

# Basics of QCD: jets & jet substructure

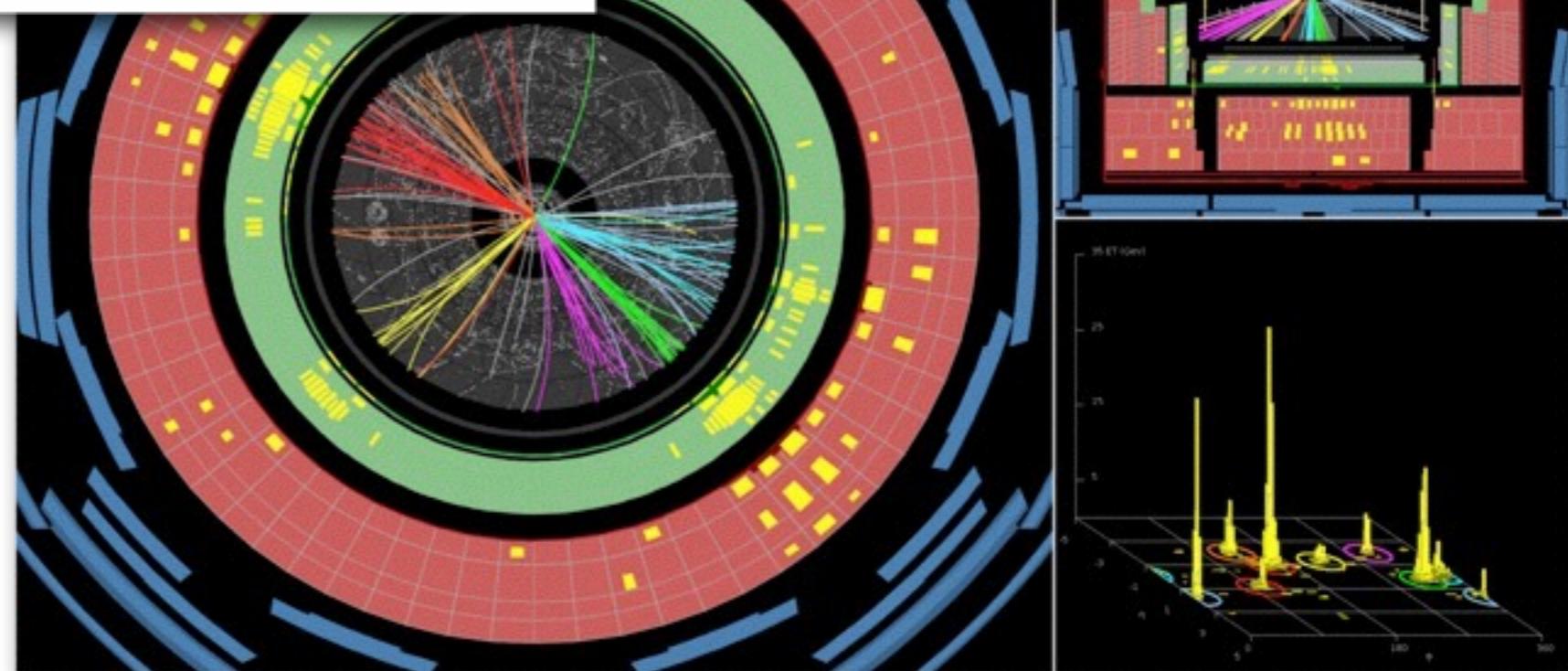
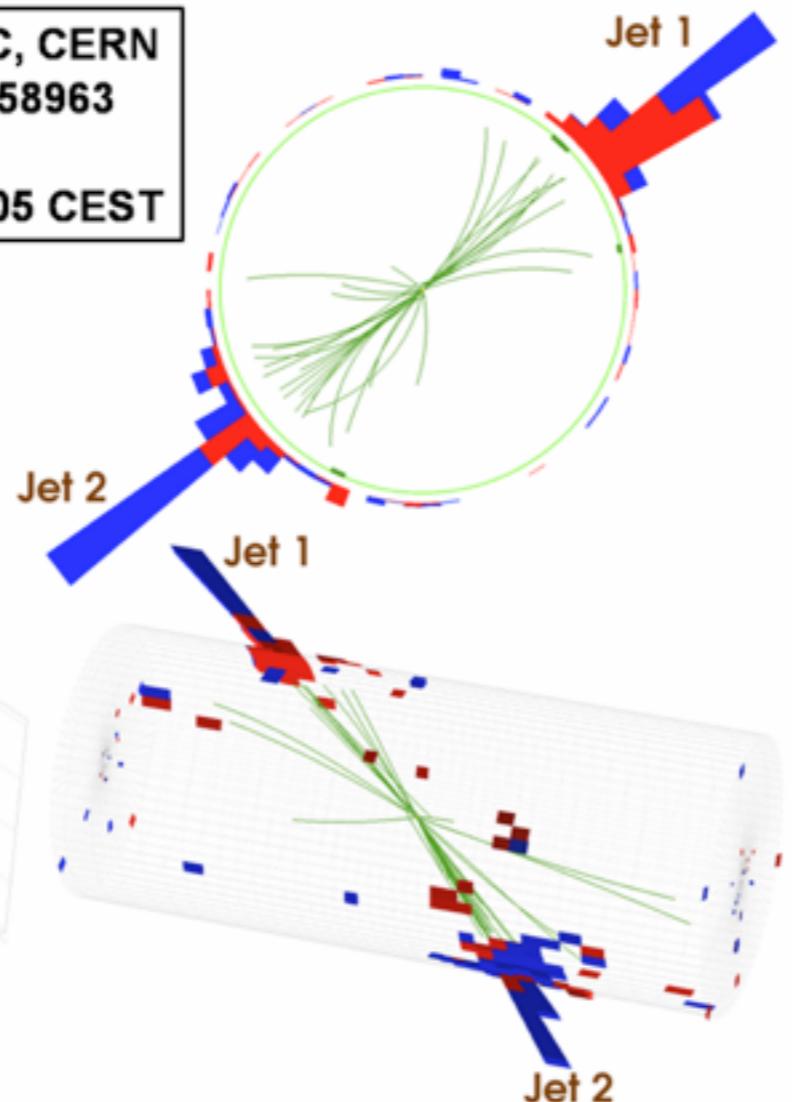
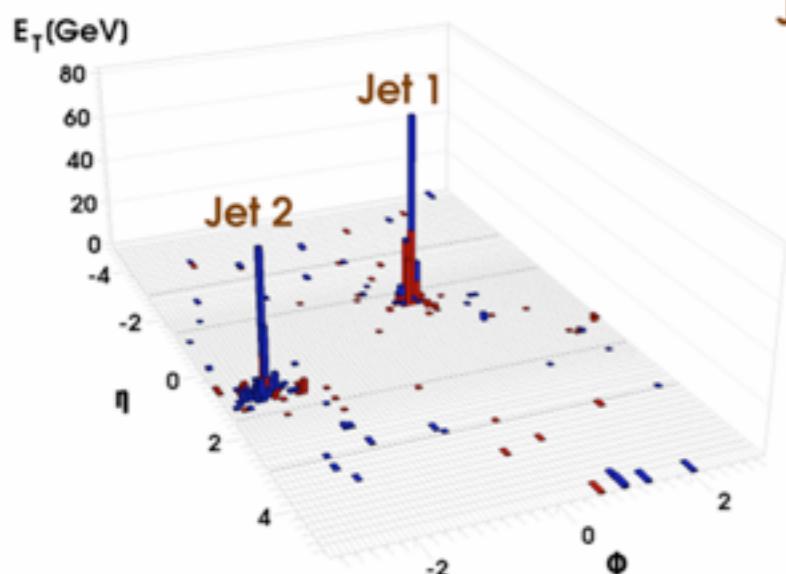
Gavin Salam (CERN)

with extensive use of material  
by Matteo Cacciari  
and Gregory Soyez

ICTP–SAIFR school on QCD and LHC physics  
July 2015, São Paulo, Brazil



CMS Experiment at LHC, CERN  
Run 133450 Event 16358963  
Lumi section: 285  
Sat Apr 17 2010, 12:25:05 CEST



**JETS**  
Collimated,  
energetic bunches  
of particles

# Find all papers by ATLAS and CMS

850 records found

reportnumber:CERN-PH-EP and (collaboration:ATLAS or collaboration:CMS)

Brief format

Search

[Easy Search](#)  
[Advanced Search](#)

[find j "Phys.Rev.Lett.,105"](#) :: [more](#)

Sort by:

Display results:

latest first desc. - or rank by 25 results single list

No exact match found for *cern-ph-ep*, using *cern ph ep* instead...

HEP

850 records found 1 - 25 ►► jump to record: 1

Search took 0.18 seconds.

## 1. Z boson production in $p + \text{Pb}$ collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ measured with the ATLAS detector

ATLAS Collaboration (Georges Aad (Marseille, CPPM) *et al.*). Jul 22, 2015. 19 pp.

CERN-PH-EP-2015-146

e-Print: [arXiv:1507.06232 \[hep-ex\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Detailed record](#)

## 2. Search for an additional, heavy Higgs boson in the $H \rightarrow ZZ$ decay channel at $\sqrt{s} = 8 \text{ TeV}$ in $pp$ collision data with the ATLAS detector

ATLAS Collaboration (Georges Aad (Marseille, CPPM) *et al.*). Jul 21, 2015. 46 pp.

CERN-PH-EP-2015-154

e-Print: [arXiv:1507.05930 \[hep-ex\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Detailed record](#)

## 3. Pseudorapidity distribution of charged hadrons in proton-proton collisions at $\text{sqrt}(s) = 13 \text{ TeV}$

CMS Collaboration (Vardan Khachatryan (Yerevan Phys. Inst.) *et al.*). Jul 21, 2015.

[CMS EPJ C 76 15001](#) | [CERN-PH-EP-2015-190](#)

# Pull out those that refer to one widely used jet-alg 538 records found

reportnumber:CERN-PH-EP and (collaboration:ATLAS or collaboration:CMS) and refersto:recid:779080 | Brief format | [Search](#) | [Easy Search](#) | [Advanced Search](#)  
[find](#) | "Phys.Rev.Lett.,105" :: [more](#)

Sort by:

Display results:

latest first | desc. | - or rank by - | 25 results | single list

> 60% of papers use jets!

No exact match found for *cern-ph-ep*, using *cern ph ep* instead...

HEP

538 records found 1 - 25 ►► jump to record: 1

Search took 0.18 seconds.

## 1. Search for an additional, heavy Higgs boson in the $H \rightarrow ZZ$ decay channel at $\sqrt{s} = 8$ TeV in $pp$ collision data with the ATLAS detector

ATLAS Collaboration (Georges Aad (Marseille, CPPM) et al.). Jul 21, 2015. 46 pp.

CERN-PH-EP-2015-154

e-Print: [arXiv:1507.05930 \[hep-ex\]](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Detailed record](#)

## 2. Summary of the searches for squarks and gluinos using $\sqrt{s} = 8$ TeV $pp$ collisions with the ATLAS experiment at the LHC

ATLAS Collaboration (Georges Aad (Marseille, CPPM) et al.). Jul 20, 2015. 91 pp.

CERN-PH-EP-2015-162

e-Print: [arXiv:1507.05525 \[hep-ex\]](#) | [PDF](#)

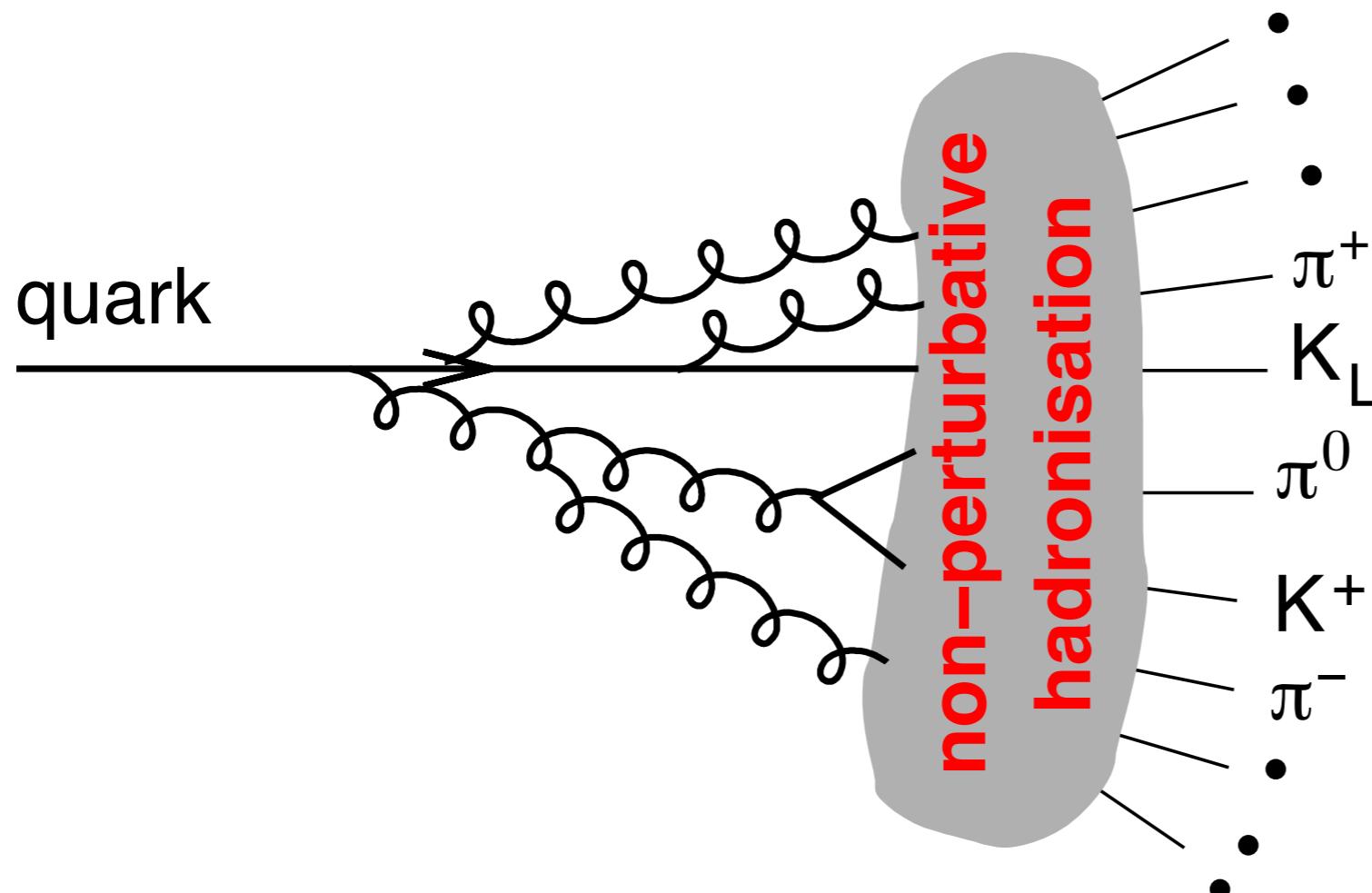
[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)  
[ADS Abstract Service](#)

[Detailed record](#) - Cited by 1 record

## 3. Search for photonic signatures of gauge-mediated supersymmetry in 8 TeV $pp$ collisions with the ATLAS detector

ATLAS Collaboration (Georges Aad (Marseille, CPPM) et al.). Jul 20, 2015. 43 pp.

# Why do we see jets?



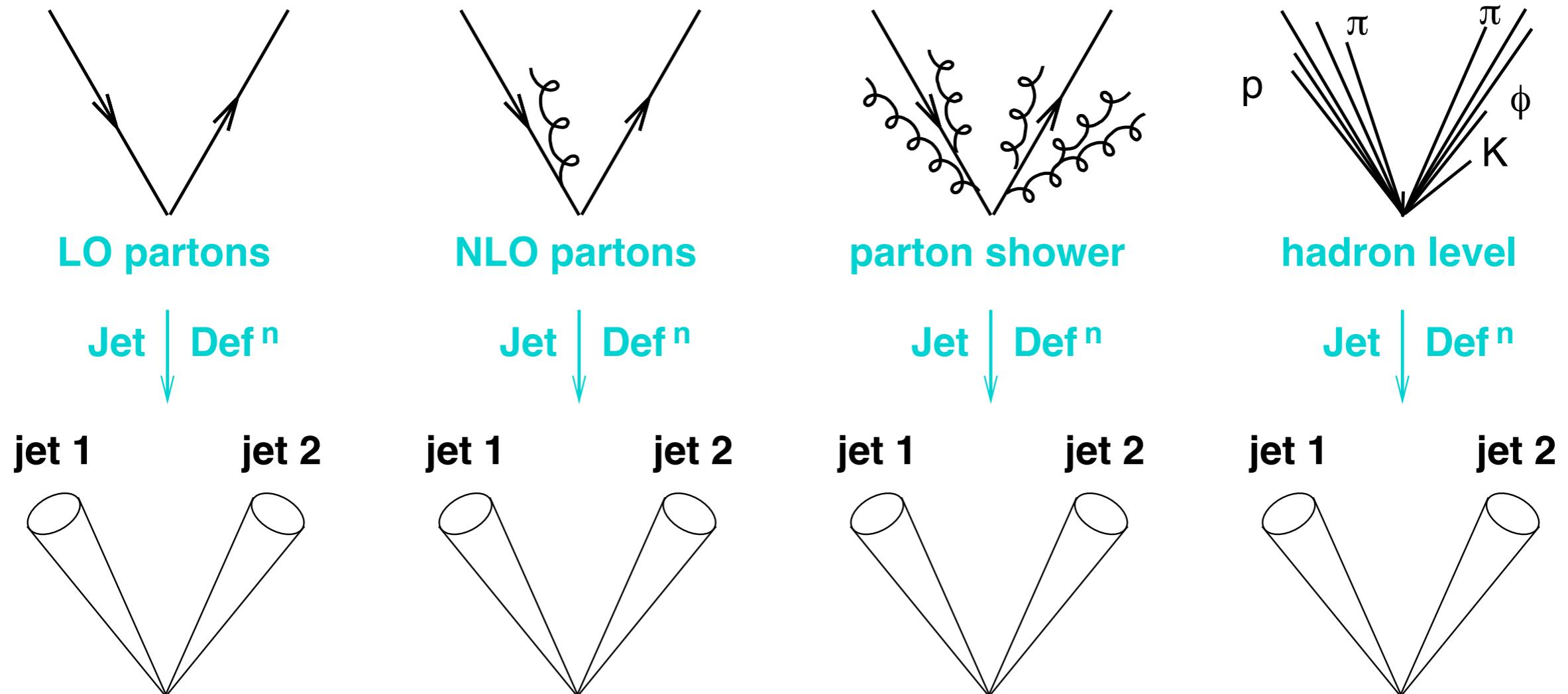
Gluon emission

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

Non-perturbative  
physics

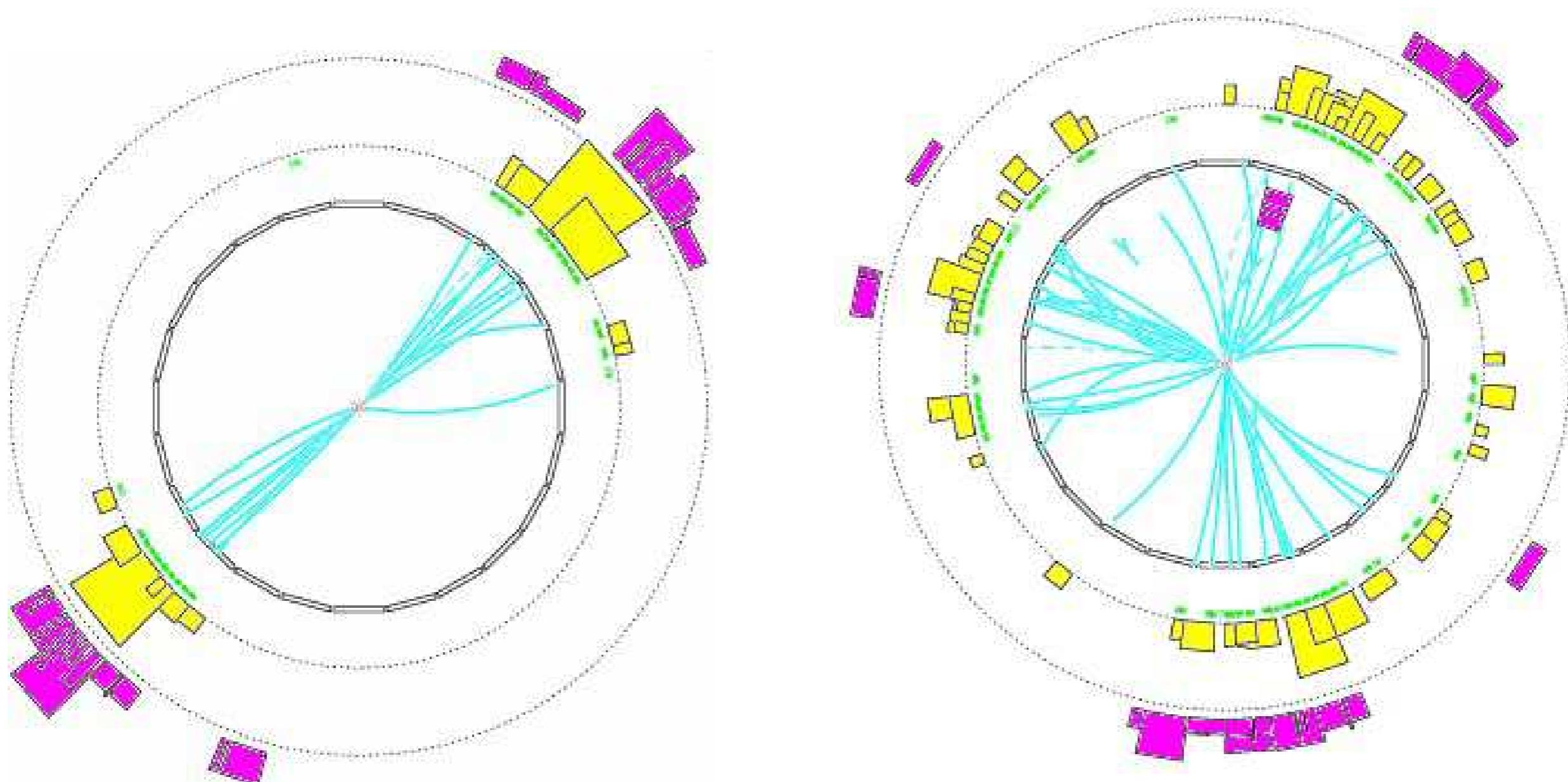
$$\alpha_s \sim 1$$

# Jet finding as a form of projection

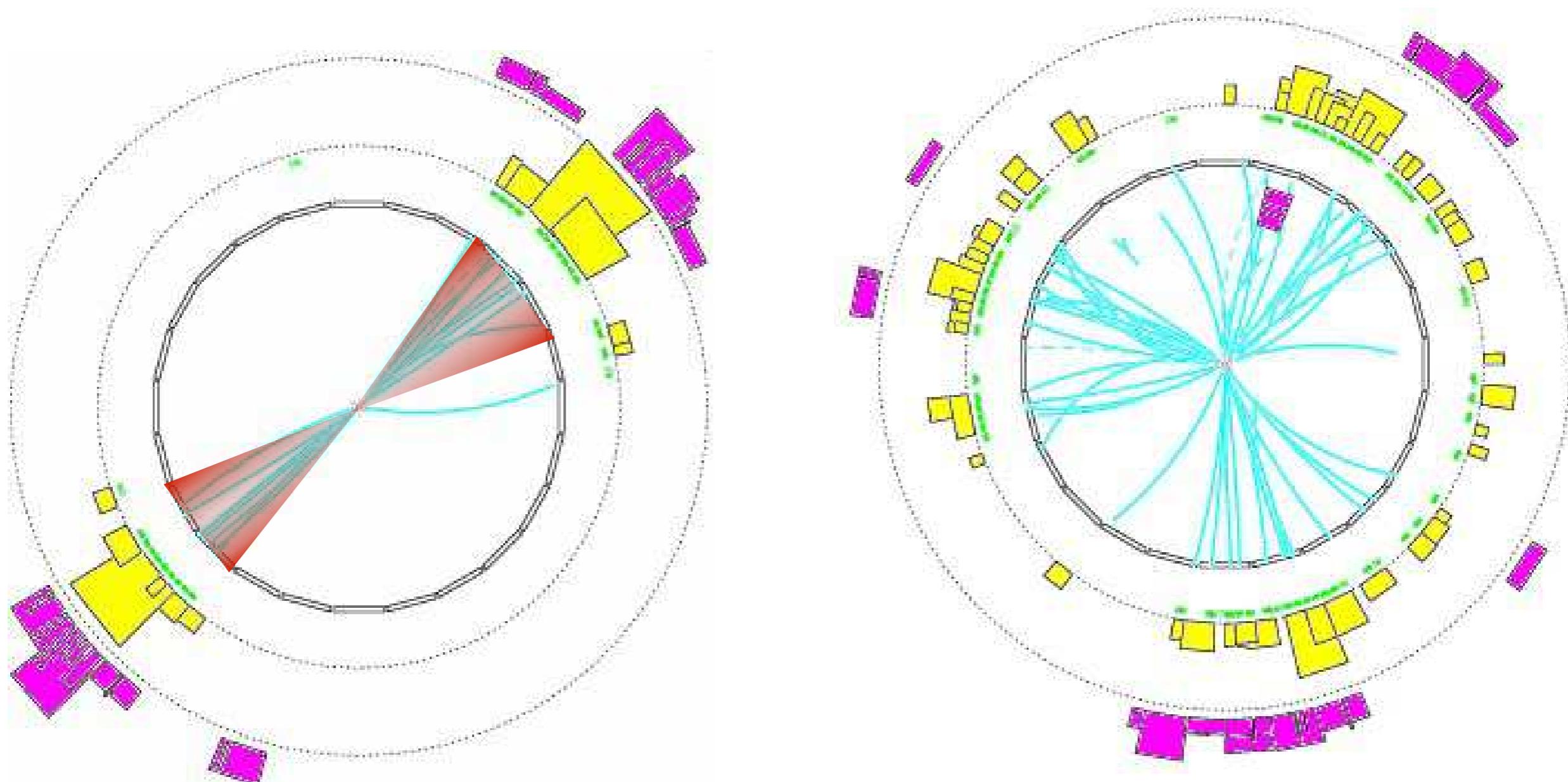


Projection to jets should be resilient to QCD effects

# Reconstructing jets is an ambiguous task

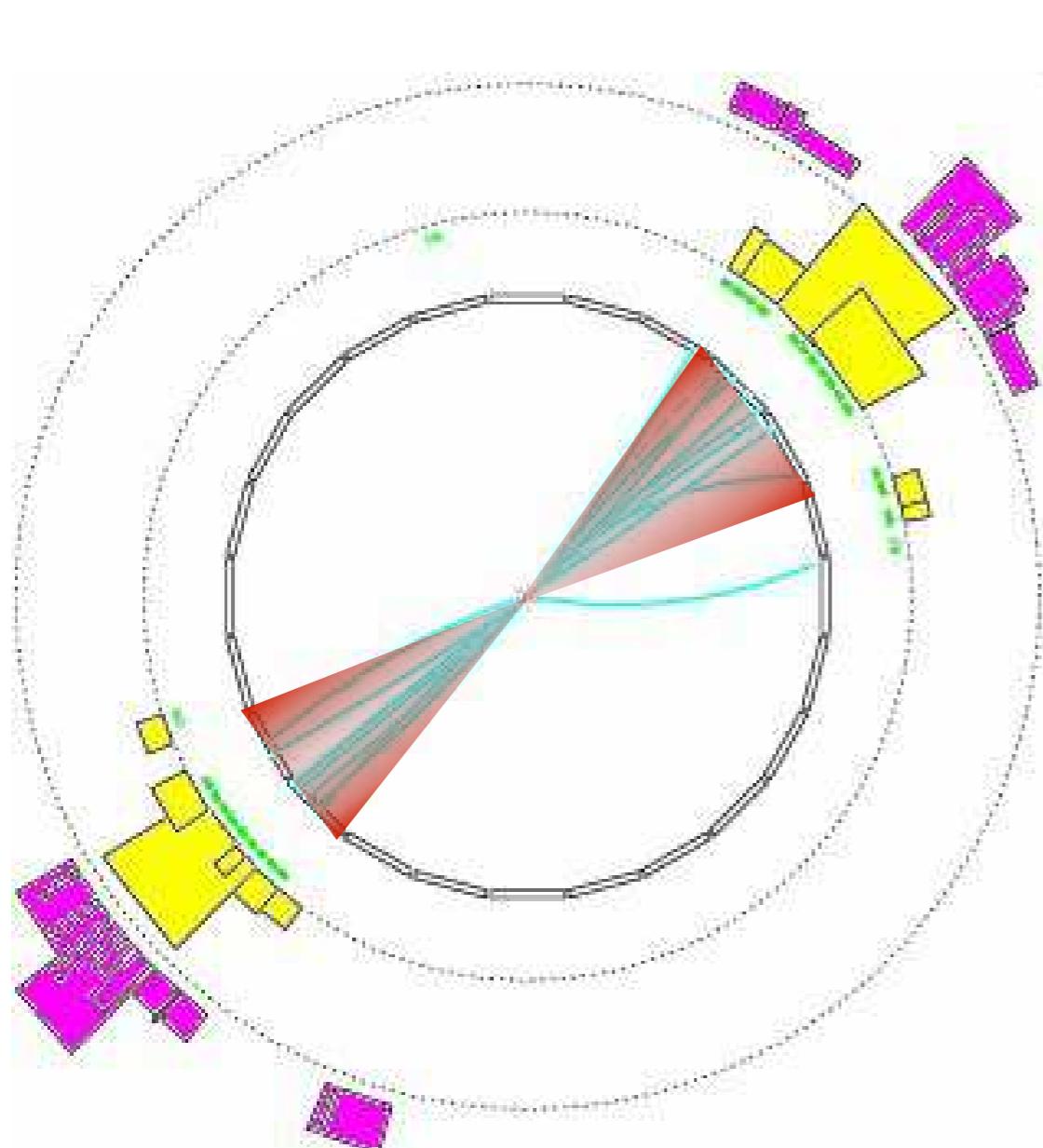


# Reconstructing jets is an ambiguous task

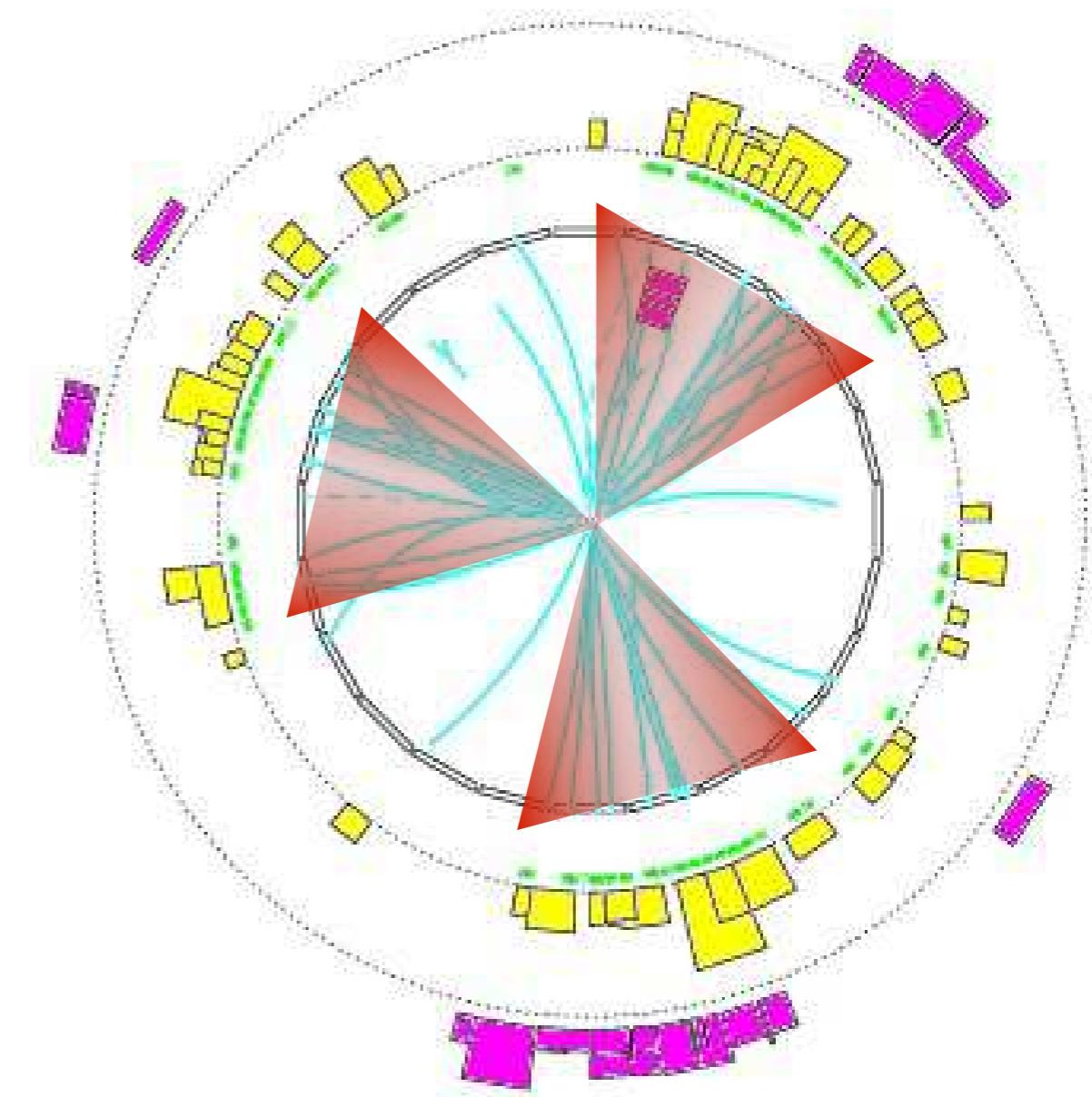


2 clear jets

# Reconstructing jets is an ambiguous task

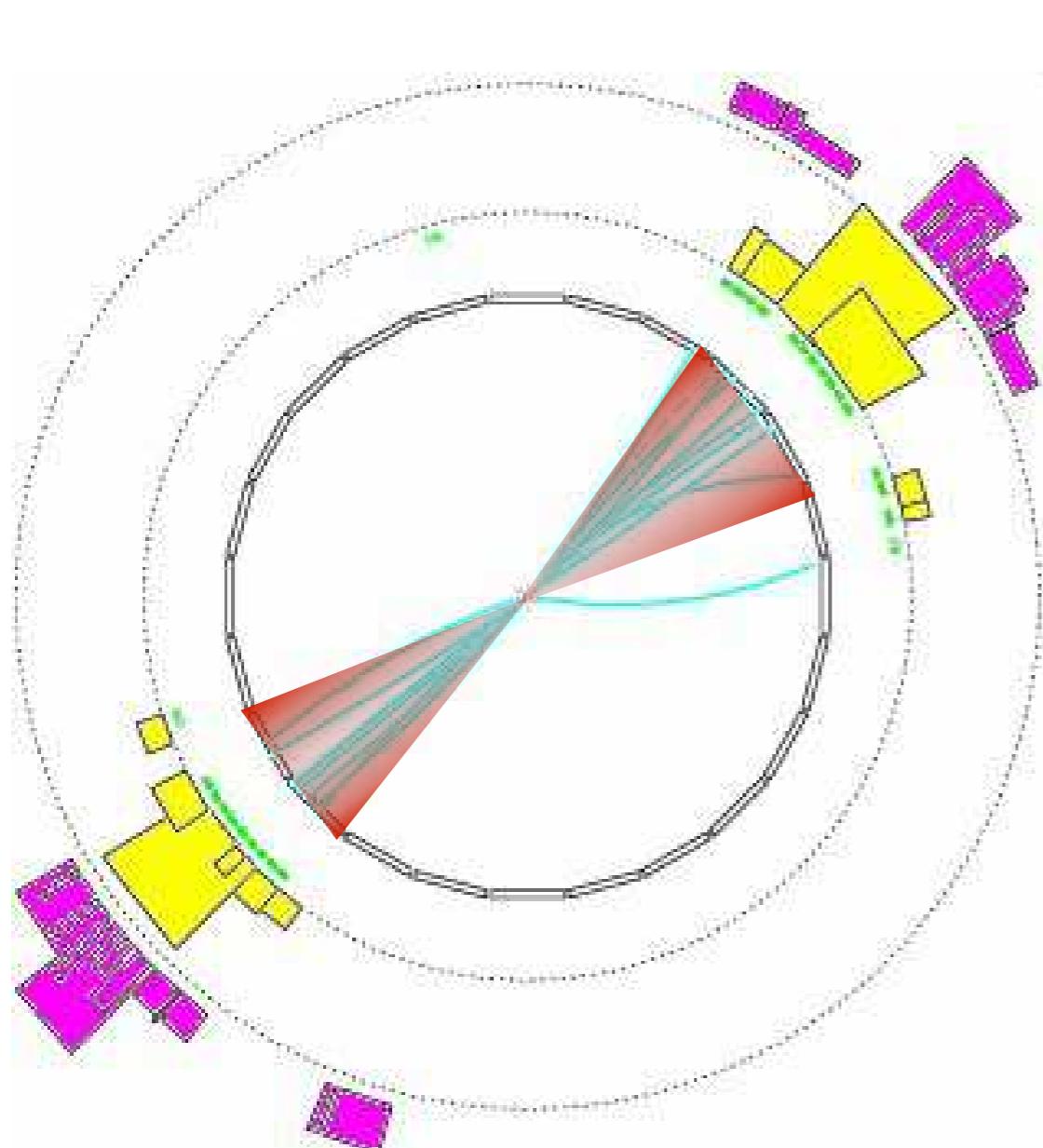


2 clear jets

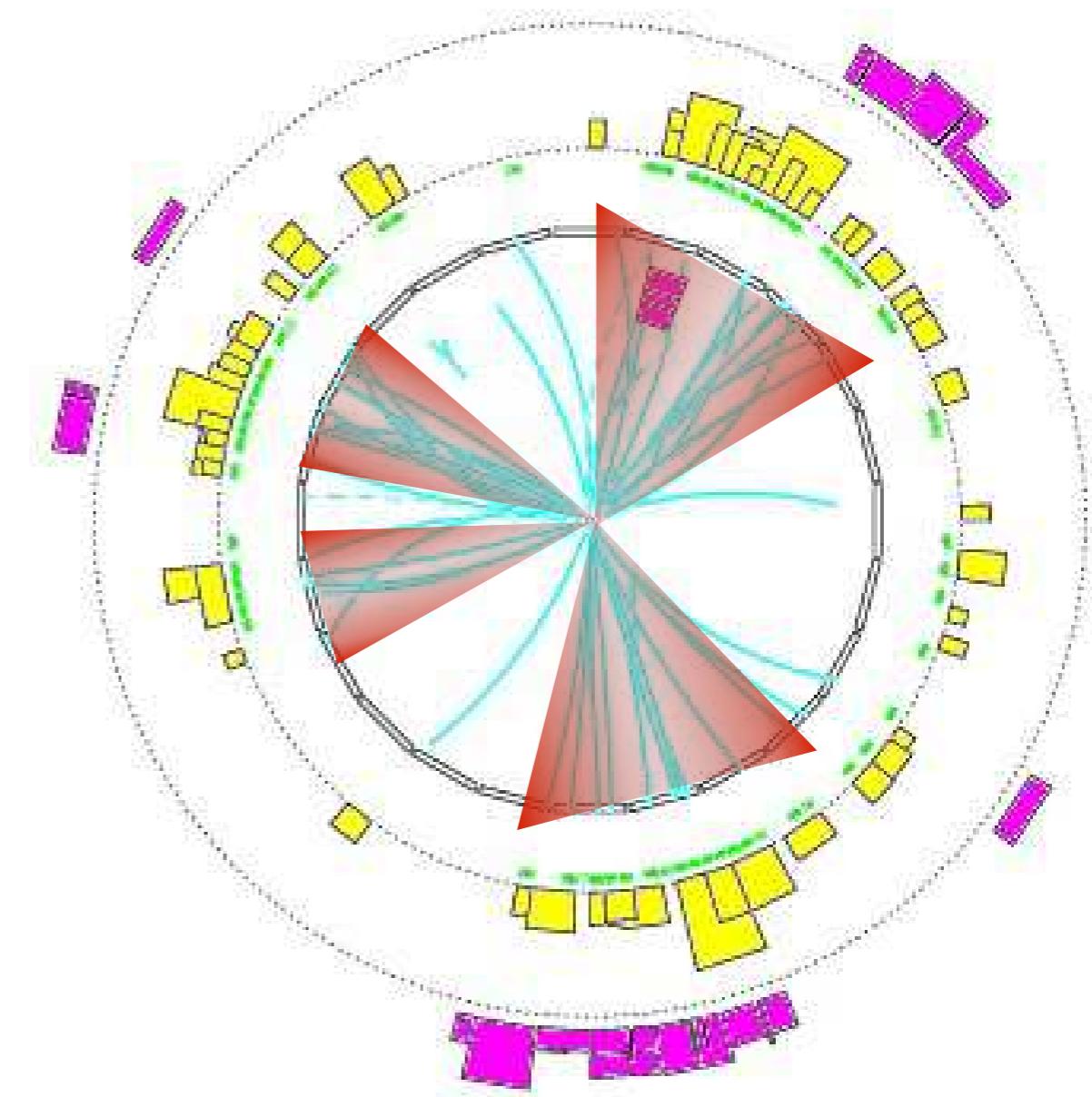


3 jets?

