# Mathematics & Computer Science

(Image Processing, Computer Vision, Intelligent System)

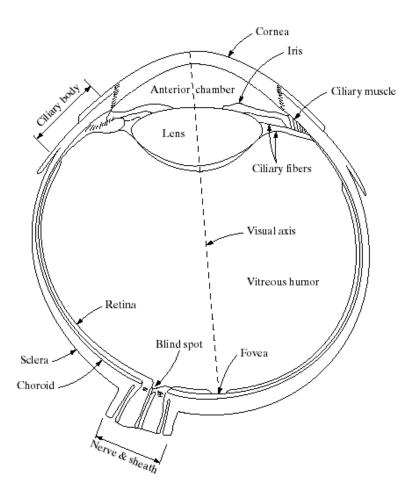


FIGURE 2.1 Simplified diagram of a cross section of the human eye.

Structure of Human Eye

FIGURE 2.3
Graphical representation of the eye looking at a palm tree. Point *C* is the optical center of the lens.

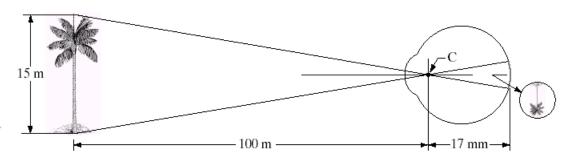
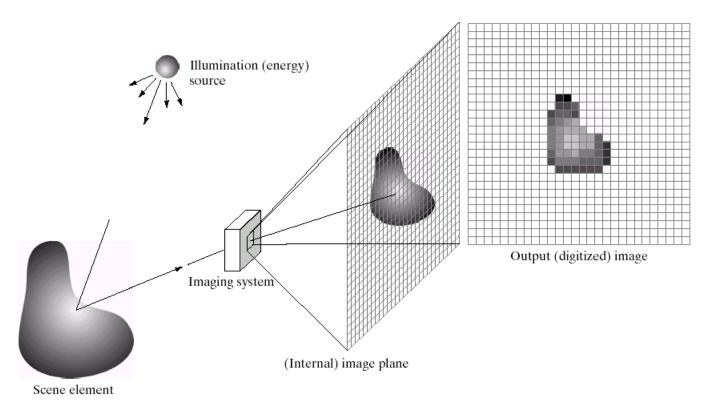


Image Formation in Human Eye

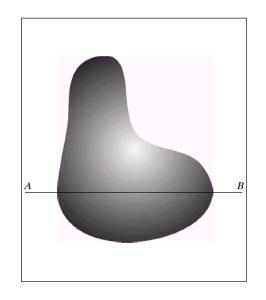


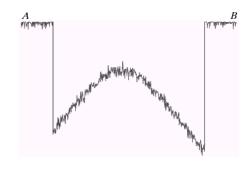
a c d e

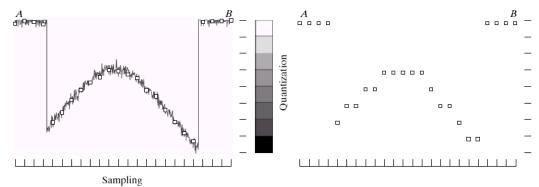
**FIGURE 2.15** An example of the digital image acquisition process. (a) Energy ("illumination") source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

#### Digital Image Formation

Image Sampling & Quantization

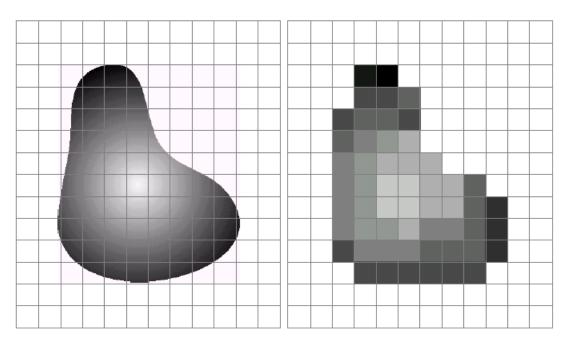








**FIGURE 2.16** Generating a digital image. (a) Continuous image. (b) A scan line from A to B in the continuous image, used to illustrate the concepts of sampling and quantization. (c) Sampling and quantization. (d) Digital scan line.



a b

**FIGURE 2.17** (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.

Digital Image

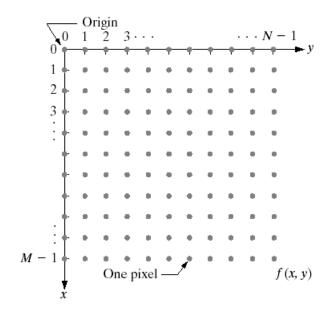


FIGURE 2.18

Coordinate convention used in this book to represent digital images.

