

EN4720: Security in Cyber-Physical Systems

Exercise — Encryption and Hashing

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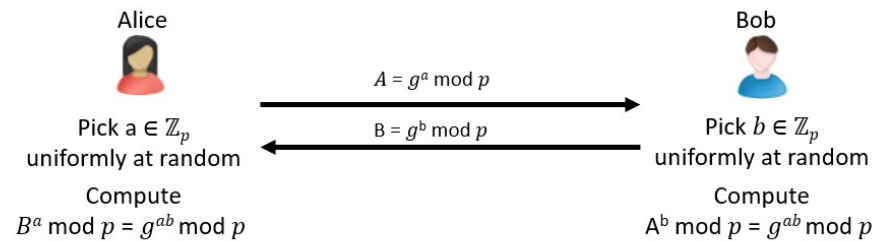
This is an individual exercise!
Due Date: 21 April 2022 by 11.59 PM

Problem 1 - Symmetric Encryption & Key Exchange

Alice and Bob are using the Diffie-Hellman protocol as shown in Figure 1. They want to extend their key exchange mechanism to include their friend Charlie.

- **Setup:**

- Prime p , generator g of \mathbb{Z}_p^* (public parameters)



- **Alice and Bob can use as shared key:**

- $X = g^{ab} \bmod p$

Figure 1: Diffie Hellman Protocol

1. Design an extension of the Diffie-Hellman protocol to allow secure key exchange between the three parties.

The below method can be used to extend the DH protocol to share a common key between three parties. The method is graphically represented in the Figure 2 as well. The answer was adopted from <https://crypto.stackexchange.com/a/1027>

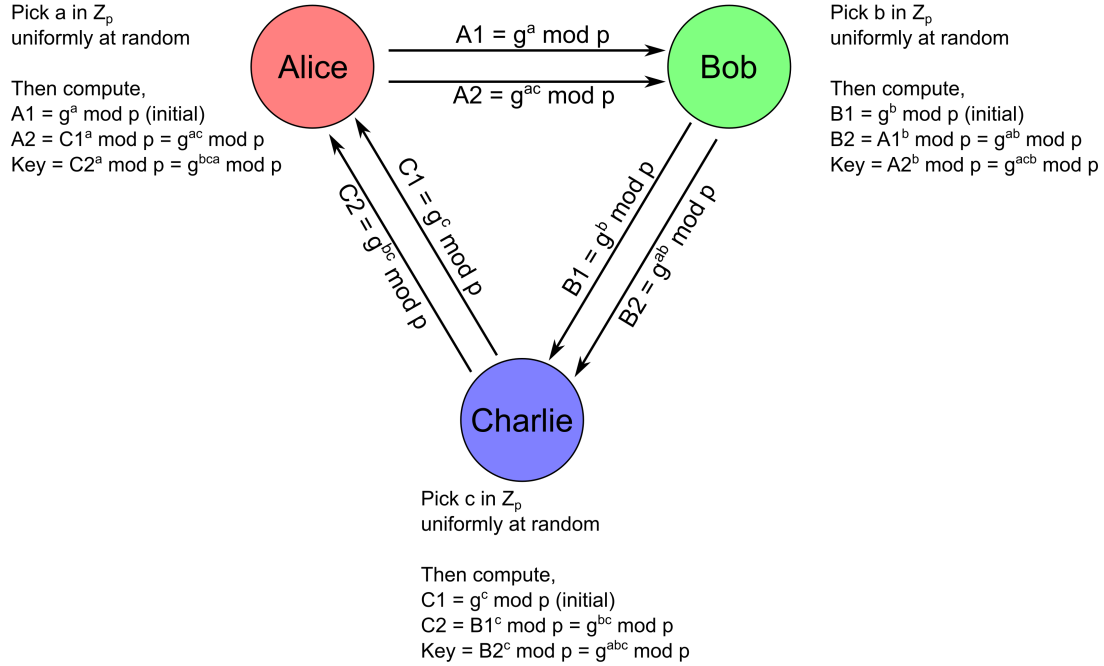


Figure 2: Extended Diffie-Hellman Protocol for three parties to share a common key

