

# Αλγοριθμική Επιχειρησιακή Έρευνα Τέταρτη Εργασία

Σιώρος Βασίλειος  
Ανδρινοπούλου Χριστίνα

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1. Consider the problem  $\min 2x_1 + 3x_2 - 10$  s.t.  $-x_1 + 2x_2 \leq 5$  and reformulate it a linear programming problem.

2. (Road lighting) Consider a road divided in  $n$  segments that is illuminated by  $m$  lamps. Let  $p_j$  be the power of the  $j$ th lamp. The illumination  $I_i$  of the  $i$ th segment is assumed to be  $\sum_{j=1}^m a_{ij} p_j$  where  $a_{ij}$  are known coefficients. Let  $I^*_i$  be the desired illumination of road  $i$ .

3. Consider a school district with  $I$  neighborhoods,  $J$  schools and  $G$  grades at each school. Each school  $j$  has a capacity  $C_{jg}$  for grade  $g$ . In each neighborhood  $i$ , the student population of grade  $g$  is  $S_{ig}$ . Finally the distance of school  $j$  from neighborhood  $i$  is  $d_{ij}$ . Formulate a linear programming problem whose objective is to assign all students to schools, while minimizing the total distance traveled by all students. (You may ignore the fact that numbers of students must be integer).

4. Consider a set  $P$  described by linear inequality constraints  $P = \{x \in \mathbb{R}^n : a_i'x \leq b_i, i = 1, \dots, m\}$ . A ball with center  $y$  and radius  $r$  is defined as the set of all points within distance  $r$  from  $y$ . We are interested in finding a ball with the largest possible radius, which is entirely contained within the set  $P$ . Provide a linear programming formulation of this problem.