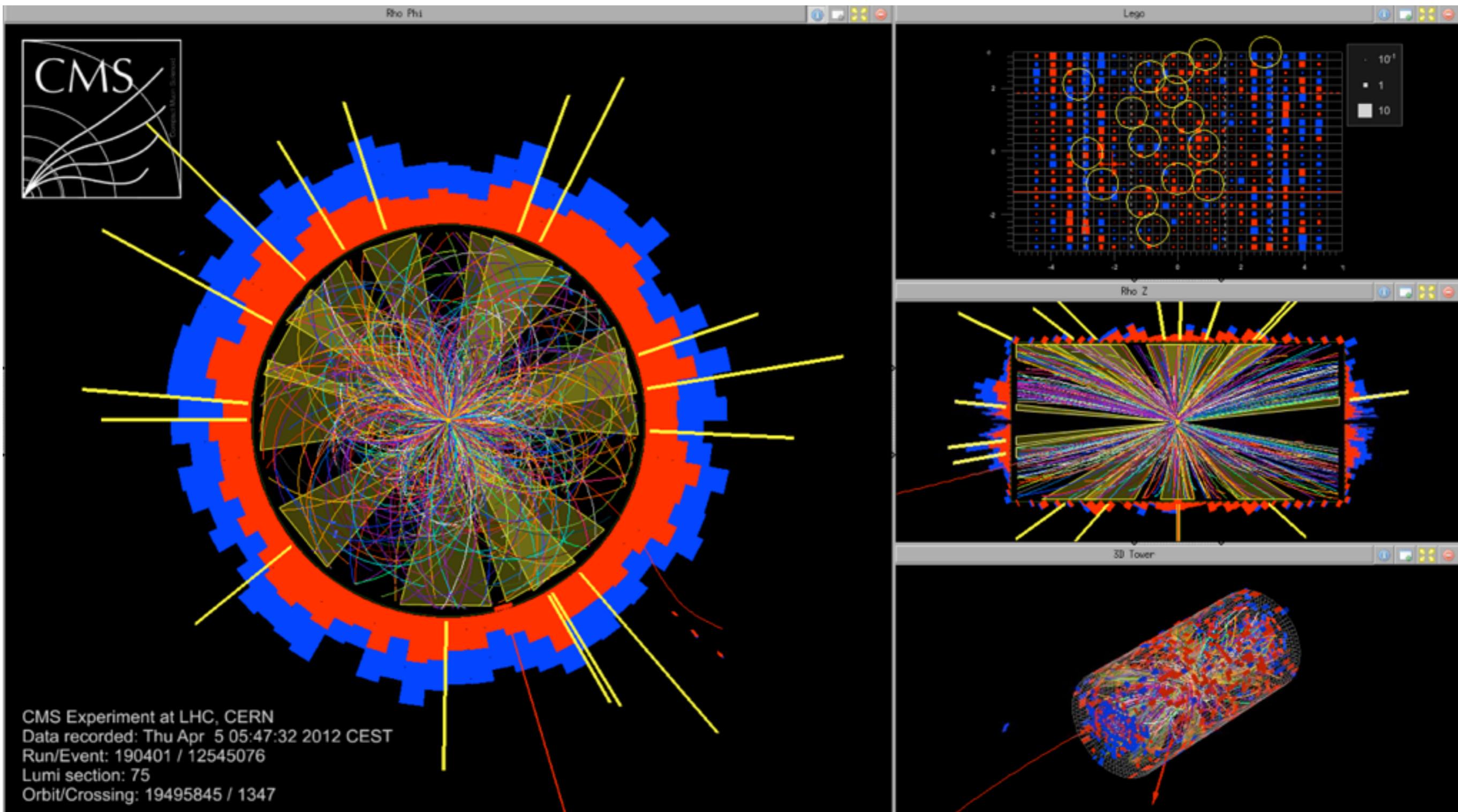
# Reconstructing jets is an ambiguous task



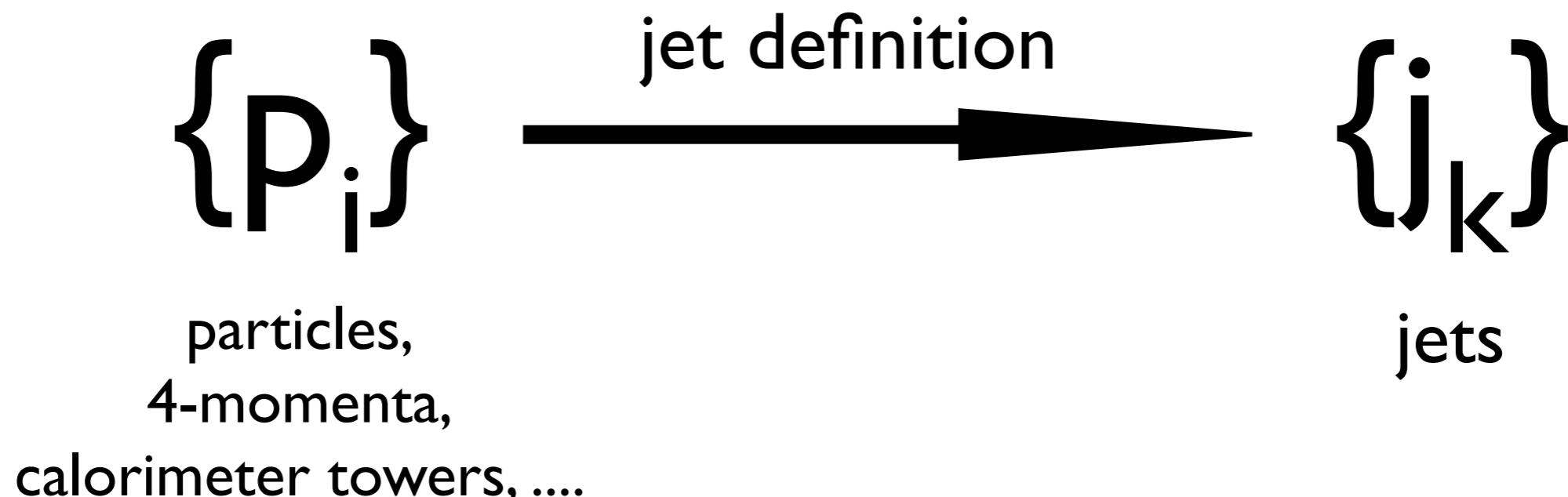
2 clear jets



3 jets?  
or 4 jets?



# Make a choice: specify a jet definition



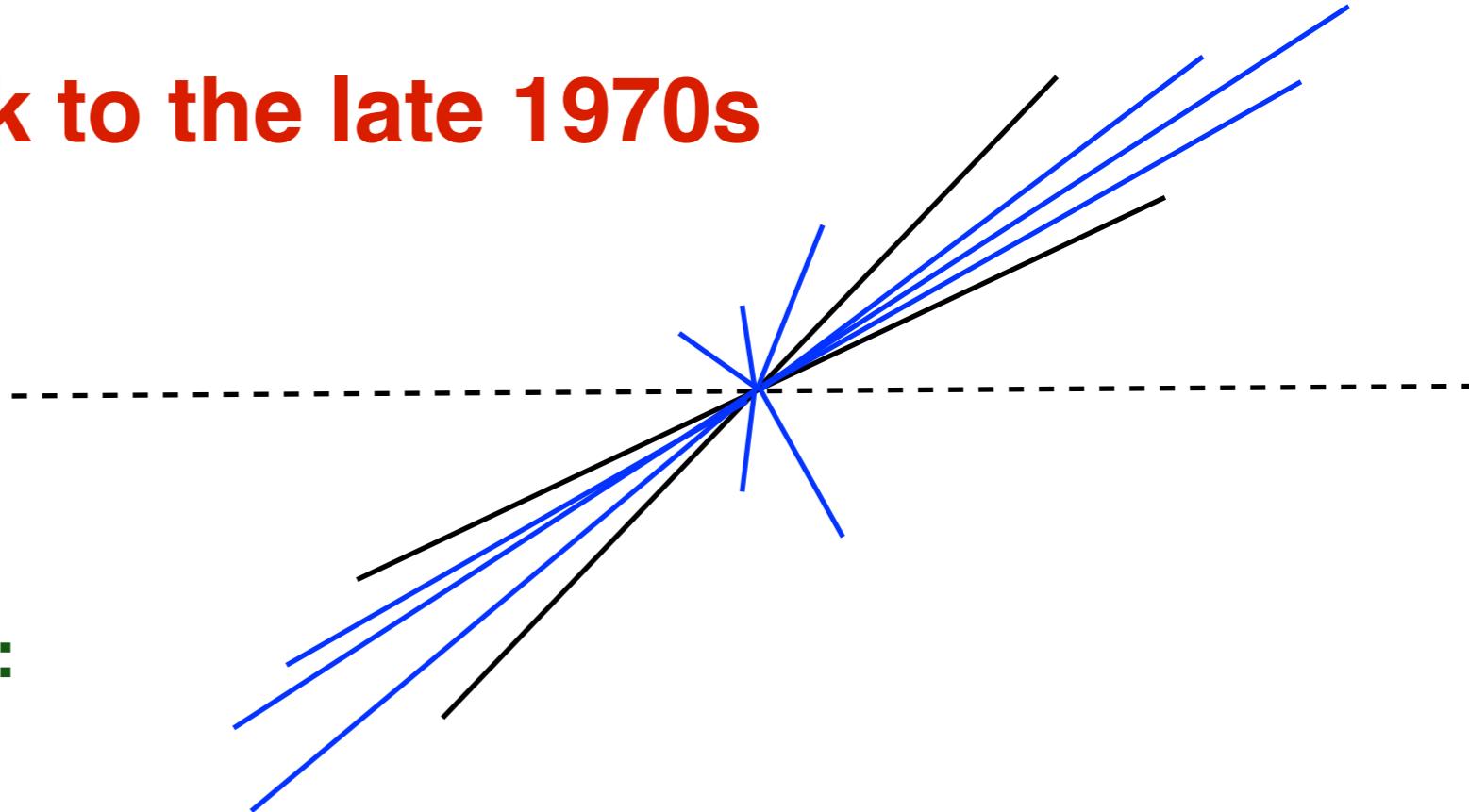
- Which particles do you put together into a same jet?
- How do you recombine their momenta  
(4-momentum sum is the obvious choice, right?)

*“Jet [definitions] are legal contracts between theorists and experimentalists”*  
-- MJ Tannenbaum

They're also a way of organising the information in an event  
1000's of particles per events, up to 20.000.000 events per second

# Jet definitions date back to the late 1970s

**Sterman and Weinberg,  
Phys. Rev. Lett. 39, 1436 (1977):**



To study jets, we consider the partial cross section

$\sigma(E, \theta, \Omega, \epsilon, \delta)$  for  $e^+e^-$  hadron production events, in which all but

a fraction  $\epsilon \ll 1$  of the total  $e^+e^-$  energy  $E$  is emitted within

some pair of oppositely directed cones of half-angle  $\delta \ll 1$ ,

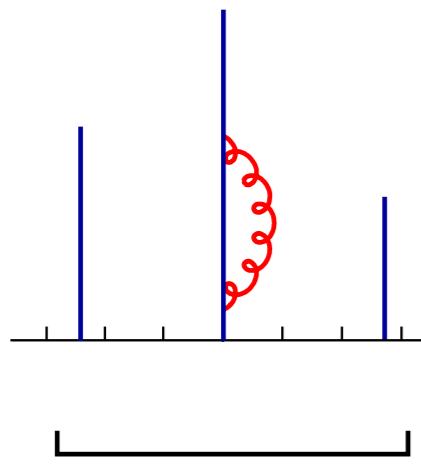
lying within two fixed cones of solid angle  $\Omega$  (with  $\pi\delta^2 \ll \Omega \ll 1$ )

at an angle  $\theta$  to the  $e^+e^-$  beam line. We expect this to be measur-

$$\sigma(E, \theta, \Omega, \epsilon, \delta) = (\frac{d\sigma}{d\Omega})_0 \Omega \left[ 1 - (g_E^2/3\pi^2) \left\{ 3\ln \delta + 4\ln \delta \ln 2\epsilon + \frac{\pi^3}{3} - \frac{5}{2} \right\} \right]$$

# Key requirement: infrared and collinear safety

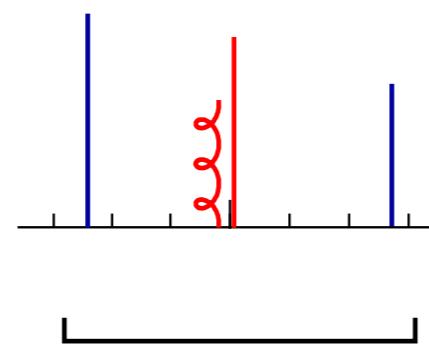
## Collinear Safe



jet 1

$$\alpha_s^n \times (-\infty)$$

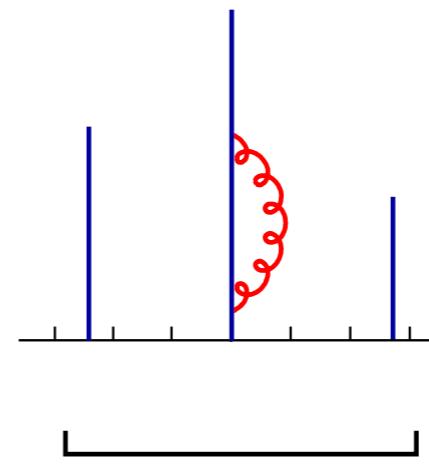
**Infinities cancel**



jet 1

$$\alpha_s^n \times (+\infty)$$

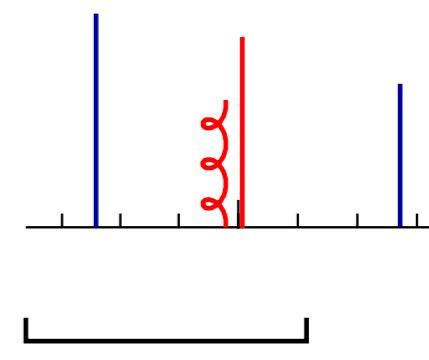
## Collinear Unsafe



jet 1

$$\alpha_s^n \times (-\infty)$$

**Infinities do not cancel**



jet 1    jet 2

$$\alpha_s^n \times (+\infty)$$

**Invalidates perturbation theory**

## Two parameters, $R$ and $p_{t,min}$

(These are the two parameters in essentially every widely used hadron-collider jet algorithm)

$$d_{ij} = \min(p_{ti}^2, p_{tj}^2) \frac{\Delta R_{ij}^2}{R^2}, \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

## Sequential recombination algorithm

1. Find smallest of  $d_{ij}$ ,  $d_{iB}$
2. If  $ij$ , recombine them
3. If  $iB$ , call i a jet and remove from list of particles
4. repeat from step 1 until no particles left

Only use jets with  $p_t > p_{t,min}$

**Inclusive  $k_t$  algorithm**

S.D. Ellis & Soper, 1993

Catani, Dokshitzer, Seymour & Webber, 1993

# Sequential recombination variants

## Cambridge/Aachen: the simplest of hadron-collider algorithms

- Recombine pair of objects closest in  $\Delta R_{ij}$
- Repeat until all  $\Delta R_{ij} > R$  – remaining objects are jets

Dokshitzer, Leder, Moretti, Webber '97 (Cambridge): more involved e+e- form

Wobisch & Wengler '99 (Aachen): simple inclusive hadron-collider form

One still applies a  $p_{t,\min}$  cut to the jets, as for inclusive  $k_t$

C/A privileges the collinear divergence of QCD;  
it ‘ignores’ the soft one

Anti- $k_t$ : formulated similarly to inclusive  $k_t$ , but with

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$

Cacciari, GPS & Soyez '08 [+Delsart unpublished]

Anti- $k_t$  privileges the collinear divergence of QCD and disfavours clustering between pairs of soft particles

Most pairwise clusterings involve at least one hard particle

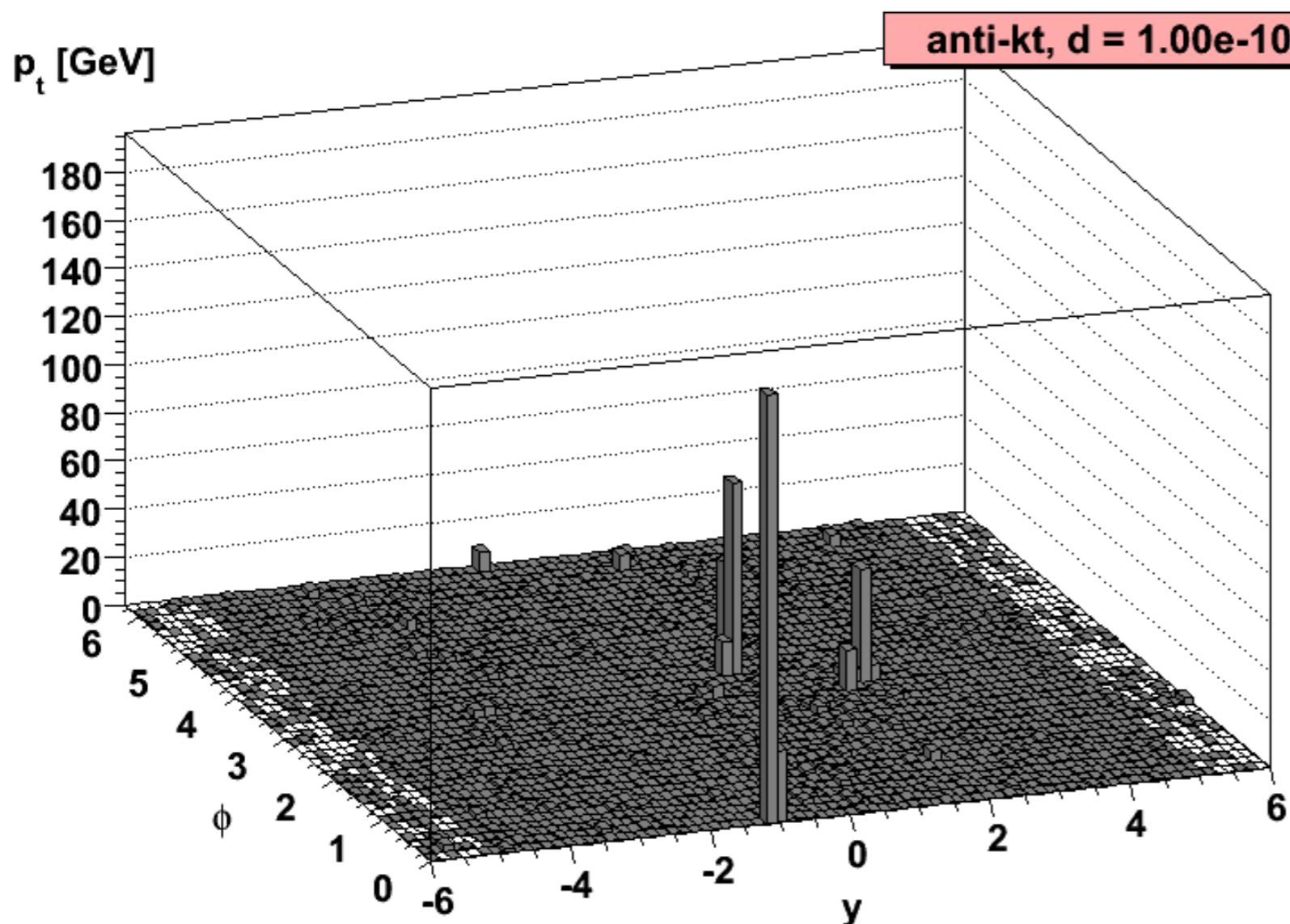
Clustering grows  
around hard cores

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$

# Anti- $k_t$ in action

Clustering grows around hard cores

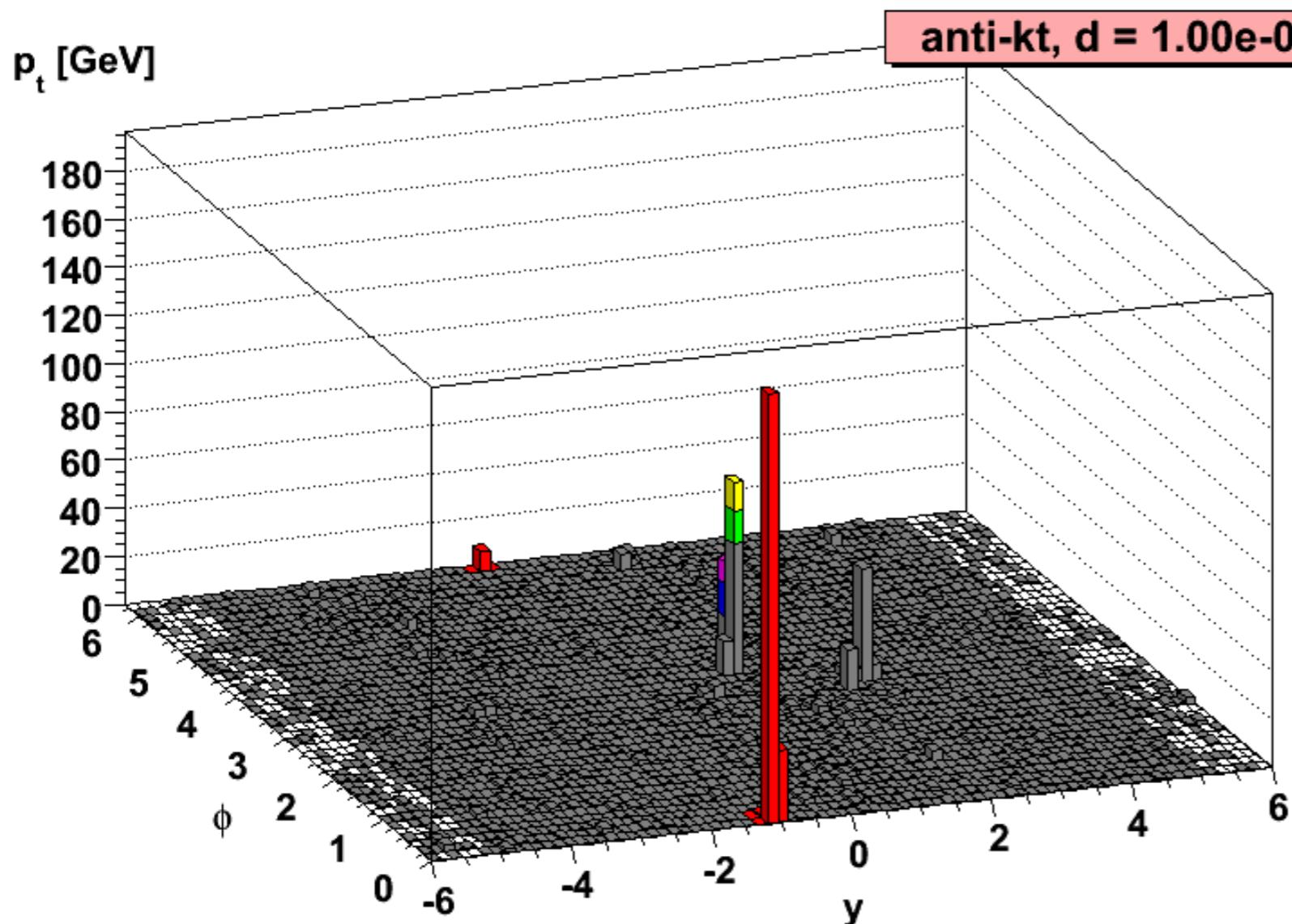
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

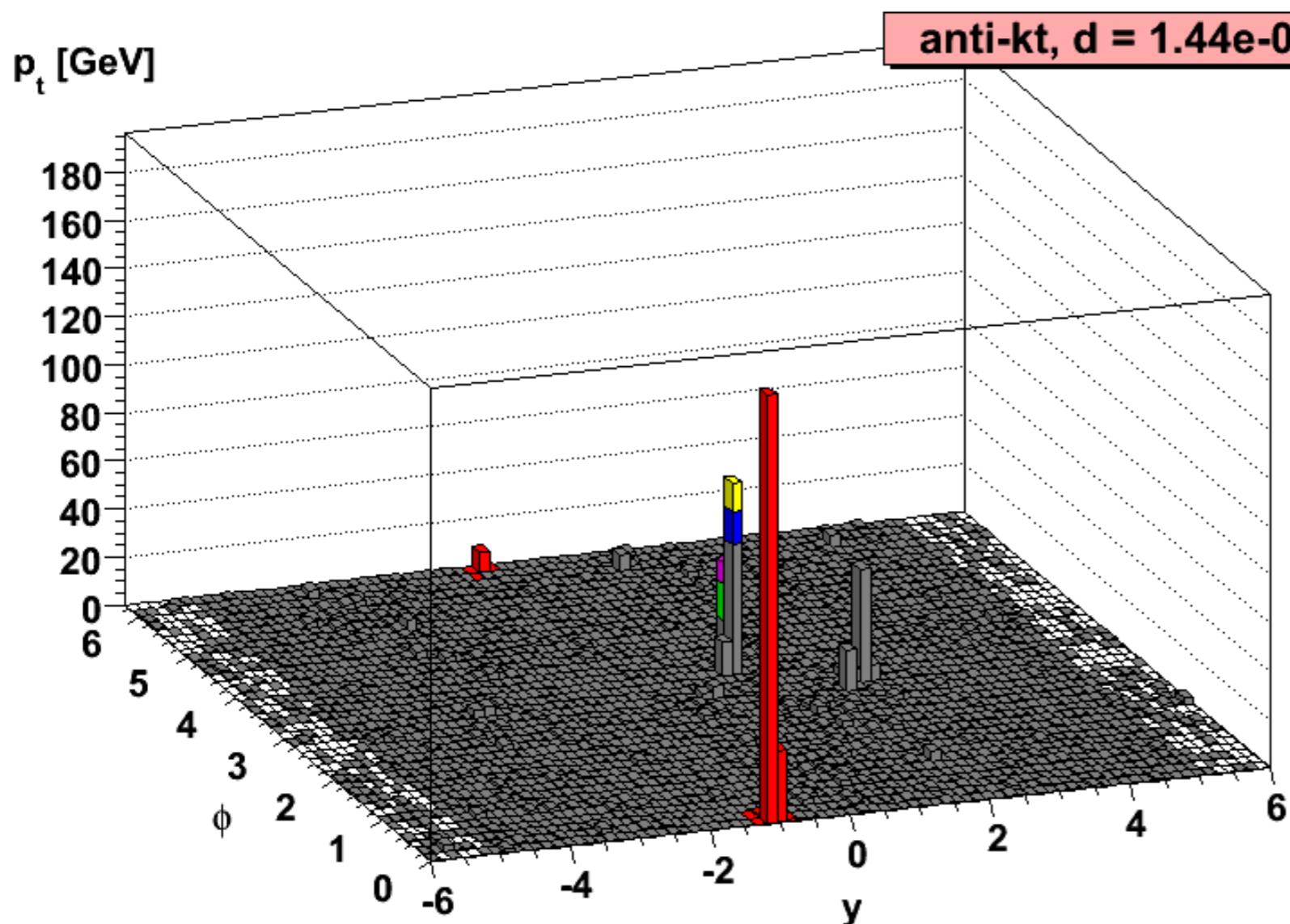
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

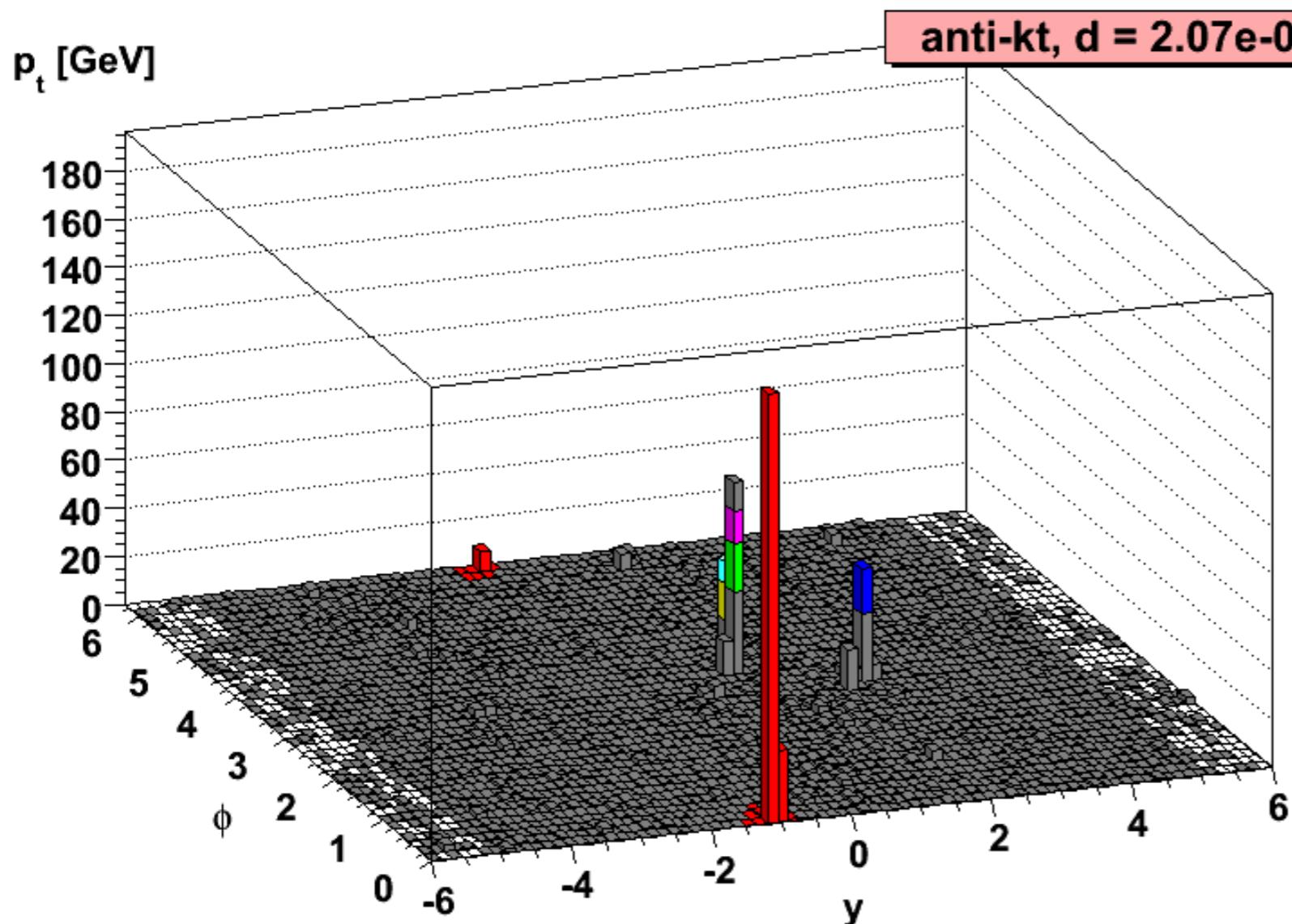
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

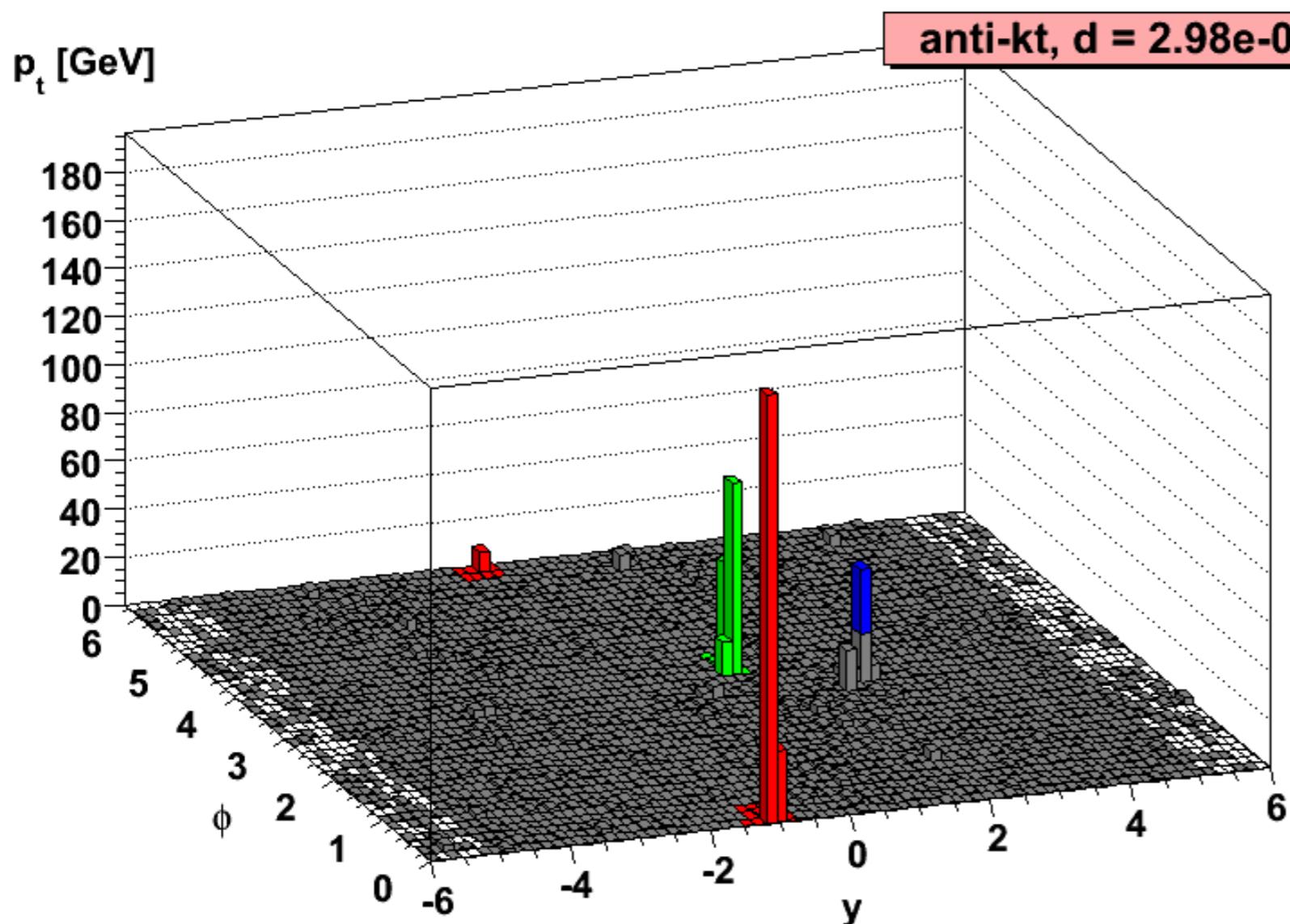
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

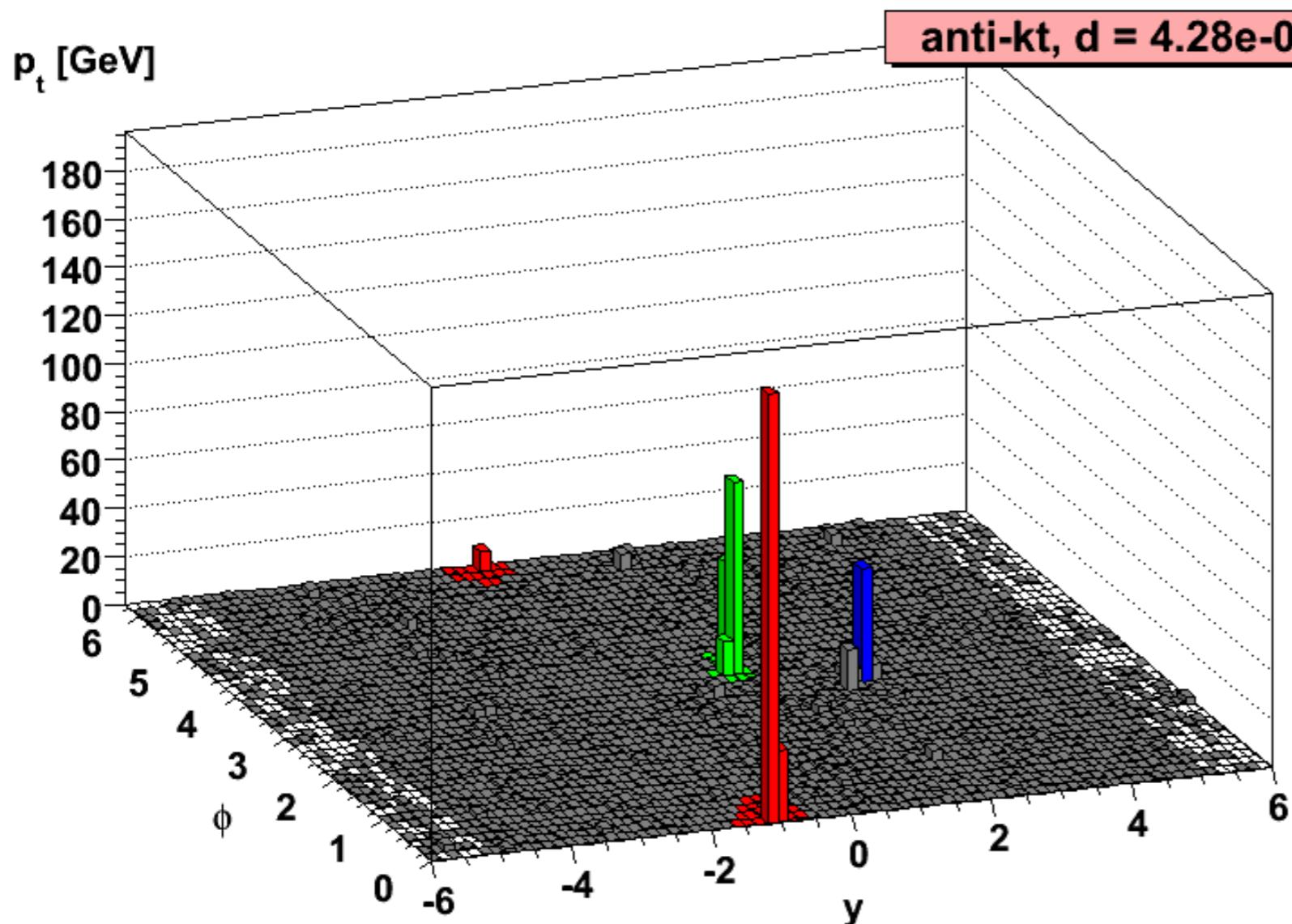
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

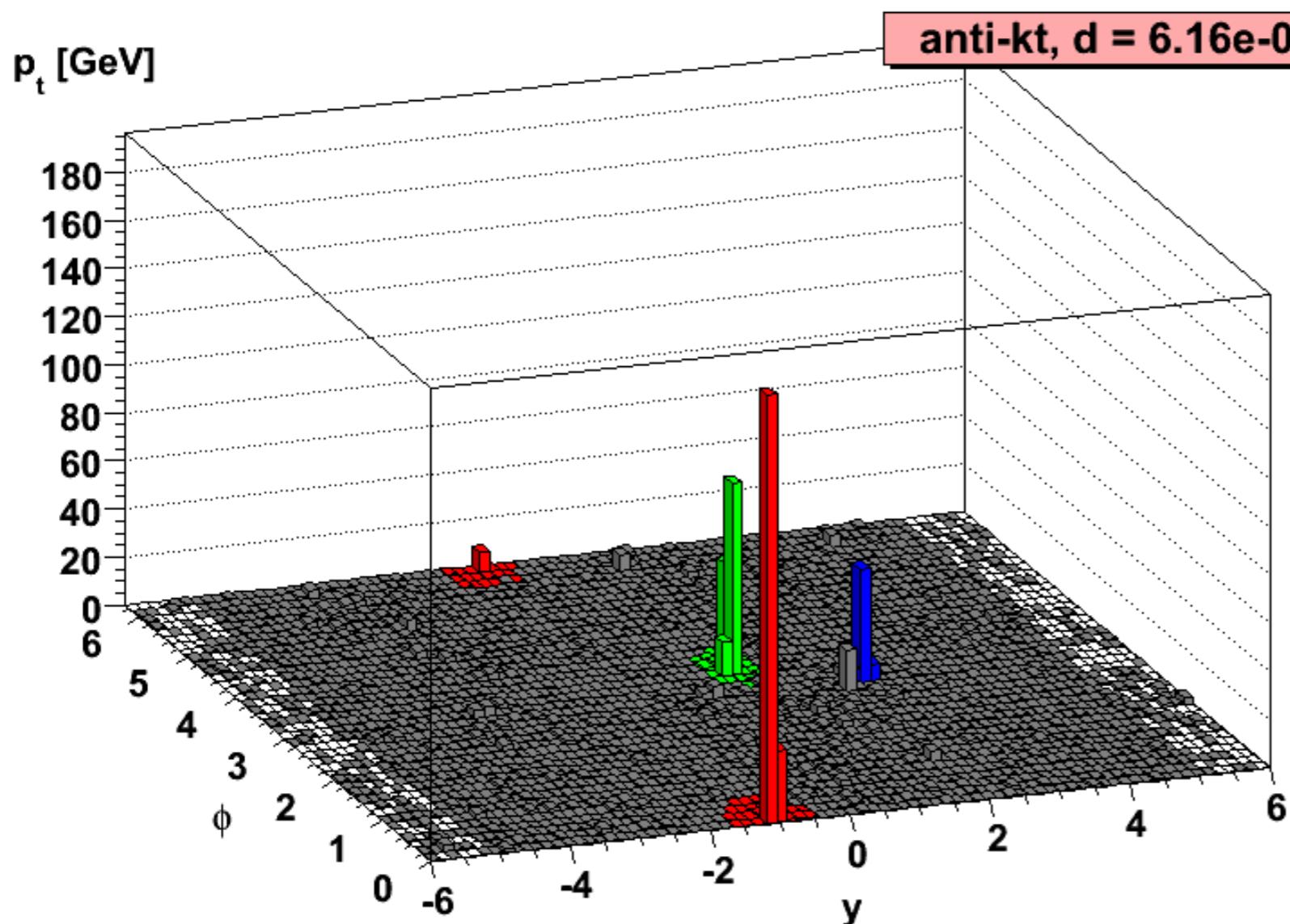
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

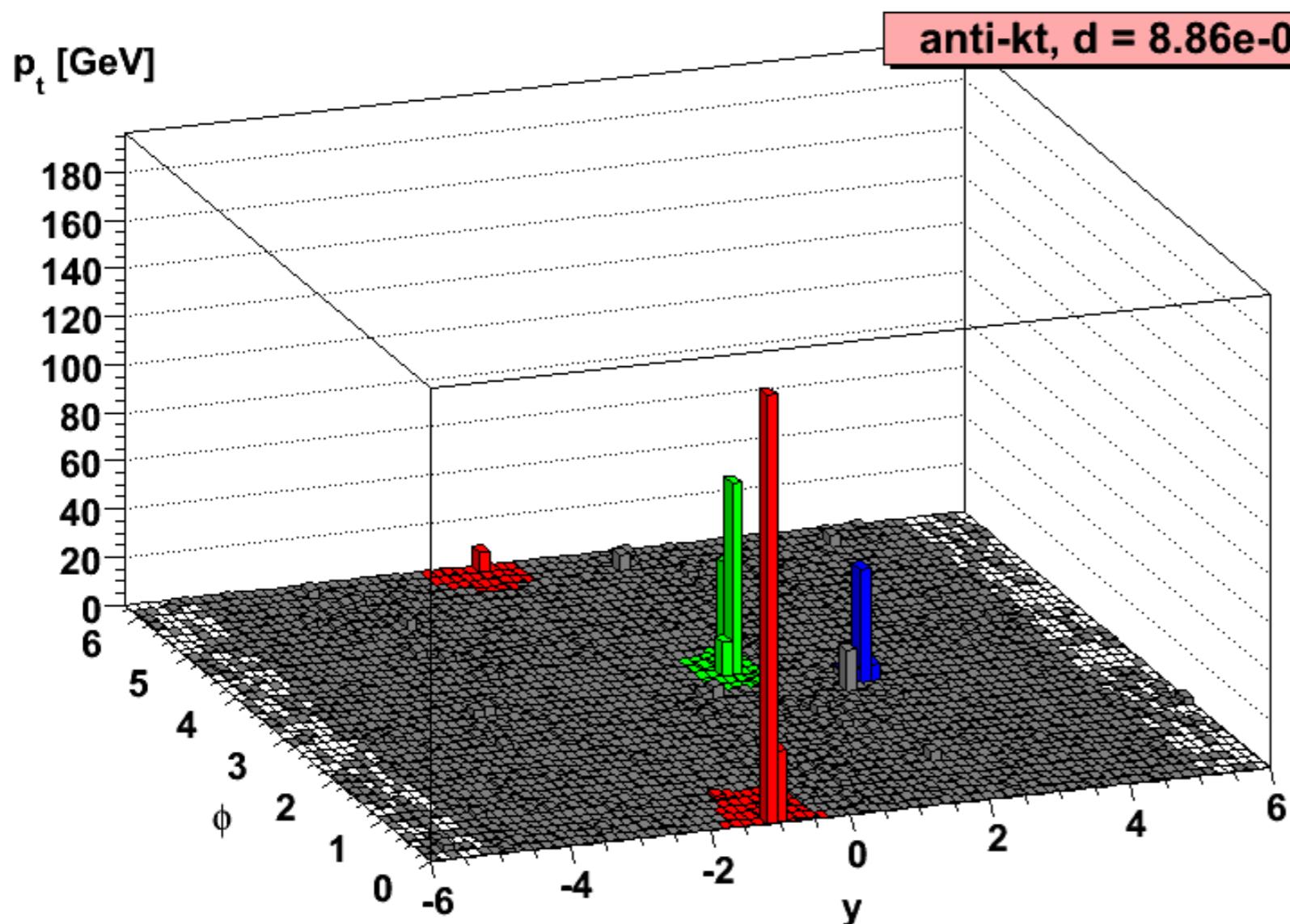
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

