]) == 1, f"in submatrix {p + 1:02d} {q + 1:02d} only one {k
+ 1:02d}"

```

Listing 6: TODO

```

for i in range(self.n):
    for j in range(self.n):
        self += lpSum([self.x[i][j][k]
                        for k in range(self.n)]] == 1, f"cell {i +
1:02d} {j + 1:02d} must be assigned exactly one value"

```

Listing 7: TODO

```

for i in range(self.n):
    for j in range(self.n):
        if self.matrix[i][j]:
            self += self.x[i][j][self.matrix[i][j] -
                                1] == 1, f"cell {i + 1:02d} {j +
1:02d} has an initial value of {self.matrix[i][j]:02d}"

```

Listing 8: TODO

```

for i in range(self.n):
    for j in range(self.n):
        if not self.matrix[i][j]:
            for value in self.illegal_values(i, j):
                self += (
                    self.x[i][j][value - 1] == 0,
                    f"cell {i + 1:02d} {j + 1:02d} cannot be assigned a
value of {value:02d}"

```

## Listing 9: TODO

```

def solve(self, solver=None, **kwargs):
    1
    super().solve(solver=solver, **kwargs)
    2
    3
    4
    if LpStatus[self.status] != "Optimal":
    5
        raise ValueError(
    6
            f"Solver failed with status '{LpStatus[self.status]}'")
    7
    8
    for i in range(self.n):
    9
        for j in range(self.n):
    10
            if not self.matrix[i][j]:
    11
                self.matrix[i][j] = [
    12
                    self.x[i][j][k].varValue for k in range(self.n)
    13
                ].index(1) + 1
    14

```

## Listing 10: TODO

```

def illegal_values(self, row, col):
    1
    2
    values = set()
    3
    4
    for j in range(self.n):
    5
        if self.matrix[row][j] is not None:
    6
            values.add(self.matrix[row][j])
    7
    8
    for i in range(self.n):
    9
        if self.matrix[i][col] is not None:
    10
            values.add(self.matrix[i][col])
    11
    12
    p, q = row // self.m, col // self.m
    13
    14
    for i in range(self.m * p, self.m * (p + 1)):
    15
        for j in range(self.m * q, self.m * (q + 1)):
    16
            if self.matrix[i][j] is not None:
    17
                values.add(self.matrix[i][j])
    18
    19
    return values
    20

```

## Listing 11: TODO

```

sudokulp_solver_9_x_9:
    1
    MINIMIZE
    2
    0*__dummy + 0
    3

```

## Listing 12: TODO

```

SUBJECT TO
in_column_01_only_one_01: x_01_01_01 + x_02_01_01 + x_03_01_01 + x_04_01_01
+ x_05_01_01 + x_06_01_01 + x_07_01_01 + x_08_01_01 + x_09_01_01 = 1
...
in_column_09_only_one_09: x_01_09_09 + x_02_09_09 + x_03_09_09 + x_04_09_09
+ x_05_09_09 + x_06_09_09 + x_07_09_09 + x_08_09_09 + x_09_09_09 = 1

in_row_01_only_one_01: x_01_01_01 + x_01_02_01 + x_01_03_01 + x_01_04_01
+ x_01_05_01 + x_01_06_01 + x_01_07_01 + x_01_08_01 + x_01_09_01 = 1
...
in_row_09_only_one_09: x_09_01_09 + x_09_02_09 + x_09_03_09 + x_09_04_09
+ x_09_05_09 + x_09_06_09 + x_09_07_09 + x_09_08_09 + x_09_09_09 = 1

in_submatrix_01_01_only_one_01: x_01_01_01 + x_01_02_01 + x_01_03_01
+ x_02_01_01 + x_02_02_01 + x_02_03_01 + x_03_01_01 + x_03_02_01 +
    x_03_03_01
= 1
...
in_submatrix_03_03_only_one_09: x_07_07_09 + x_07_08_09 + x_07_09_09
+ x_08_07_09 + x_08_08_09 + x_08_09_09 + x_09_07_09 + x_09_08_09 +
    x_09_09_09
= 1

