

$$\begin{array}{ccccccc}
 0 & & 2 & & 5 & & 7 \\
 | & & | & & | & & | \\
 -a & + & a(1.05)^2 & - & 250000 & + & b(1.05)^7 \\
 -b & & & & & &
 \end{array}
 \quad i = 5\%$$

$$a + b = \frac{250000}{(1.05)^5}$$

$$5 = \frac{2a}{a+b} + \frac{7b}{a+b}$$

$$5a + 5b = 2a + 7b$$

$$3a = 2b$$

$$a = \frac{2}{3}b$$

$$\frac{2}{3}b + b = \frac{250000}{(1.05)^5} \quad \Rightarrow \quad \frac{5}{3}b$$

$$\begin{array}{l}
 a = 78352.616 = \$78352.62 \quad 2 \text{ yr bonds} \\
 b = 117528.925 = \$117528.93 \quad 7 \text{ yr bonds}
 \end{array}$$

$$\frac{2^2 a}{a+b} + \frac{7^2 b}{a+b} = 2^2 \frac{2}{5} + 7^2 \frac{3}{5} = 31 > 25 = 5^2$$

convexity condition
holds

cont. on next page

$i = 5\%$
78352.62 2yr bonds redeems @ $t=2$ for ≈ 86383.763
117528.93 7yr bonds redeems @ $t=7$ for ≈ 165375.007
250000 5yr liability

@ $t=2$ $i = 1\%$

$$\left(86383.763 + \frac{165375.007}{(1.01)^5} \right) (1.01)^3 = \$251117.74 > 250000$$

* can still cover liability