- (a) Alice, Bob and Charlie each picks a random number from the chosen multiplicative group (\mathbb{Z}_p). Let those numbers be a , b and c respectively, and Alice, Bob and Charlie are in a loop as shown in the Figure 2.
- (b) Initially each party computes $Init_{val} = g^i \bmod p$ (**A1**, **B1**, **C1** in the Figure 2), for their selected i where $i \in \{a, b, c\}$ and passes to the next person in the loop.
- (c) Upon receiving an $Init_{val}$ from the previous party of the loop, each party again computes $Inter_{val} = Init_{val}^i \bmod p$, (**A2**, **B2**, **C2** in the Figure 2) and passes to the next person in the loop.
- (d) Finally, upon receiving the $Inter_{val}$ from the previous party, each party calculates $Key_{val} = Inter_{val}^i \bmod p$ (**Key** in the Figure 2), which becomes the common key between the three parties.

The key will take the form $g^{abc} \bmod p$ after the above described process and will be a common key that can be used among the three parties for information encryption and decryption.

2. Alice, Bob, and Charlie are planning to use $(p, g) = (23, 9)$ to agree on a key for a Caesar cipher. Assume that the Caesar cipher is right shifting the number of letters equal to the key to produce the ciphertext (e.g., if the key is 5 and the plaintext letter is U, it will be replaced by Z in the ciphertext). Assuming 4, 7, and 13 to be secret exponents of Alice, Bob, and Charlie respectively, find the common key that they need to use in Caesar's cipher.

$$\begin{aligned} \text{Key} &= g^{abc} \bmod p \\ &= 9^{4 \times 7 \times 13} \bmod 23 \\ &= 9 \end{aligned}$$

3. Derive the encrypted message for the message "Hello" using the above encryption key. Show all the major steps in deriving the answer.

- (a) *Since the key is 9, each letter in the original message is right shifted by 9 letters to produce the Caesar cipher.*
- (b) *Assume there is no requirement to preserve the case sensitivity of the message. Then the message is "HELLO"*
- (c) *Now for each letter in the word, replace it by the letter 9 slots to its right. Then 'H' is replaced by 'Q', 'E' is replaced by 'N', 'L' is replaced by 'U' and 'O' is replaced by 'X'.*
- (d) *Then the ciphertext will be "QNUUX".*

Problem 2 - Symmetric Encryption - Security Analysis

For this part of the exercise you are required to install [CrypTool](#). CrypTool is a software tool that comes with several encryption techniques.

Instructions

1. Create a text file named “**sampletext.txt**” in your computer. Add the text “EN4720: This is a sample text file for encryption.” to the text file and save it.
2. Open the “**sampletext.txt**” file with CrypTool software.
3. Encrypt your message with RC2 encryption following **Encrypt/Decrypt >Symmetric (modern) >RC2**. Choose key size of 8 bits and add some random hexadecimal key to encrypt your text file. (Add screenshots)
4. Run brute force analysis of the encrypted message by following **Analysis >Symmetric Encryption (modern) >RC2**. (Add screenshots)
5. Repeat steps 3,4 for the key sizes 16, 24, 64, and 128 bits.
6. Answer the questions given below.