cell_01_01_must_be_assigned_exactly_one_value: x_01_01_01 + x_01_01_02
+ x_01_01_03 + x_01_01_04 + x_01_01_05 + x_01_01_06 + x_01_01_07 +
    x_01_01_08
+ x_01_01_09 = 1
...
cell_09_09_must_be_assigned_exactly_one_value: x_09_09_01 + x_09_09_02
+ x_09_09_03 + x_09_09_04 + x_09_09_05 + x_09_09_06 + x_09_09_07 +
    x_09_09_08
+ x_09_09_09 = 1

cell_01_08_has_an_initial_value_of_02: x_01_08_02 = 1
...
cell_09_02_has_an_initial_value_of_01: x_09_02_01 = 1

cell_01_01_cannot_be_assigned_a_value_of_02: x_01_01_02 = 0
...
cell_09_09_cannot_be_assigned_a_value_of_09: x_09_09_09 = 0

```

## Listing 13: TODO

```

VARIABLES
__dummy = 0 Continuous
0 <= x_01_01_01 <= 1 Integer

```

```
...  
0 <= x_09_09_09 <= 1 Integer
```

4  
5

---

Listing 14: TODO

## 1.2 Sudoku X

```
super().__init__(matrix)
```

1

Listing 15: TODO

```
for k in range(self.n):
```

1

```
    self += lpSum([
```

2

```
        self.x[r][r][k] for r in range(self.n)
```

3

```
    ]) == 1, f"in the diagonal only one {k + 1}"
```

4

5

Listing 16: TODO

```
for k in range(self.n):
```

1

```
    self += lpSum([
```

2

```
        self.x[r][self.n - 1 - r][k] for r in range(self.n)
```

3

```
    ]) == 1, f"in the anti diagonal only one {k + 1}"
```

4

5

Listing 17: TODO

## 1.3 Four Square Sudoku

```
super().__init__(matrix)
```

1

Listing 18: TODO

```
for i in [1, self.n - self.m - 1]:
    for j in [1, self.n - self.m - 1]:
        for k in range(self.n):
            self += lpSum([
                [
                    lpSum([
                        self.x[r][c][k]
                        for c in range(j, j + self.m)
                    ])
                ]
                for r in range(i, i + self.m)
            ]) == 1, f"in square {i + 1:02d} {j + 1:02d} {i + self.m:02d} {j + self.m:02d} only one {k + 1:02d}"
```

1

2

3

4

5

6

7

8

9

10

11

12

Listing 19: TODO



## 1.4 Four Pyramid Sudoku

```
super().__init__(matrix)
```

1

Listing 20: TODO

```
for k in range(1, self.n + 1):
    self += lpSum([
        lpSum([
            self.x[r - 1][c - 1][k - 1]
            for c in range(self.m + r, self.n - r + 1)
        ]) for r in range(1, self.m + 1)
    ]) == 1, f"in pyramid 1 only one {k + 1}"
```

1  
2  
3  
4  
5  
6  
7

Listing 21: TODO

```
for k in range(1, self.n + 1):
    self += lpSum([
        lpSum([
            self.x[r - 1][c - 1][k - 1]
            for r in range(1 + c, self.n - self.m + 1 - c + 1)
        ]) for c in range(1, self.m + 1)
    ]) == 1, f"in pyramid 2 only one {k + 1}"
```

1  
2  
3  
4  
5  
6  
7

Listing 22: TODO

```
for k in range(1, self.n + 1):
    self += lpSum([
        lpSum([
            self.x[r - 1][c - 1][k - 1]
            for c in range(self.n + self.m - 1 - r, r - self.m + 1)
        ]) for r in range(self.n - self.m + 1, self.n + 1)
    ]) == 1, f"in pyramid 3 only one {k + 1}"
```

1  
2  
3  
4  
5  
6  
7

Listing 23: TODO

```
for k in range(1, self.n + 1):
    self += lpSum([
        lpSum([
            self.x[r - 1][c - 1][k - 1]
            for r in range(self.n + self.m + 1 - c, c - 1 + 1)
        ]) for c in range(self.n - self.m + 1, self.n + 1)
    ]) == 1, f"in pyramid 4 only one {k + 1}"
```

1  
2  
3  
4  
5  
6  
7

---

Listing 24: TODO

```
options = {
    "sdk": SudokuLP,
    "sdkx": SudokuXLP,
    "sdkfs": FourSquareSudokuLP,
    "sdkfp": FourPyramidSudokuLP
}

extension = path.splitext(args.load)[1][1:]

matrix = load(args.load)
problem = options[extension](matrix)
```

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11

---

Listing 25: TODO

## 2 Generating Sudoku Puzzles

