# B+ Tree's: Primary method for managing data on disks (in RDBMS)

Objective: Understand the implications disk access on the design of data structures.

- fat fanout
- split/promote

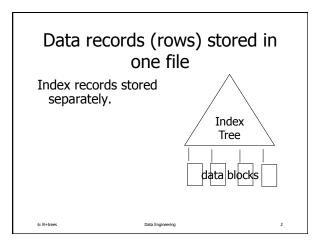
### Reading:

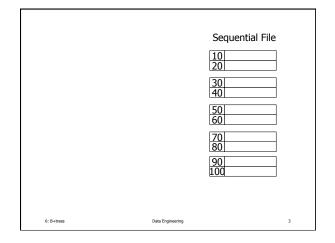
- Text Ch. 14
- · For very helpful interactive demo, see

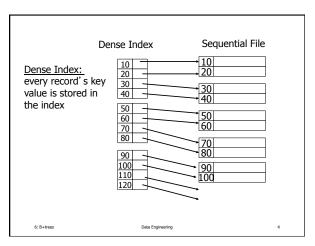
https://www.cs.usfca.edu/~galles/visualization/BPlusTree.html
Slide thanks: many slides, Garcia-Molina, (but you may want to see his original
set), http://infolab.stanford.edu/~hector/cs245/notes.htm

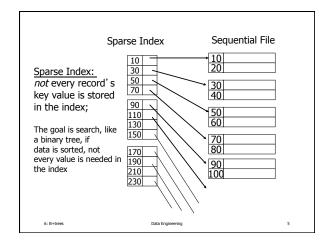
6: B+trees

Data Engineerin









## Sparse vs. Dense Tradeoff

- Sparse: Less index space per record can keep more of index in memory
- Dense: Can tell if any record exists without accessing file

### (Later:

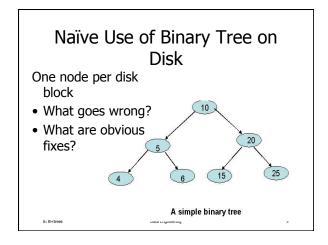
- sparse better for insertionsdense needed for secondary indexes)

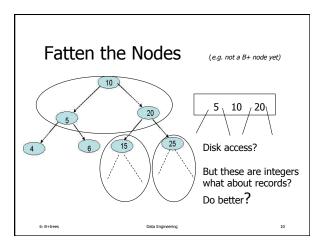
## Terms

- Index sequential file
- Search key ( ≠ primary key)
- Primary index (on Sequencing field)
- Secondary index
- Dense index (all Search Key values in)
- Sparse index
- Multi-level index

## The B+ Tree

- Main memory binary trees evolved to
- First there were B Trees
- Then B+ Trees.
  - So superior, B Trees are gone,
    - So gone, we say B Trees and mean B+ Tree



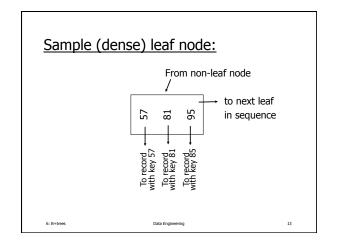


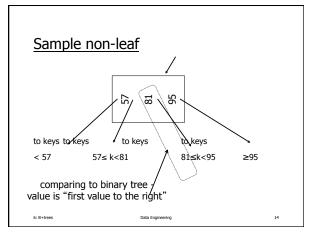
# In databases

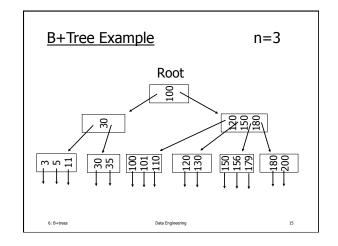
- We like algorithmic complexity (why?)
- But we don't really get to throw away the constants, etc.

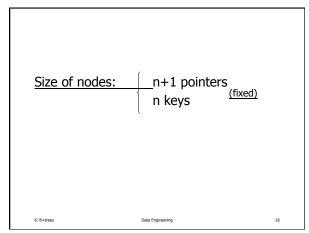
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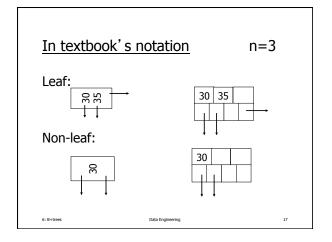
# In the index, store only search keys, not the records • Fatter fanout - more space for split keys • All the data is in the data file. • (if dense index, all keys are in the index) This is the primary difference between, B and B+ trees











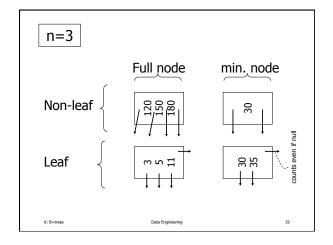
# Don't want nodes to be too empty

• Use at least

Non-leaf:  $\lceil (n+1)/2 \rceil$  pointers

Leaf:  $\lfloor (n+1)/2 \rfloor$  pointers to data

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## B+tree rules

- (1) All leaves at same lowest level (balanced tree)
- (2) Pointers in leaves point to records except for "sequence pointer"