Questions

1. Add screenshots requested in Step #3.

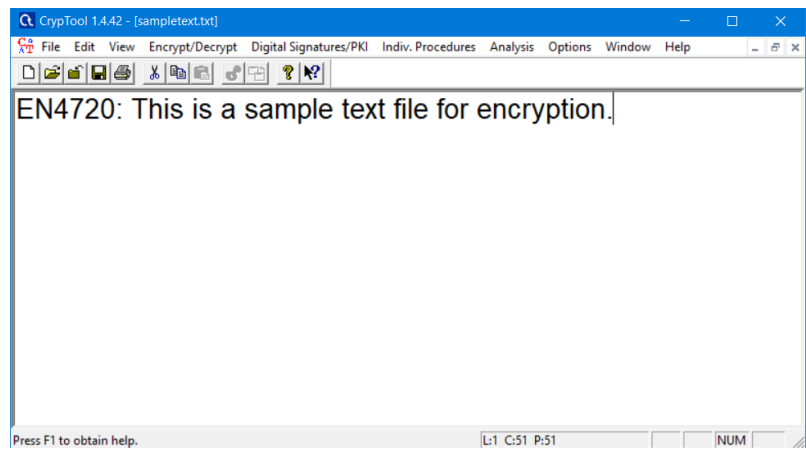


Figure 3: Open the *sampletext.txt* file using the CrypTool software

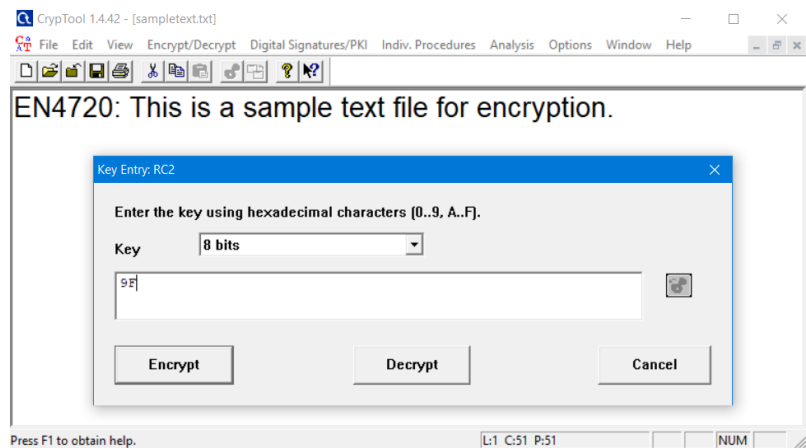


Figure 4: Enter the 8 bit Hexadecimal key for encryption

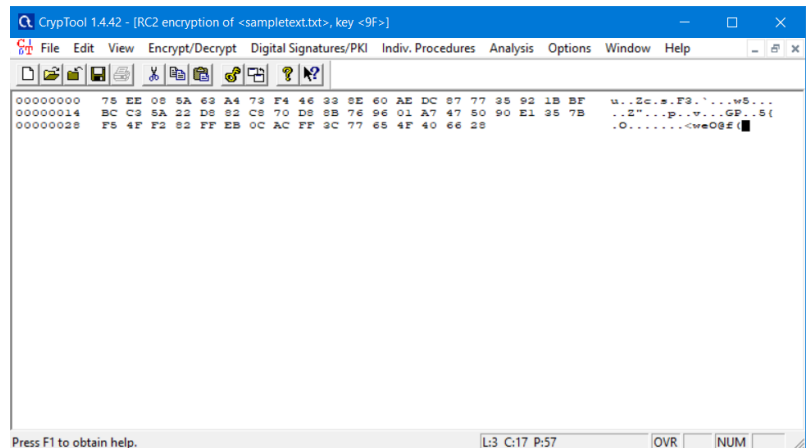


Figure 5: Encrypted text using the selected key

2. Add screenshots requested in Step #4.

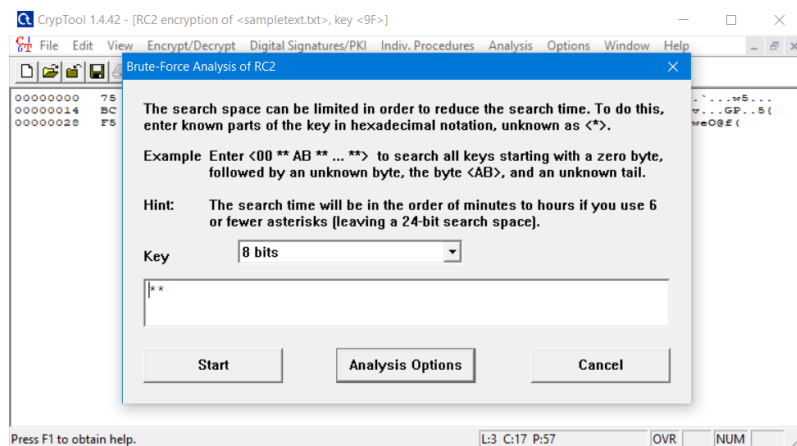


Figure 6: Configure the Brute Force analysis of RC2

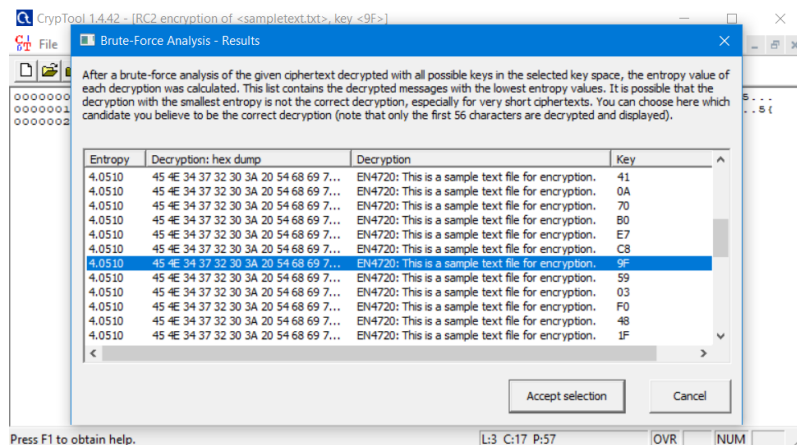


Figure 7: All possible keys obtained through the Brute Force attack

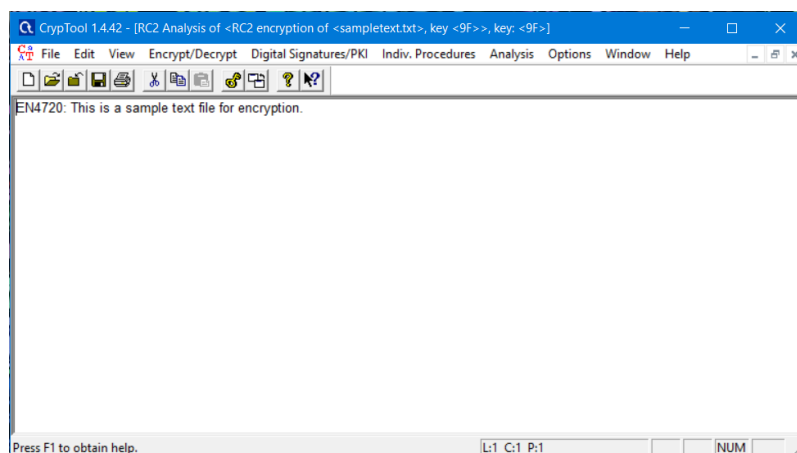


Figure 8: Decrypted message

3. Complete Table 1.

Table 1: Time taken to brute force

Key length (bits)	Time to brute force	Maximum number of keys
8	< 1 s	33
16	< 1 s	1
24	1 min 34 s	1
64	3.8×10^6 years	None
128	7.5×10^{25} years	None

4. What is the impact of key length on time to decrypt a message using brute force?

When the key length is increased, time to decrypt the message grows drastically

5. What could be done to diminish the amount of time required to perform the attack?

- Guess some of the characters or enter the known parts in the key and fix them, rather than letting computer to perform every possible combination of the characters. This limits the search space of keys.*
- Carry out the decryption in parallel using several computers.*

Problem 3 - Public Key Encryption

You are given that $n = 65$ and $\phi(n) = 48$ for a certain RSA scheme.

1. Calculate the private key d assuming the public key $e = 7$.

*d , takes the form $1 = e * d \bmod \phi = 7 * d \bmod 48$ and it can be calculated using the Extended Euclidean Algorithm. The steps are given below.*

(a) Euclidean Algorithm

$$48 = 6 * (7) + 6$$

$$7 = 1 * (6) + 1$$

(b) Back Substitution

$$1 = 7 - 1 * (6)$$

$$1 = 7 - 1 * (48 - 6 * (7))$$

$$1 = 7 * (7) - 1 * (48)$$

(c) The coefficient in front of the $e = 7$, is the required d . Therefore $d = 7$.