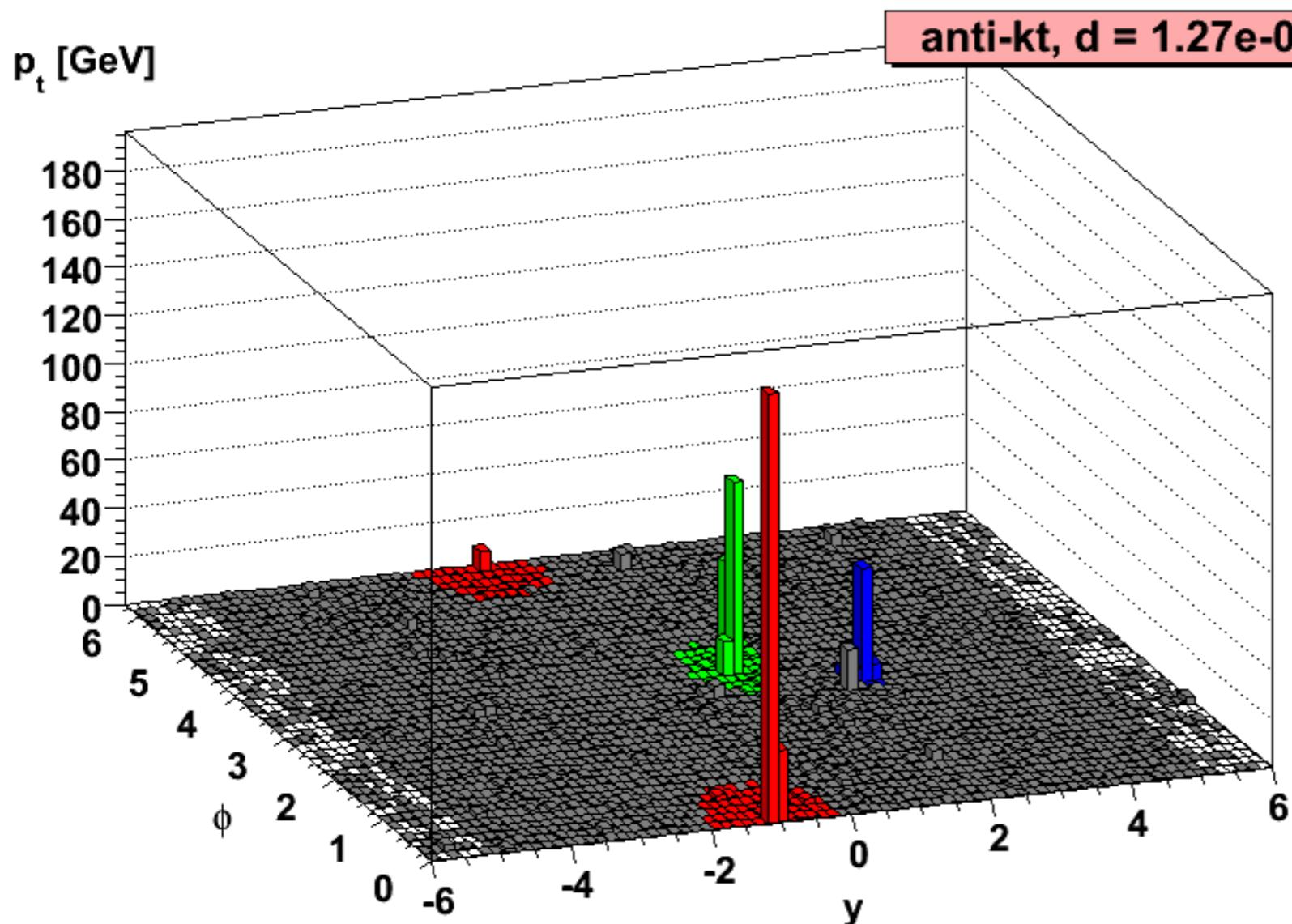
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

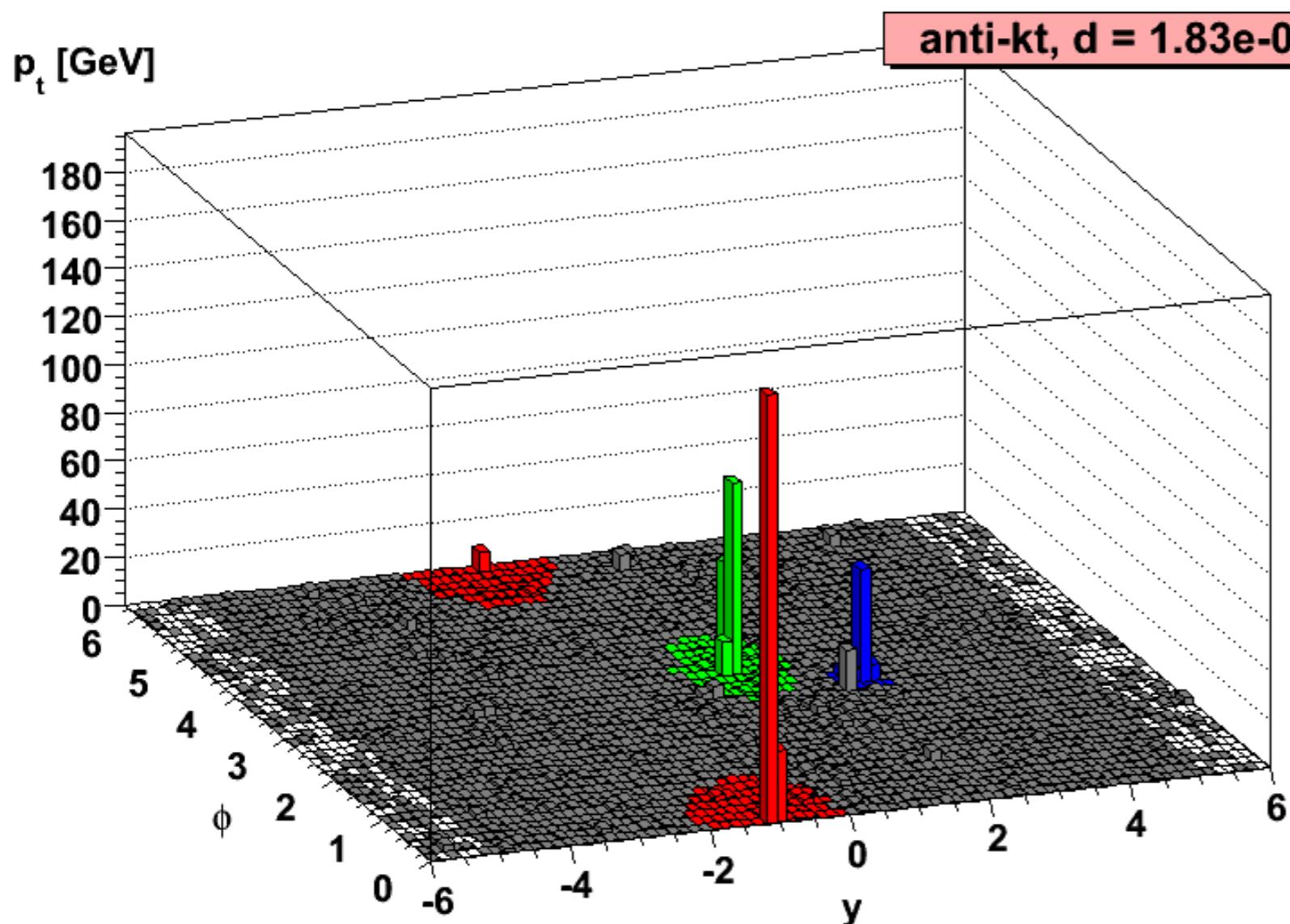
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

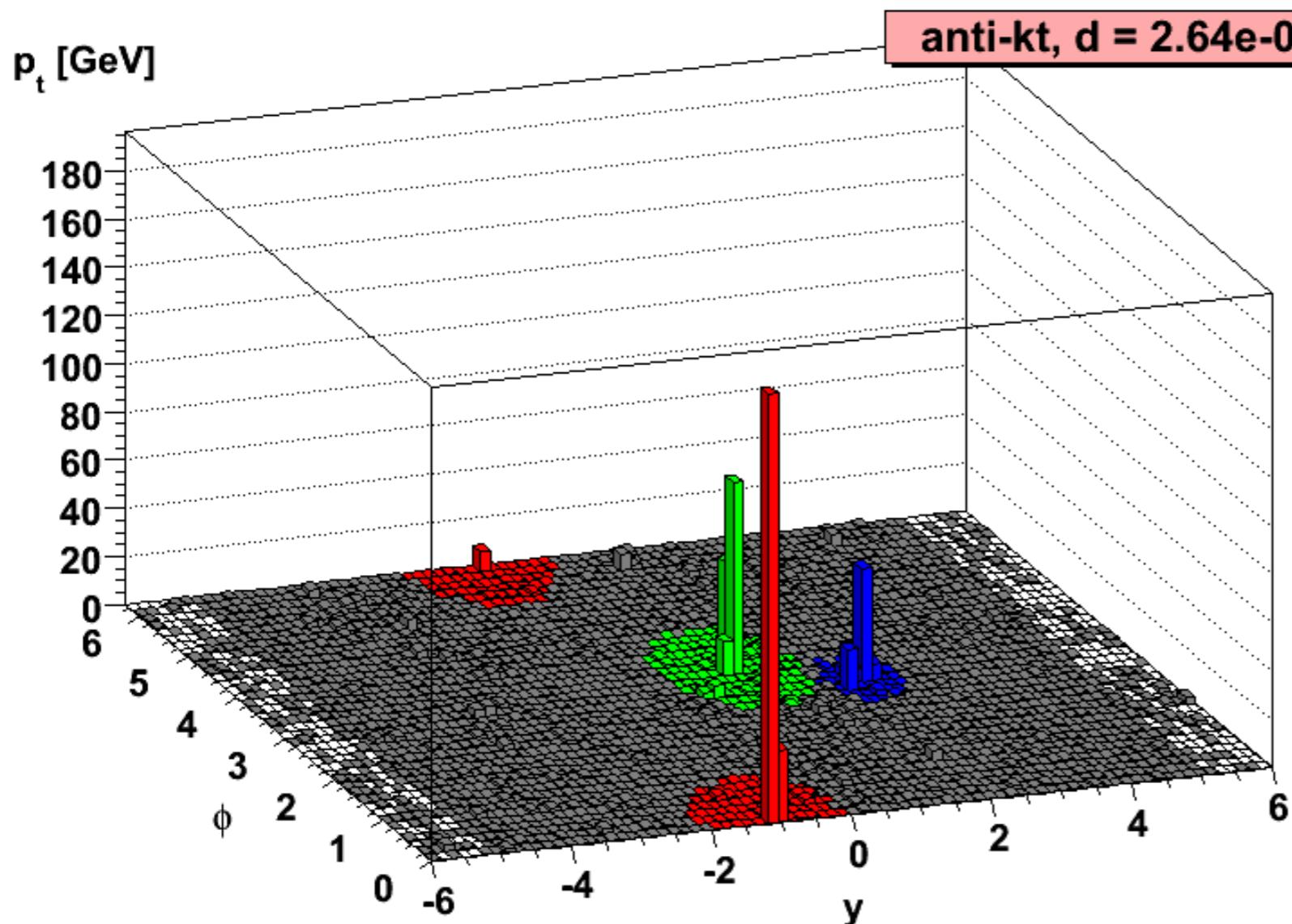
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

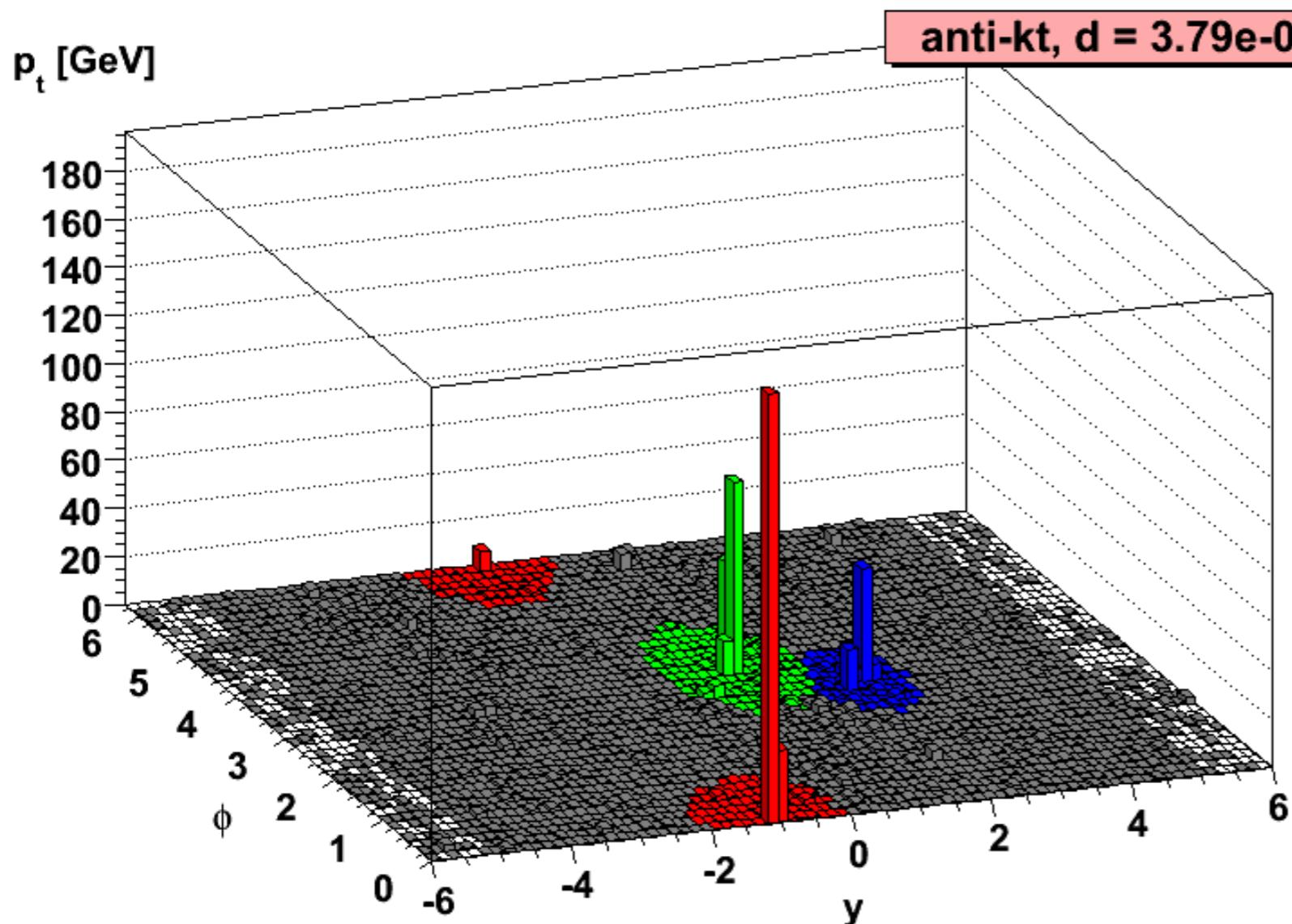
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

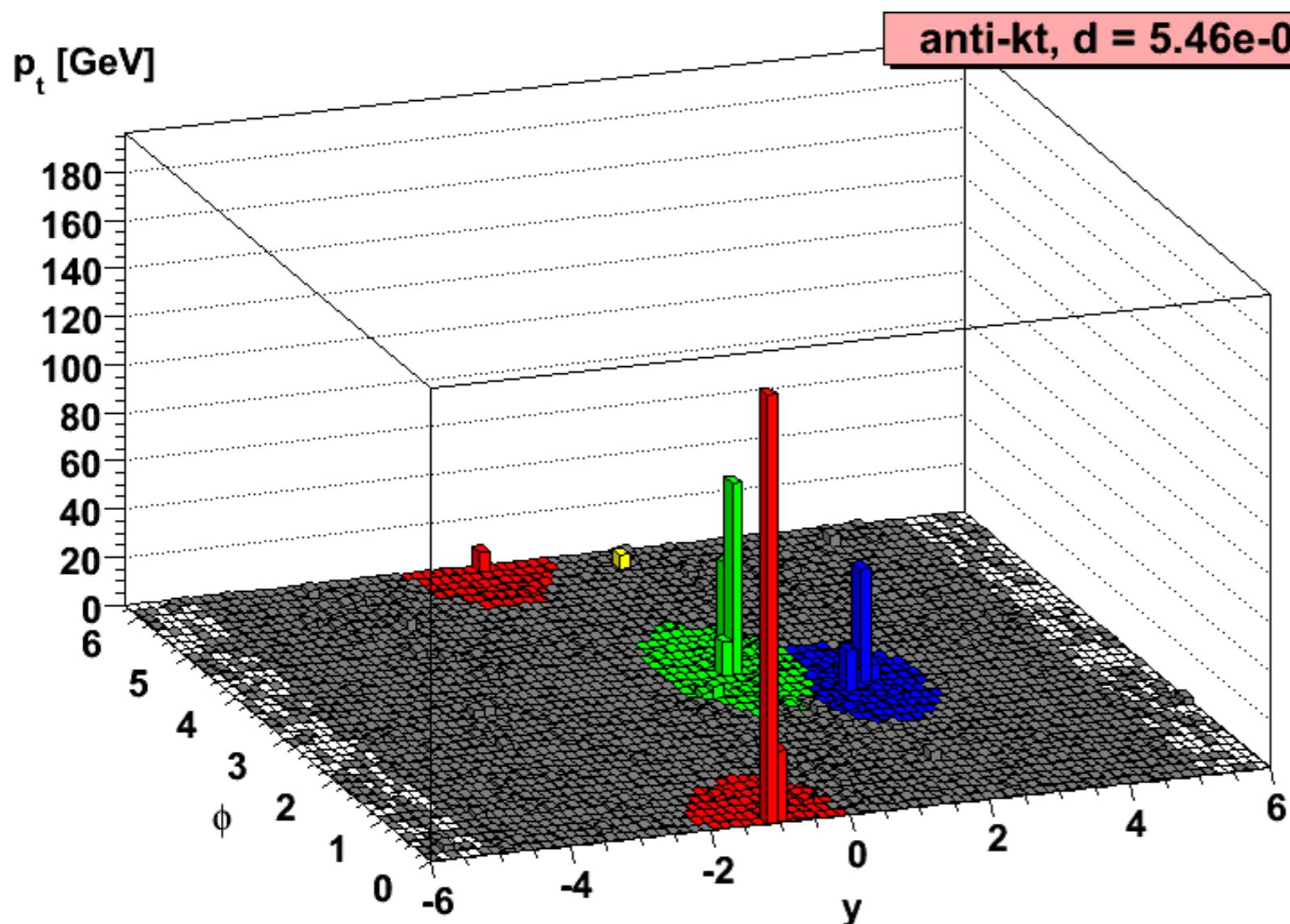
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

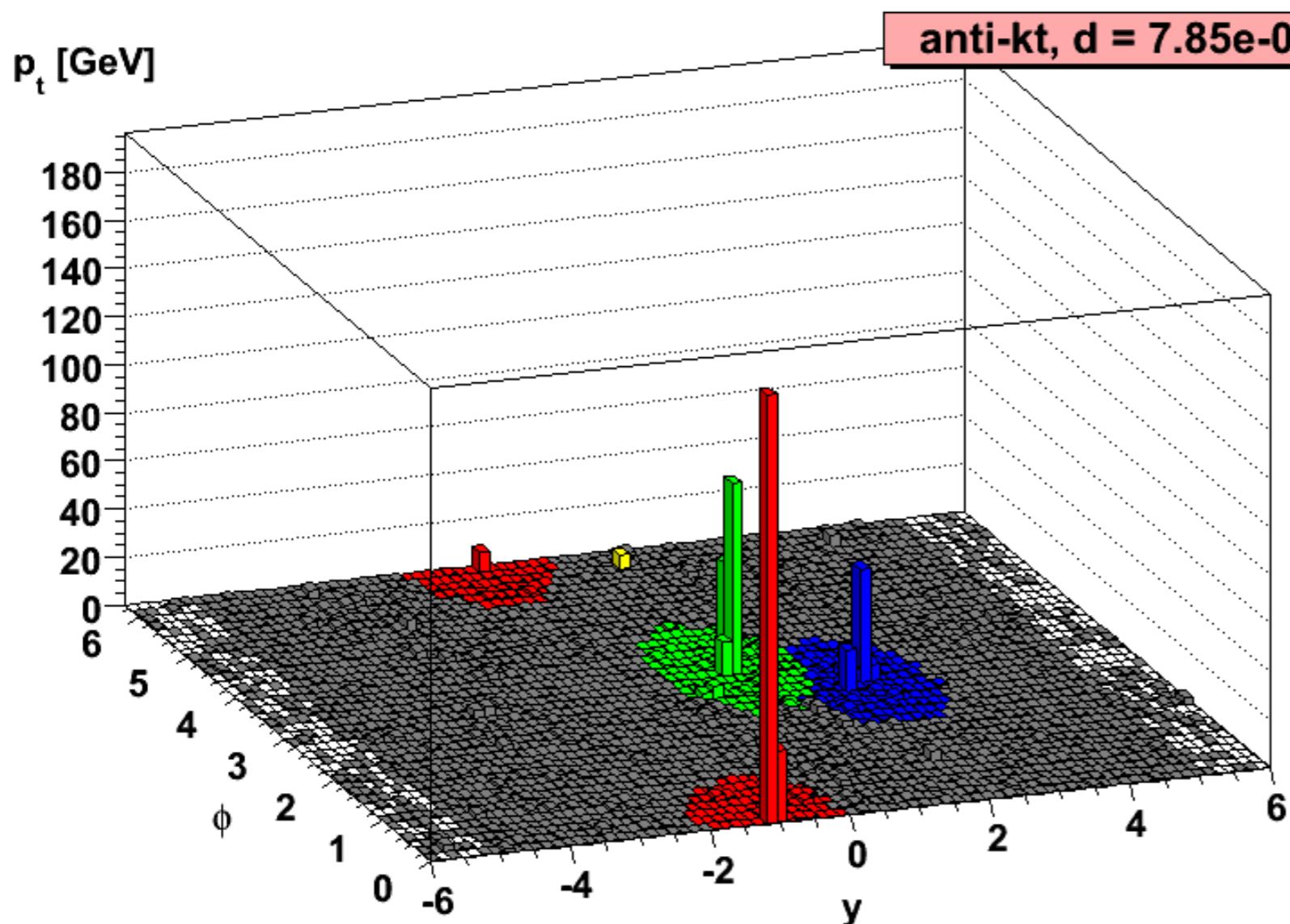
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

Clustering grows around hard cores

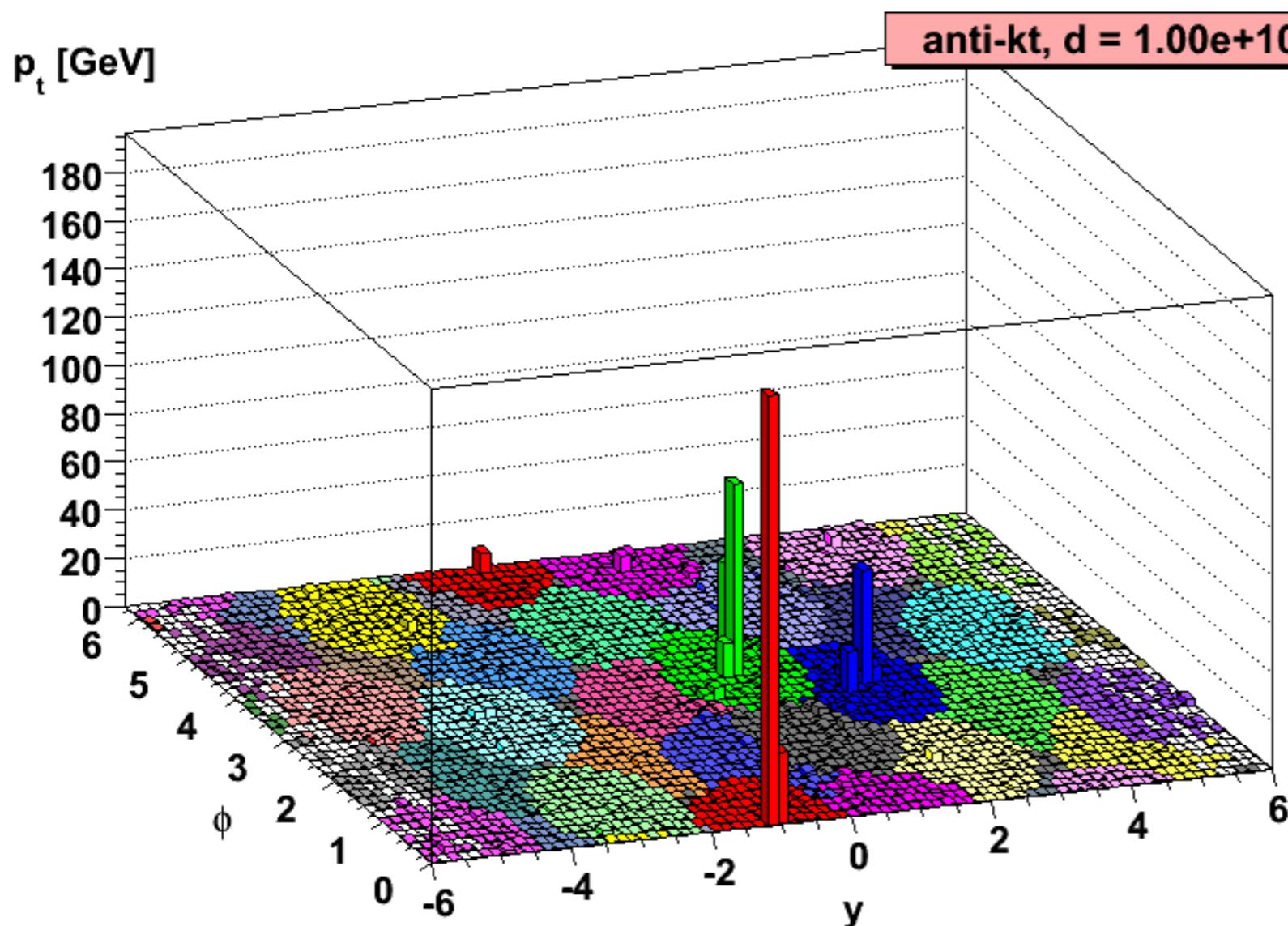
$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$



# Anti- $k_t$ in action

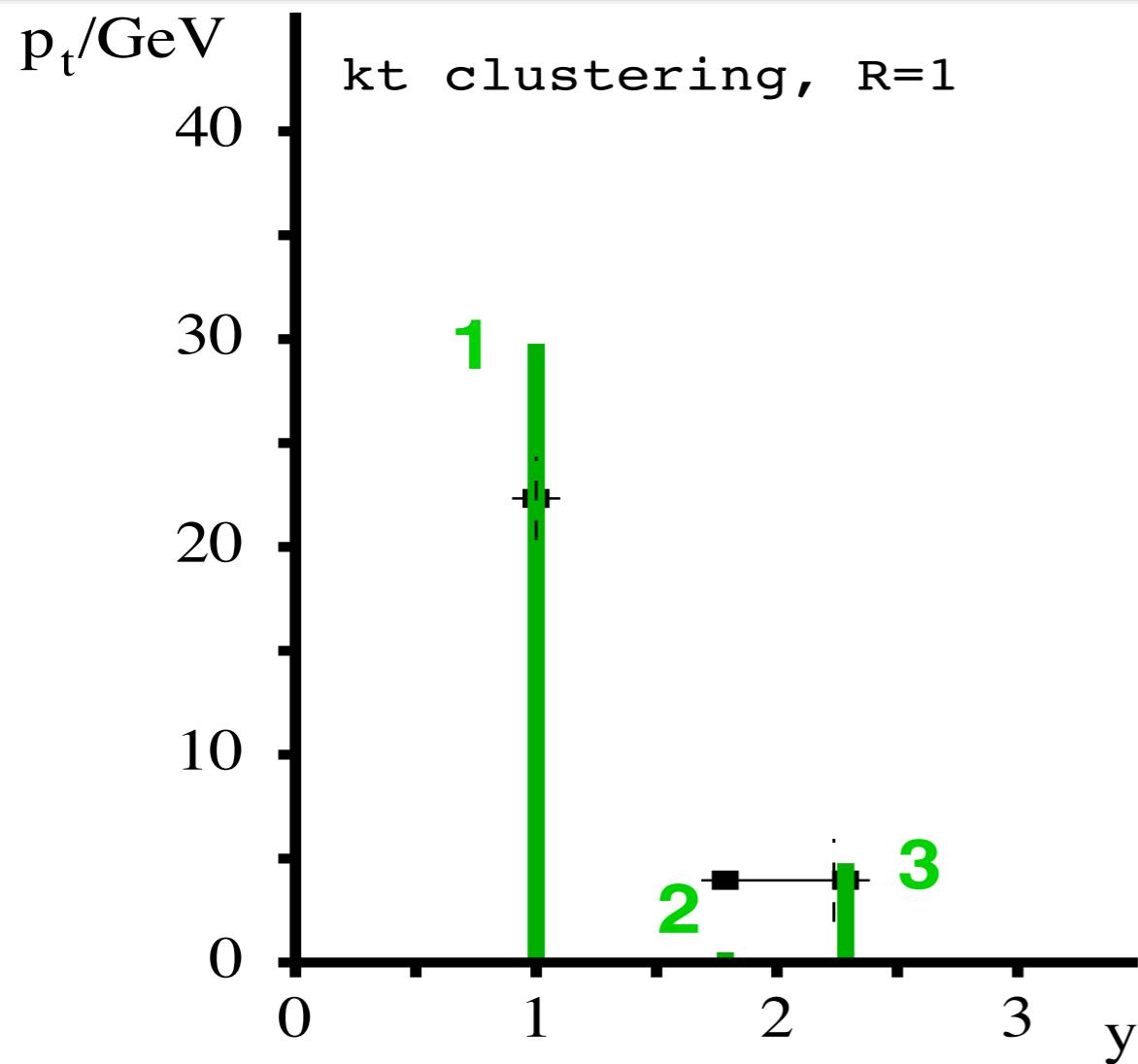
Clustering grows around hard cores

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}, \quad d_{iB} = \frac{1}{p_{ti}^2}$$