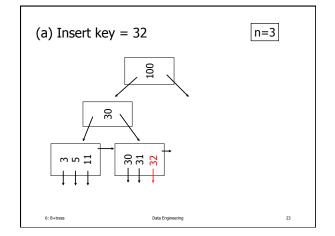
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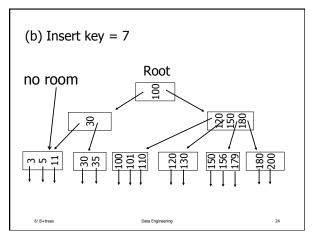
# (3) Number of pointers/keys for B+tree

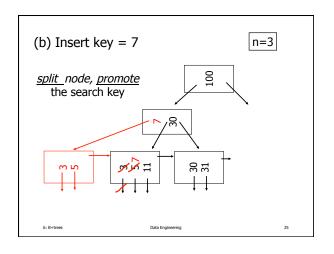
	Max ptrs	Max keys	Min ptrs→data	Min keys
Non-leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]- 1
Leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]
Root	n+1	n	1	1

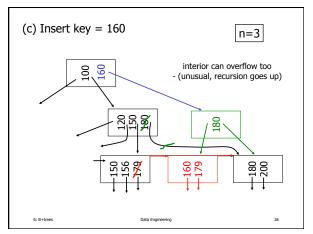
# Insert into B+tree

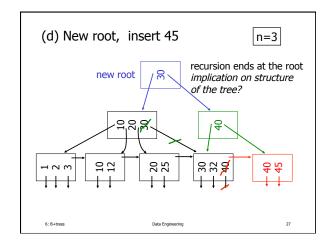
- (a) simple case
   space available in leaf
- (b) leaf overflow
- (c) non-leaf overflow
- (d) new root

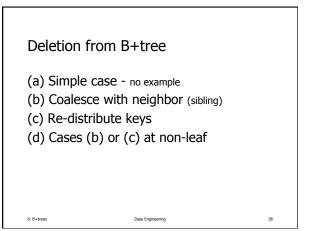


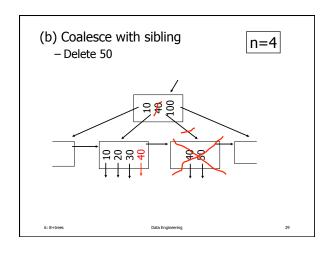


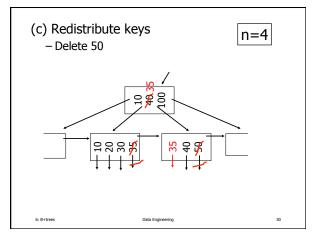


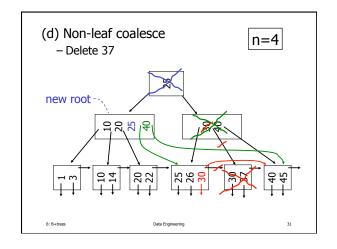


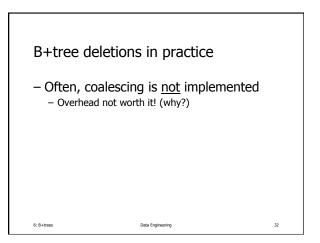








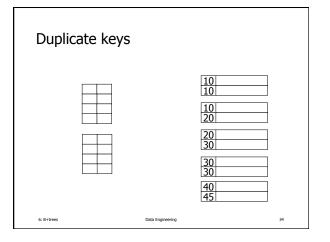


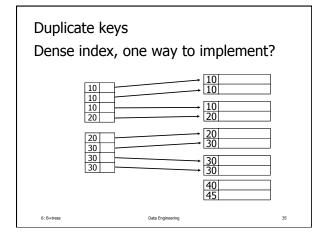


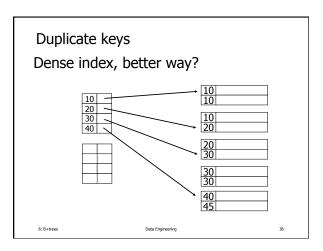
# Next:

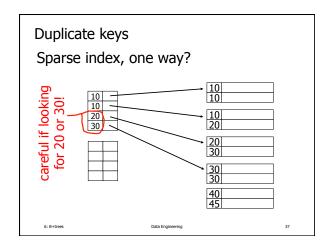
- Duplicate keys
- Deletion/Insertion
- Secondary indexes

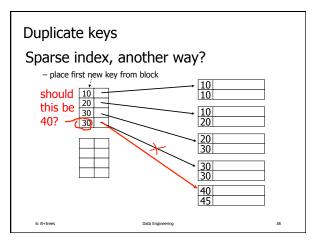
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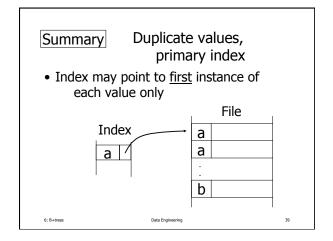












# Primary vs. Secondary Index • Primary is sorted on the index key and placed on disk that way • Secondary index, – does not "cluster" – consider (x, y)