Digital Image Representation



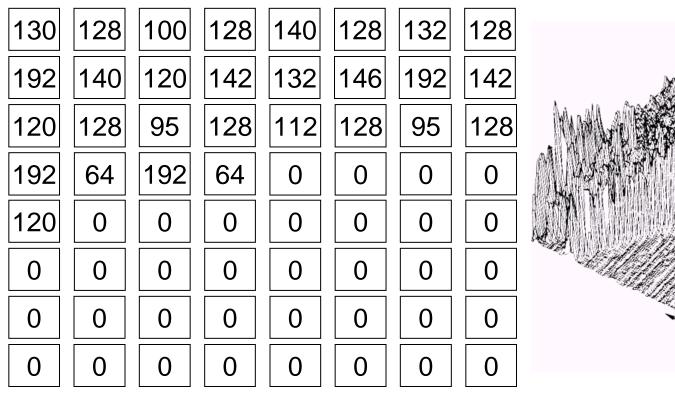
Image

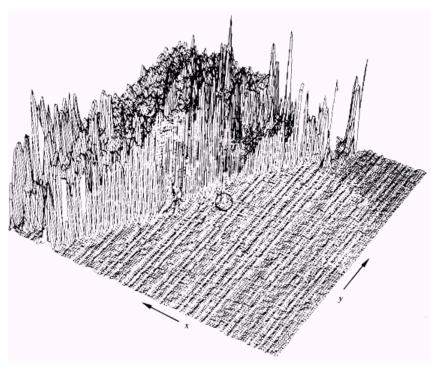


Image

130	128	100	128	140	128	132	128
192	140	120	142	132	146	192	142
120	128	95	128	112	128	95	128
192	64	192	64	0	0	0	0
120	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

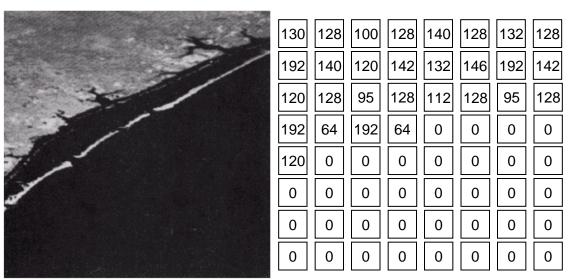
Matrix





Matrix

f(x, y)



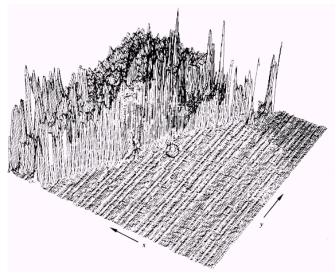


Image Matrix f(x, y)



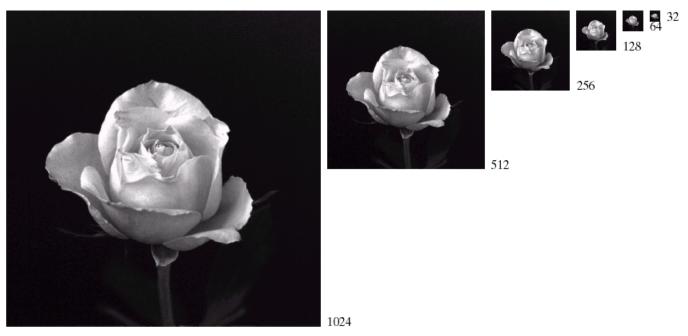
Digital Image



**FIGURE 2.19** A 1024  $\times$  1024, 8-bit image subsampled down to size 32  $\times$  32 pixels. The number of allowable gray levels was kept at 256.