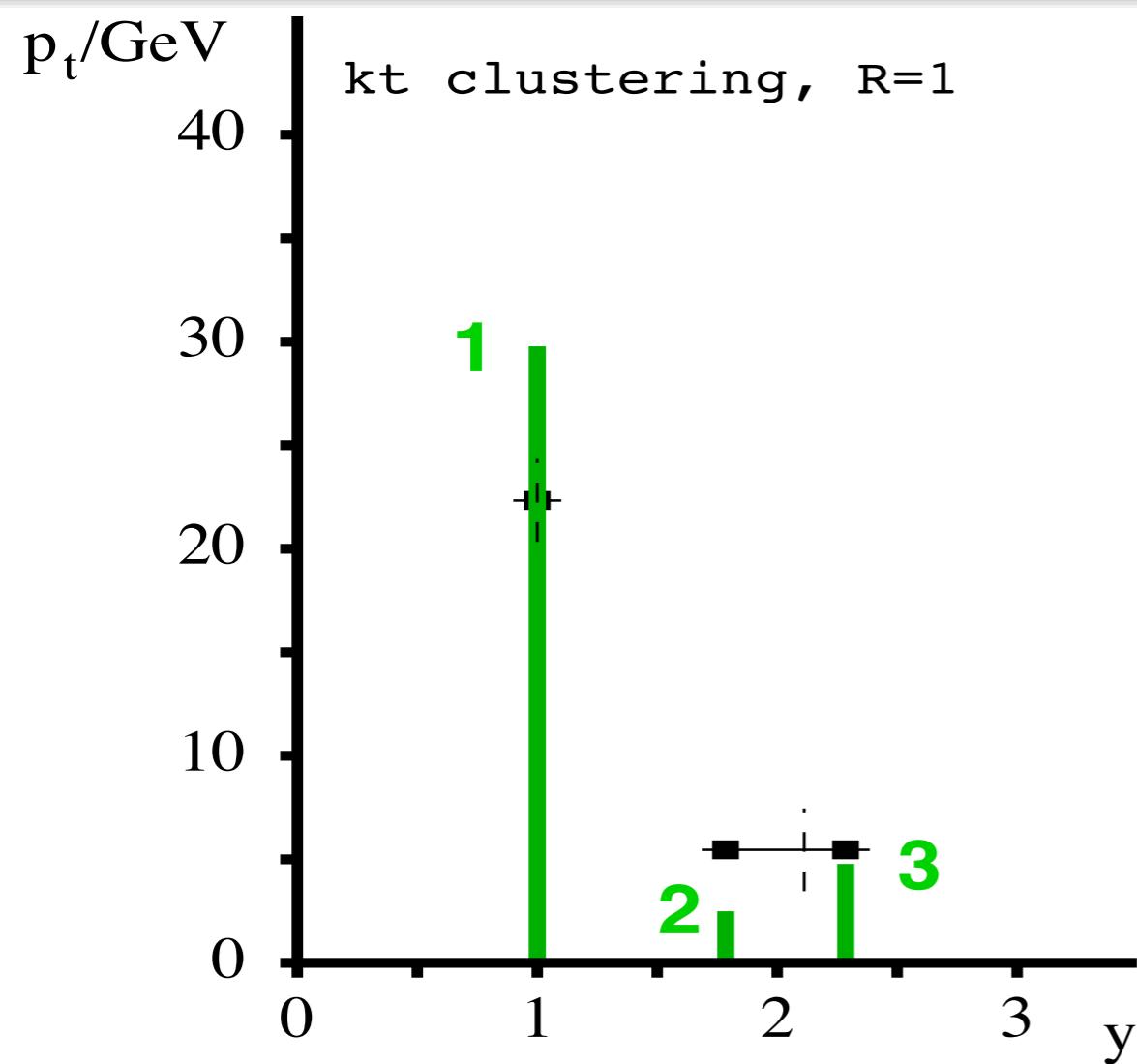


Anti- $k_t$  gives circular jets (“cone-like”) in a way that’s infrared safe

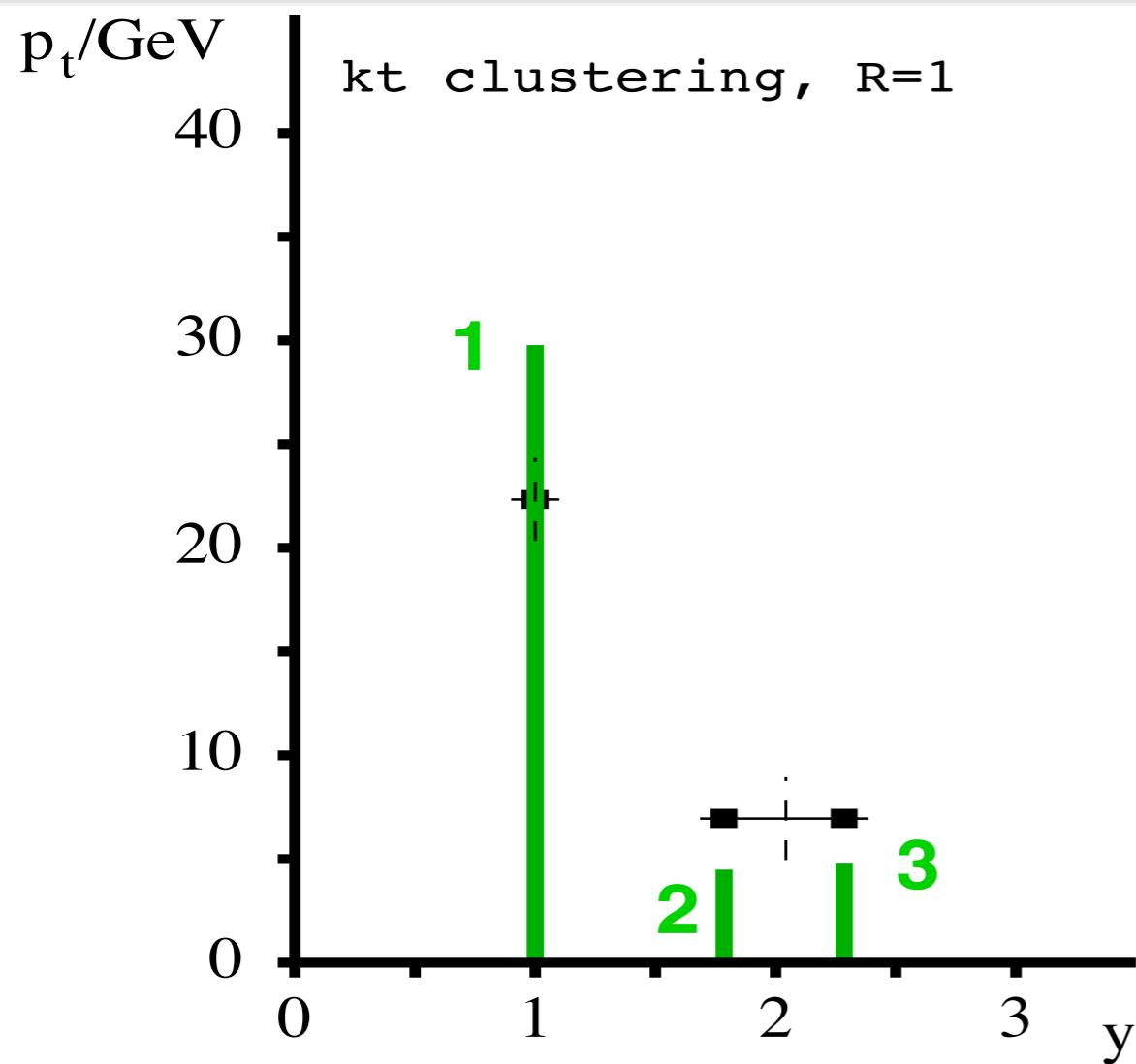
# Linearity: $k_t$ v. anti- $k_t$



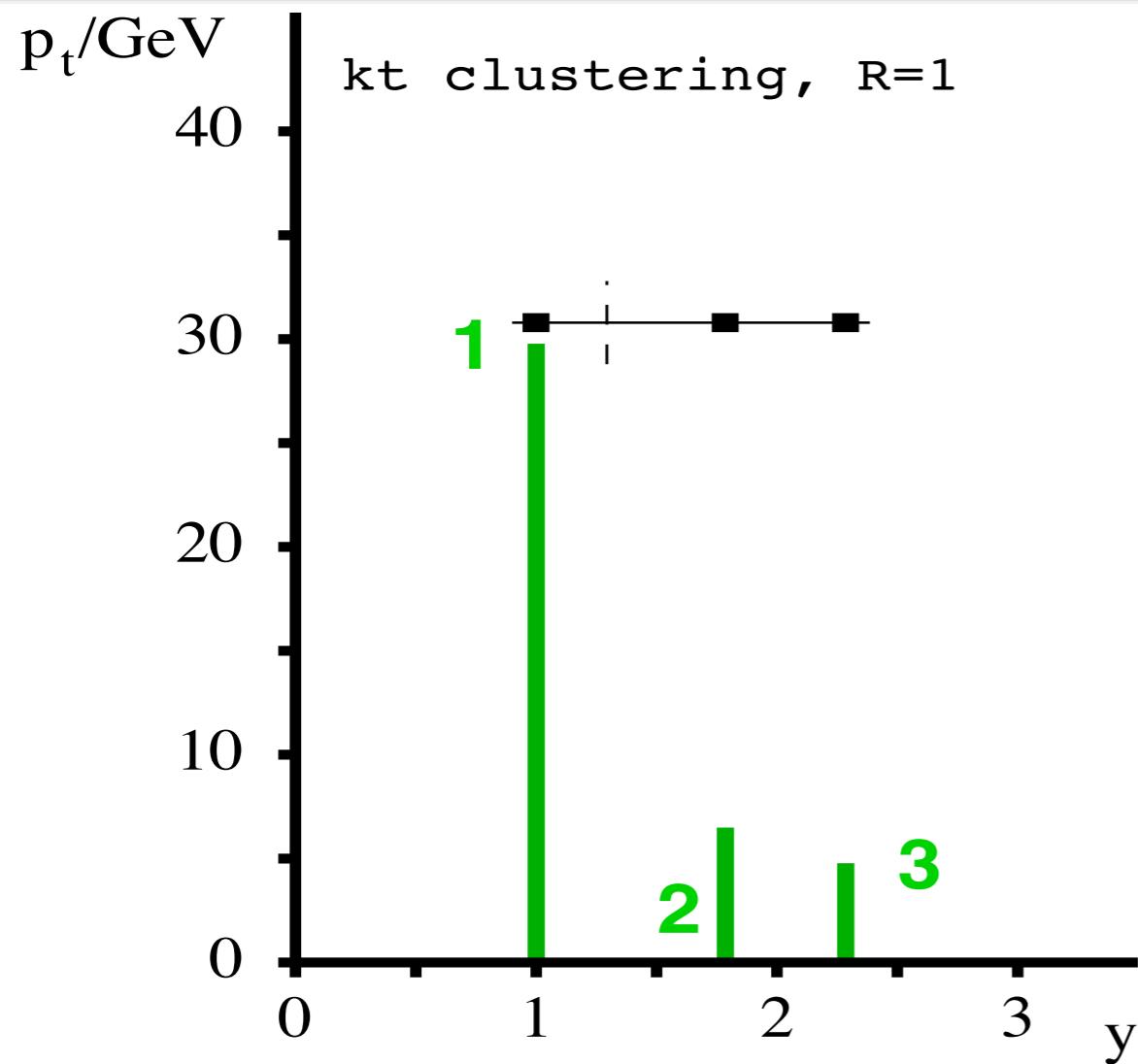
# Linearity: $k_t$ v. anti- $k_t$



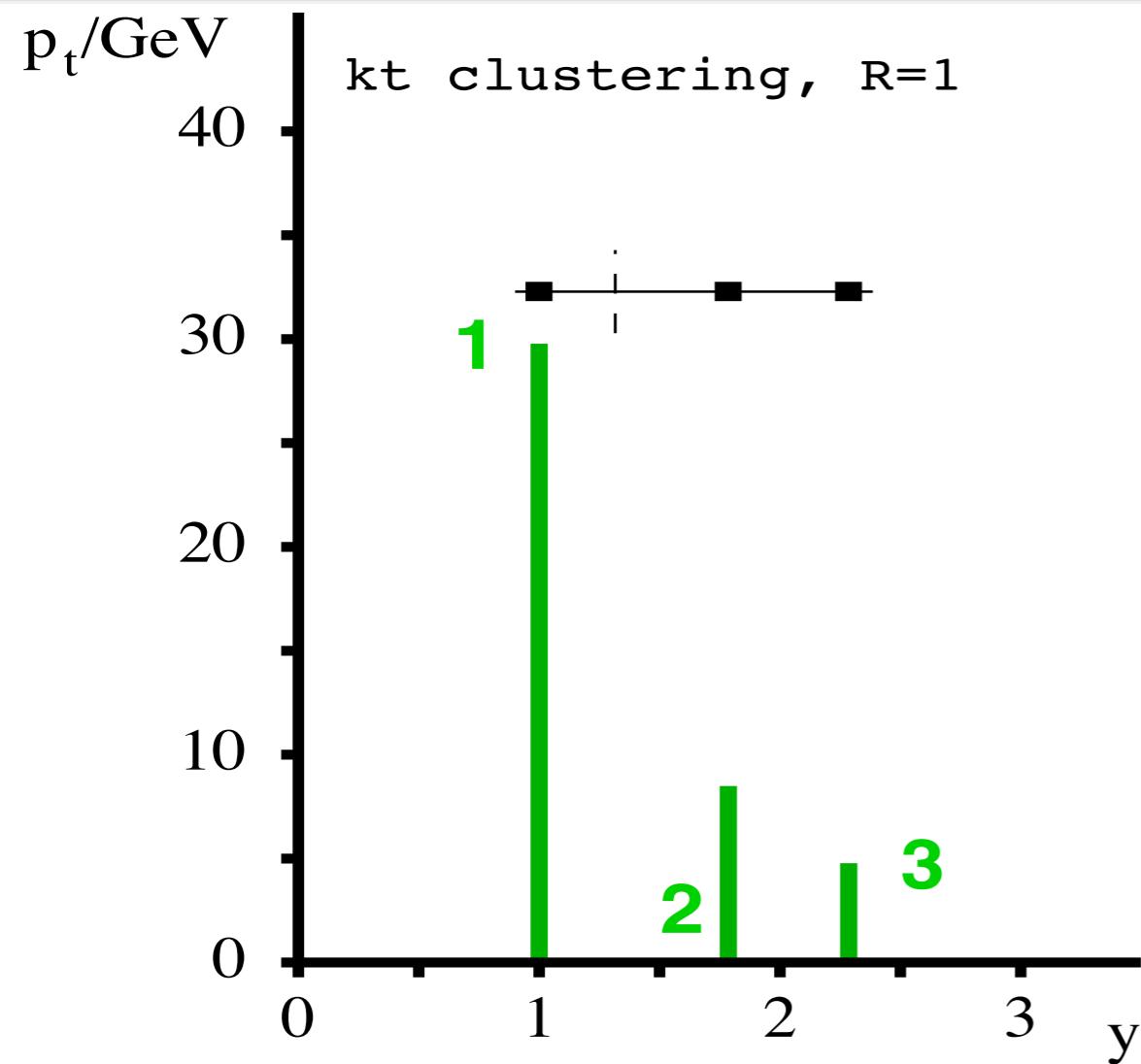
# Linearity: $k_t$ v. anti- $k_t$



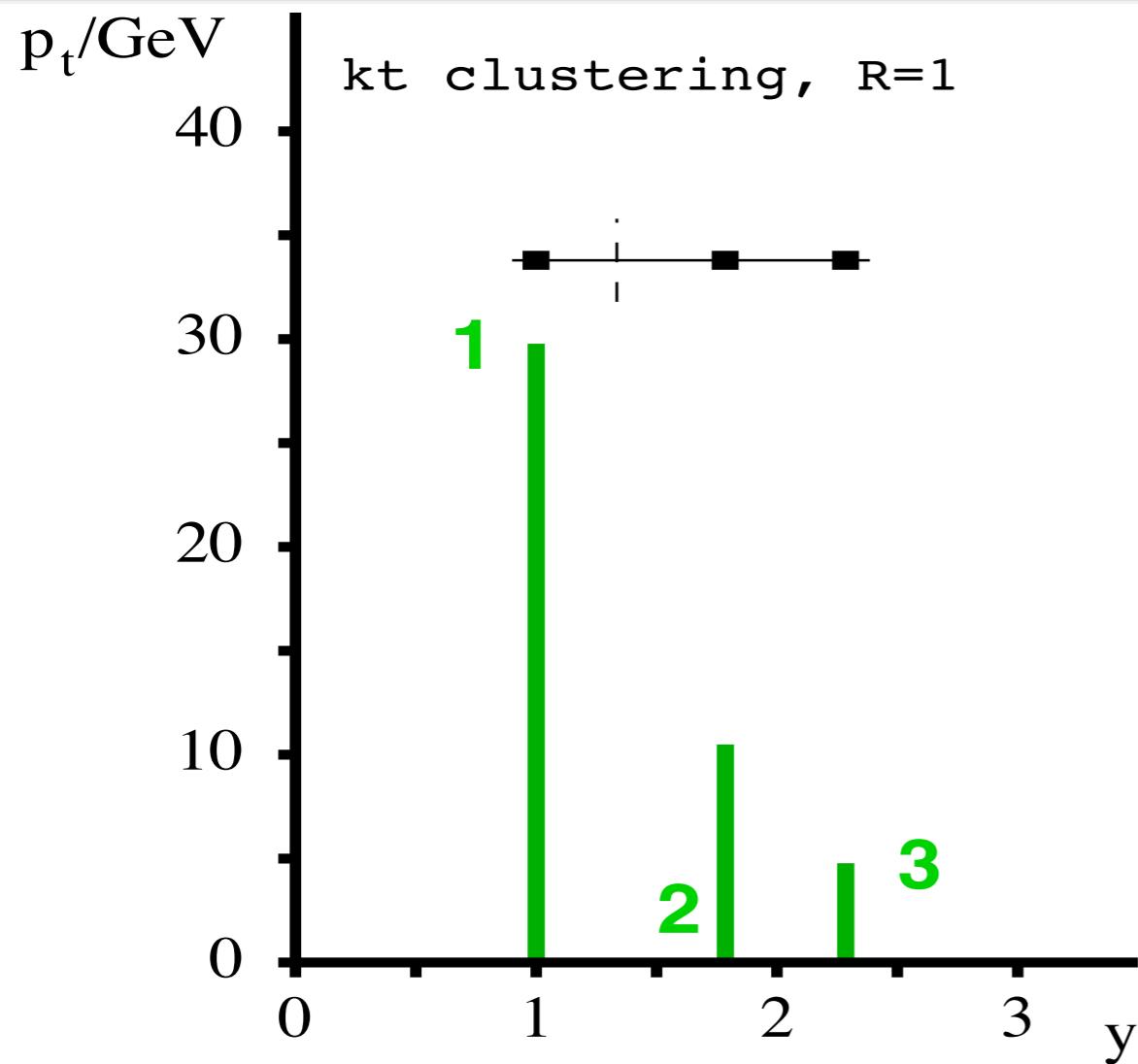
# Linearity: $k_t$ v. anti- $k_t$



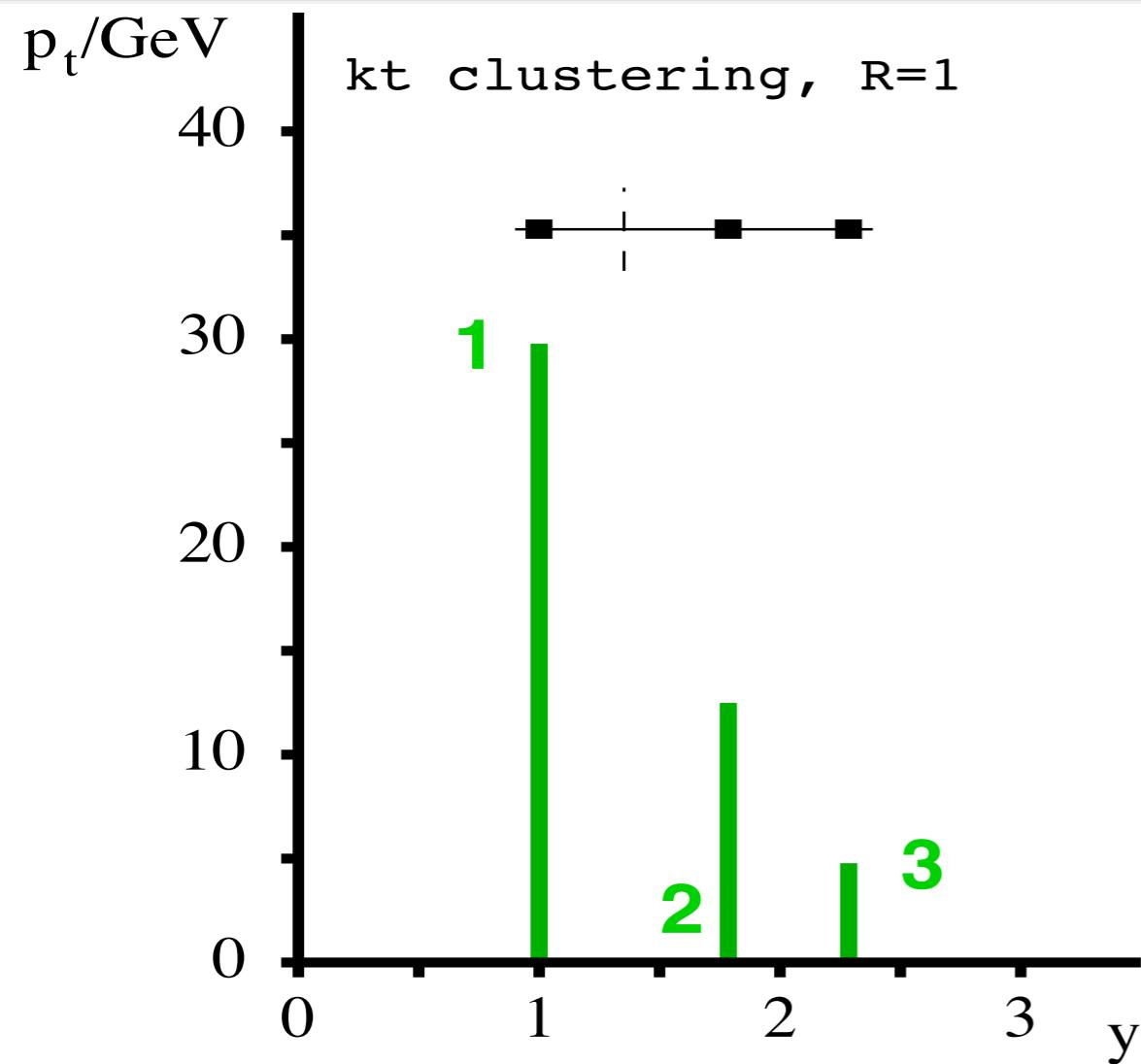
# Linearity: $k_t$ v. anti- $k_t$



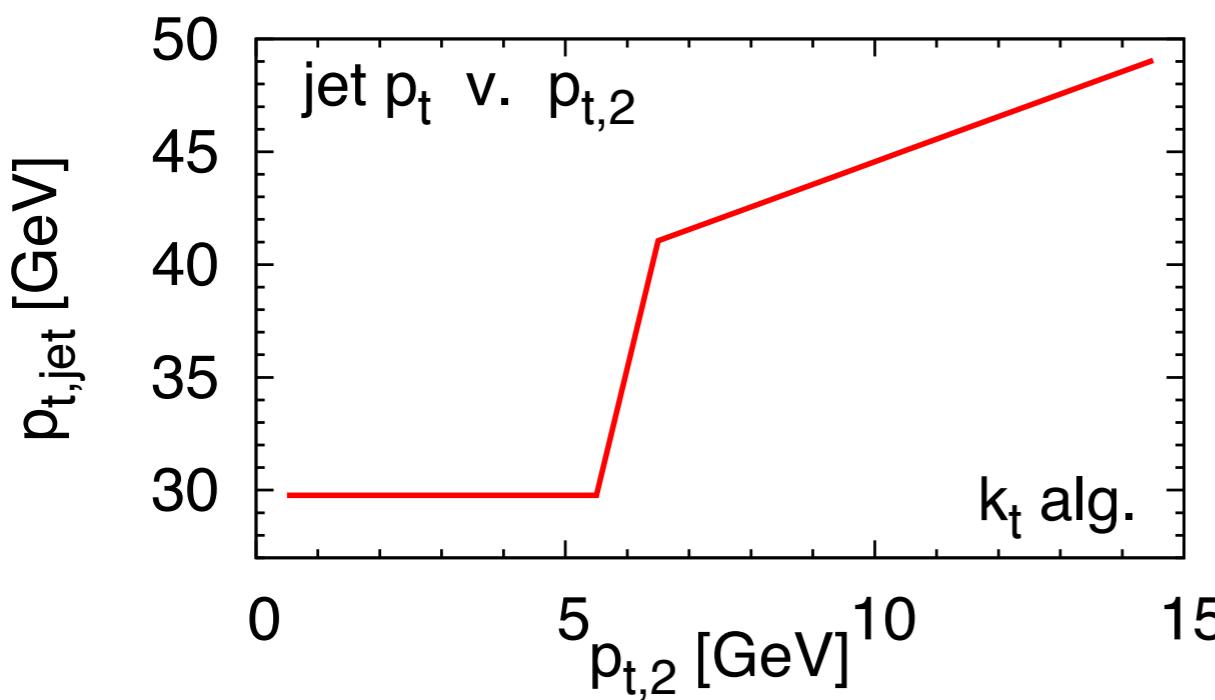
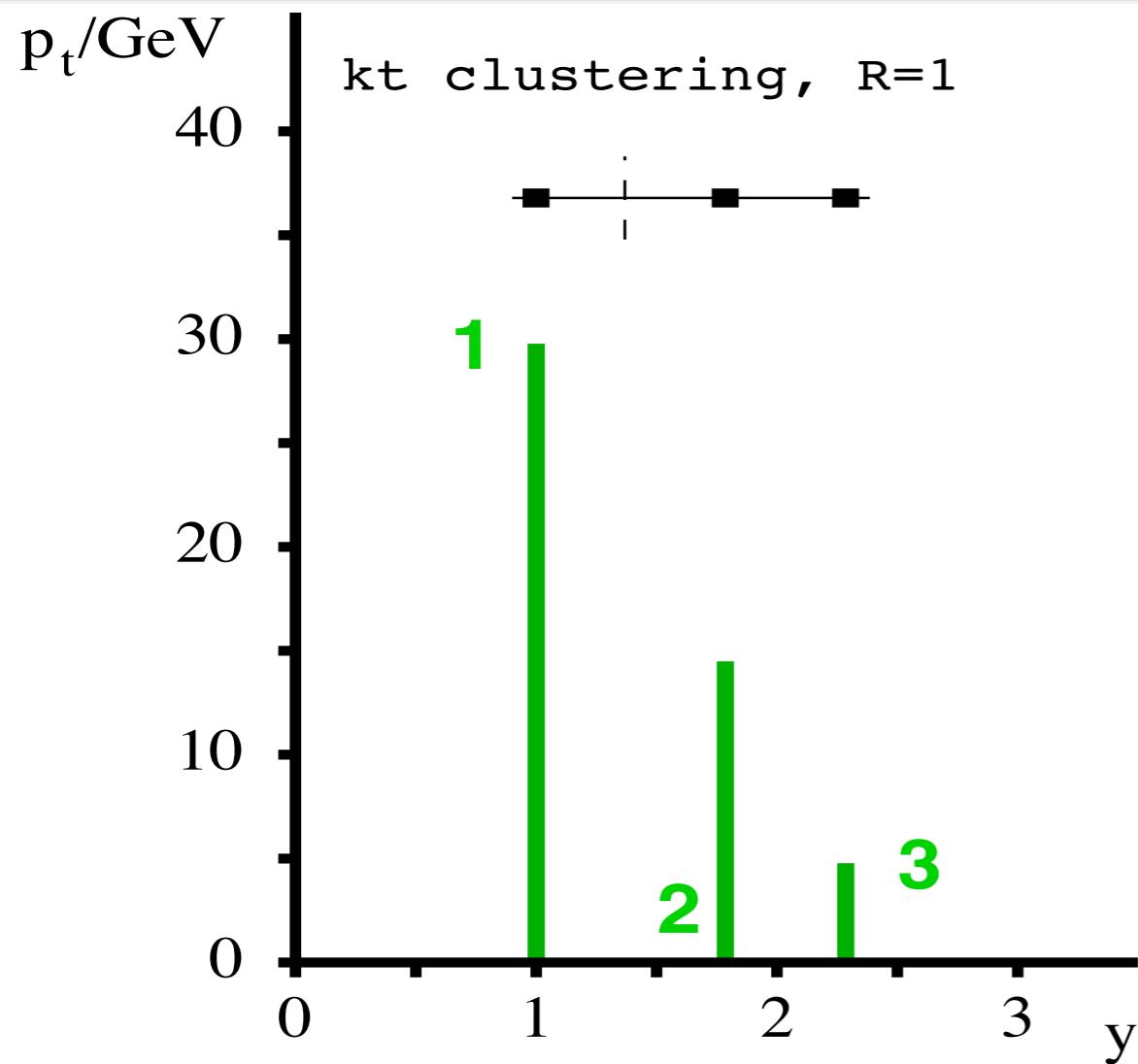
# Linearity: $k_t$ v. anti- $k_t$



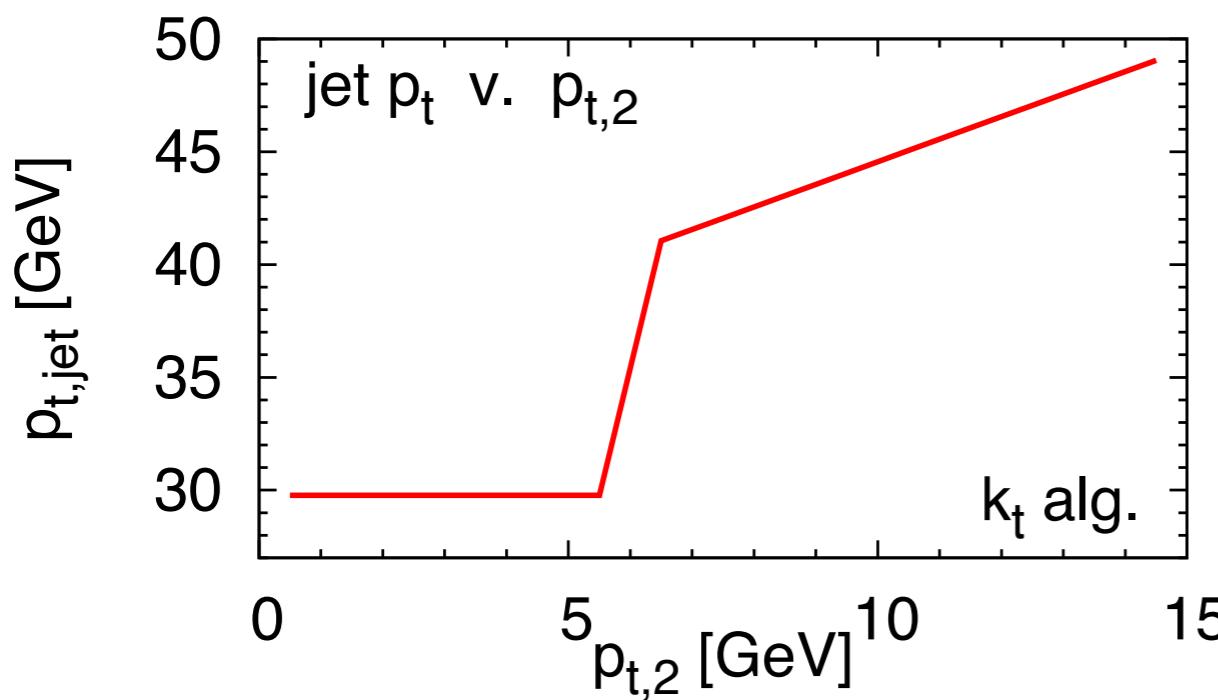
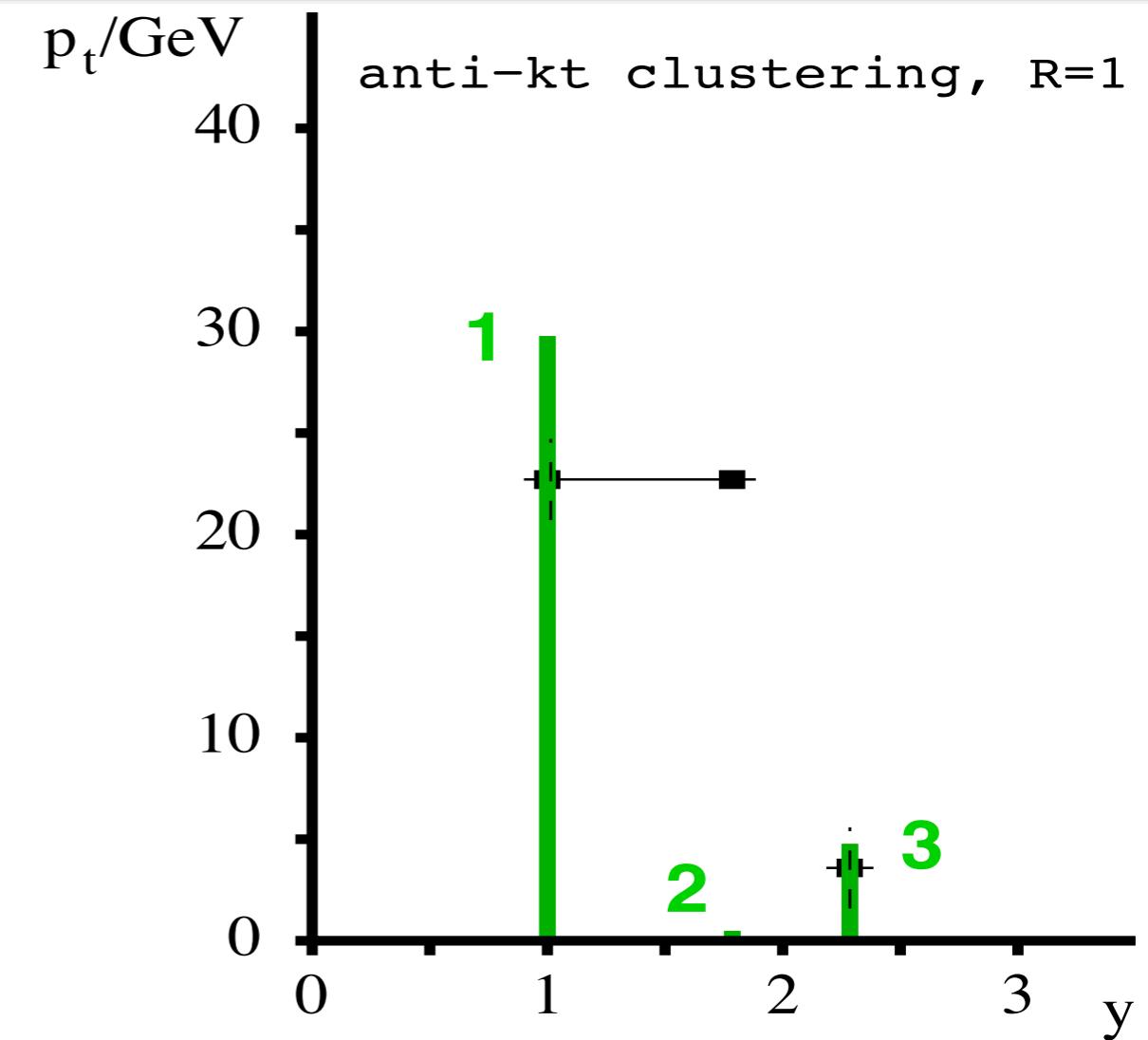
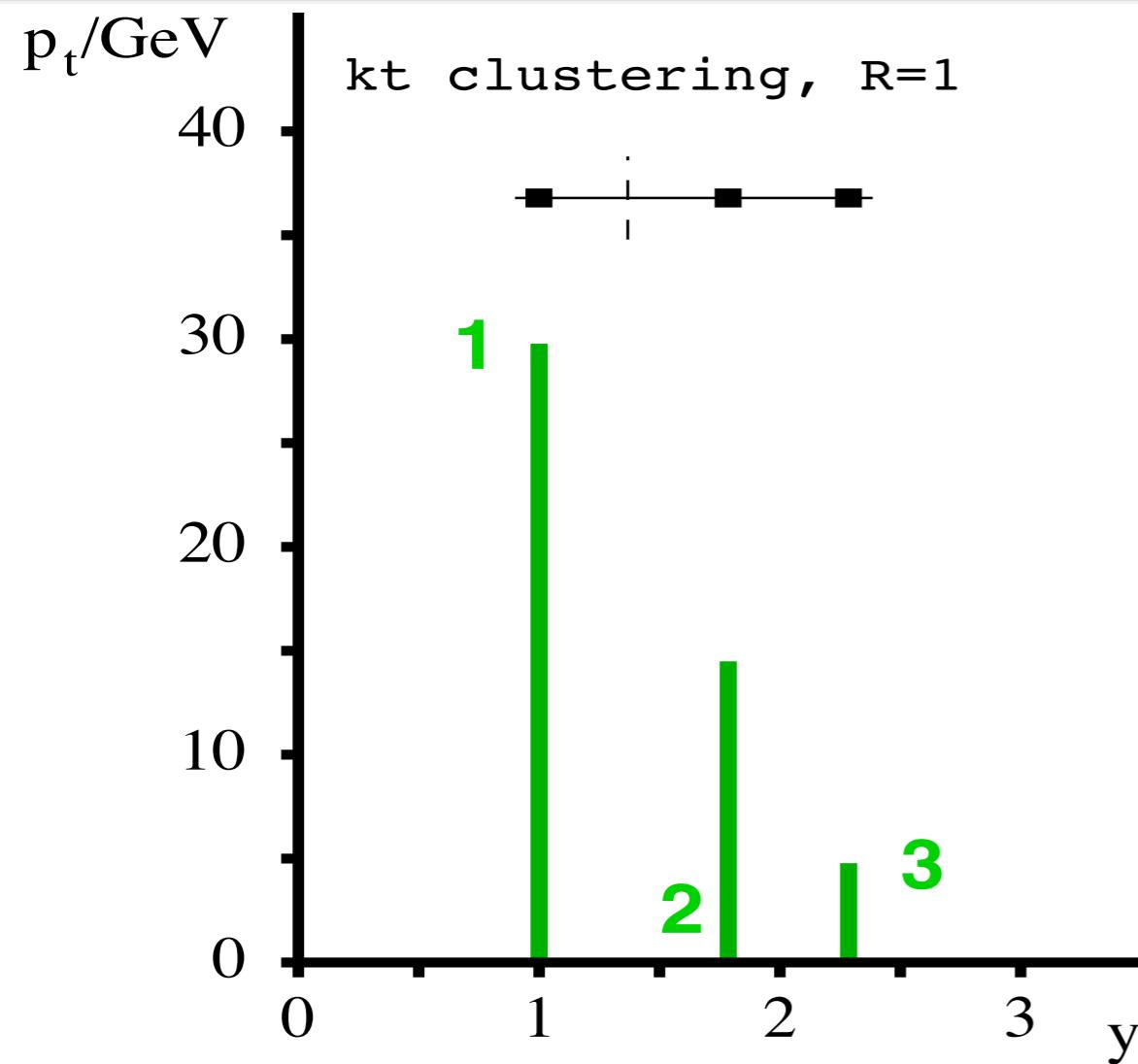
# Linearity: $k_t$ v. anti- $k_t$



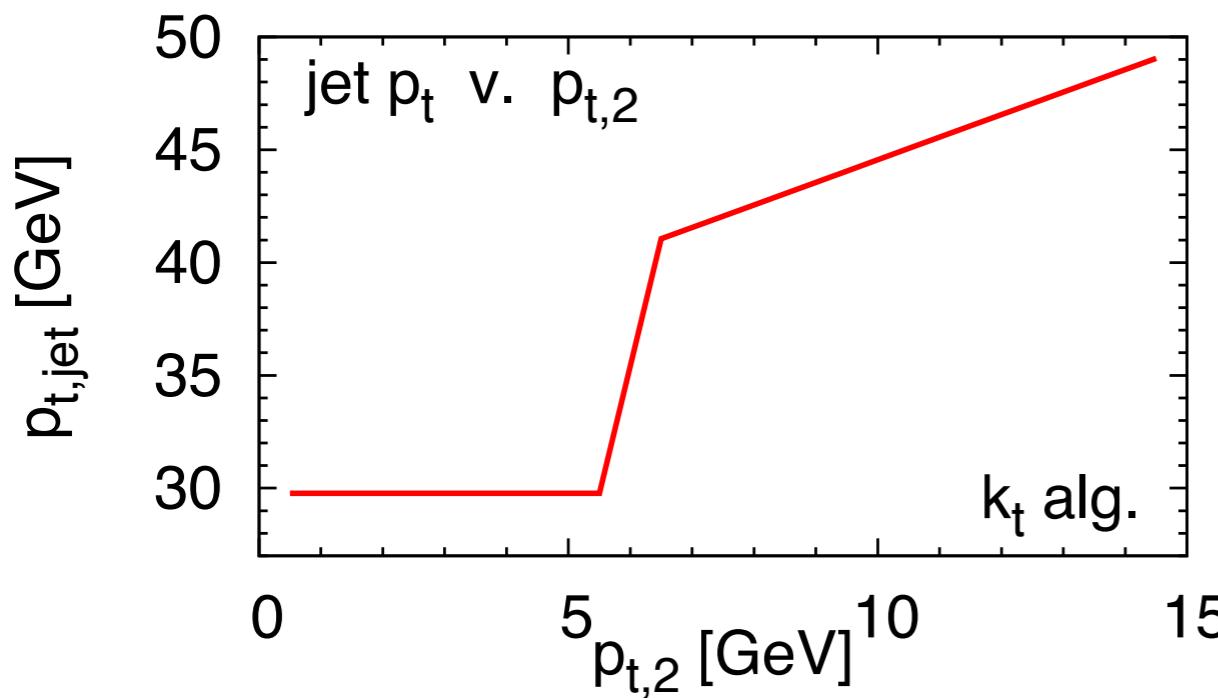
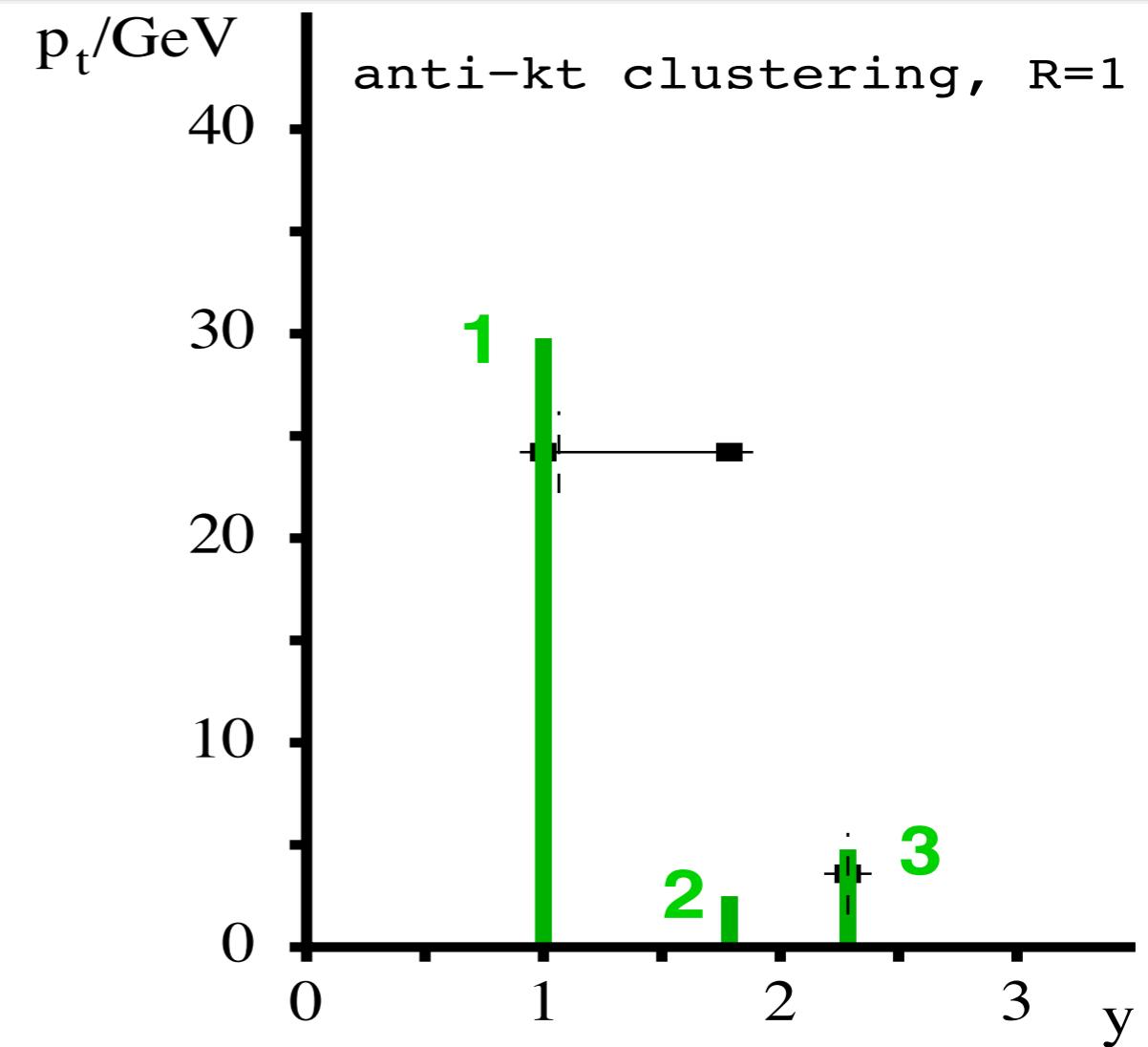
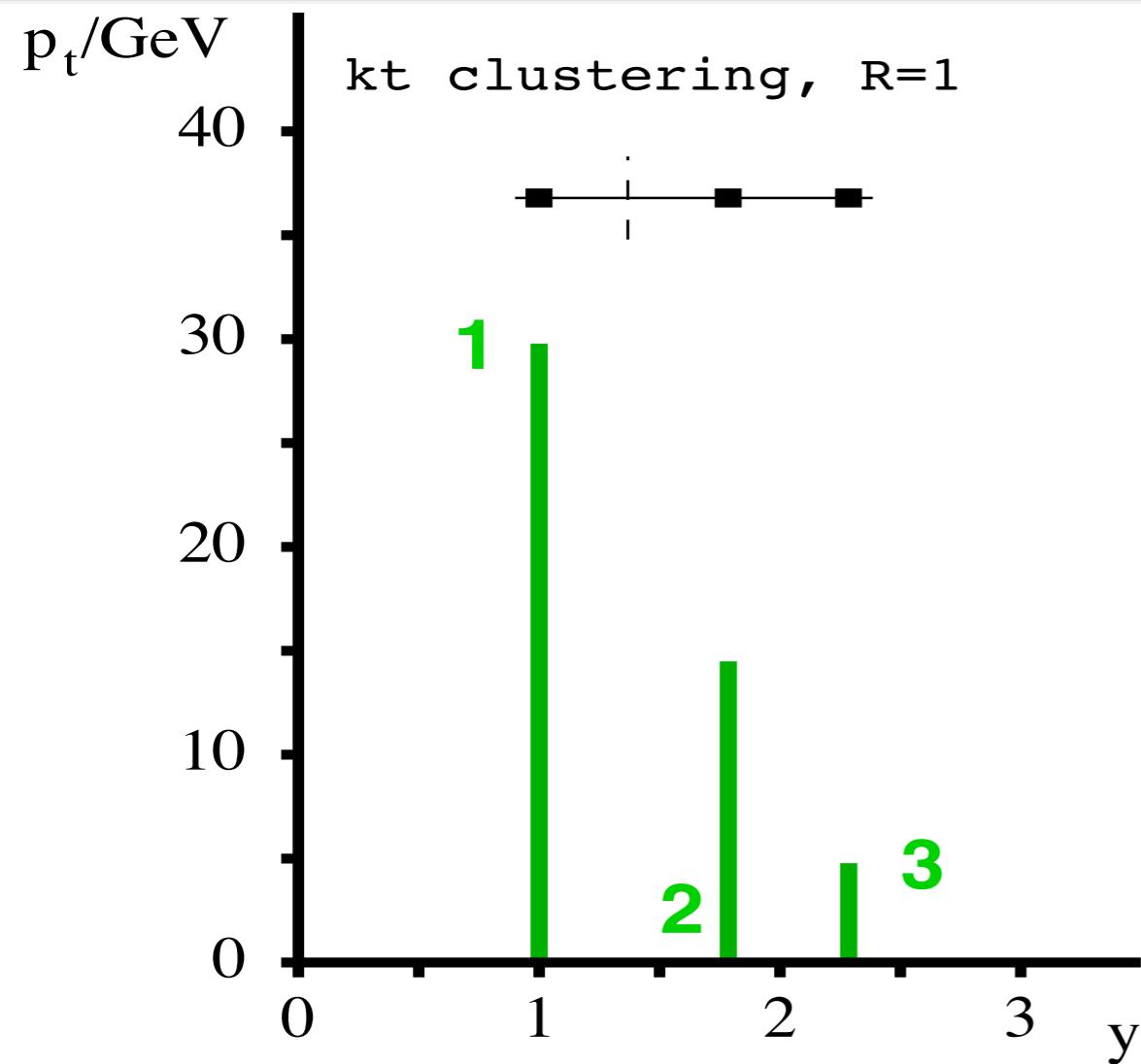
# Linearity: $k_t$ v. anti- $k_t$



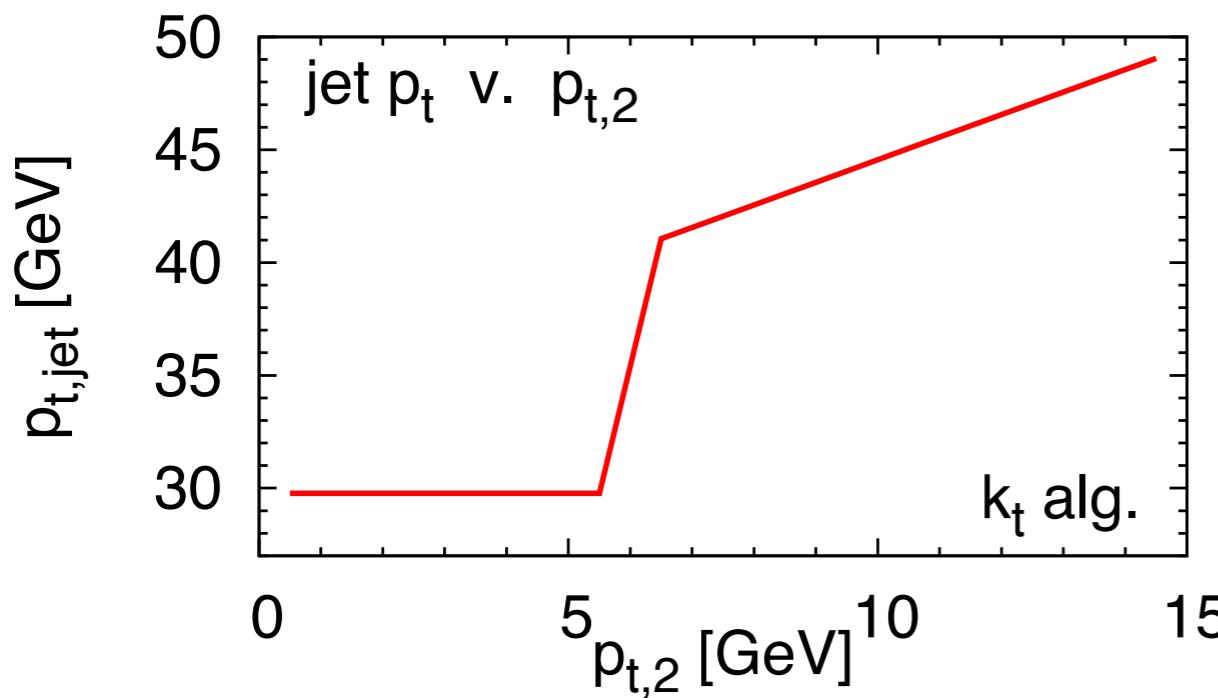
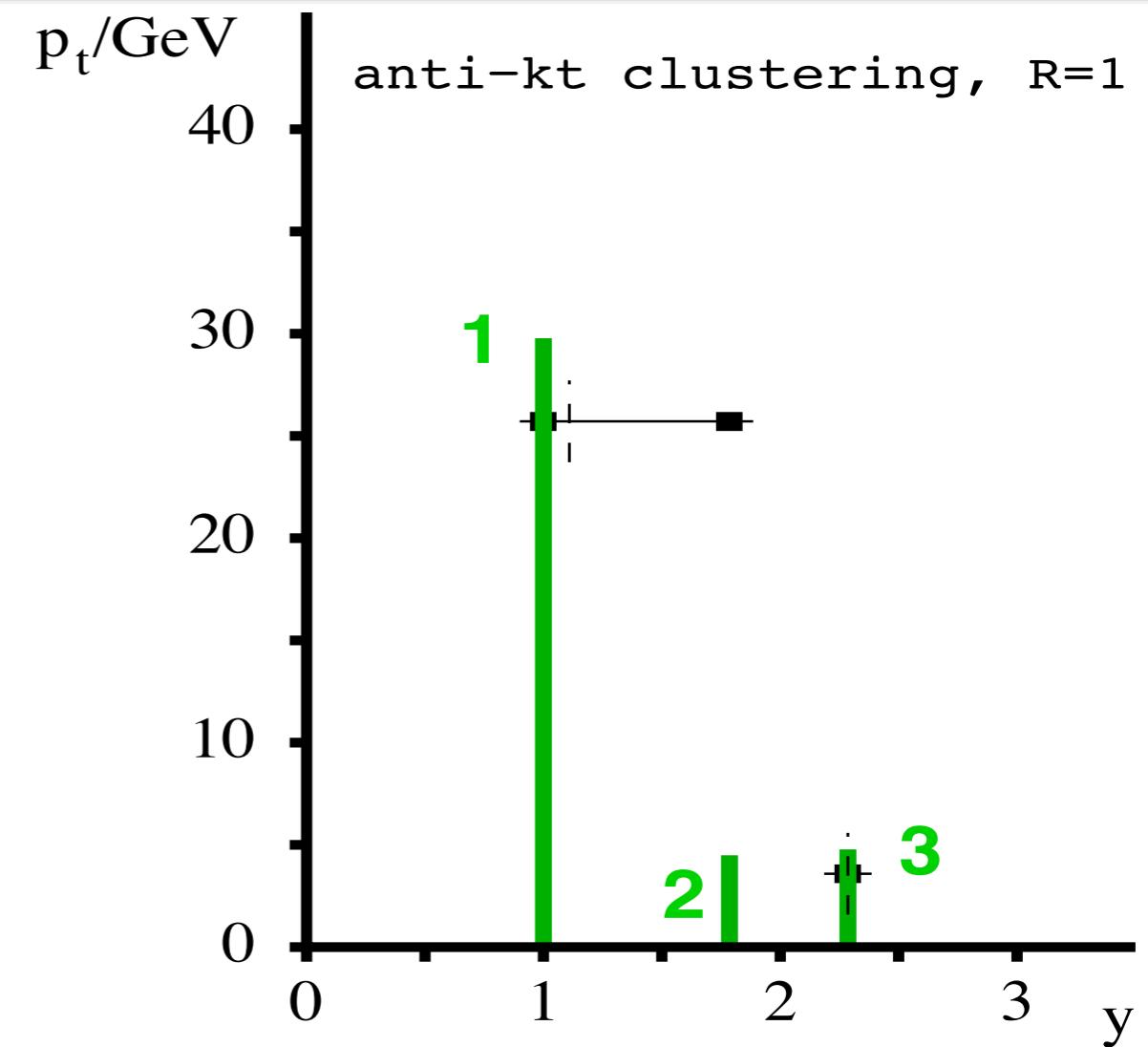
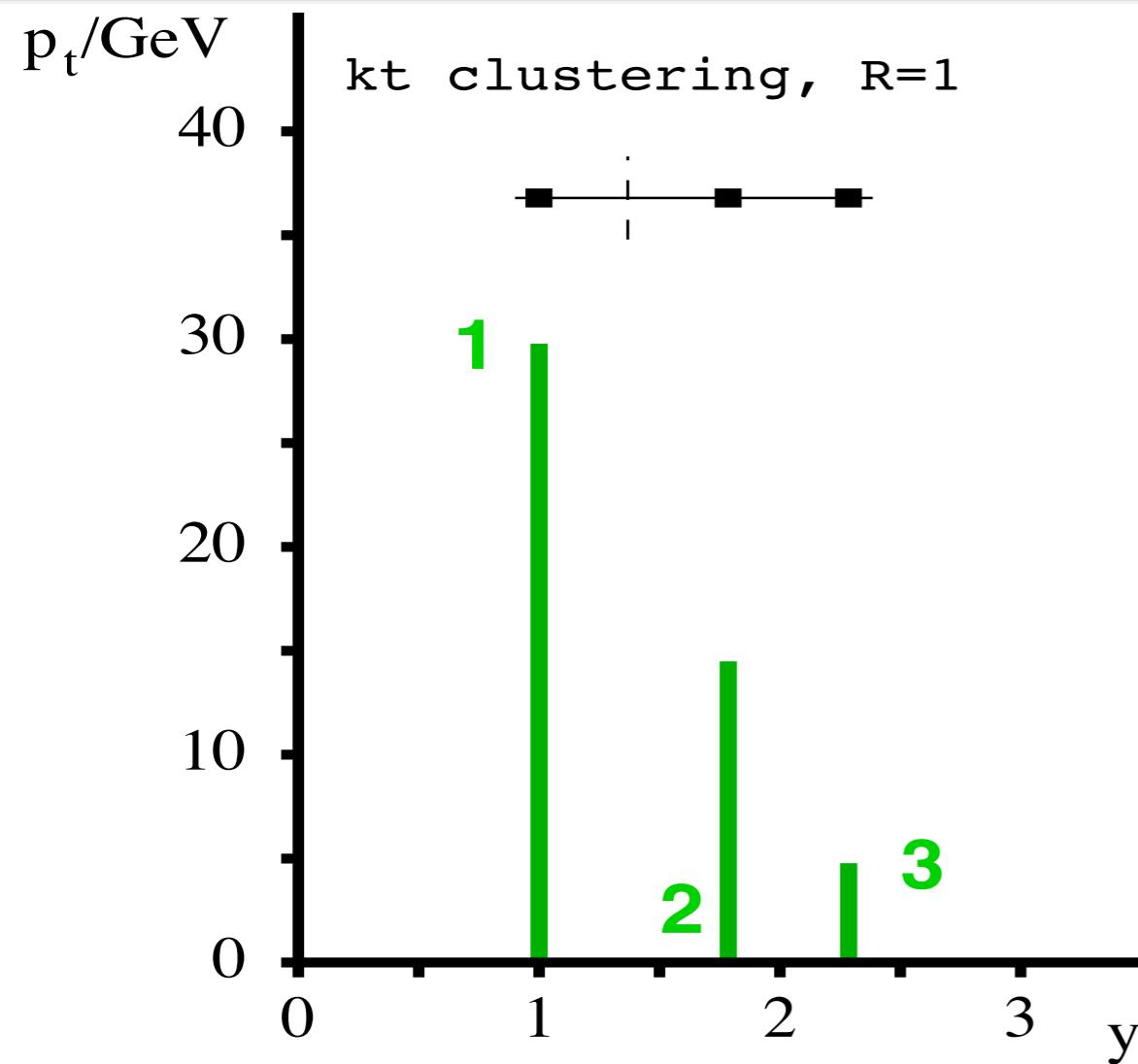
# Linearity: $k_t$ v. anti- $k_t$