2. Show all major steps of encryption and decryption using textbook RSA for the message given below. Specifically, derive the ciphertext and show that the plaintext can be recovered at the receiver after decrypting.

m = last digit of your index number (e.g., if the index number is 180234N, $m = 4$). If the last digit is 0 (zero) or 1 (one), use $m = 5$.

(a) Encryption for $m = 5$ since last digit of index number is 1.

$$\text{ciphertext} = m^e \bmod n$$

$$= 5^7 \bmod 65$$

$$= 60 \quad \because (5^7 = 1201 * 65 + 60)$$

(b) Decryption

$$\text{plaintext} = c^d \bmod 65$$

$$= 60^7 \bmod 65$$

$$= \{(60^2 \bmod 65) * (60^2 \bmod 65) * (60^2 \bmod 65) * (60^1 \bmod 65)\} \bmod 65$$

$$= \{(25) * (25) * (25) * (60)\} \bmod 65$$

$$= 5 \quad \because (25^3 * 60 = 14423 * 65 + 5)$$

\therefore the plaintext can be recovered at the receiver after decrypting.

3. Find the candidates for the primes p, q that were used to generate this RSA scheme.

*(a) 48 can be written as, $48 = 12 * 4$*

*(b) 65, can be written as, $65 = (12 + 1) * (4 + 1)$*

\therefore the used prime factors to generate n , are 13 and 5.

4. Suppose that c is the ciphertext that you find above for the message m . Show how an attacker can recover the plaintext message m from the ciphertext c assuming that he can request a decryption of a single ciphertext $c' \neq c$.

Problem 4 - Hash Functions

For this part of the exercise you are required to install [Kali Linux](#). Kali Linux comes preinstalled with several hashing utilities. These include **md5sum**, **sha1sum**, **sha256sum**, and **sha512sum**. Follow the given instructions to complete the problem.

Instructions

1. Create a new directory and a new text file “**originalhashfile**” in the directory using **nano originalhashfile** command. Add the text “EN4720: Some text here” in the created file and save the file using the hotkey **CTRL+X** followed by **Y** and **Enter**.
2. Run the *ls* command in the directory to show the file (add screenshot) and run the *cat* command to show the contents of the created file (add screenshot).
3. calculate the hash digest of the **originalhashfile** using these hash algorithms: MD5, SHA1, SHA256, SHA512 (add screenshots). Add your observations in Table [2](#). You can use the following commands to get the results.
 - `md5sum <hashfile_name>`
 - `sha1sum <hashfile_name>`
 - `sha256sum <hashfile_name>`
 - `sha512sum <hashfile_name>`
4. Change the contents of the **originalhashfile** by adding your index at the end of the line (“EN4720: Some text here <index_no>”) and save it as “**modifiedhashfile**” in the same directory.
5. Run the *ls* command in the directory to show the files (add screenshot) and run the *cat* command to show the contents of the modified file (add screenshot).
6. Calculate the hash digest of the **modifiedhashfile** using these hash algorithms: MD5, SHA1, SHA256, SHA512 (add screenshots). Add your observations in Table [3](#).
7. Answer the questions given below.

Questions

1. Add screenshots requested in Step #2.

Your answer here

2. Complete Table 2. Add screenshots requested in Step #3 below the table.

Table 2: Hash digests of the original file

Hash Algorithm	Hash of the Original File
MD5	
SHA1	
SHA256	
SHA512	

3. Among the hash algorithms used, which one is the most cryptographically secure? Justify your answer.

Your answer here

4. Why is MD5 not considered as a reliable hashing algorithm?

Your answer here

5. Which of the algorithms fall under the category of SHA-2?

Your answer here

6. Add screenshots requested in Step #5.

Your answer here

7. Complete Table 3. Add screenshots requested in Step #6 below the table.

Table 3: Hash digests of the modified file

Hash Algorithm	Hash of the Modified File
MD5	
SHA1	
SHA256	
SHA512	

8. Comparing the output from one algorithm in Table 2 and Table 3, is there a difference between the hash digests? If yes, why?

Your answer here