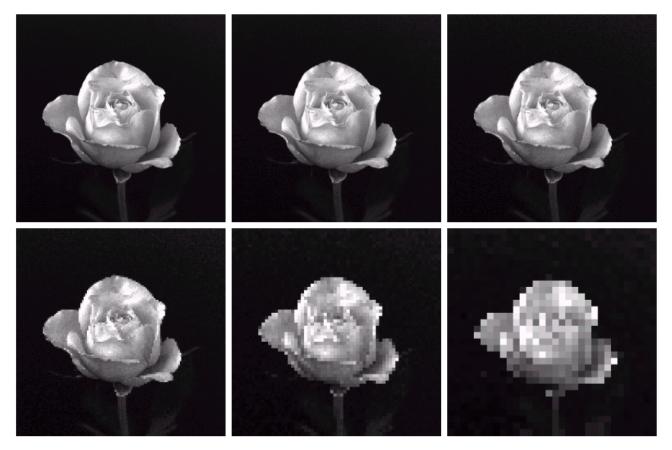
Digital Image Resizing (Shrinking)

How can we reduce size (shrink) of a digital image?



**FIGURE 2.19** A 1024  $\times$  1024, 8-bit image subsampled down to size 32  $\times$  32 pixels. The number of allowable gray levels was kept at 256.

How can we enlarge a digital image?

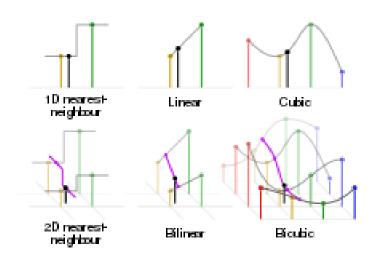


abc def

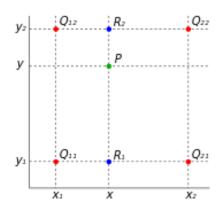
**FIGURE 2.20** (a)  $1024 \times 1024$ , 8-bit image. (b)  $512 \times 512$  image resampled into  $1024 \times 1024$  pixels by row and column duplication. (c) through (f)  $256 \times 256$ ,  $128 \times 128$ ,  $64 \times 64$ , and  $32 \times 32$  images resampled into  $1024 \times 1024$  pixels.

#### Digital Image Resizing (zooming)

#### **Digital Image Resizing Functions**



#### Digital Image Resizing (zooming) by Bilinear Interpolation



The four red dots show the data points and the green dot is the point at which we want to interpolate.

$$f(x,y) \approx a_0 + a_1 x + a_2 y + a_3 x y$$

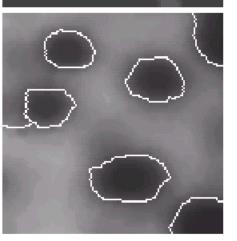
$$\begin{bmatrix} 1 & x_1 & y_1 & x_1 y_1 \\ 1 & x_1 & y_2 & x_1 y_2 \\ 1 & x_2 & y_1 & x_2 y_1 \\ 1 & x_2 & y_2 & x_2 y_2 \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \\ a_3 \end{bmatrix} = \begin{bmatrix} f(Q_{11}) \\ f(Q_{21}) \\ f(Q_{22}) \end{bmatrix}$$
the four red dots show the

Object Recognition

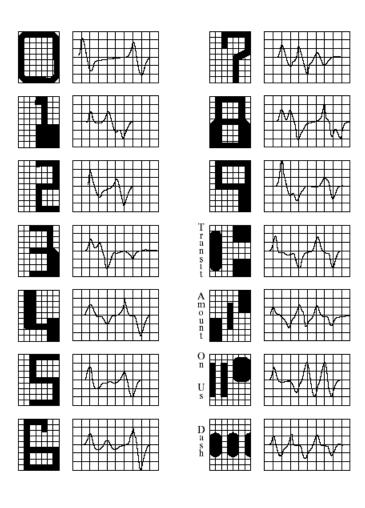
a b

#### **FIGURE 10.46**

(a) Image of blobs. (b) Image gradient. (c) Watershed lines. (d) Watershed lines superimposed on original image. (Courtesy of Dr. S. Beucher, CMM/Ecole des Mines de Paris.)



Detect Boundary & Compute Area



#### FIGURE 12.7

American Bankers Association E-13B font character set and corresponding waveforms.

#### **Digit Recognition**