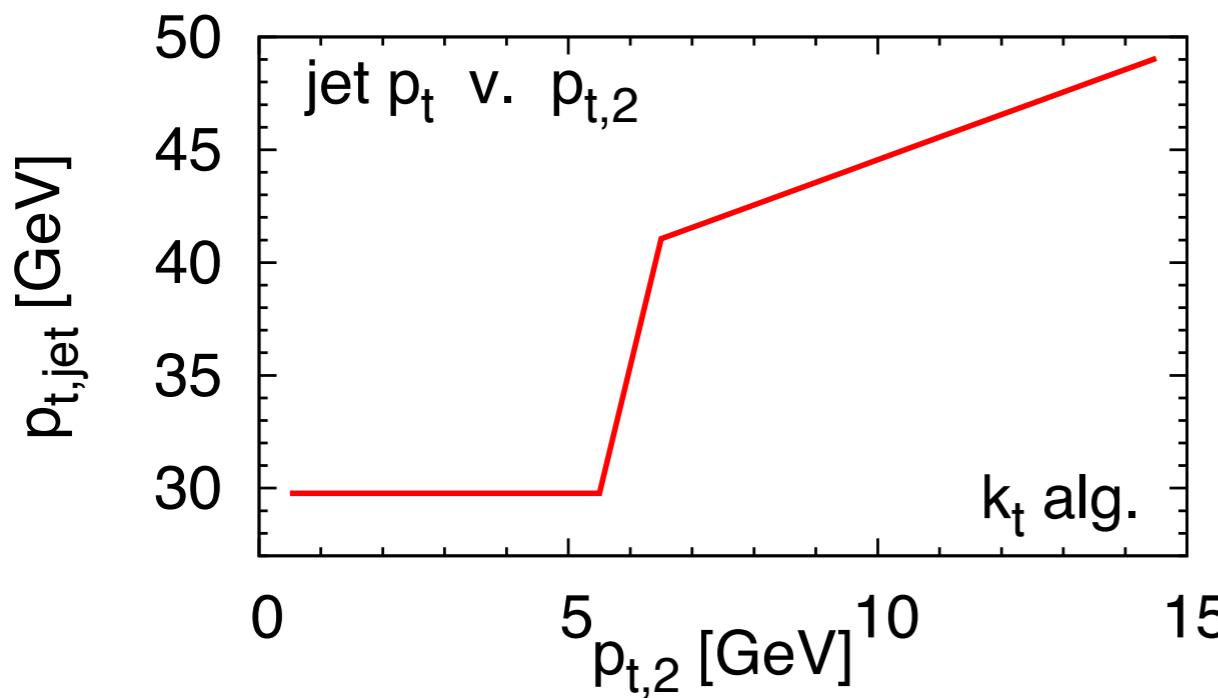
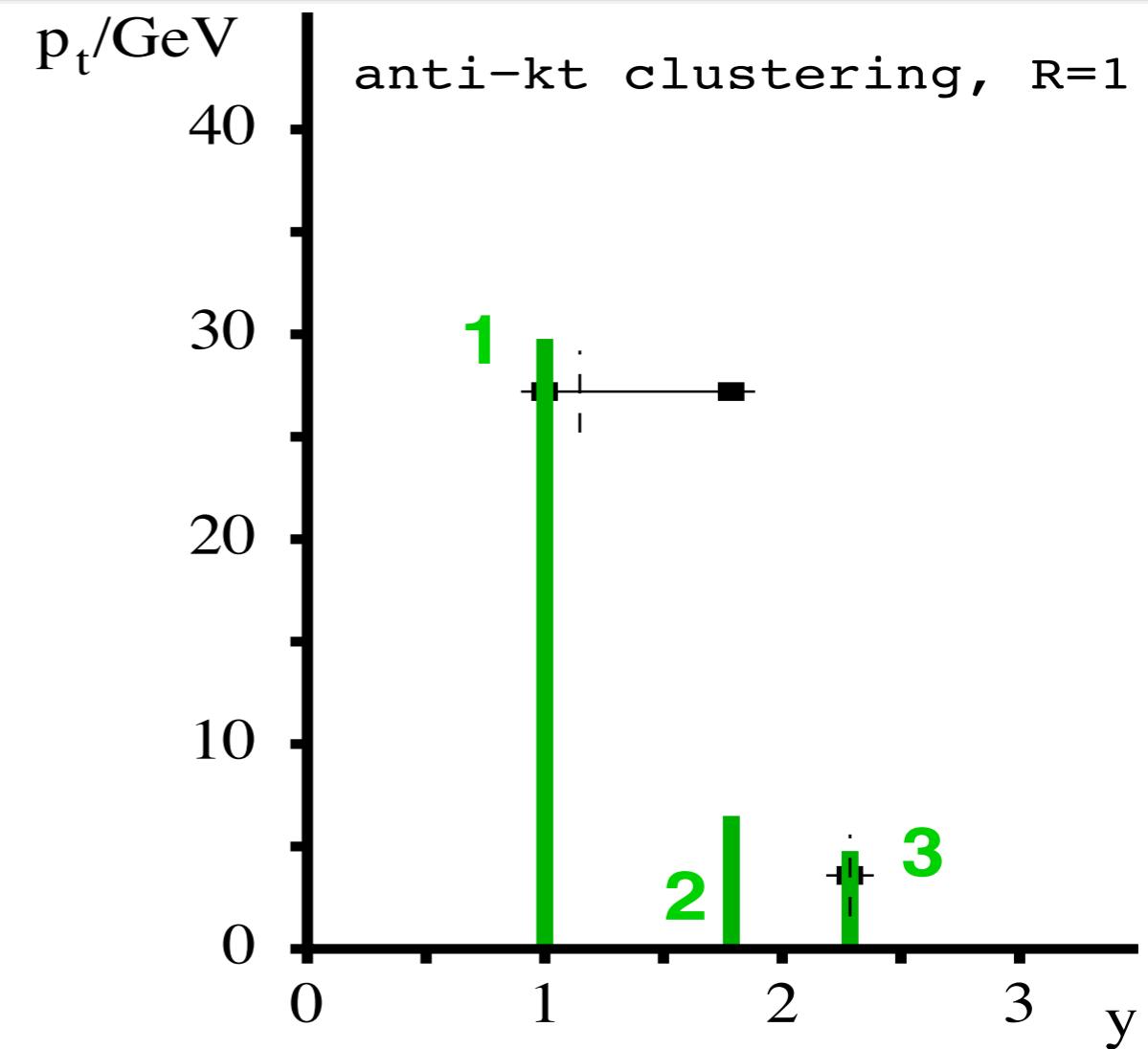
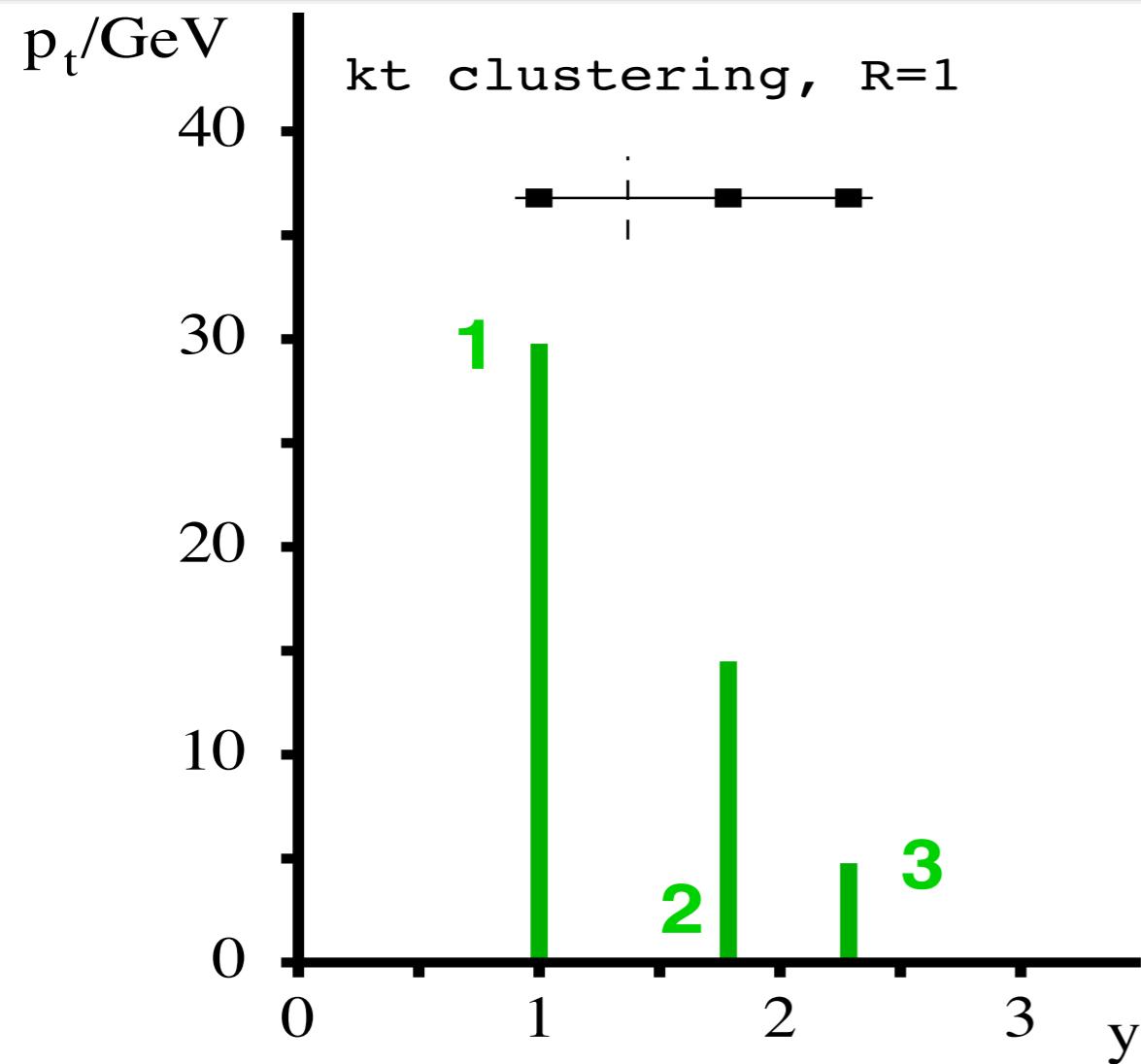
# Linearity: $k_t$ v. anti- $k_t$



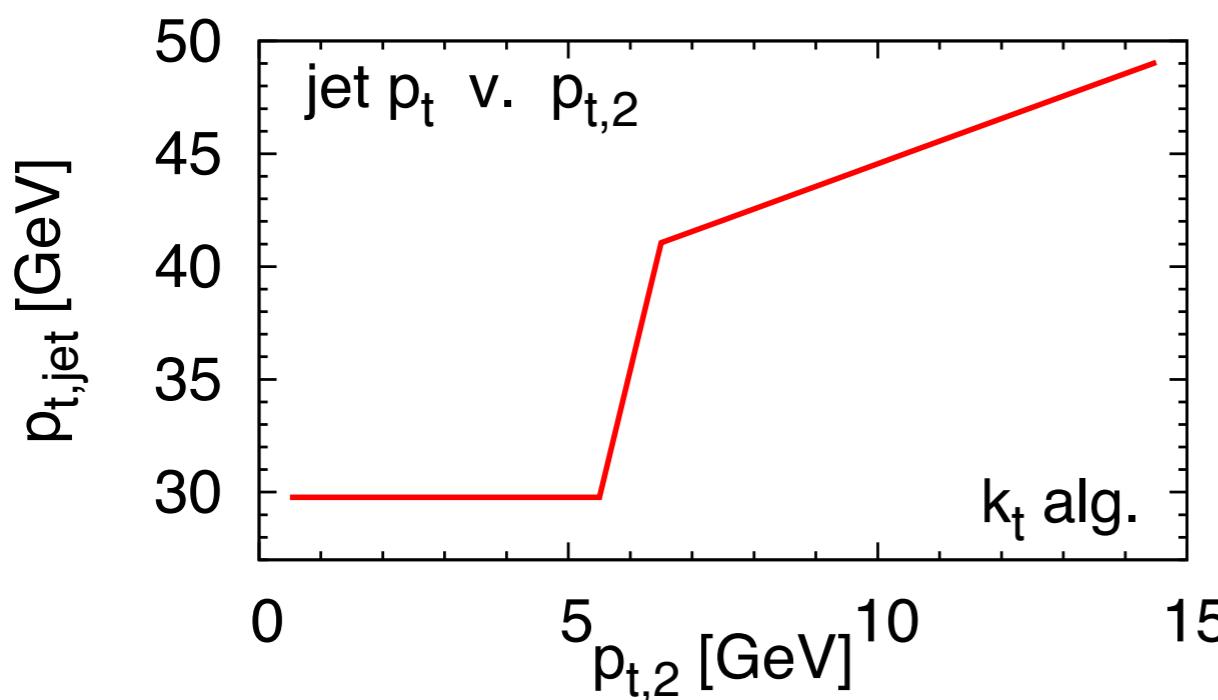
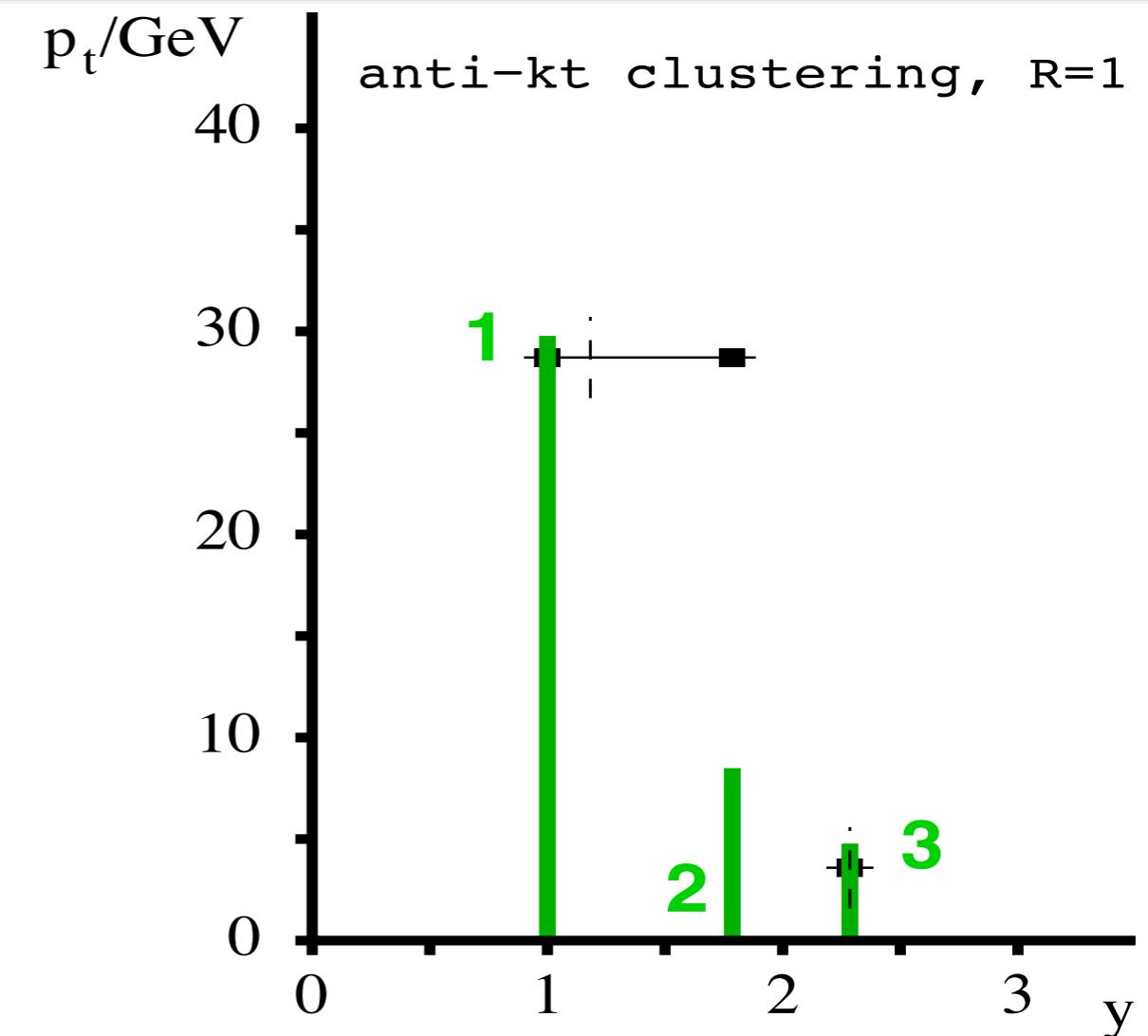
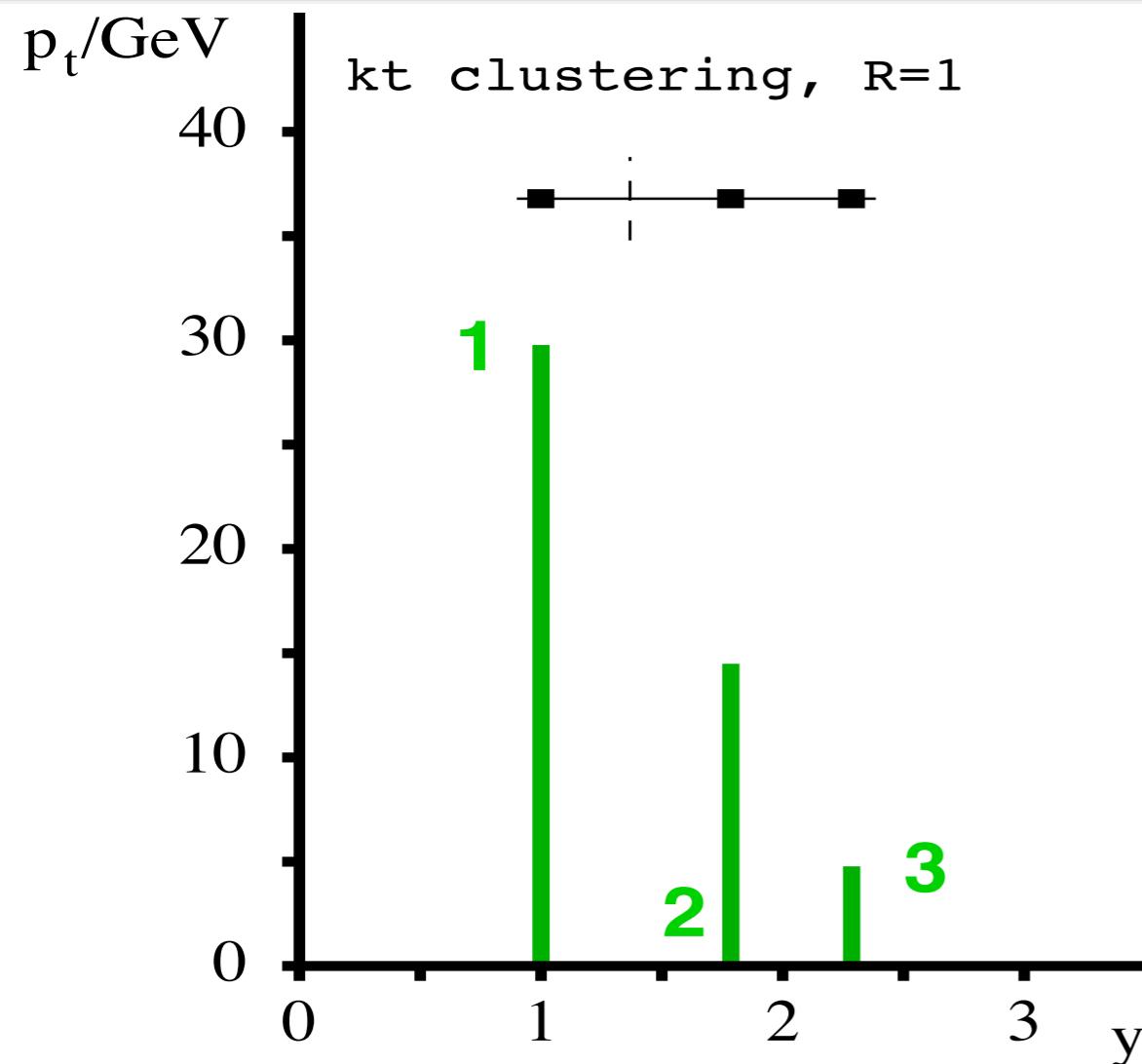
# Linearity: $k_t$ v. anti- $k_t$



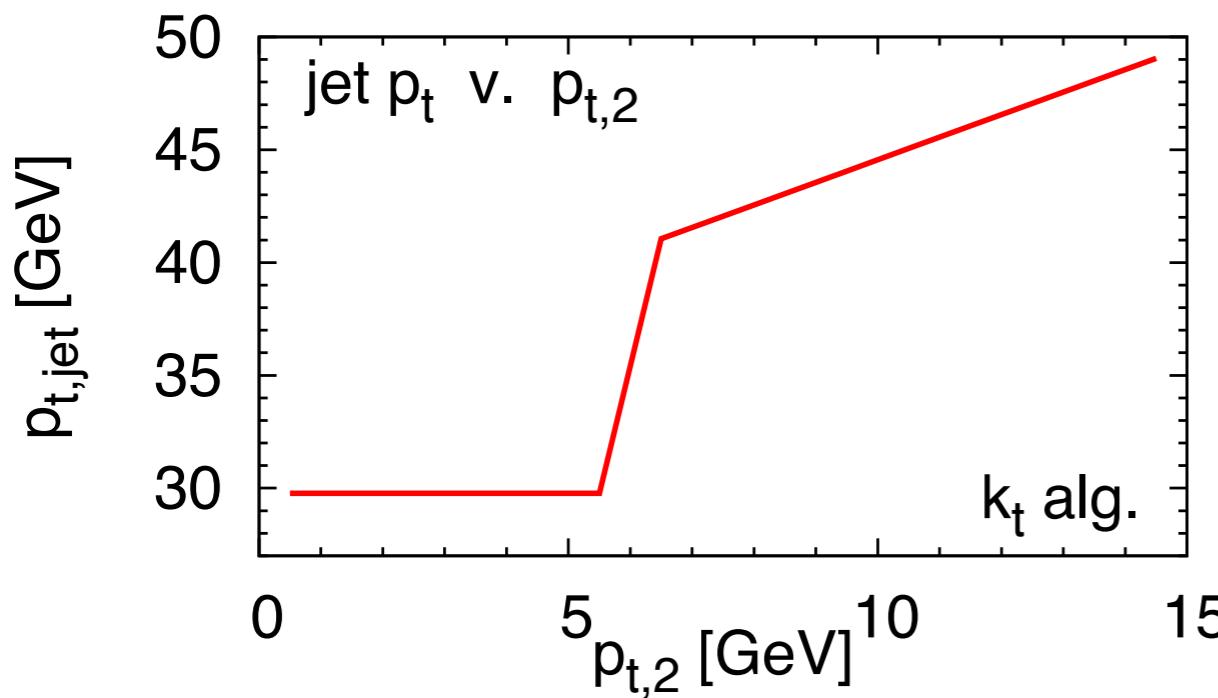
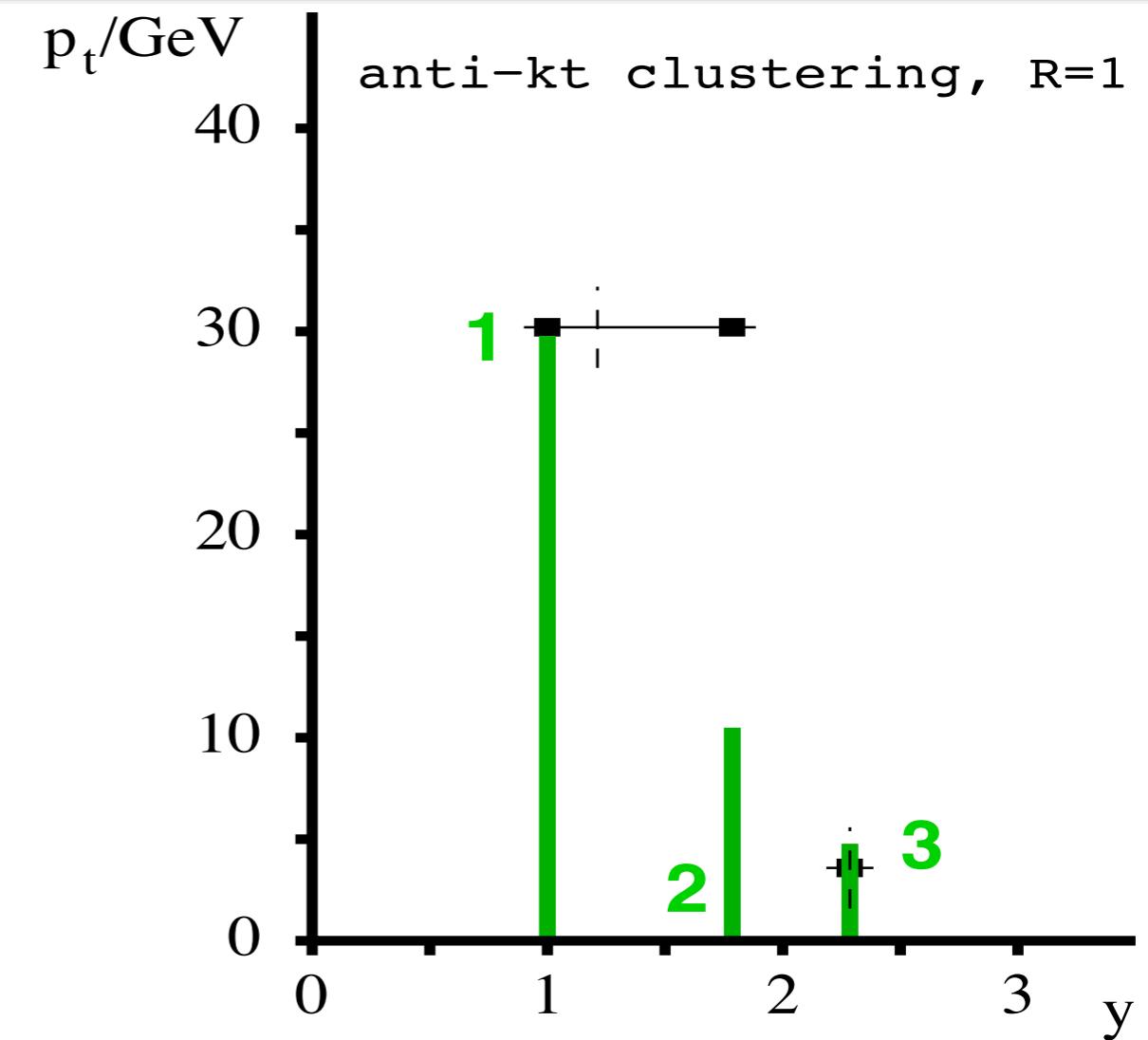
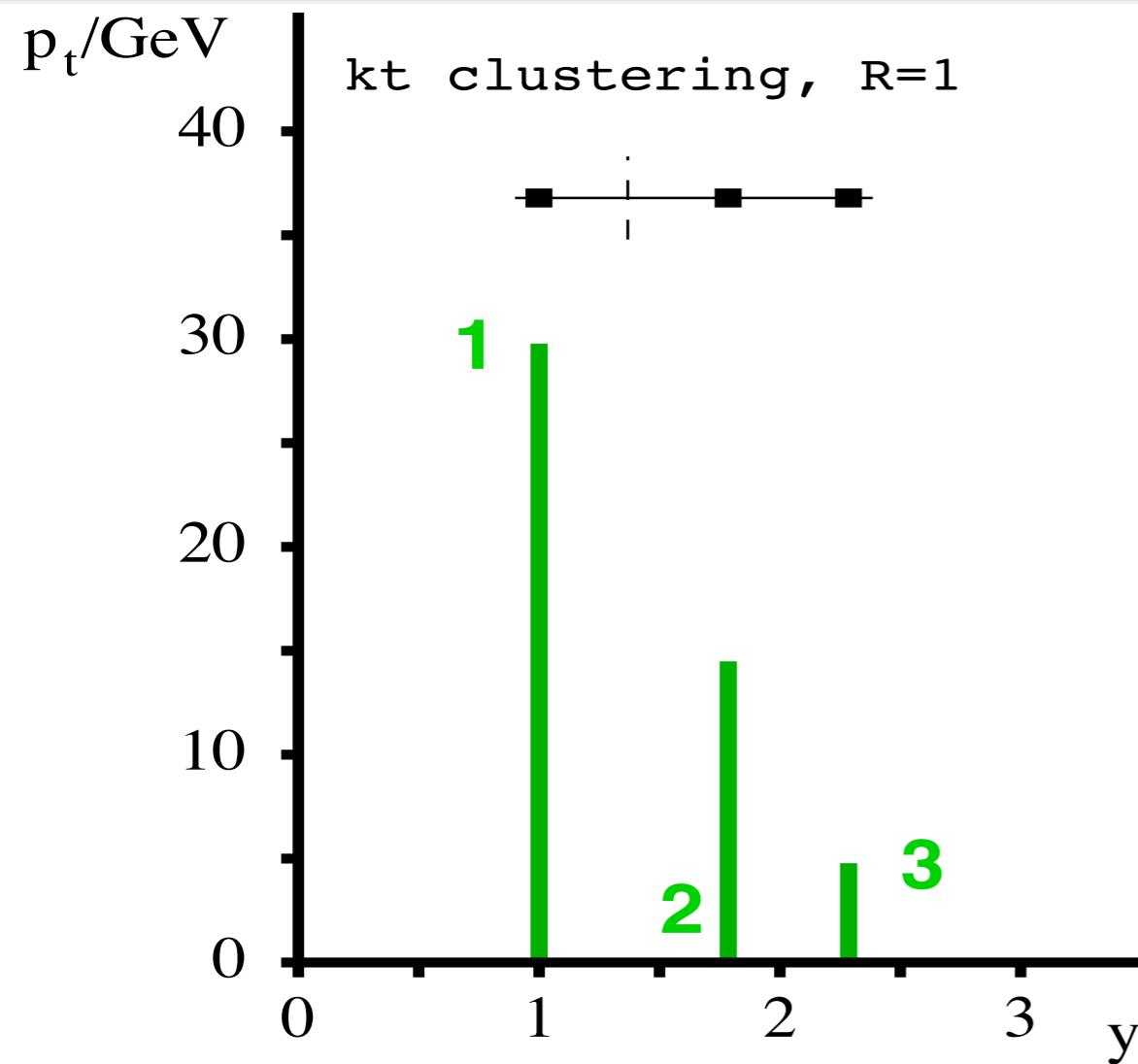
# Linearity: $k_t$ v. anti- $k_t$



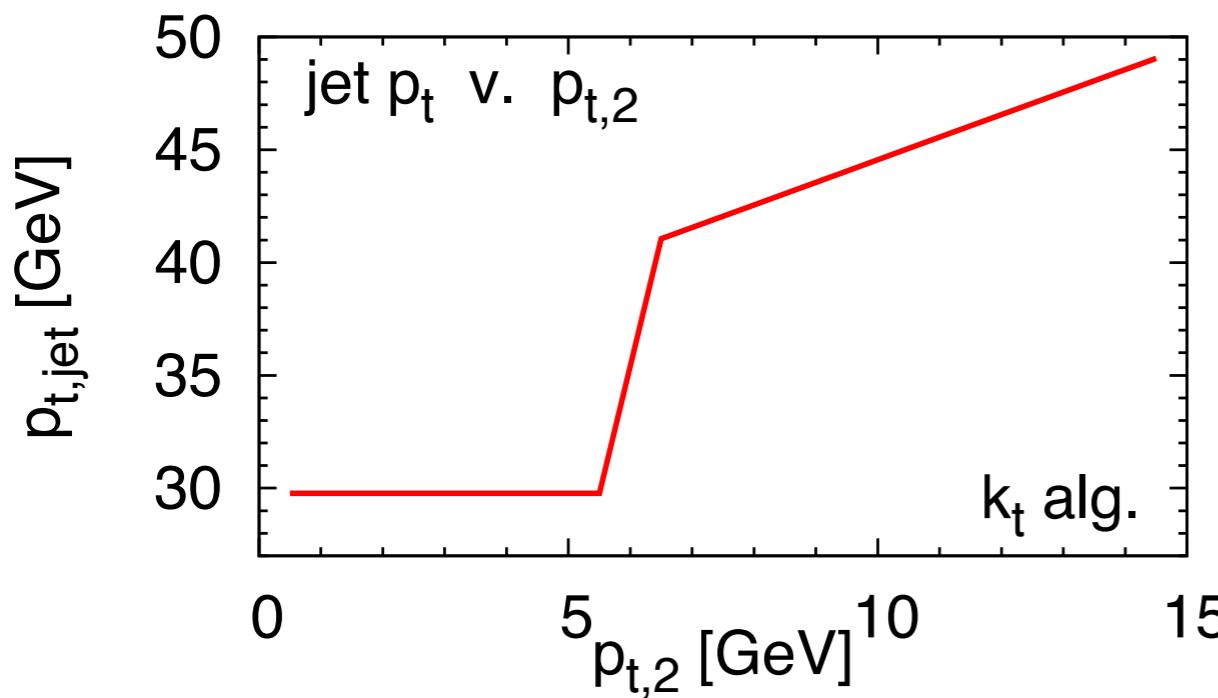
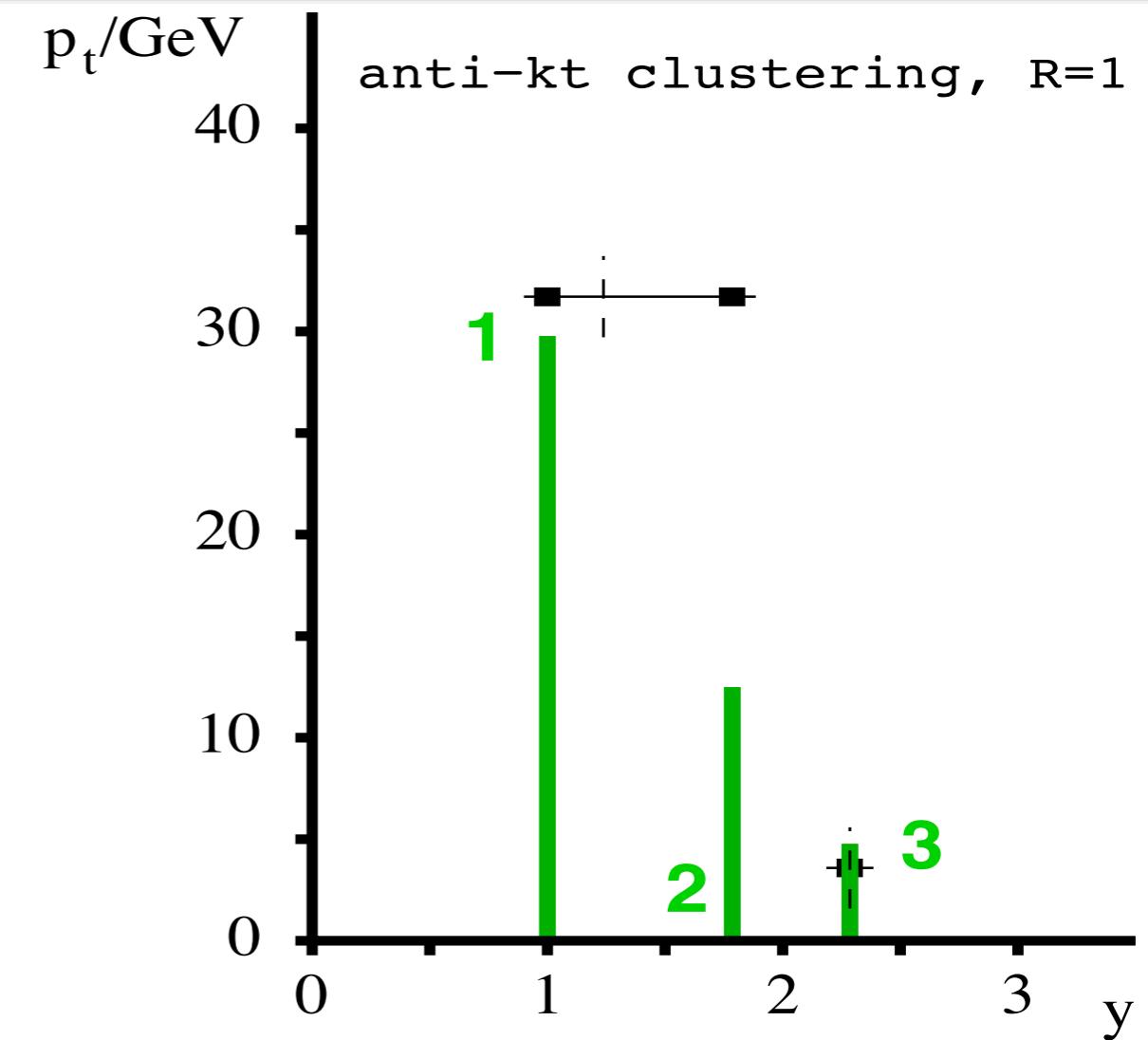
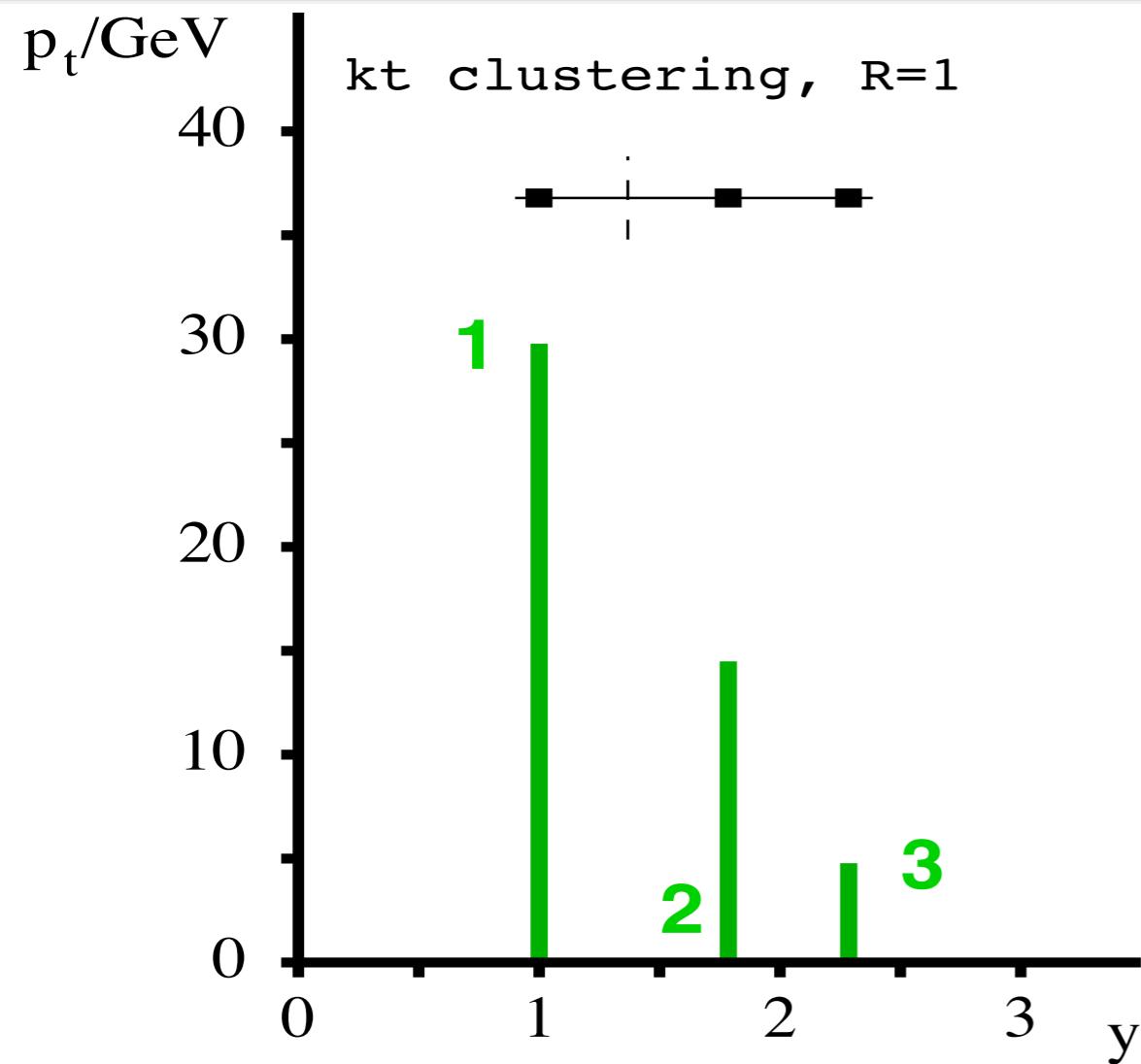
# Linearity: $k_t$ v. anti- $k_t$



