

Recap: Where are we, structurally,  
in the organization of the course.

- So far: All about *access*... and what?
  - Recall what is an access path?

Recap: We know...

- Where/how to place data on the disk,
  1. Row store: sorted rows in blocks
  2. Parallel partitioning
  3. Column store
  4. Key, value store
- How to get the data off the disk.
  1. B\_\_\_\_\_
  2. B\_\_\_\_\_
  3. B\_\_\_\_\_

Recap: Where are we, structurally,  
in the organization of the course.

✓Storage Management

Next Section

- Given a [large] quantity of disk resident data  
i.e.  $| \text{Data} | > | \text{Memory} |$
- How to implement database functions

## Had a Peek: B+ trees

- Fat fanout. → shortens the tree height
- Primary index, leverages sorted data
  - Sparse Index
  - Shorten the tree

Why shorten the tree? Fewer accesses

## Two Phase Multiway Merge Sort a.k.a. External, Two Phase Sort

Objectives:

- External (of RAM) Algorithm
  - explicitly understand and incorporate movement of data into the algorithm
- The algorithm

Reading: Text 15.4.1

Reminder:

Simple I/O cost models – and how they fail

I/O models:

- Linear:
  - 1 average seek per block
  - $n$  blocks,  $f(n) = cn$ ,  $c$  = average seek time
- Affine:
  - seek first block,
  - weighted average of rotational latency + track to track seek time for each additional block
  - $n$  block  $f(n) = c + c'(n-1)$
- and how they fail
  - buffering (hardware and software)
  - prefetch

## Text & Class Cost Model

- $B(R)$  number of blocks of relation  $R$
- $T(R)$  number of tuples [rows] in relation  $R$

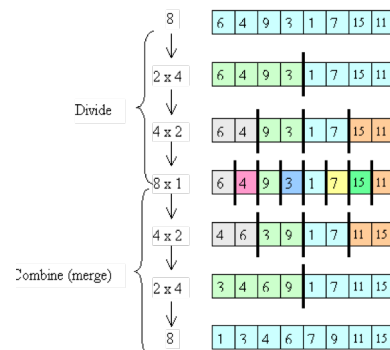
Count the number of blocks read

- Not yet: commonly, no cost for writing output.

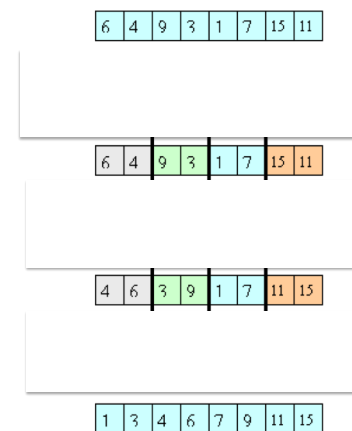
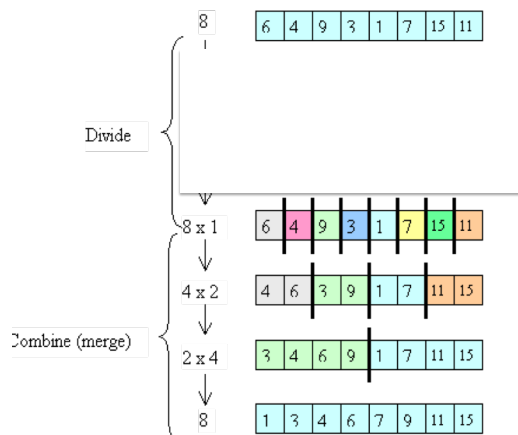
## A word about notation

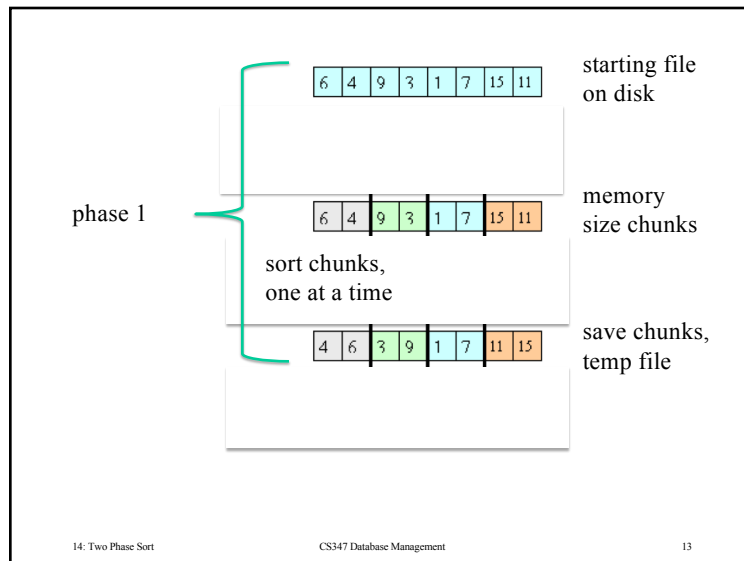
- text & class:  $B(R)$  and  $T(R)$
- common in the literature
  - $T(R) = |R|$  // number of rows/tuples
  - $B(R) = ||R||$  // number of blocks/pages

