

PSTAT 174/274 Fall 2024 – Lab Assignment 4

Due by midnight (11:59pm) on November 27(Wednesday), 2024.

1. Modelling Global Temperature We consider the *gtemp_ocean* data from the *astsa* package. Our aim is to fit an appropriate $ARIMA(p, d, q)$ model and to evaluate our model's performance using residual diagnostics before constructing a 10 year ahead forecast.

1. Using the following code to load the data and produce a time series plot. Is the data stationary? Comment on any possible linear or seasonal trends and how best to remove them.

```
library(astsa)
plot.ts(gtemp_ocean)
```

2. Difference the data lag 1 and produce a new time series plot. Does the data now appear stationary? You may want to use the function `diff(,)`.
3. Produce both an ACF and a PACF of the differenced data and comment on your observations. What potential $ARIMA(p, d, q)$ models do they suggest? (Hint: Recall that the d parameter just indicates how many times we needed to differencing to obtain stationarity.)
4. This time use the `sarima()` function from the *astsa* package to fit your selected ARIMA model.
5. Using our final model produce a 20 year ahead forecast for global temperature using the `sarima.for()` function from *astsa* package. Comment on your forecast.

2. Modelling AirPassengers In this question we shall be analyzing the *AirPassengers* data set from the *astsa* package. Our aim is to determine an appropriate model from the SARIMA family.

1. Begin by producing a time series plot of the data using the `plot.ts()` function. Note your observations about any trends, seasonality and stationarity (is the variance constant?).
2. We investigate possible transformations to obtain a stationary time series on which we can consider potential SARIMA models. Use the following codes to compute 3 transformed time series:
 - (1) `log.data` taking the natural log of the data;
 - (2) `dlog.data` taking the difference (lag 1) of the log data; and
 - (3) `ddlog.data` taking the difference (lag 12) of the differenced log data.

```
# computing transformed series
log.data <- log(AirPassengers)
dlog.data <- diff(log.data, 1)
ddlog.data <- diff(dlog.data, 12)
```

Create a matrix of all four series called **plot.data** using the **cbind()** function and use **plot.ts()** to produce our combined plot.

3. We continue our data exploration by producing both an ACF and PACF plot for our twice differenced log data using the **acf2()** function. Note your observations about the significant spikes in autocorrelation and partial autocorrelation.
4. Let us first consider a non-seasonal ARMA(1,1) model which we fit using the **sarima()** function (this time fitting the model to the twice differenced log data).
5. Use your ACF and PACF plot above to suggest possible parameters for the parameters SARIMA(p, d, q)(P, D, Q) s . Consider two potential models and fit each in turn using the **sarima()** function.
6. Produce a 24 month ahead forecast for our data using the **sarima.for()** function. Does our forecast appear reasonable?