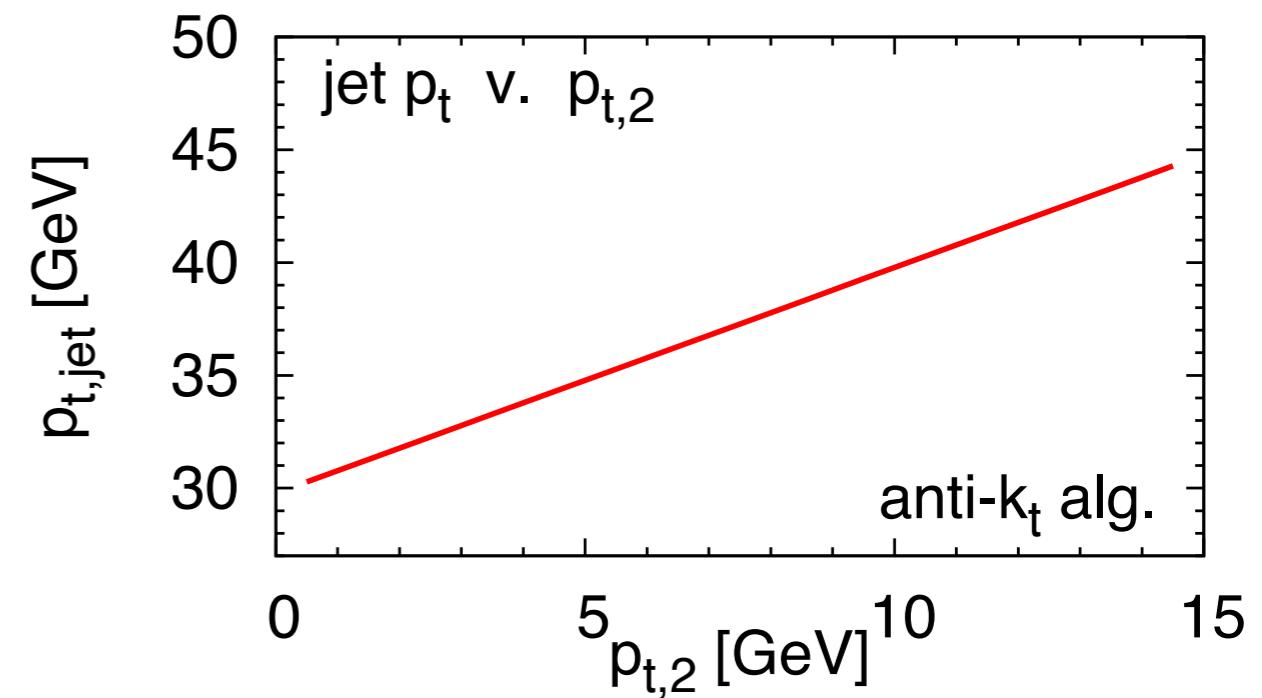
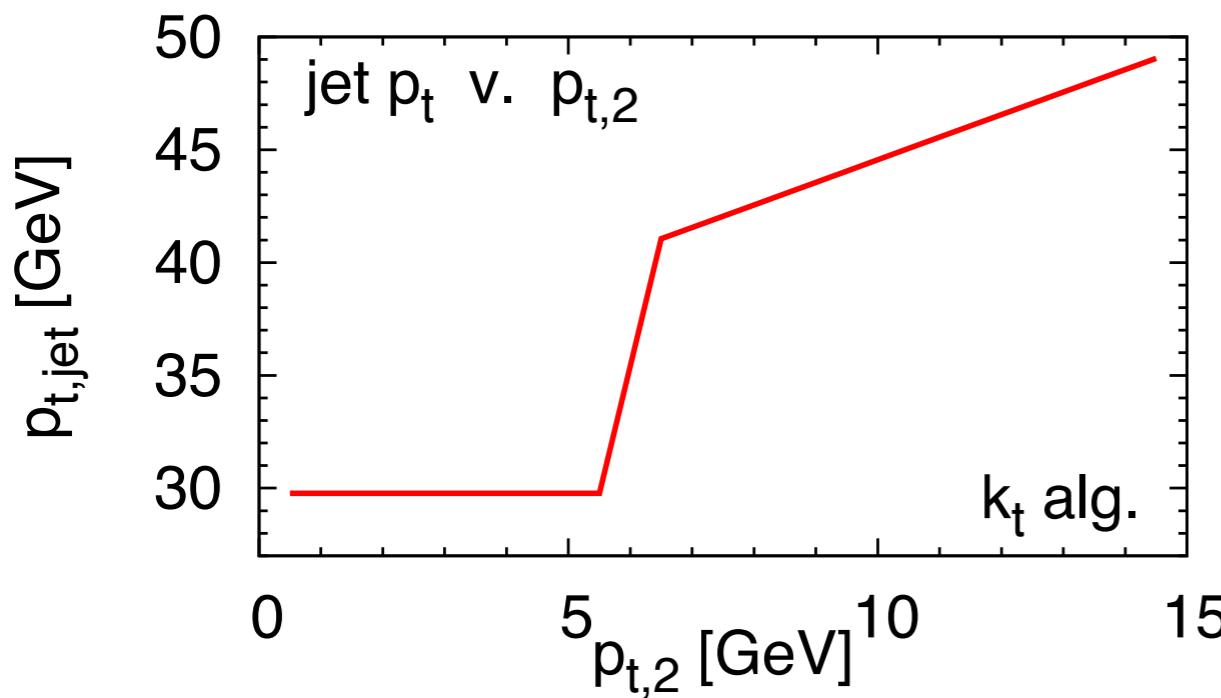
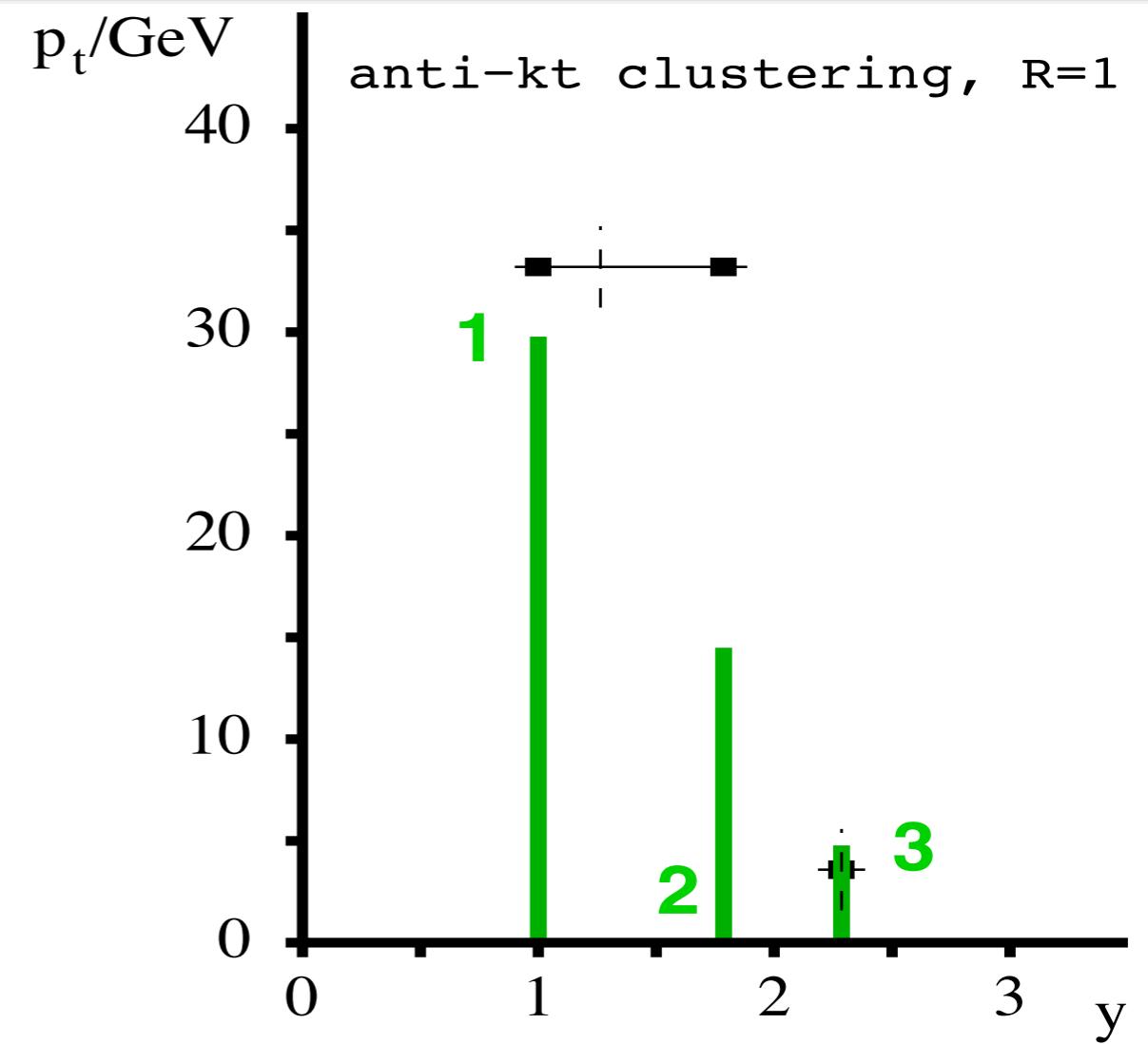
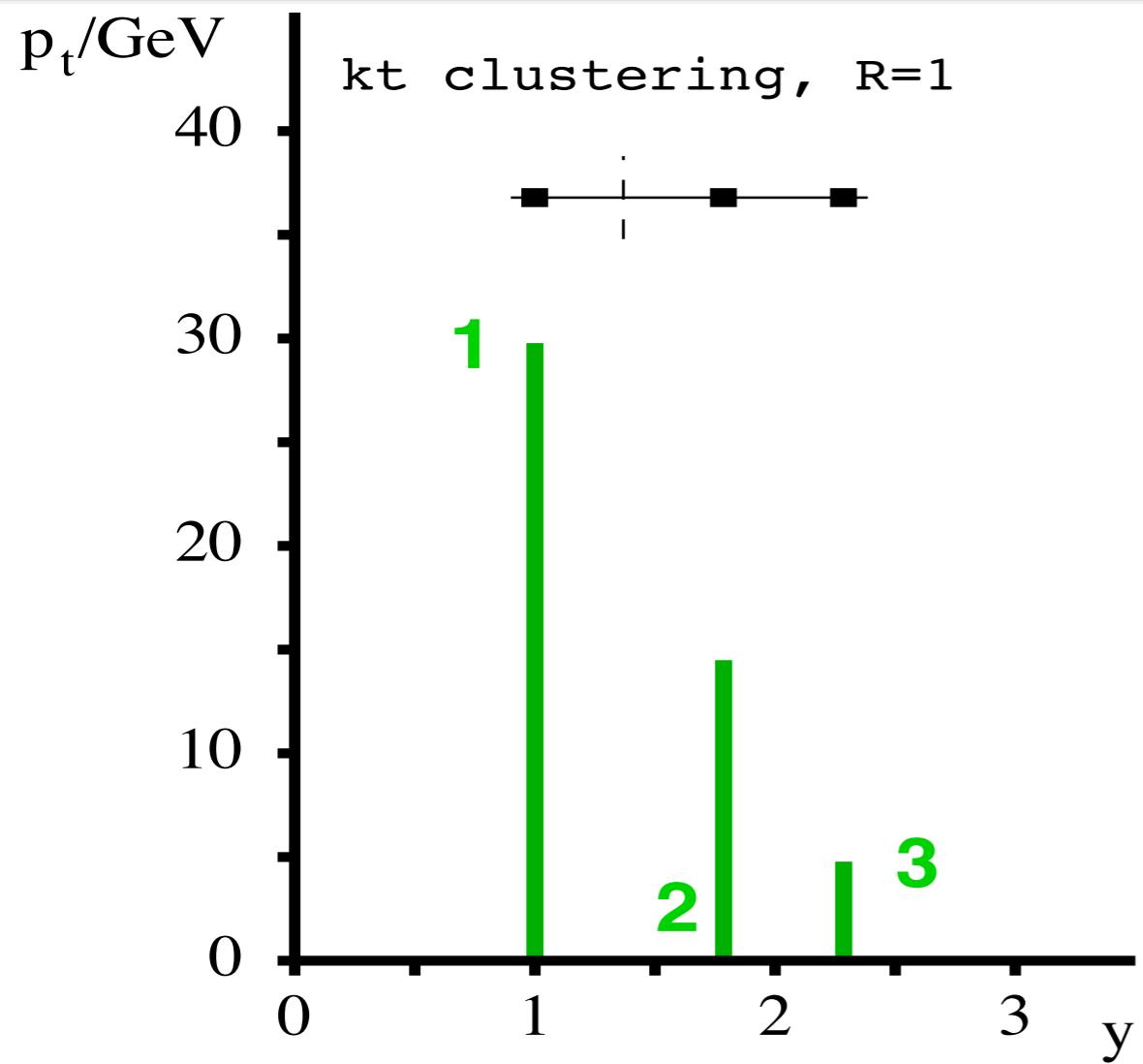
# Linearity: $k_t$ v. anti- $k_t$



# Linearity: $k_t$ v. anti- $k_t$



# Linearity: $k_t$ v. anti- $k_t$



```
// specify a jet definition
double R = 0.4
JetDefinition jet_def(antikt_algorithm, R);
```

jet\_algorithm can be any one of the four IRC safe algorithms, or also  
most of the old IRC-unsafe ones, for legacy purposes

```
// specify the input particles
vector<PseudoJet> input_particles = . . .;
```

## More this afternoon in the tutorial

```
// specify a jet definition
double R = 0.4
JetDefinition jet_def(antikt_algorithm, R);
```

jet\_algorithm can be any one of the four IRC safe algorithms, or also most of the old IRC-unsafe ones, for legacy purposes

```
// specify the input particles
vector<PseudoJet> input_particles = . . .;
```

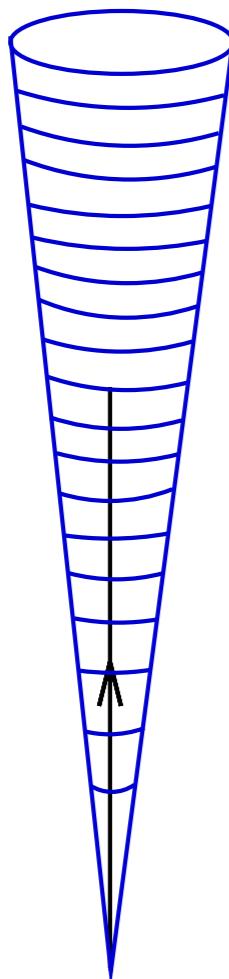
```
// extract the jets
vector<PseudoJet> jets = jet_def(input_particles);

// pt of hardest jet
double pt_hardest = jets[0].pt();

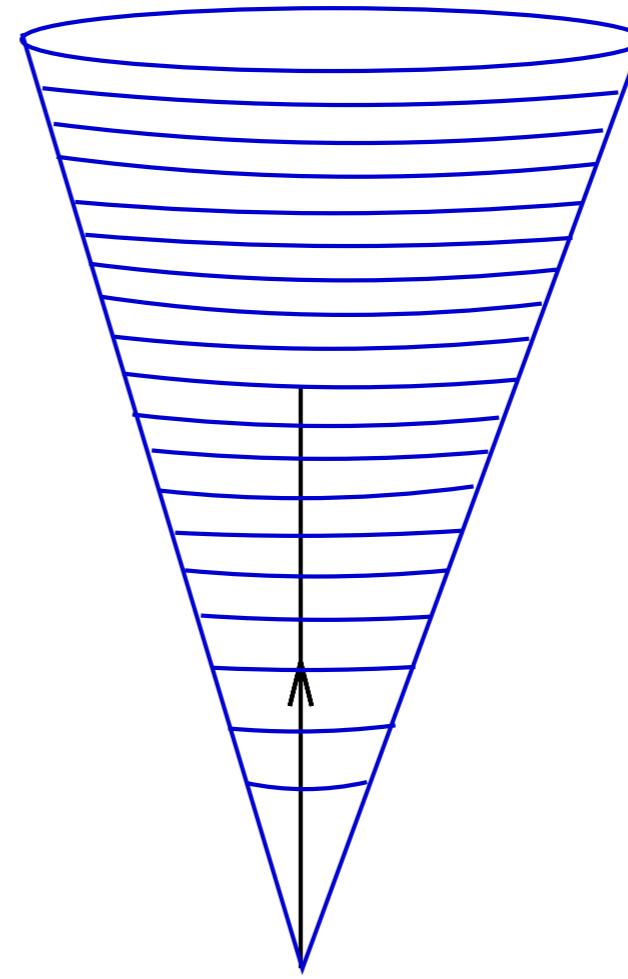
// constituents of hardest jet
vector<PseudoJet> constituents = jets[0].constituents();
```

More this afternoon in the tutorial

Small jet radius

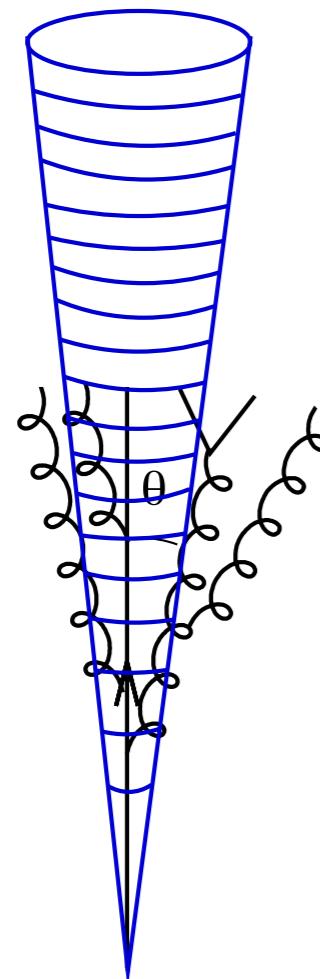


Large jet radius

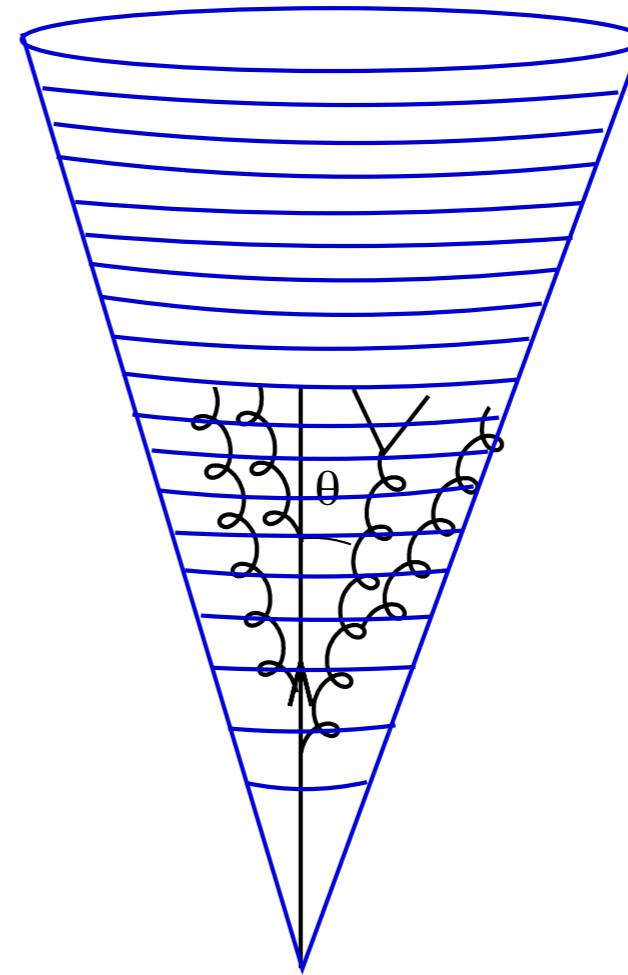


single parton @ LO: **jet radius irrelevant**

Small jet radius

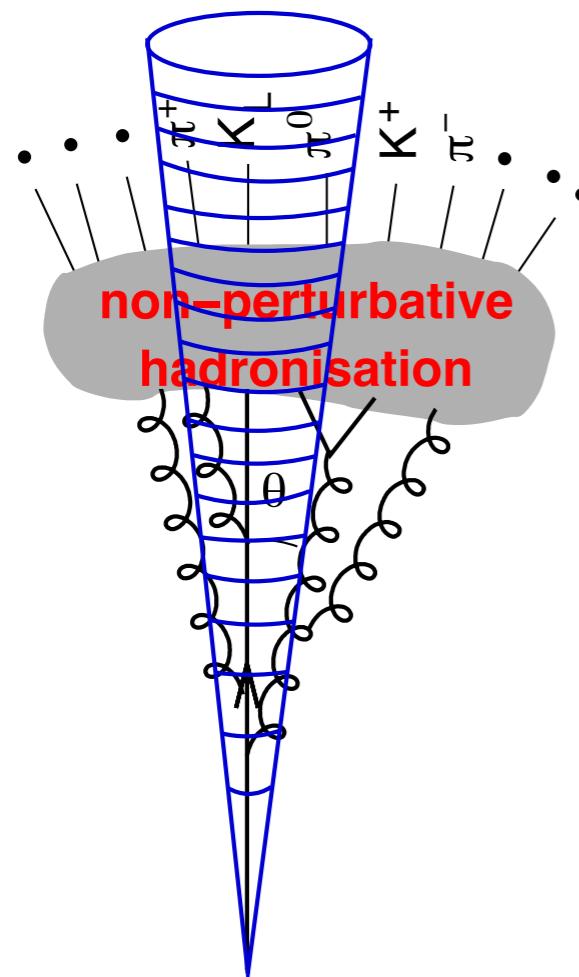


Large jet radius

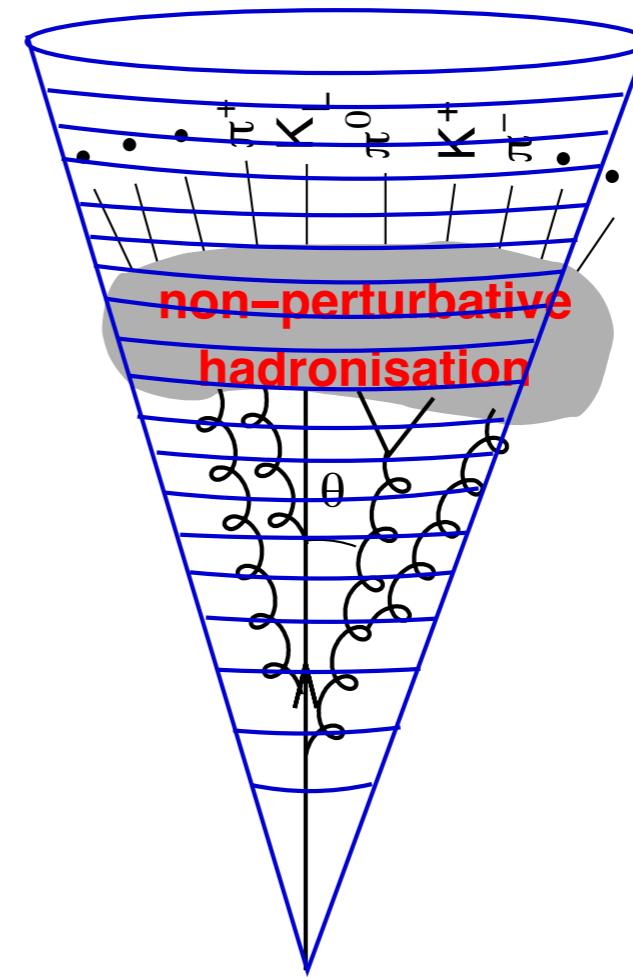


perturbative fragmentation: **large jet radius better**  
(it captures more)

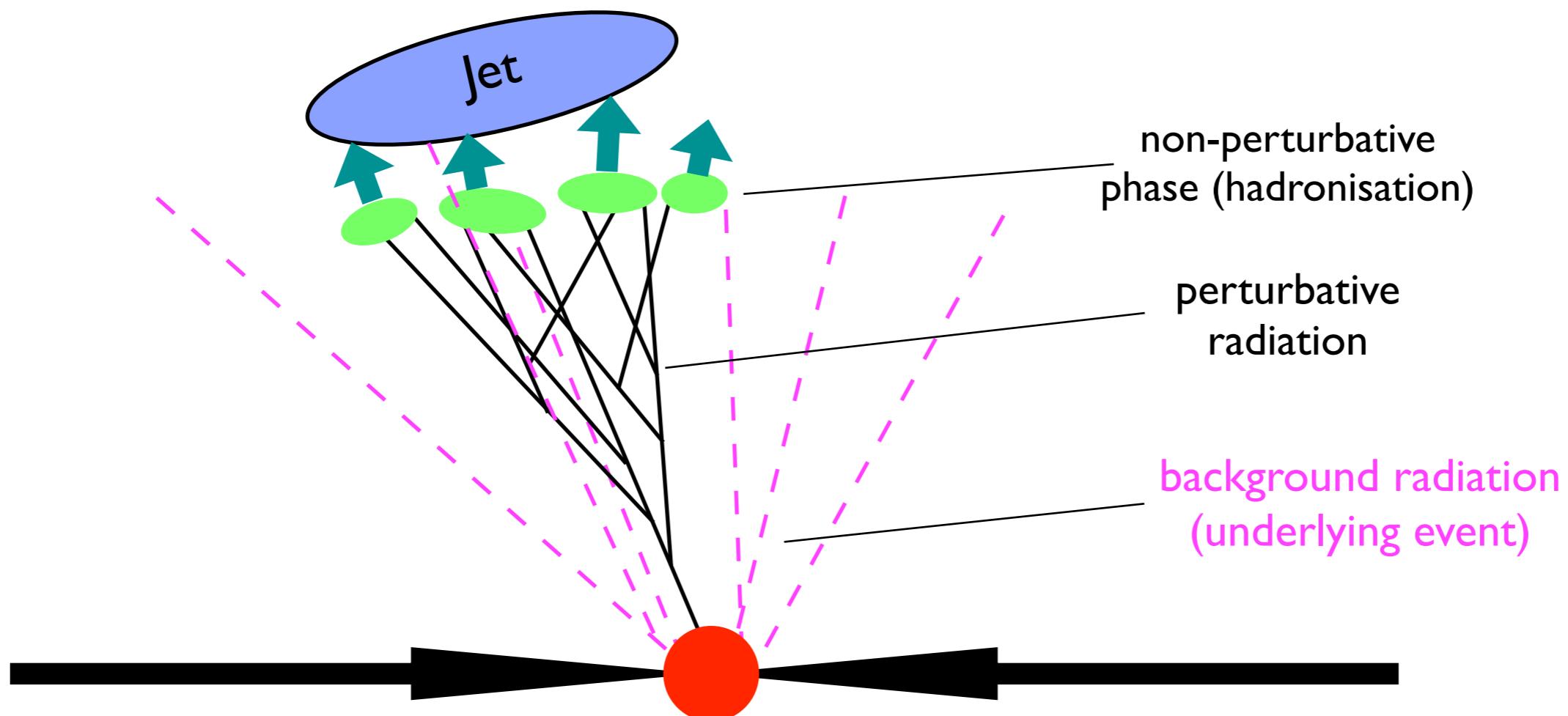
## Small jet radius

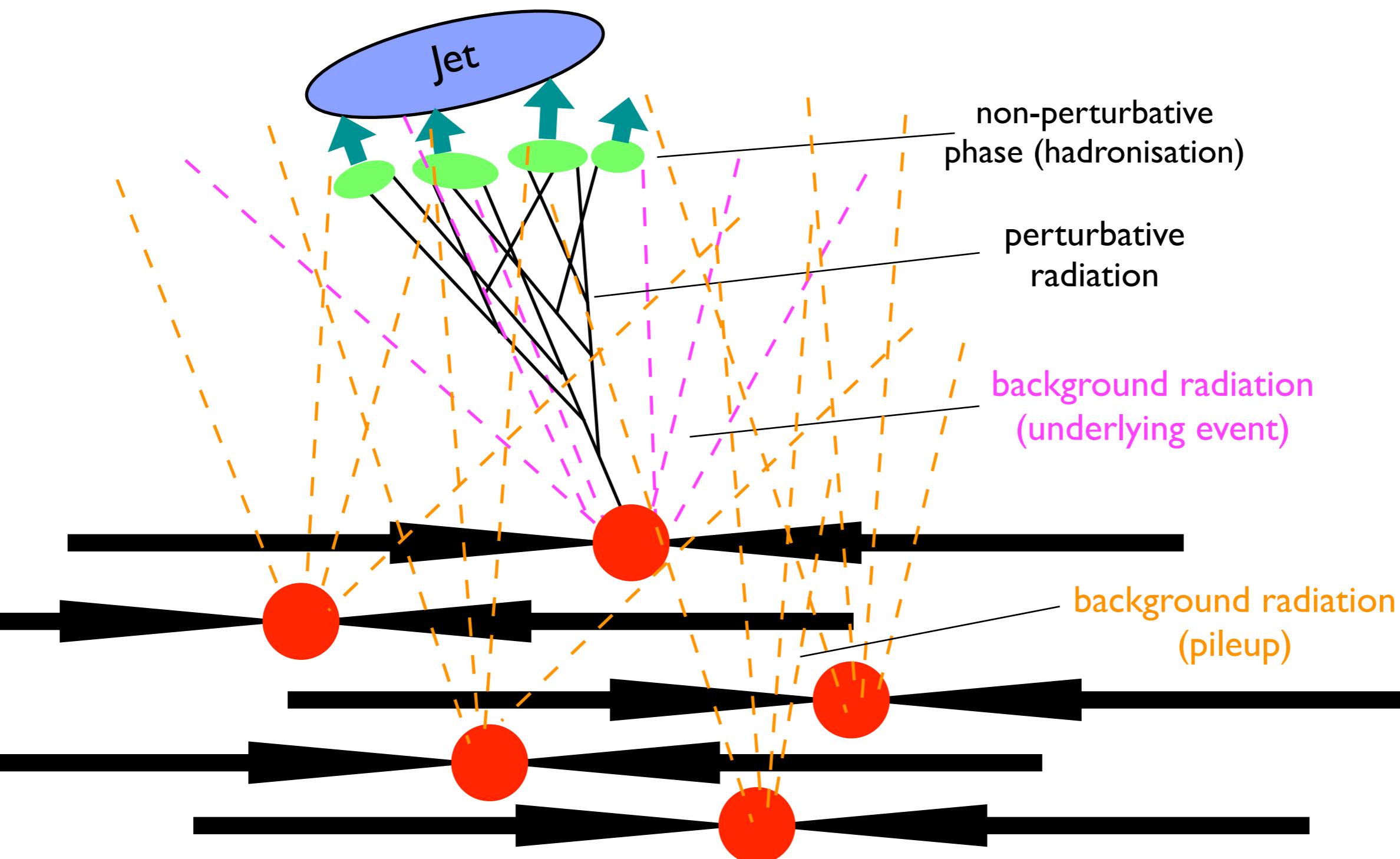


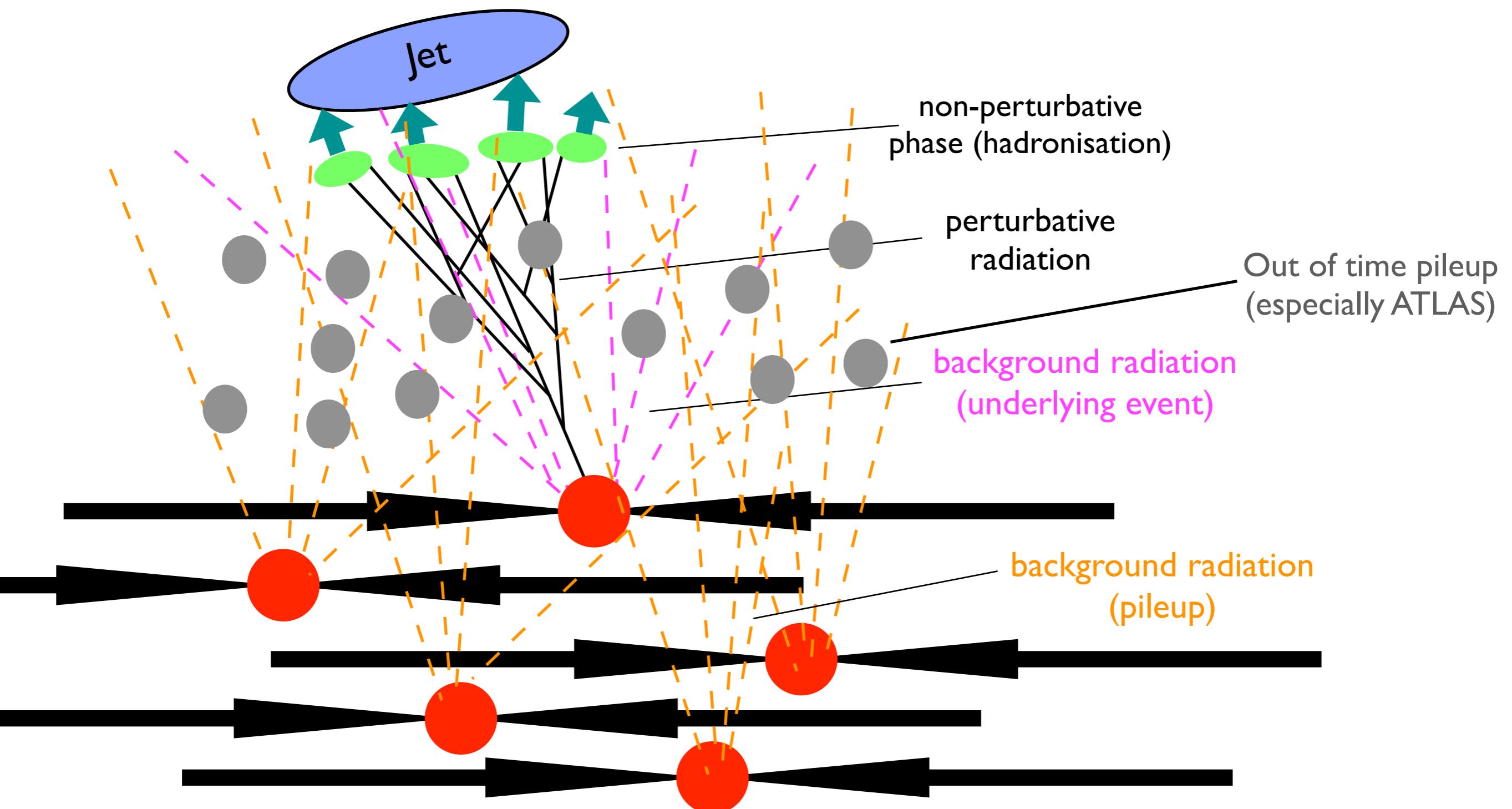
## Large jet radius



non-perturbative fragmentation: **large jet radius better**  
(it captures more)



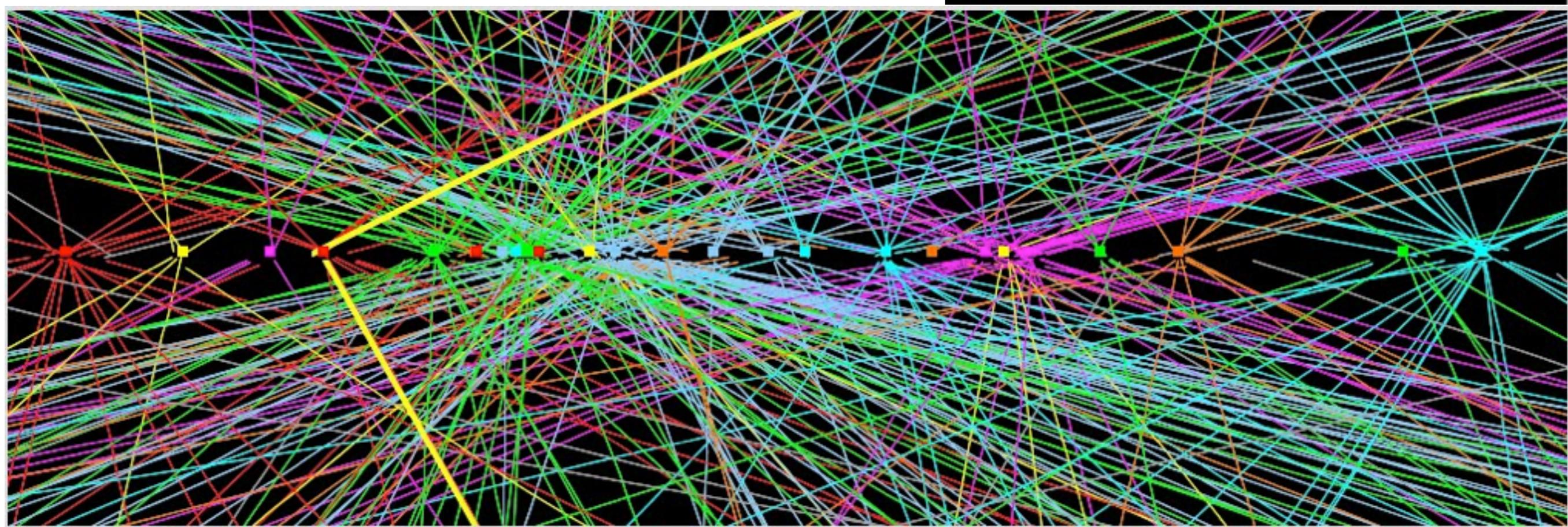
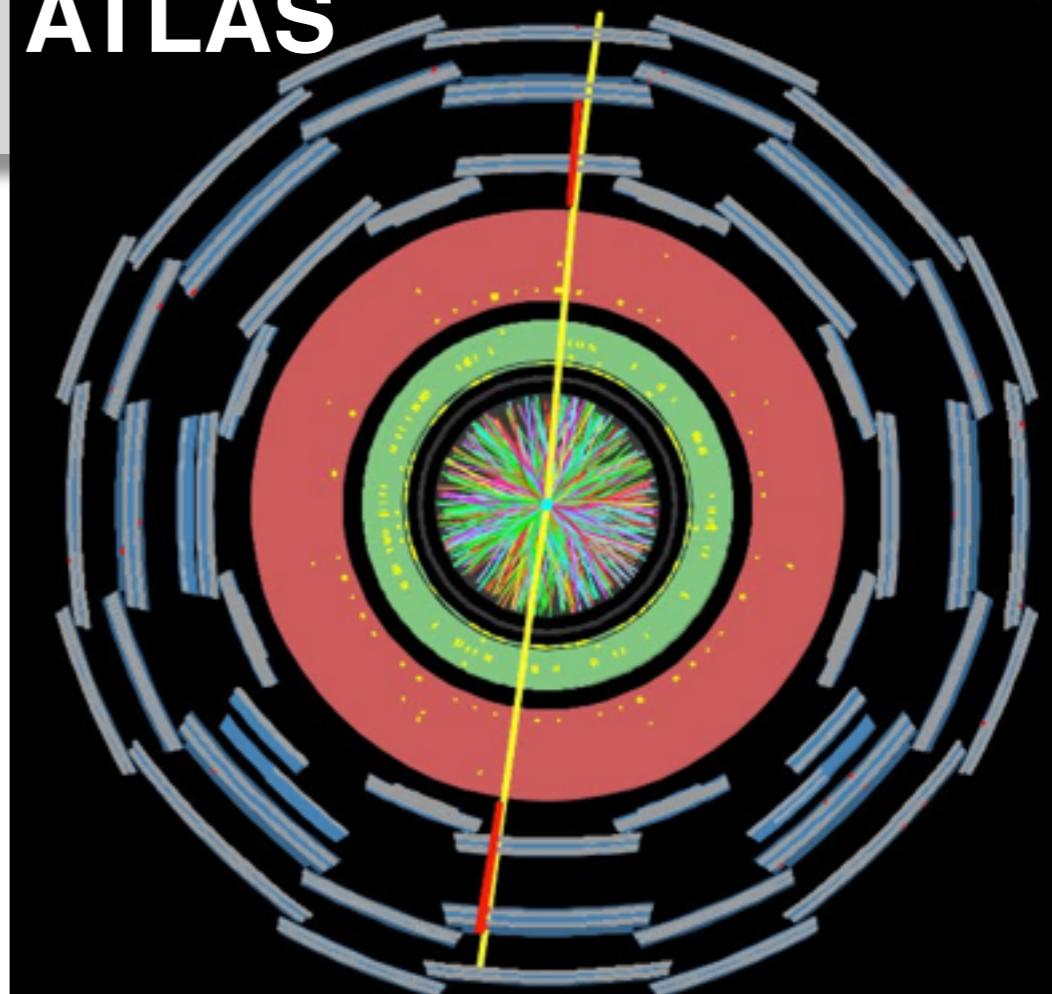




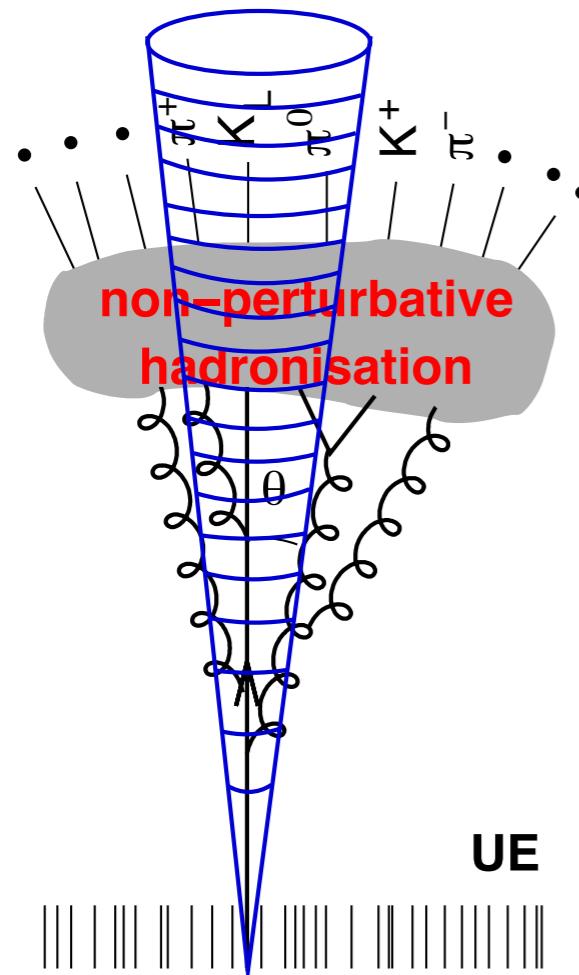
# Pileup for real

a few cm

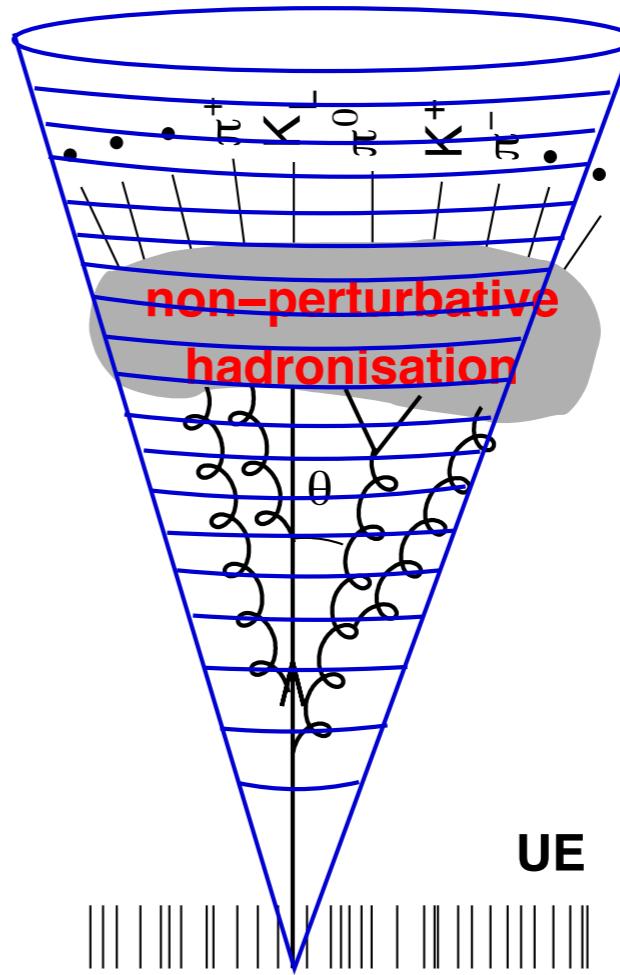
$\sim 20$  m



## Small jet radius

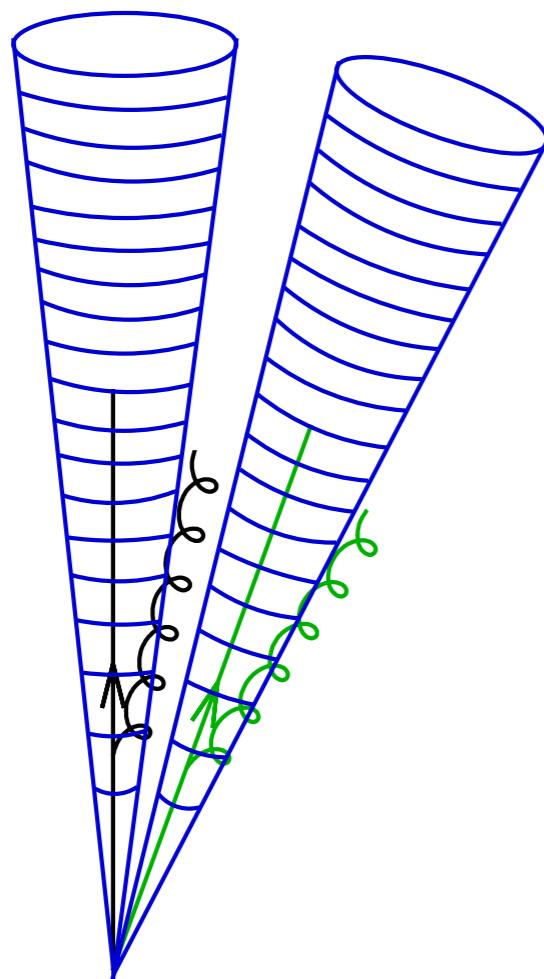


## Large jet radius

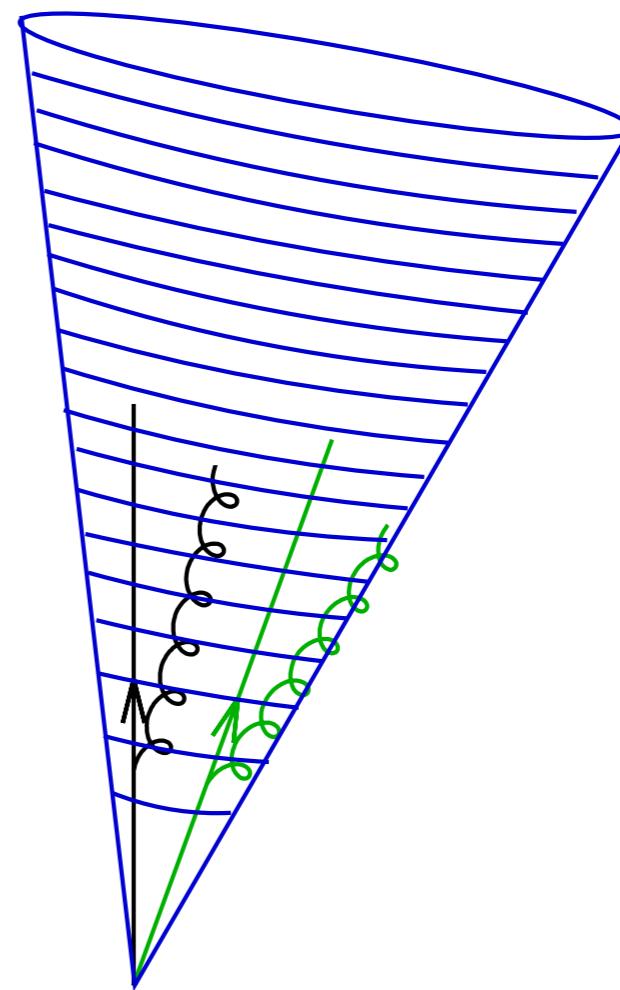


underlying ev. & pileup “noise”: **small jet radius better**  
 (it captures less)