```
def transpose(matrix):
    return list(map(list, [*zip(*matrix)]))
```

1  
2

---

Listing 26: TODO

```
def relabel(matrix):
    replacements = {
        original: replacement
        for original, replacement in zip(
            range(1, len(matrix) + 1),
            np.random.permutation(range(1, len(matrix) + 1))
        )
    }

    for i in range(len(matrix)):
        for j in range(len(matrix)):
            if matrix[i][j] is not None:
                matrix[i][j] = replacements[matrix[i][j]]

    return matrix
```

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15

---

Listing 27: TODO

```
def reorder(matrix):
```

1

```

def swap_rows(matrix):
    m = int(sqrt(len(matrix)))

    for p in range(m):
        for q in range(m):
            for r in range(m):
                i1 = randint(m * p, m * (p + 1) - 1)
                i2 = randint(m * p, m * (p + 1) - 1)

                matrix[i1], matrix[i2] = matrix[i2], matrix[i1]

    return matrix

return transpose(swap_rows(transpose(swap_rows(matrix))))

```

Listing 28: TODO

```

methods = {
    "transpose": transpose,
    "relabel": relabel,
    "reorder": reorder
}

matrix = load(args.load)
matrix = methods[args.method](matrix)

dump(matrix, args.save)

```

Listing 29: TODO

### 3 The Sudoku (.sdk\*) file format

```

9
1, 1, 5
1, 2, 3
1, 5, 7
2, 1, 6
2, 4, 1
2, 5, 9
2, 6, 5
3, 2, 9
3, 3, 8
3, 8, 6
4, 1, 8
4, 5, 6
4, 9, 3
5, 1, 4

```

5, 4, 8  
5, 6, 3  
5, 9, 1  
6, 1, 7  
6, 5, 2  
6, 9, 6  
7, 2, 6  
7, 7, 2  
7, 8, 8  
8, 4, 4  
8, 5, 1  
8, 6, 9  
8, 9, 5  
9, 5, 8  
9, 8, 7  
9, 9, 9

16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31

Listing 30: TODO

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

Figure 1: A Sudoku Puzzle  
[Taken from Wikipedia](#)

## 3.1 Loading Sudoku Puzzles

```
lines = file.readlines() 1
lines = map(lambda line: sub(r"#.*", "", line), lines) 2
lines = map(lambda line: sub(r"\s+", "", line), lines) 3
lines = enumerate(lines) 4
lines = filter(lambda data: len(data[1]) > 0, lines) 5
```

Listing 31: TODO

```
try: 1
    index, line = next(lines) 2
    3
    size = int(line) 4
    5
    if size <= 0: 6
        raise ValueError 7
    8
except ValueError: 9
    raise ParseError( 10
        index, line, "is not a valid size specifier") 11
```

Listing 32: TODO

```
_sqrt = sqrt(size) 1
2
if _sqrt != int(_sqrt): 3
    raise ParseError( 4
        index, line, f"{size} is not a perfect square") 5
```

Listing 33: TODO

```
matrix = [[None for _ in range(size)] for _ in range(size)] 1
2
for index, line in lines: 3
    try: 4
        x, y, z = tuple(map(int, line.split(','))) 5
        6
        if x < 0 or y < 0 or z < 0 or z > size: 7
            raise IndexError 8
        9
        if matrix[x - 1][y - 1] is not None: 10
            raise ParseError( 11
                index, line, 12
                f"the cell has already been assigned") 13
```

matrix[x - 1][y - 1] = z	14
	15
	16
except IndexError:	17
raise ParseError(	18
index, line,	19
f" <i>is not a valid entry for a puzzle of size {size}</i> ")	20
	21
except ParseError as parse_error:	22
raise parse_error	23
	24
except:	25
raise ParseError(	26
index, line, " <i>Malformed entry</i> ")	27
	28
return matrix	29

---

Listing 34: TODO

## 3.2 Dumping Sudoku Puzzles

```
file.write(f"{len(matrix)}\n")
1
2
for i in range(len(matrix)):
3
    for j in range(len(matrix)):
4
        if matrix[i][j] is not None:
5
            file.write(f"{i + 1}, {j + 1}, {matrix[i][j]}\n")
6
```

Listing 35: TODO