## Two Phase Multiway Merge Sort Sort-of Start With Merge Sort



<http://pages.cs.wisc.edu/~vemon/cs367>

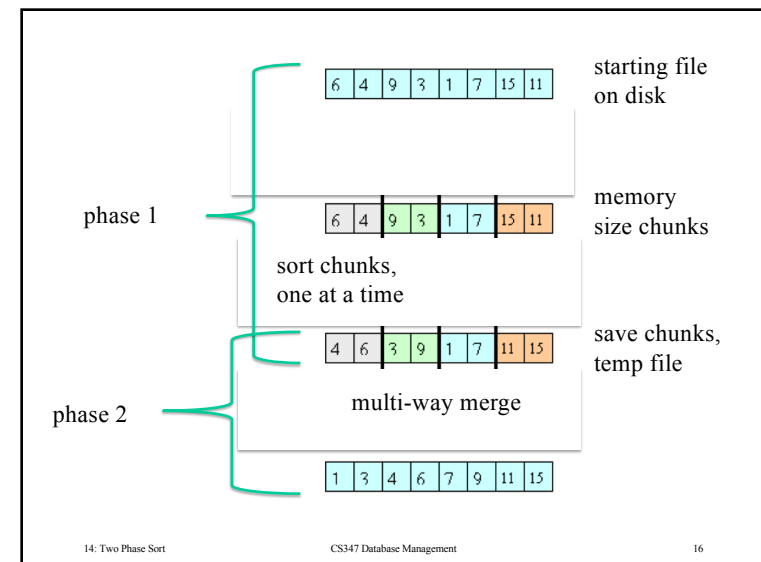
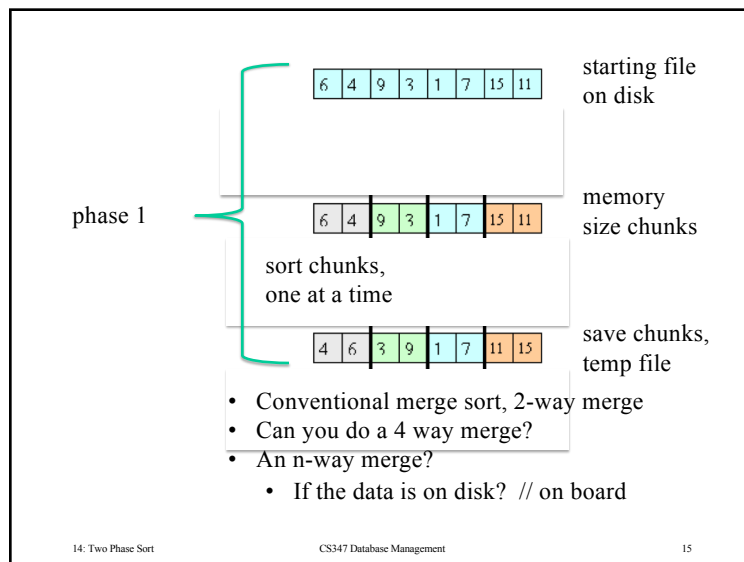




## Merge-Sort (divide and conquer) that considers external storage

- Phase 1 == Divide
  - until done
    - read file until memory full
    - sort that portion
    - write result in its own temp file

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## Merge-Sort (divide and conquer) that considers external storage

- Phase 1 == Divide
  - until done
    - read file until memory full
    - sort that portion
    - write result in its own temp file
- Phase 2 == n-way Merge for n temp files
  - read 1 block of each temp file
  - until done
    - n-way merge to produce sorted block in an output buffer
      - upon full output buffer, write to disk
    - if a temp file's block is exhausted, read another block

In how long? How large a file can we sort?

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## Two Phase External Sorting

- For all intents and purposes, sorting a file,  $f$ ,  
bigger than available memory requires

$$- 2 * B(f) \text{ I/O reads} + 2 * B(f) \text{ I/O writes}$$

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## Bottleneck is the Merge Phase

- Given RAM,  $M$
- Can't have more [temporary] sorted chunks  
than  $B(M) - 1$ , // number of page buffers + 1 for output
- How big is each chunk?  
 $M$
- So we can sort  $\sim B(M) * M$

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## Suppose 4 GBytes of RAM

- 4 Kbyte pages [buffers]
- $B(M) = 4\text{GB}/4\text{KB} = \underline{\hspace{2cm}}$

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