## Small jet radius



## Large jet radius

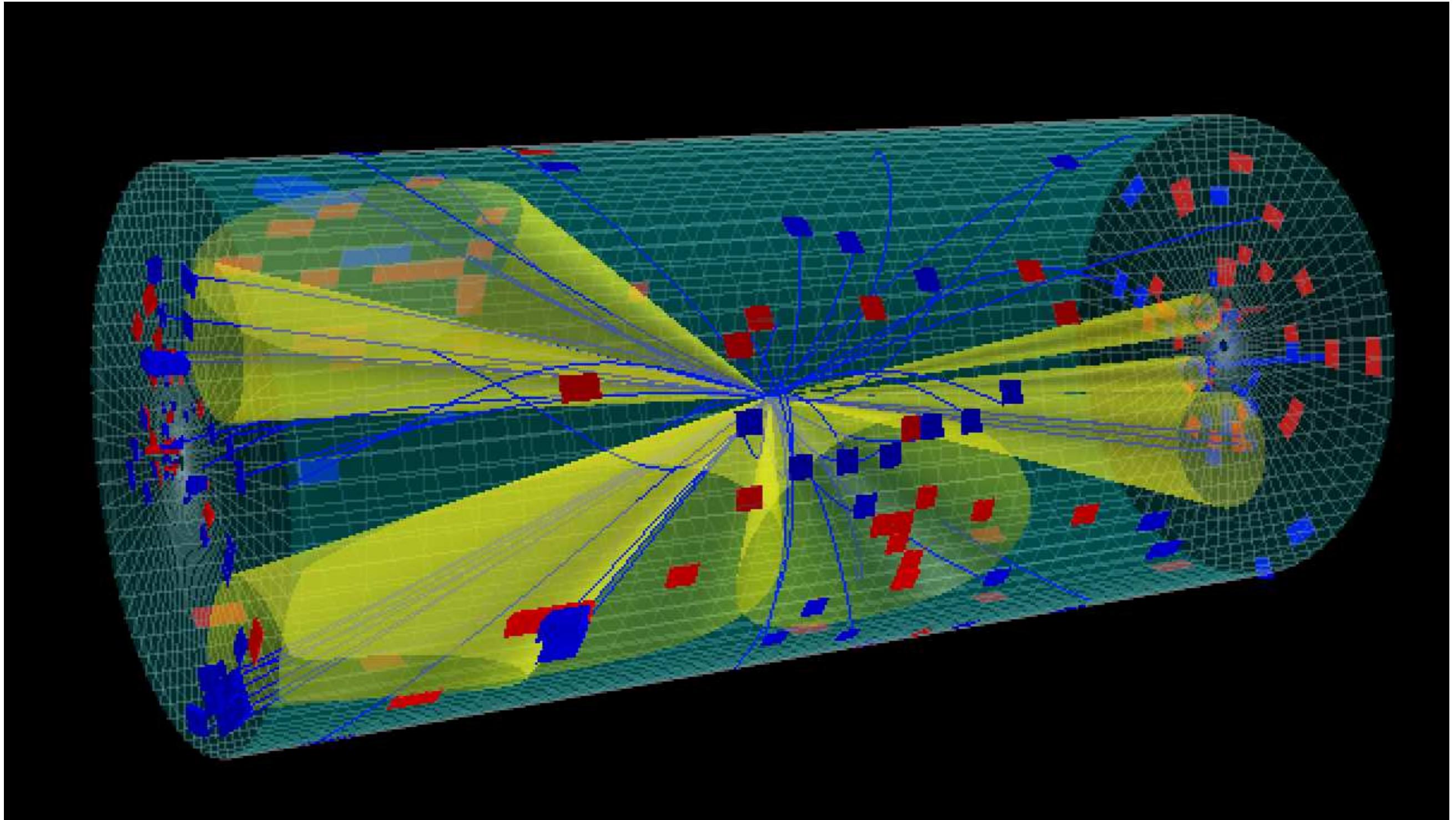


multi-hard-parton events: **small jet radius better**  
(it resolves partons more effectively)

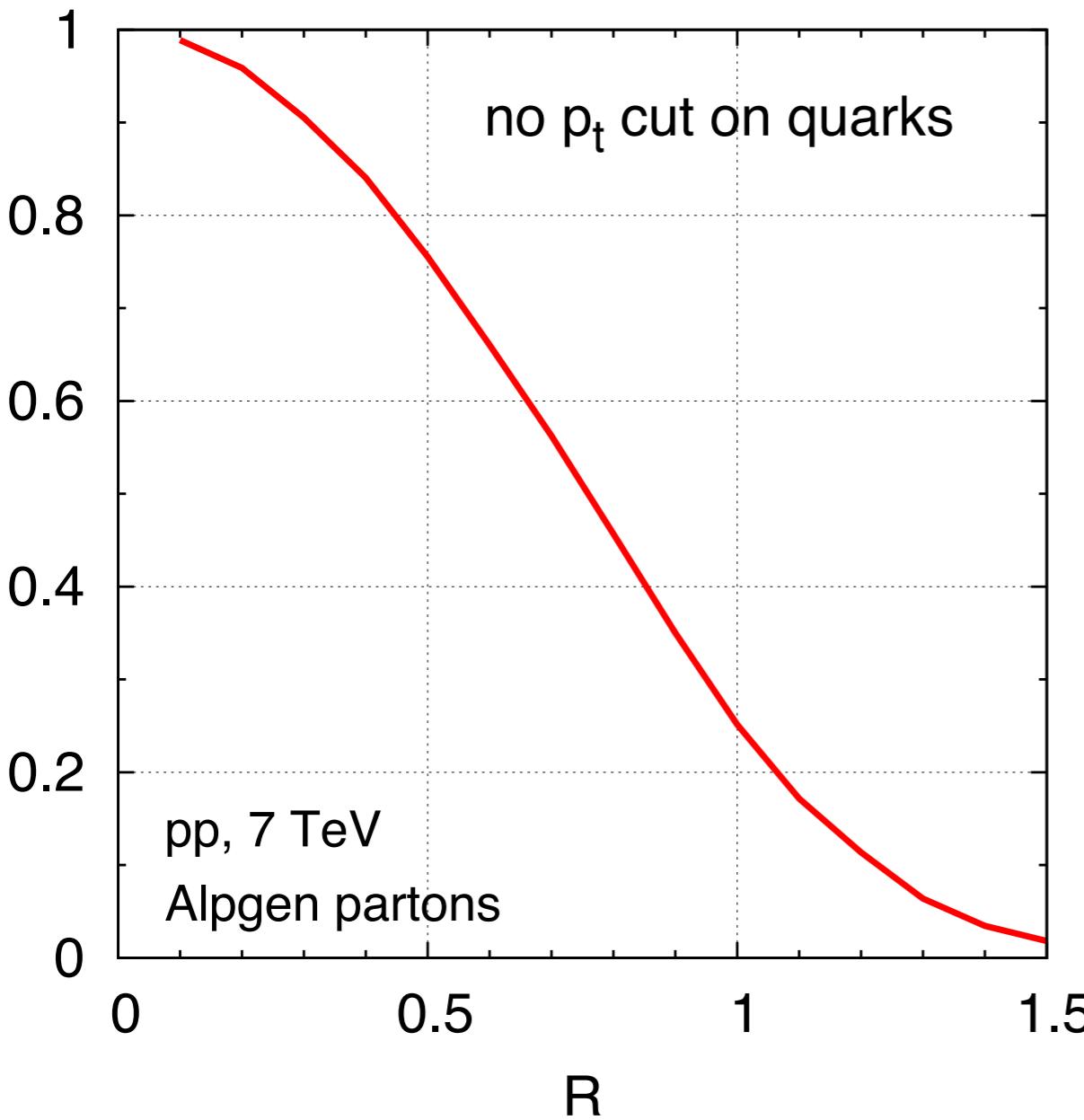
Can we capture all quarks and gluons?

Should we capture all quarks and gluons?

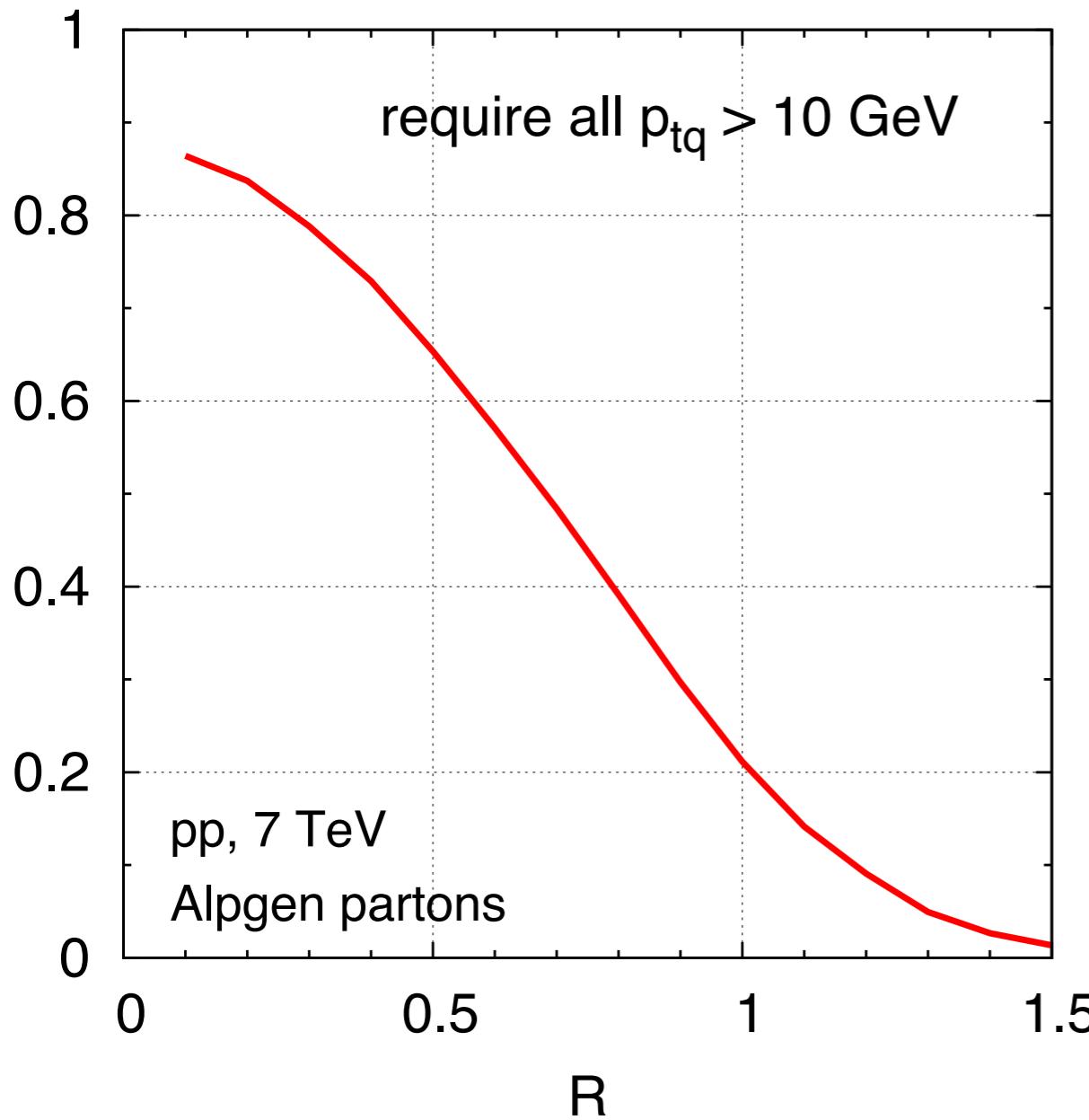
$pp \rightarrow t\bar{t}$   
simulated with Pythia, displayed with Delphes



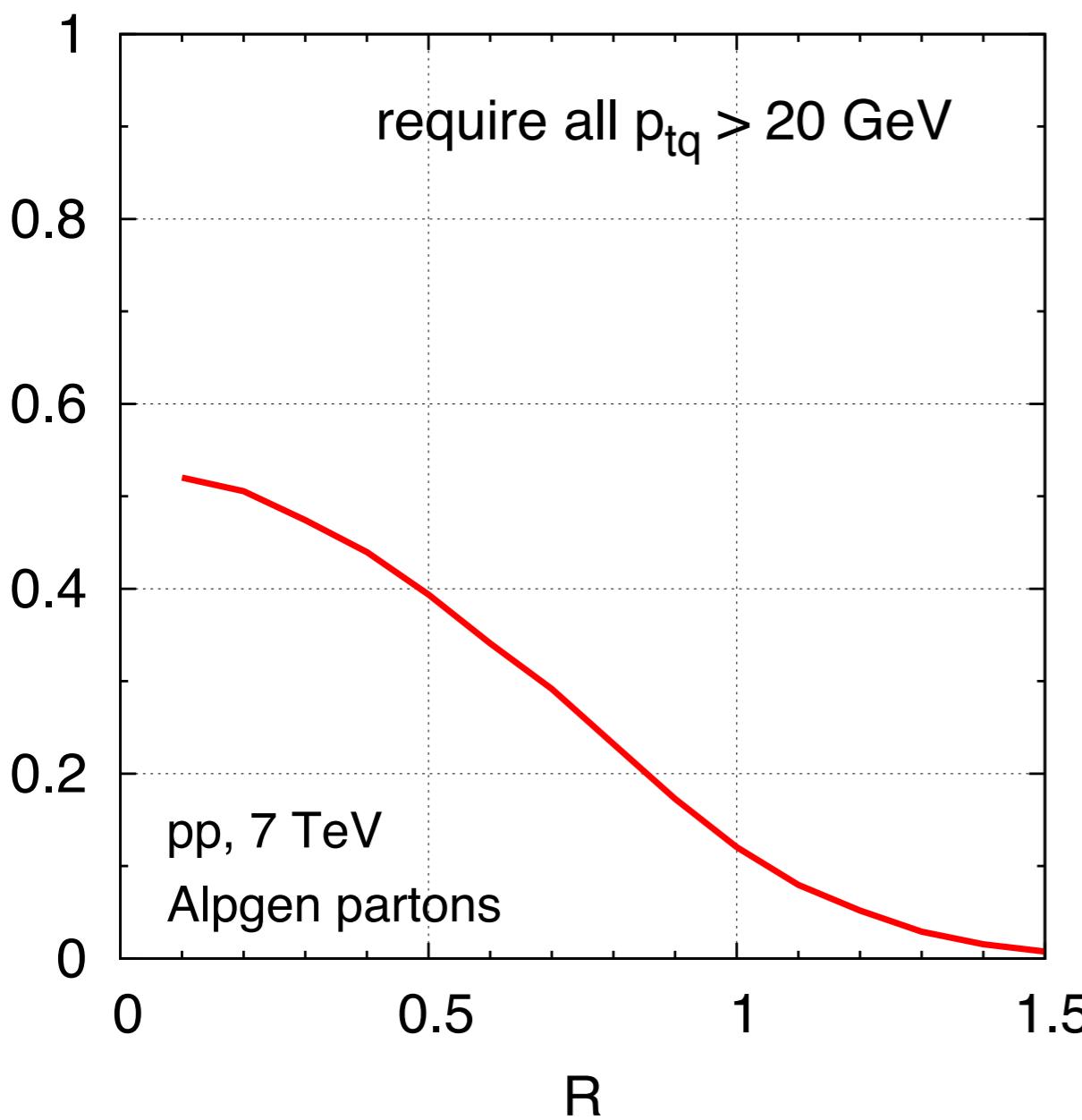
**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$**   
fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$



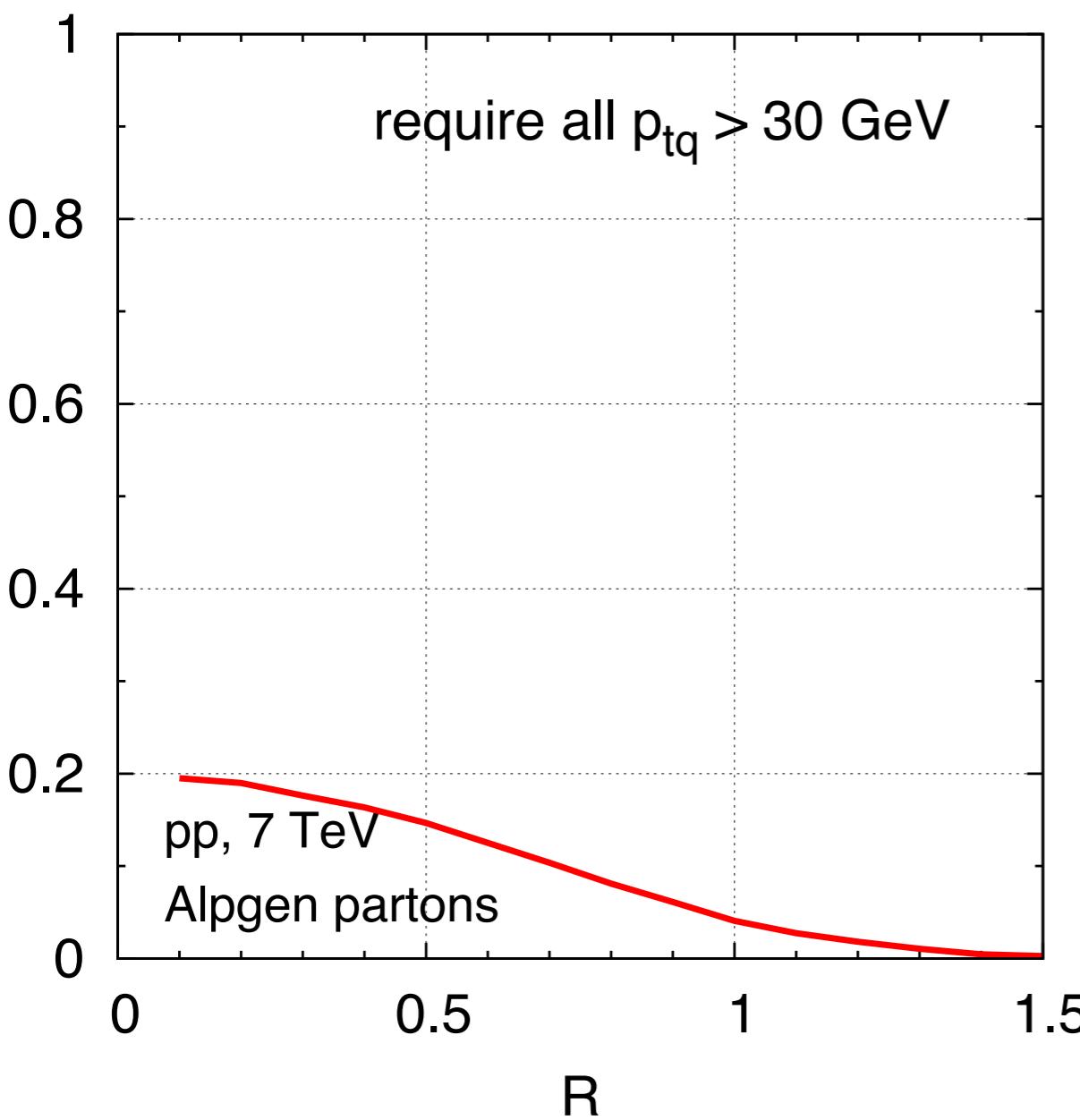
**Alpgen  $pp \rightarrow t\bar{t} \rightarrow 6q$**   
fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$

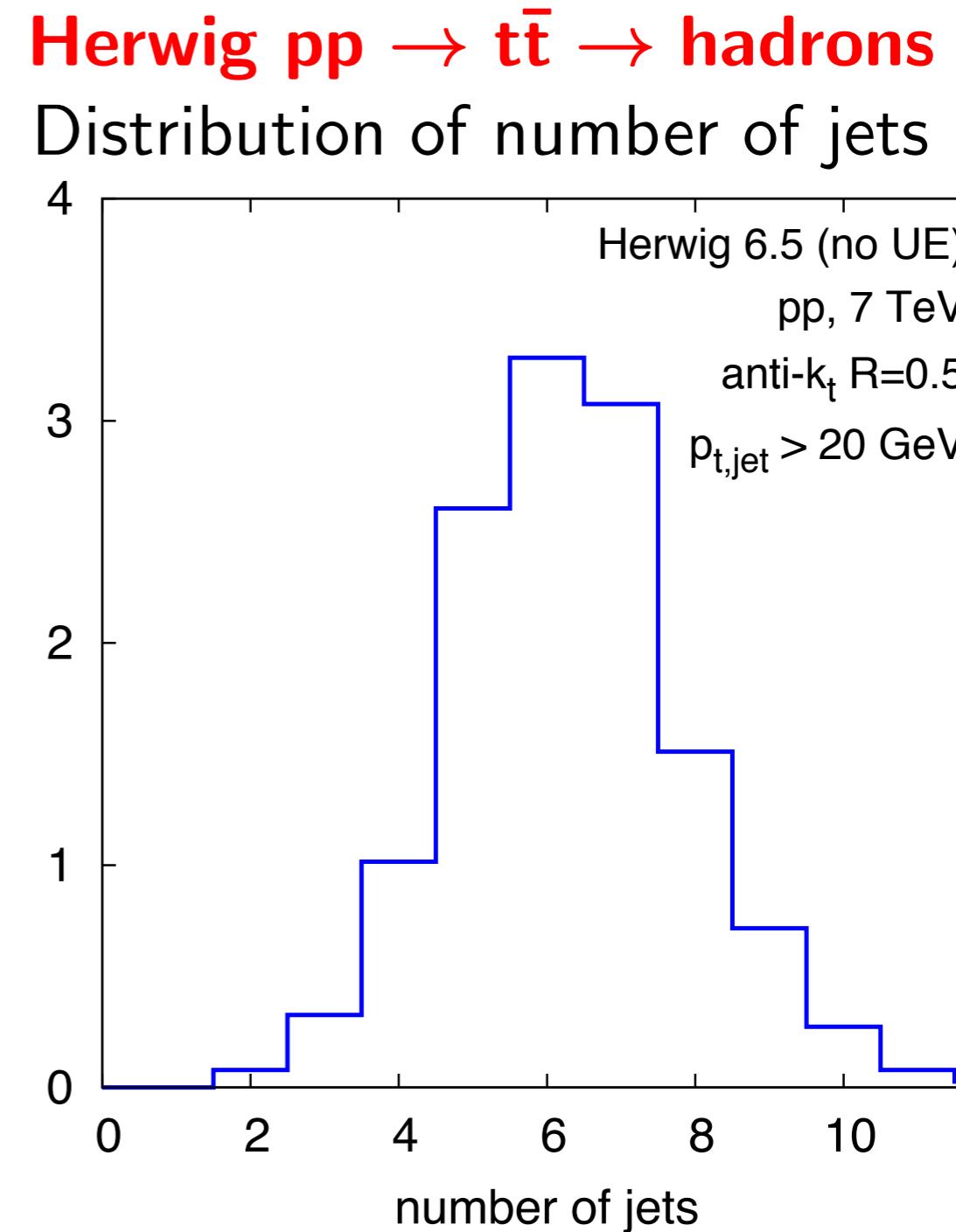
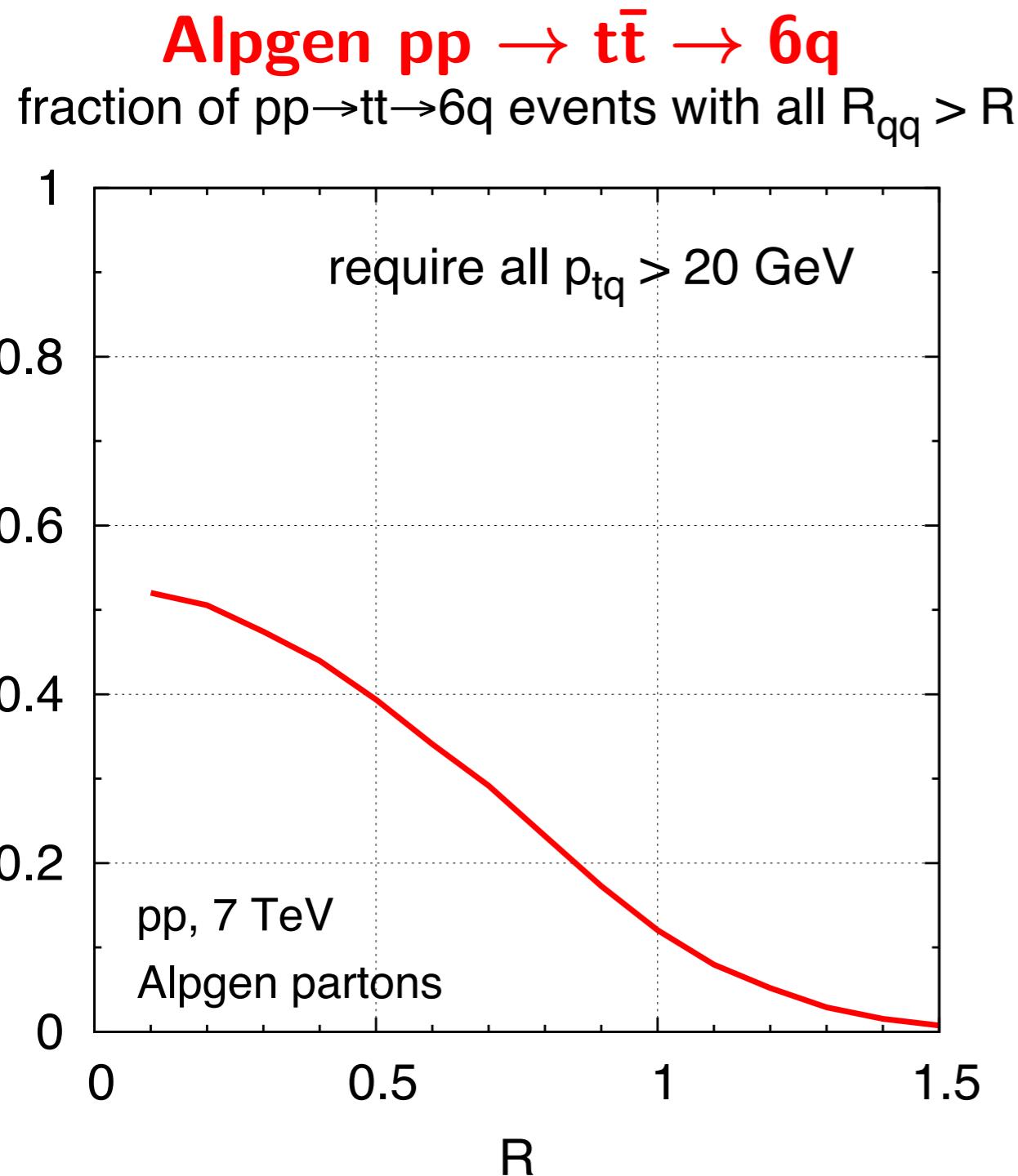


**Alpgen**  $pp \rightarrow t\bar{t} \rightarrow 6q$   
fraction of  $pp \rightarrow t\bar{t} \rightarrow 6q$  events with all  $R_{qq} > R$



**Alpgen**  $pp \rightarrow t\bar{t} \rightarrow 6q$   
fraction of  $pp \rightarrow tt \rightarrow 6q$  events with all  $R_{qq} > R$





# Two things that make jets@LHC special

The large hierarchy of scales

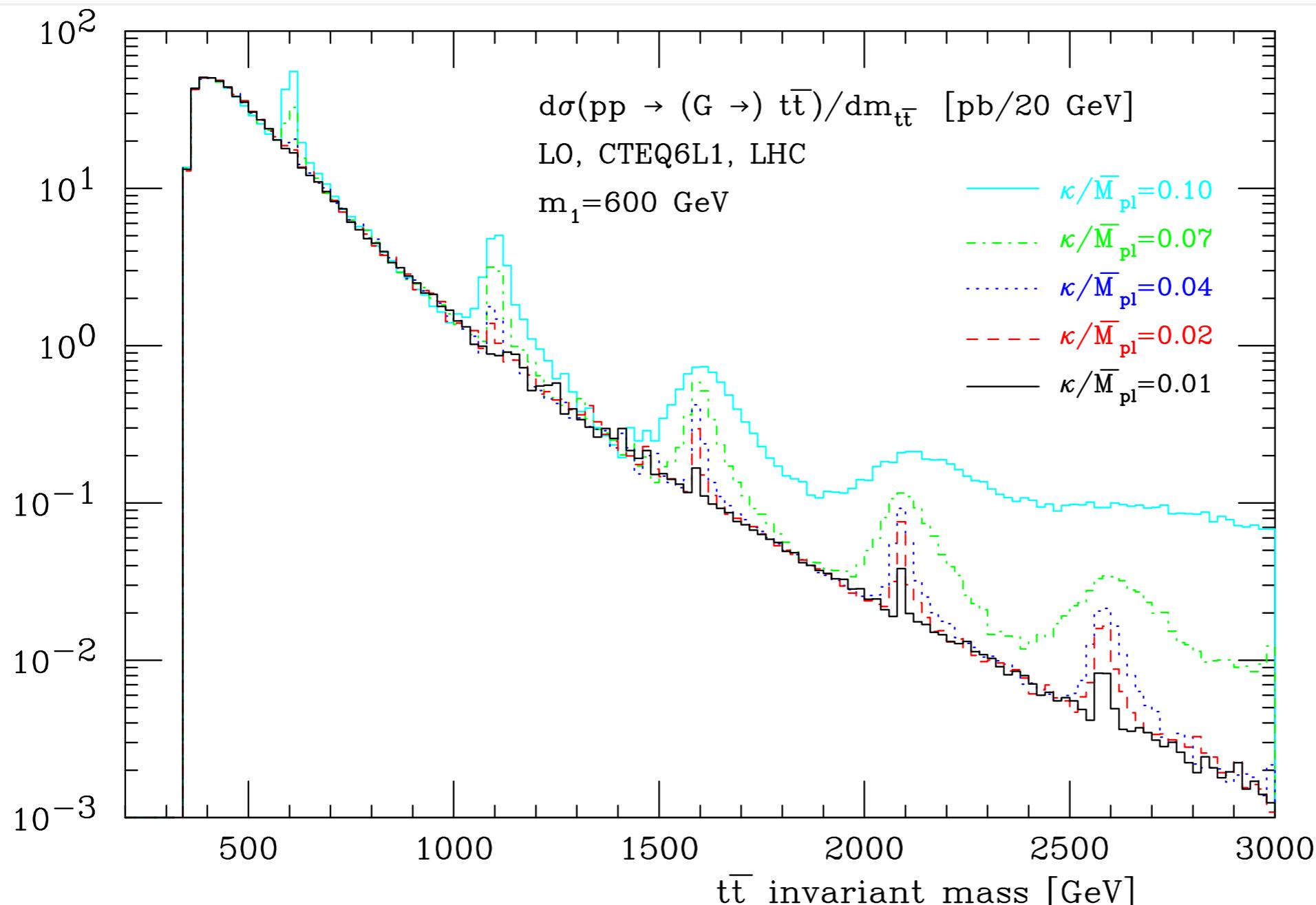
$$\sqrt{s} \gg M_{EW}$$

The huge pileup

$$n_{\text{pileup}} \sim 20 - 40$$

*[These involve two opposite extremes: low  $p_t$  and high  $p_t$ , which nevertheless talk to each other]*

# e.g. ttbar resonances

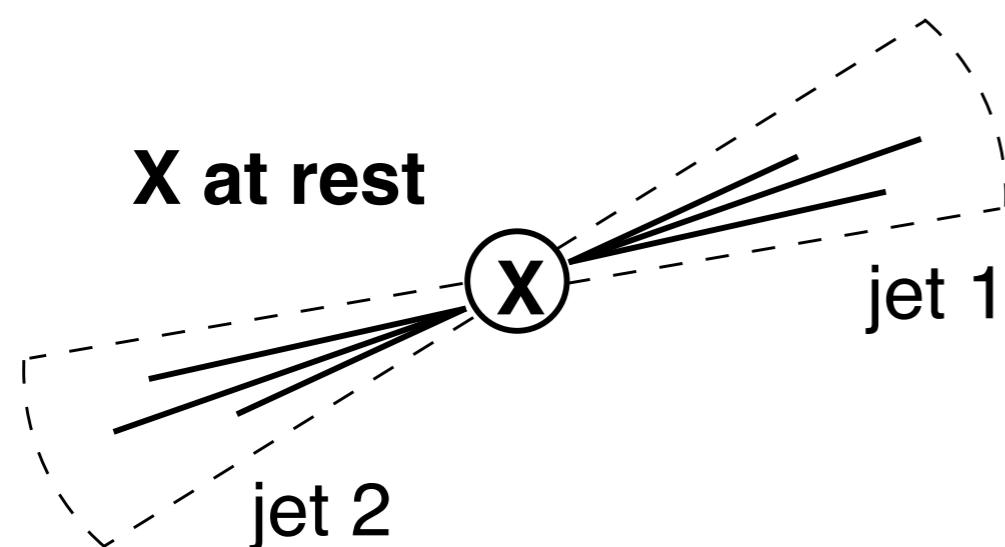


RS KK resonances  $\rightarrow t\bar{t}$ , from Frederix & Maltoni, 0712.2355

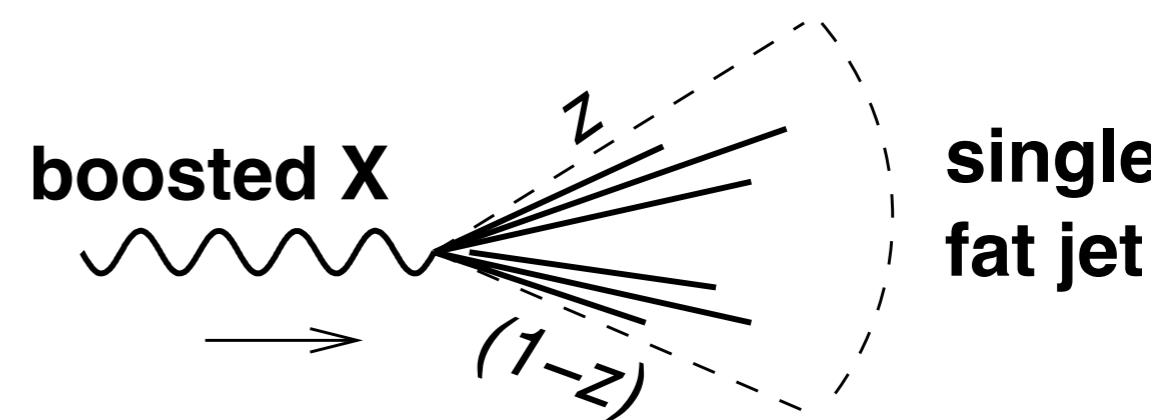
NB: QCD dijet spectrum is  $\sim 10^3$  times  $t\bar{t}$

# Boosted EW scale objects

Normal analyses: two quarks from  $X \rightarrow q\bar{q}$  reconstructed as two jets



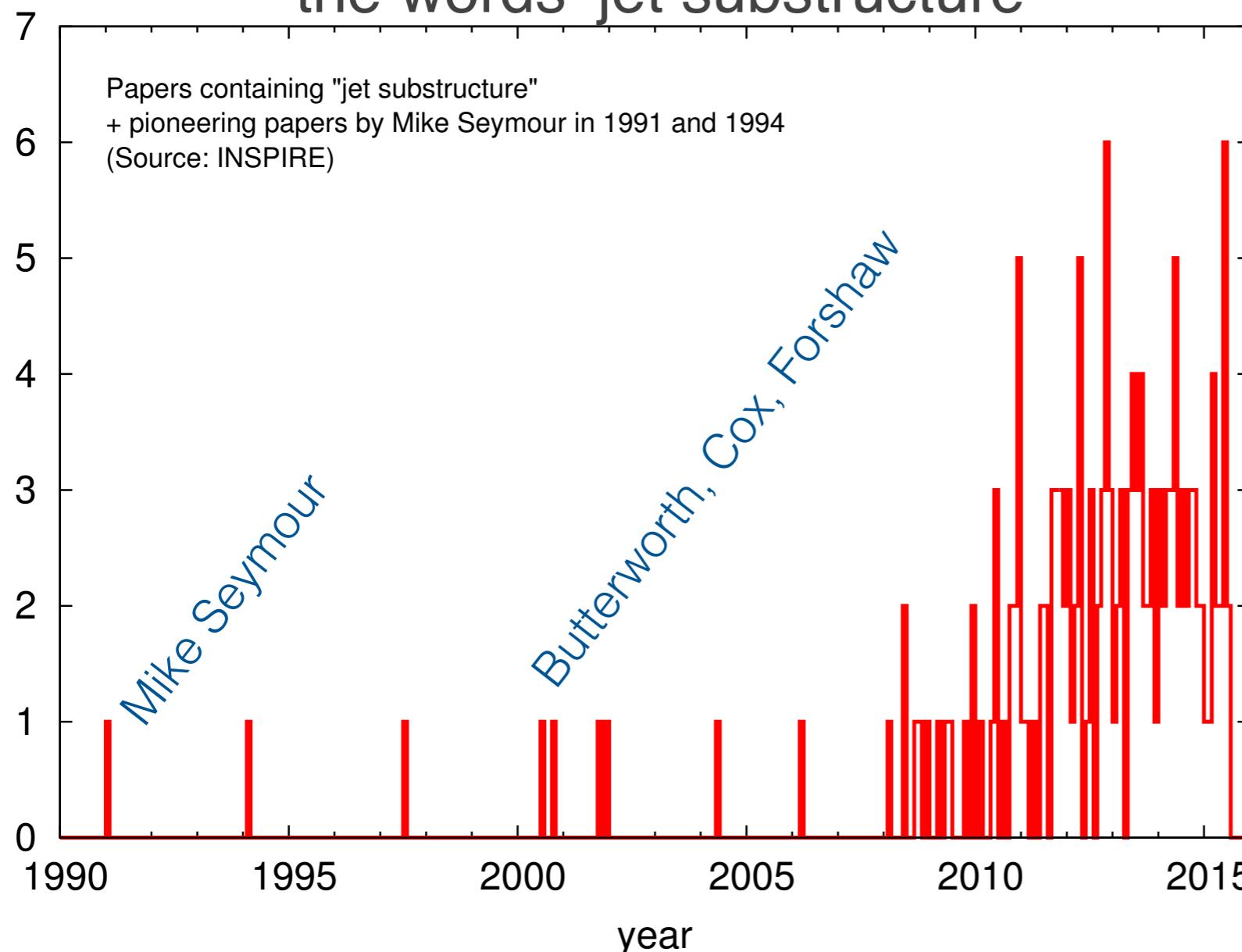
**High- $p_t$  regime: EW object X is boosted, decay is collimated,  $q\bar{q}$  both in same jet**



Happens for  $p_t \gtrsim 2m/R$   
 $p_t \gtrsim 320 \text{ GeV}$  for  $m = m_W$ ,  $R = 0.5$

# Papers on jet substructure

Number of papers containing  
the words 'jet substructure'



More than 150 papers  
since 2008

(+ some background noise)

Pioneered by M. Seymour  
in the early '90s

Exploded around 2008

# Tagging & Grooming

Two widely used terms  
though there's not a  
consensus about  
what they mean

## Tagging

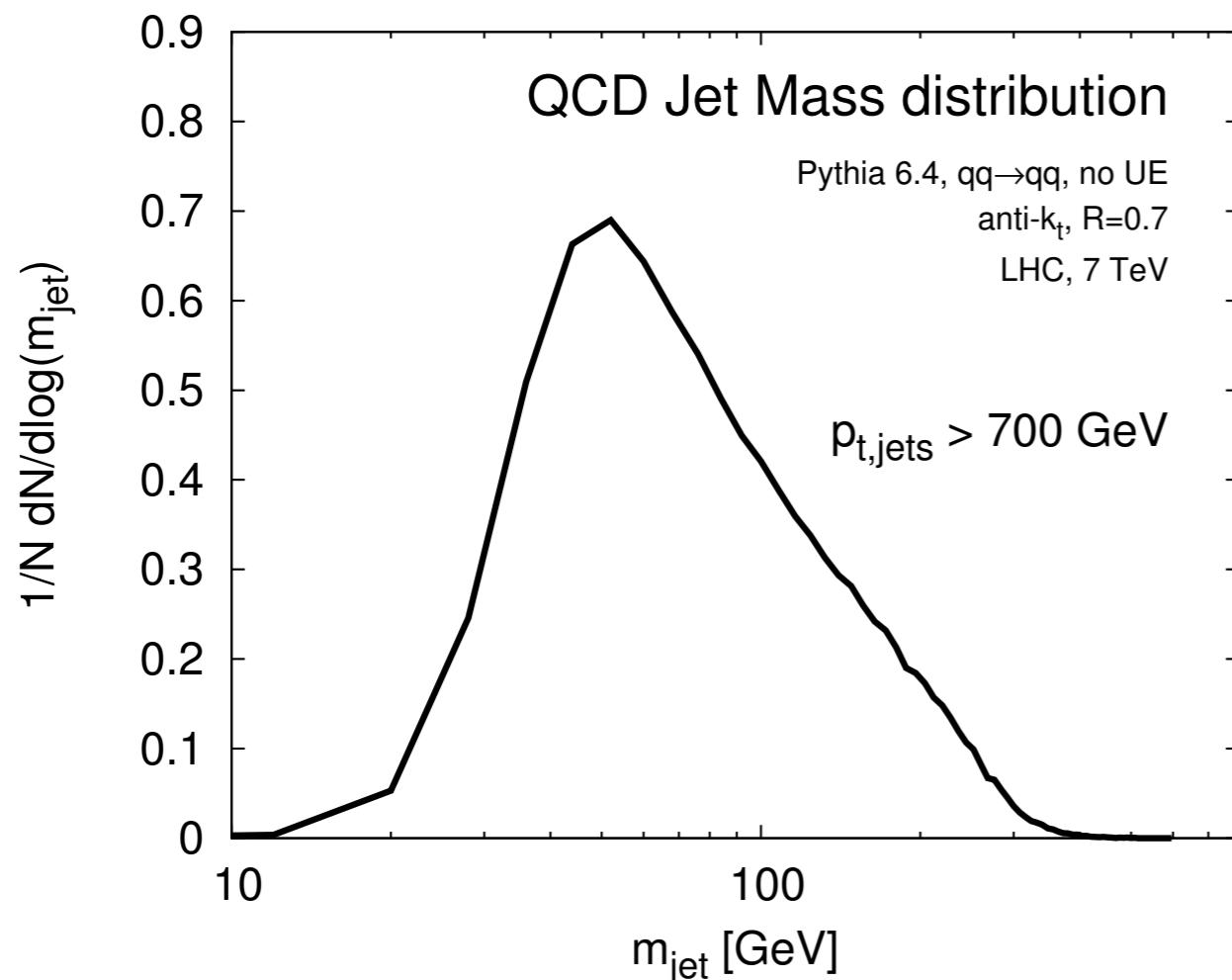
- reduces the background, leaves much of signal

## Grooming

- improves signal mass resolution (removing pileup, etc.), without significantly changing background & signal event numbers

# One core idea for tagging

# Inside the jet mass

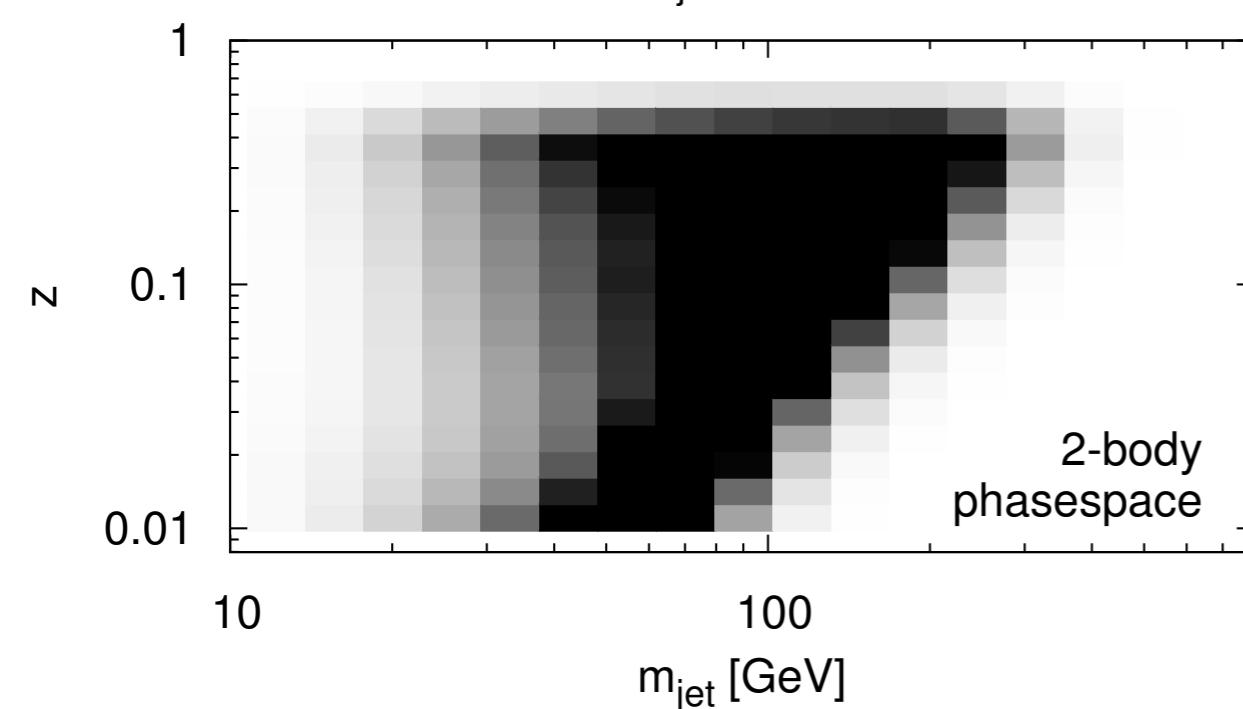
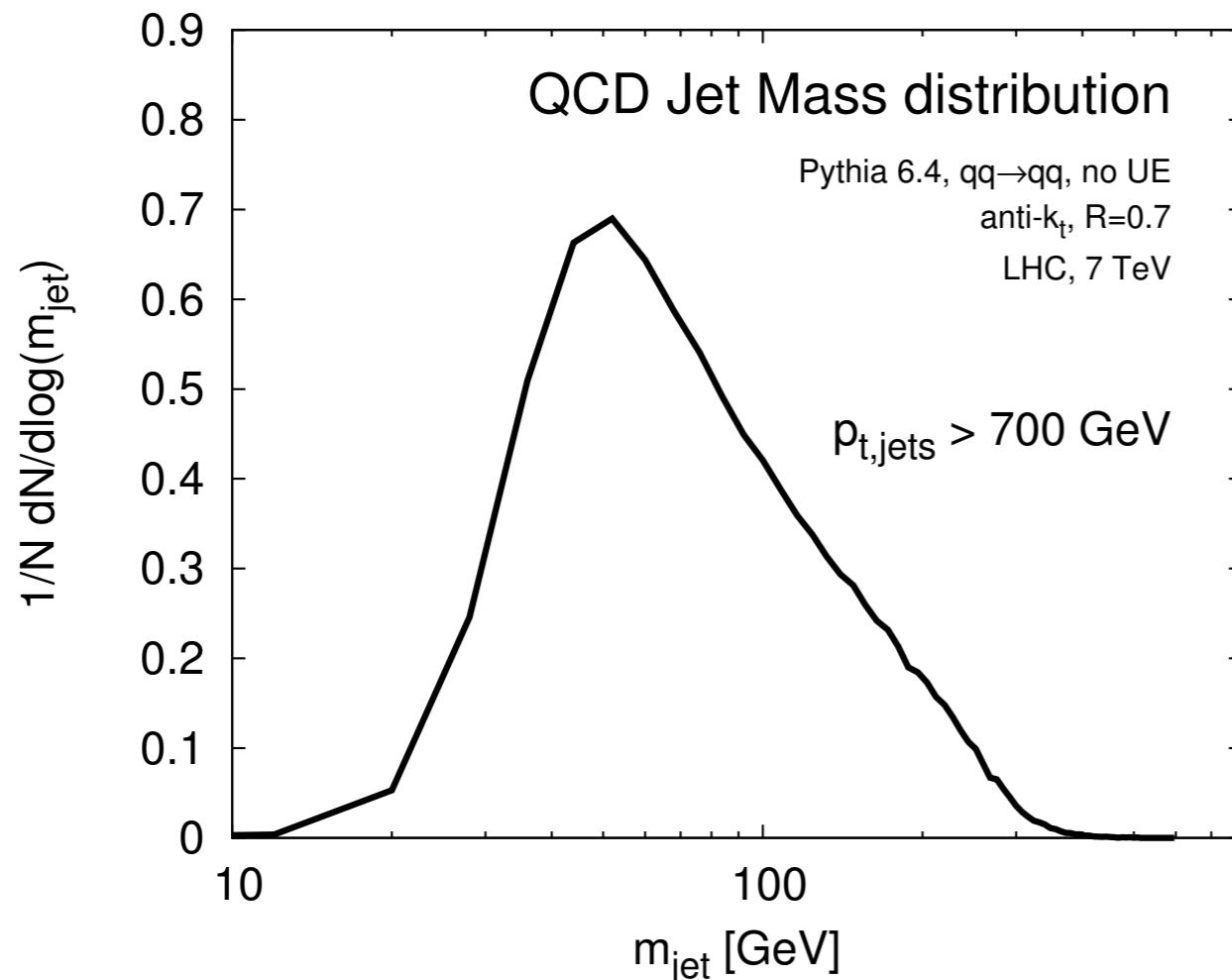


QCD jet mass distribution has the approximate

$$\frac{dN}{d \ln m} \sim \alpha_s \ln \frac{p_t R}{m} \times \text{Sudakov}$$

Work from '80s and '90s  
+ Almeida et al '08

# Inside the jet mass



QCD jet mass distribution has the approximate

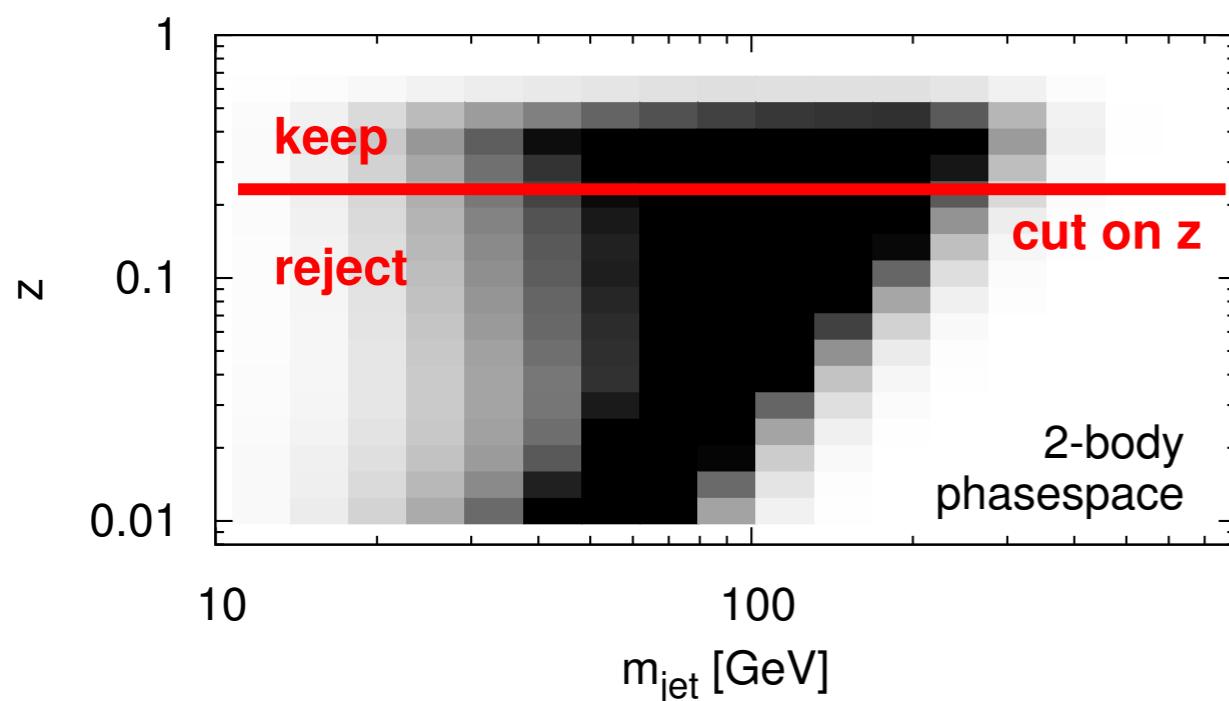
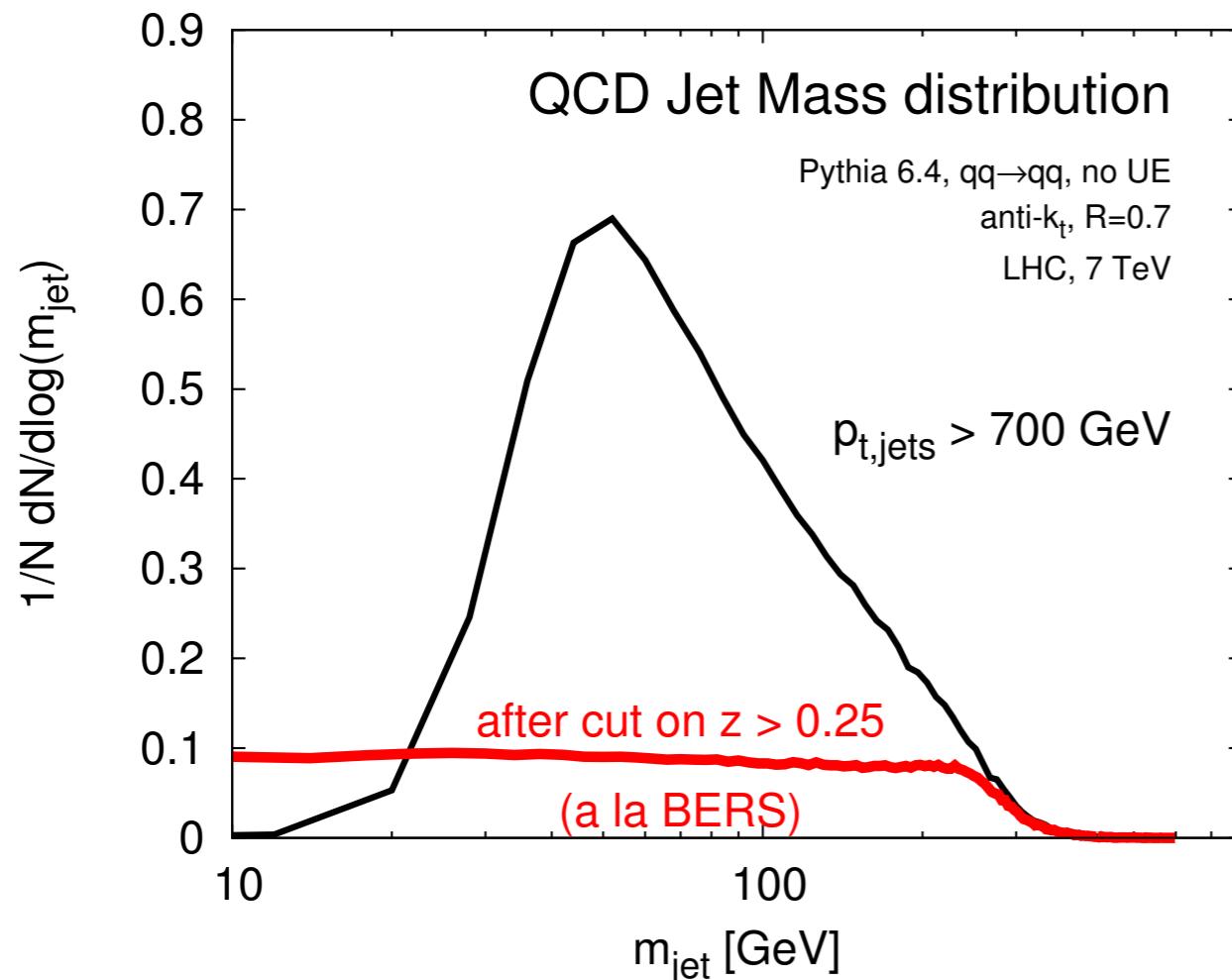
$$\frac{dN}{d \ln m} \sim \alpha_s \ln \frac{p_t R}{m} \times \text{Sudakov}$$

Work from '80s and '90s  
+ Almeida et al '08

The logarithm comes from integral over soft divergence of QCD:

$$\int \frac{1}{\frac{m^2}{p_t^2 R^2}} \frac{dz}{z}$$

# Inside the jet mass



QCD jet mass distribution has the approximate

$$\frac{dN}{d \ln m} \sim \alpha_s \ln \frac{p_t R}{m} \times \text{Sudakov}$$

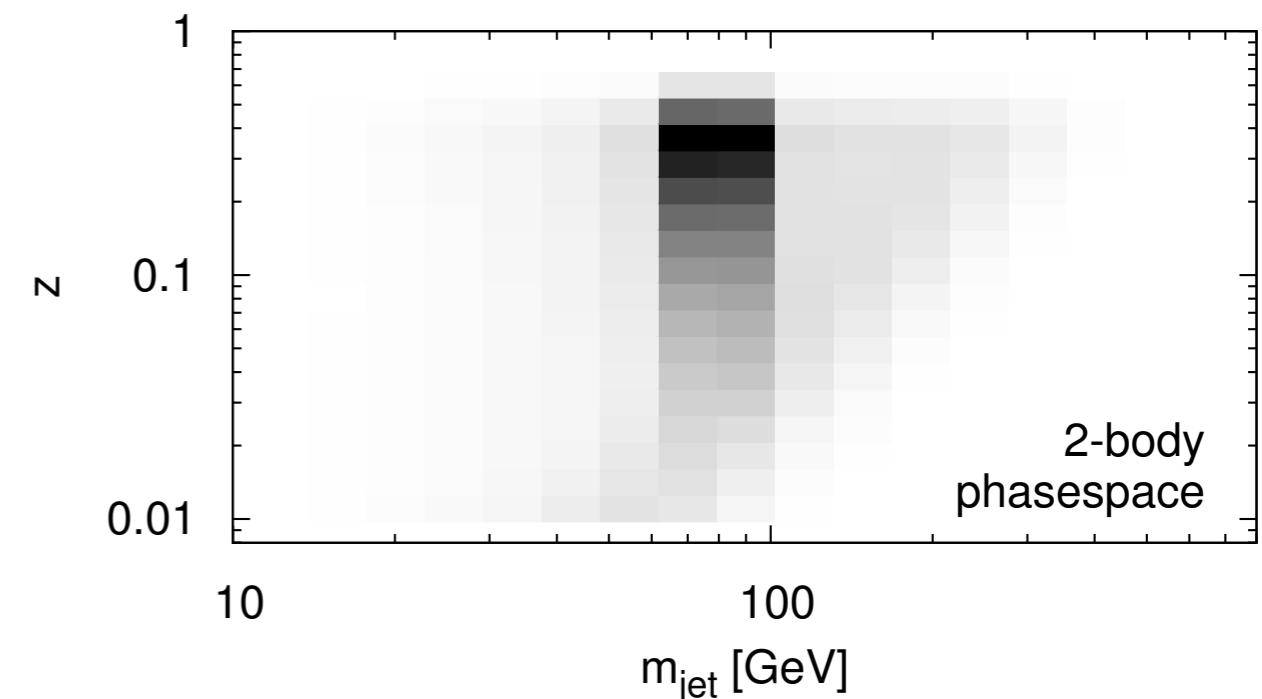
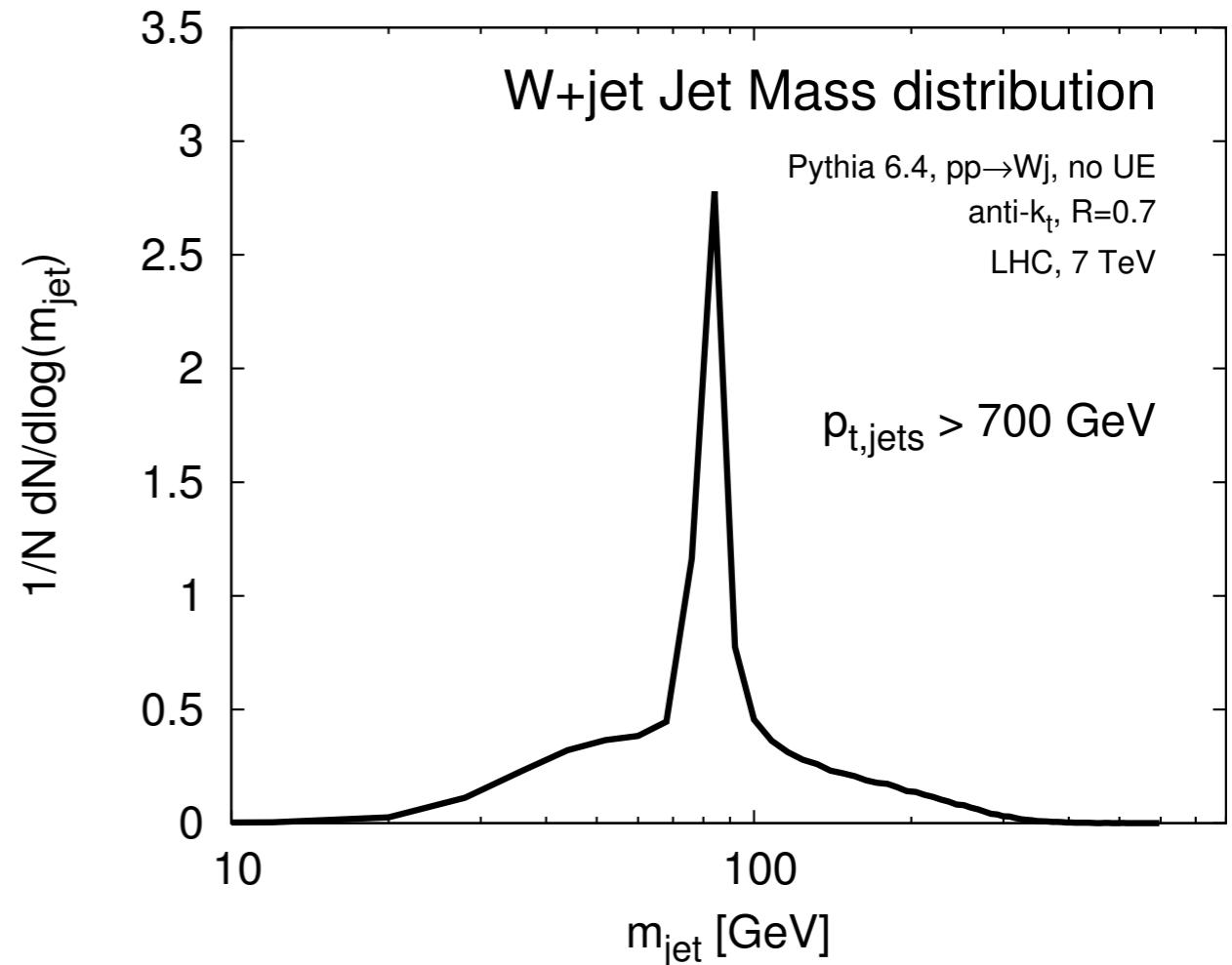
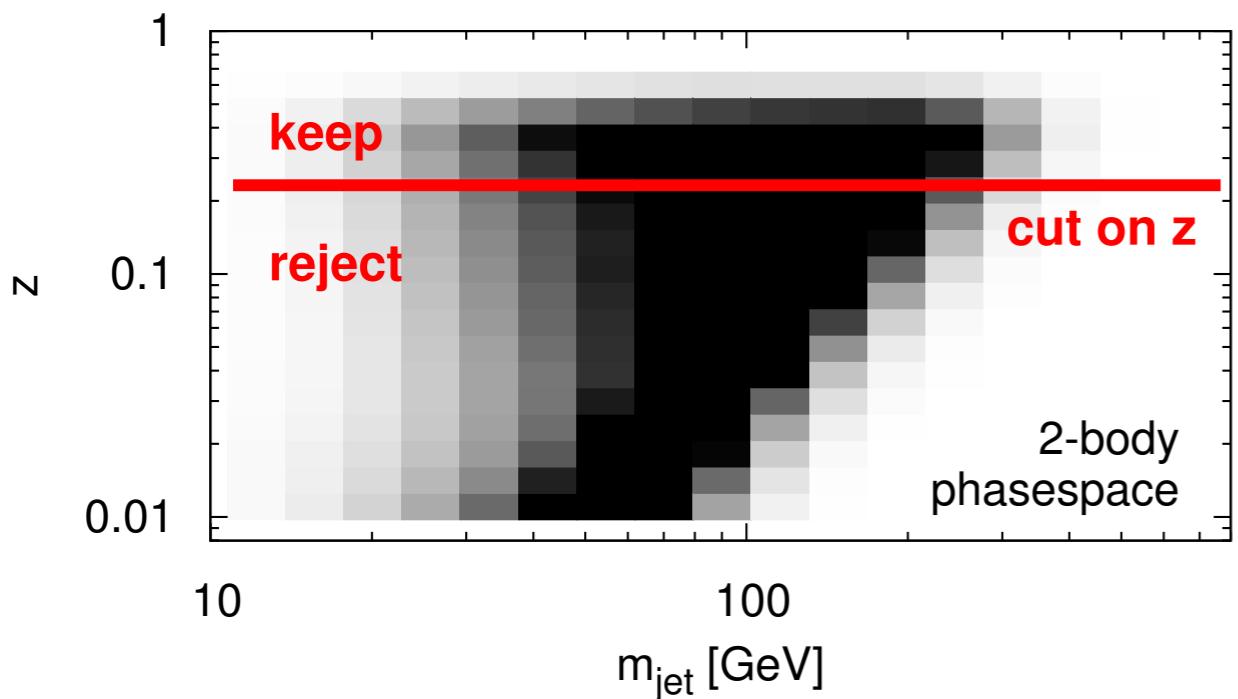
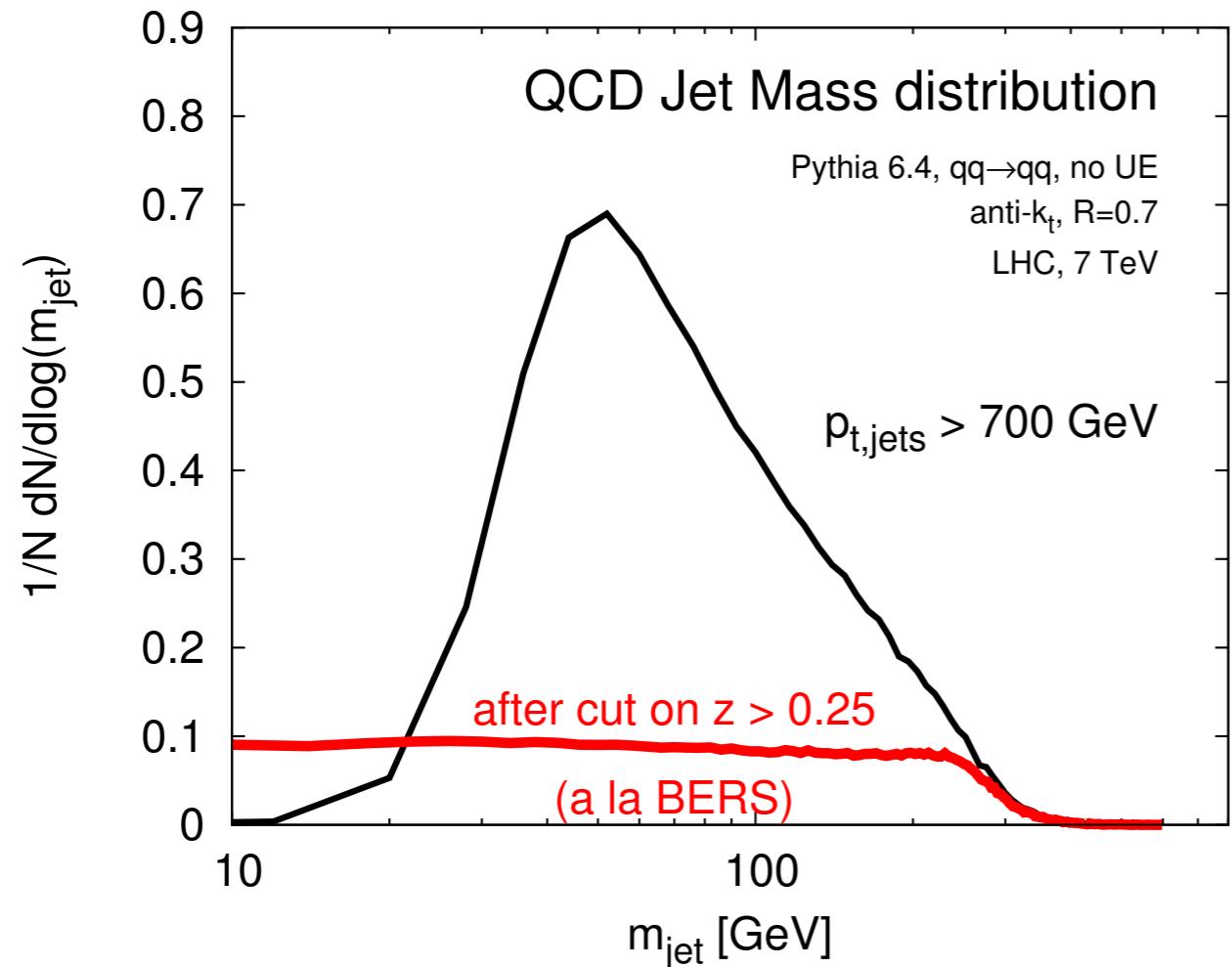
Work from '80s and '90s  
+ Almeida et al '08

The logarithm comes from integral over soft divergence of QCD:

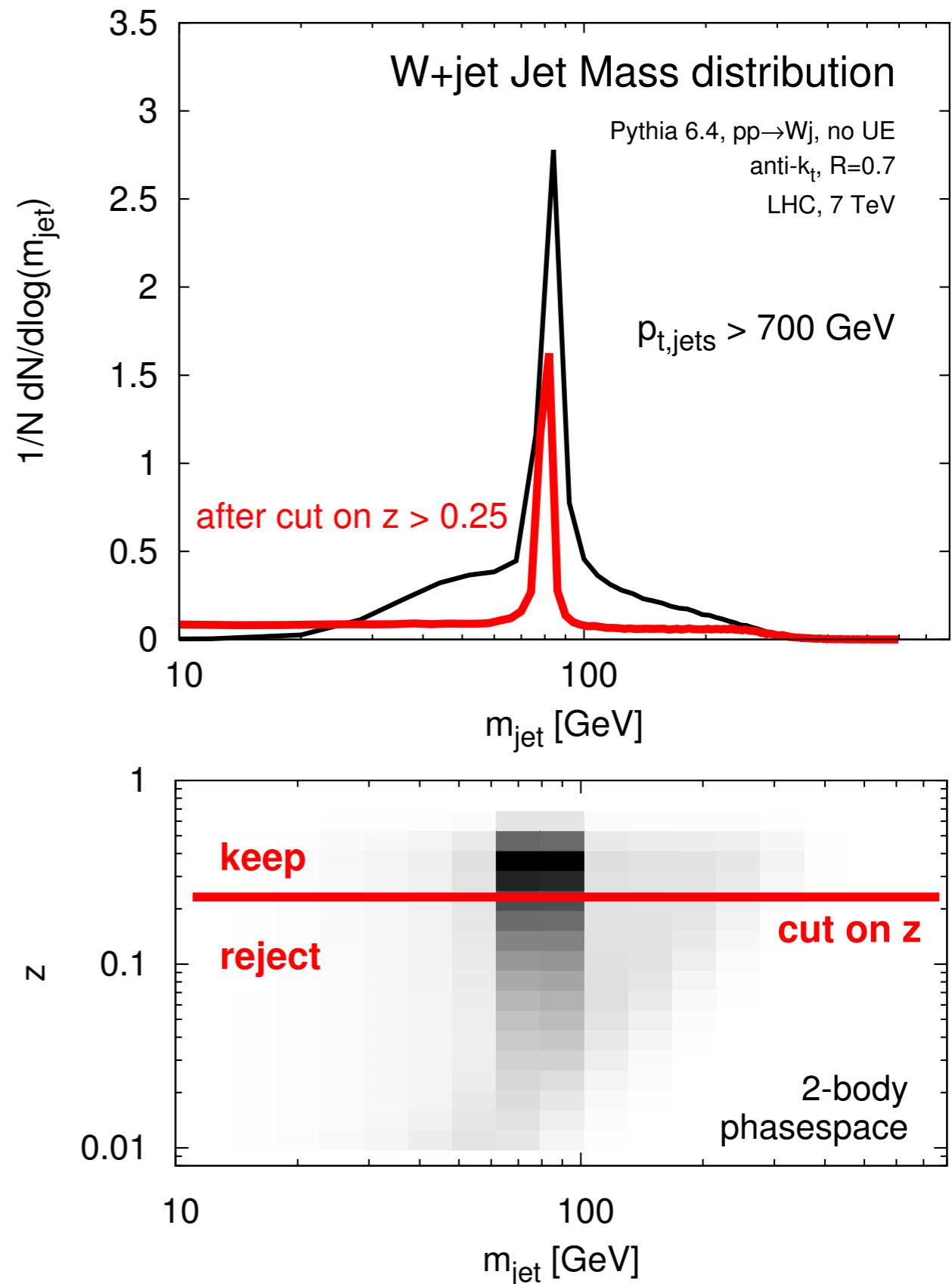
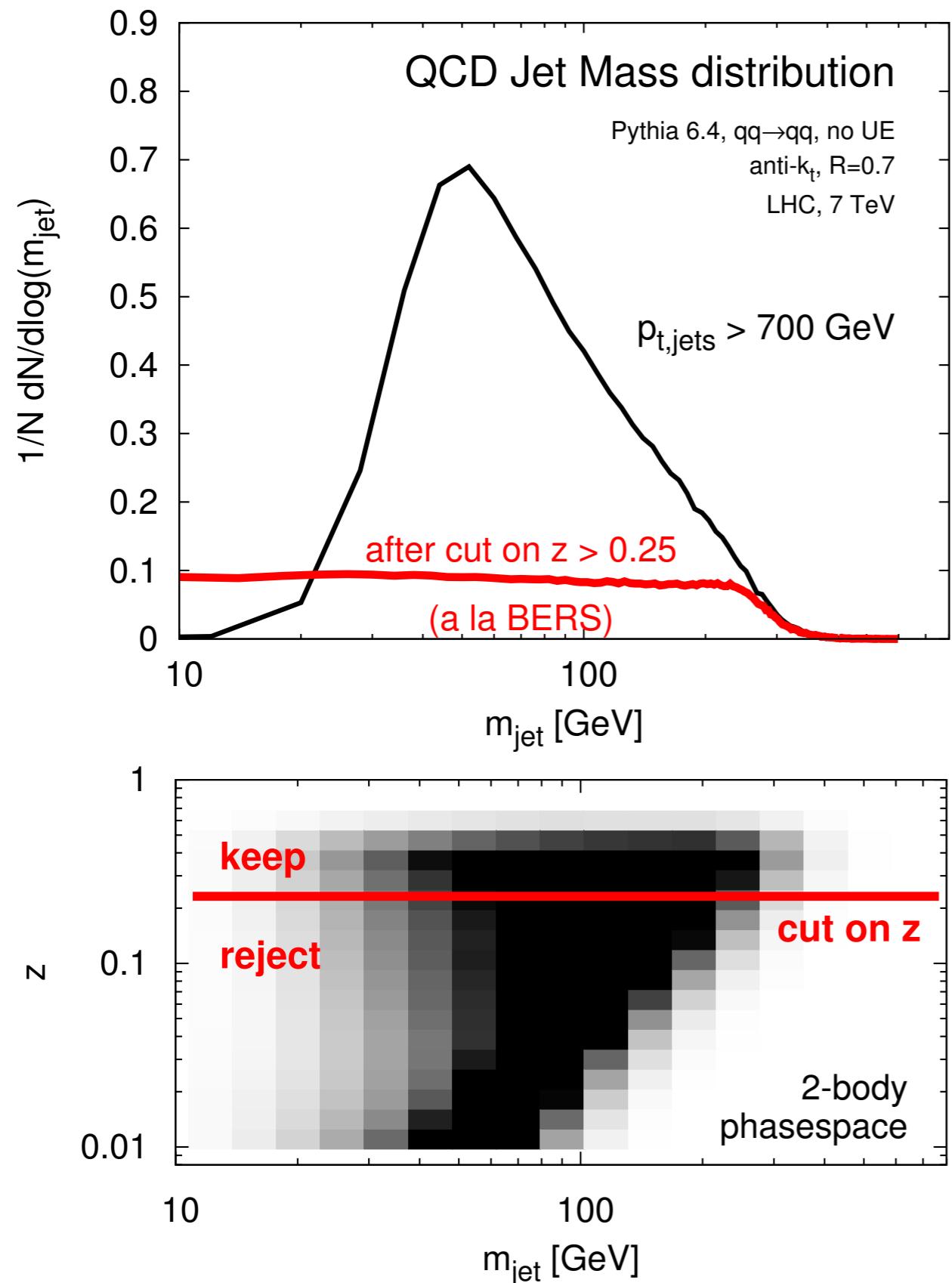
$$\int \frac{\frac{1}{2}}{\frac{m^2}{p_t^2 R^2}} \frac{dz}{z}$$

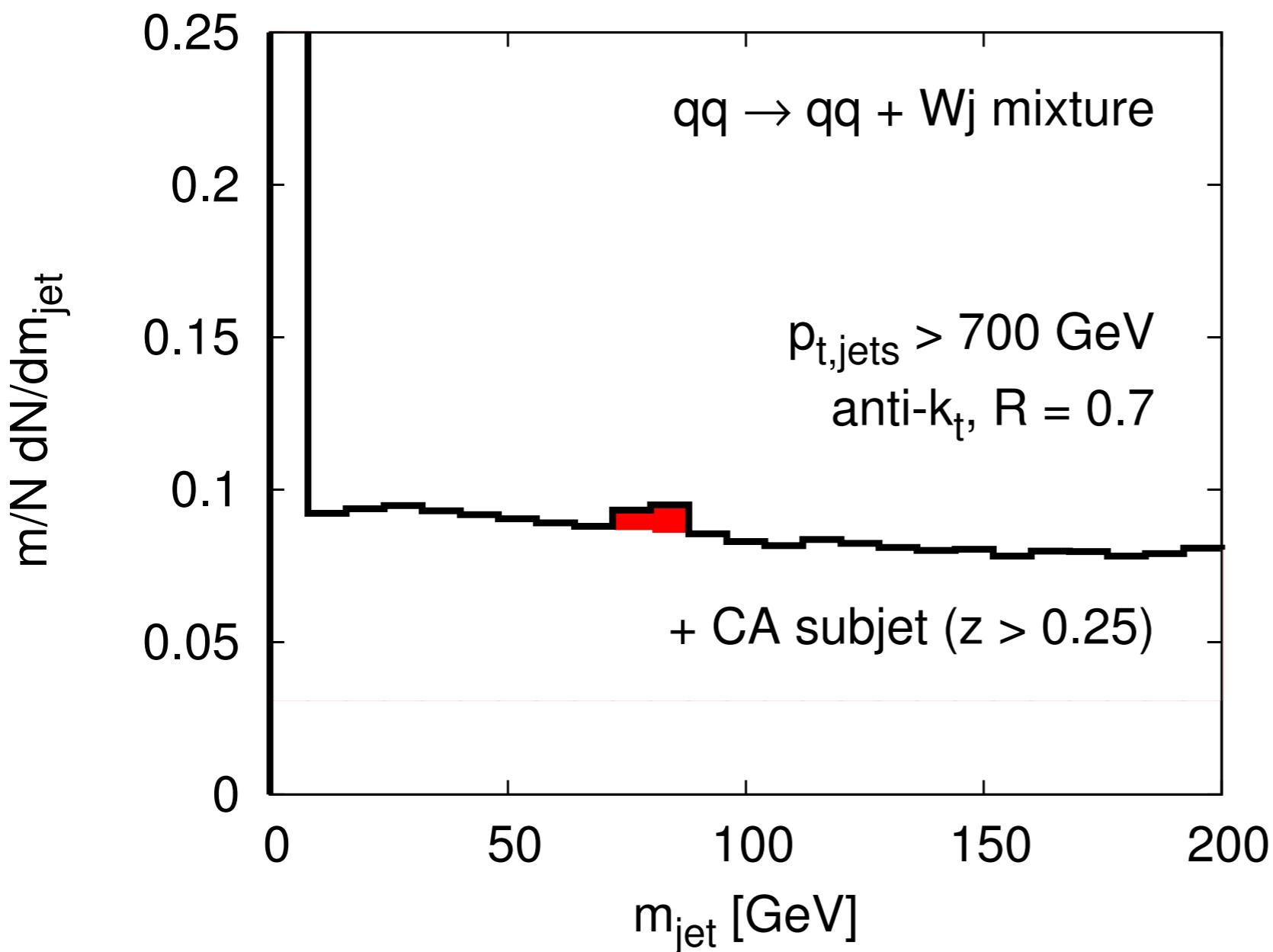
A hard cut on  $z$  reduces QCD background & simplifies its shape

# Inside the jet mass



# Inside the jet mass



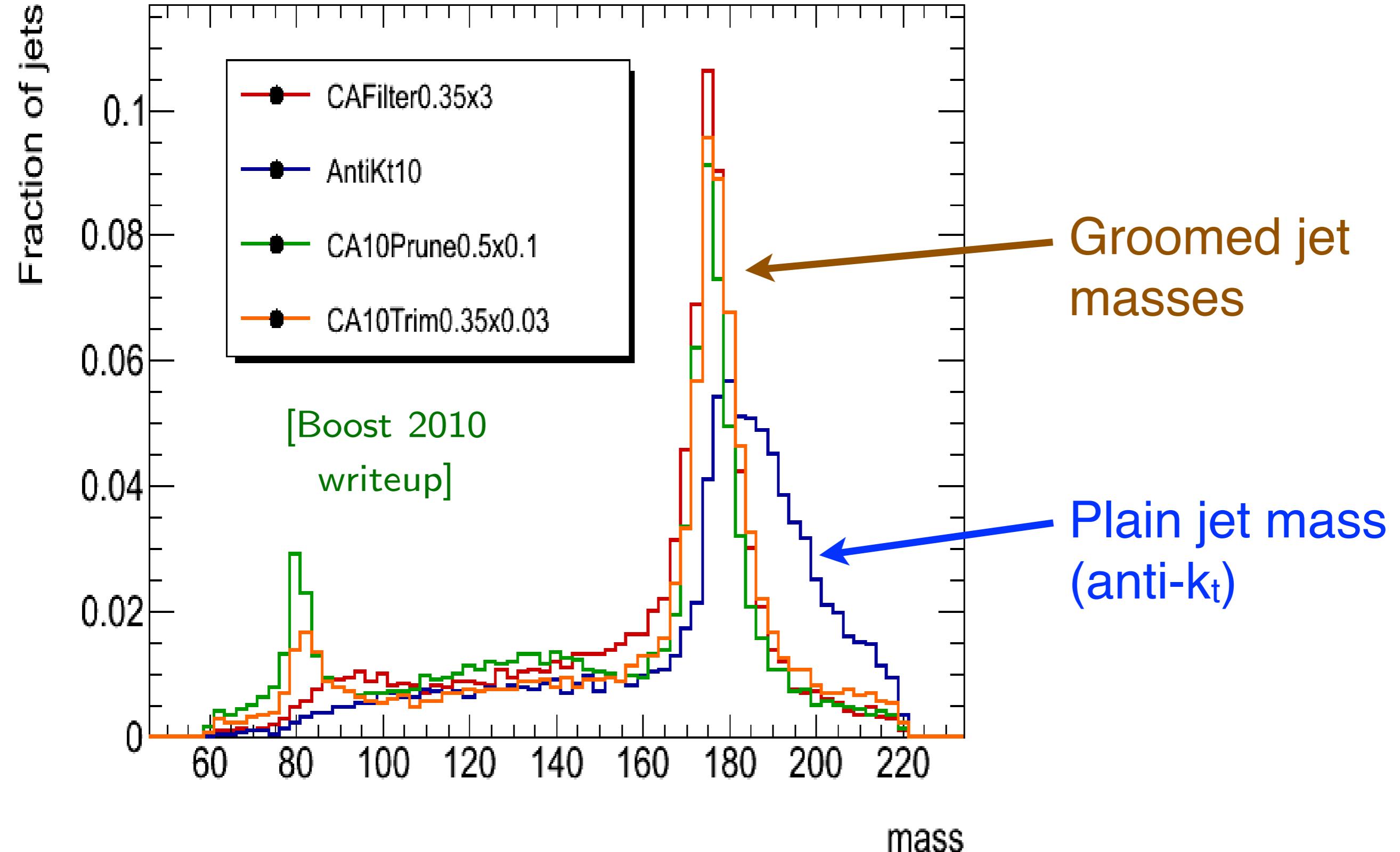


Signal + bkgd  
after cut on  $z$

# One core idea for grooming

[see blackboard]

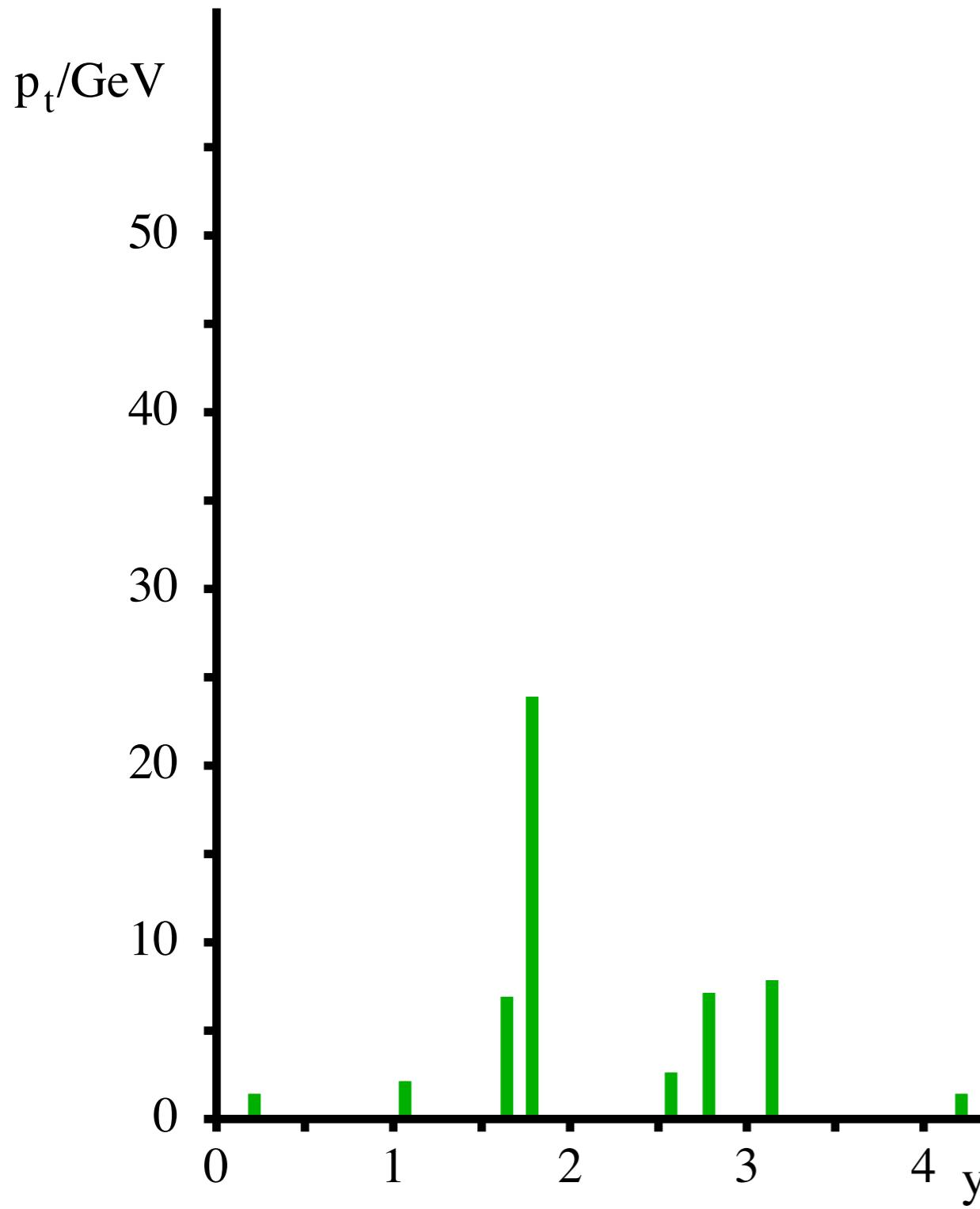
# “Grooming”



# How do the tools work in practice?

# Identifying jet substructure: try out anti- $k_t$

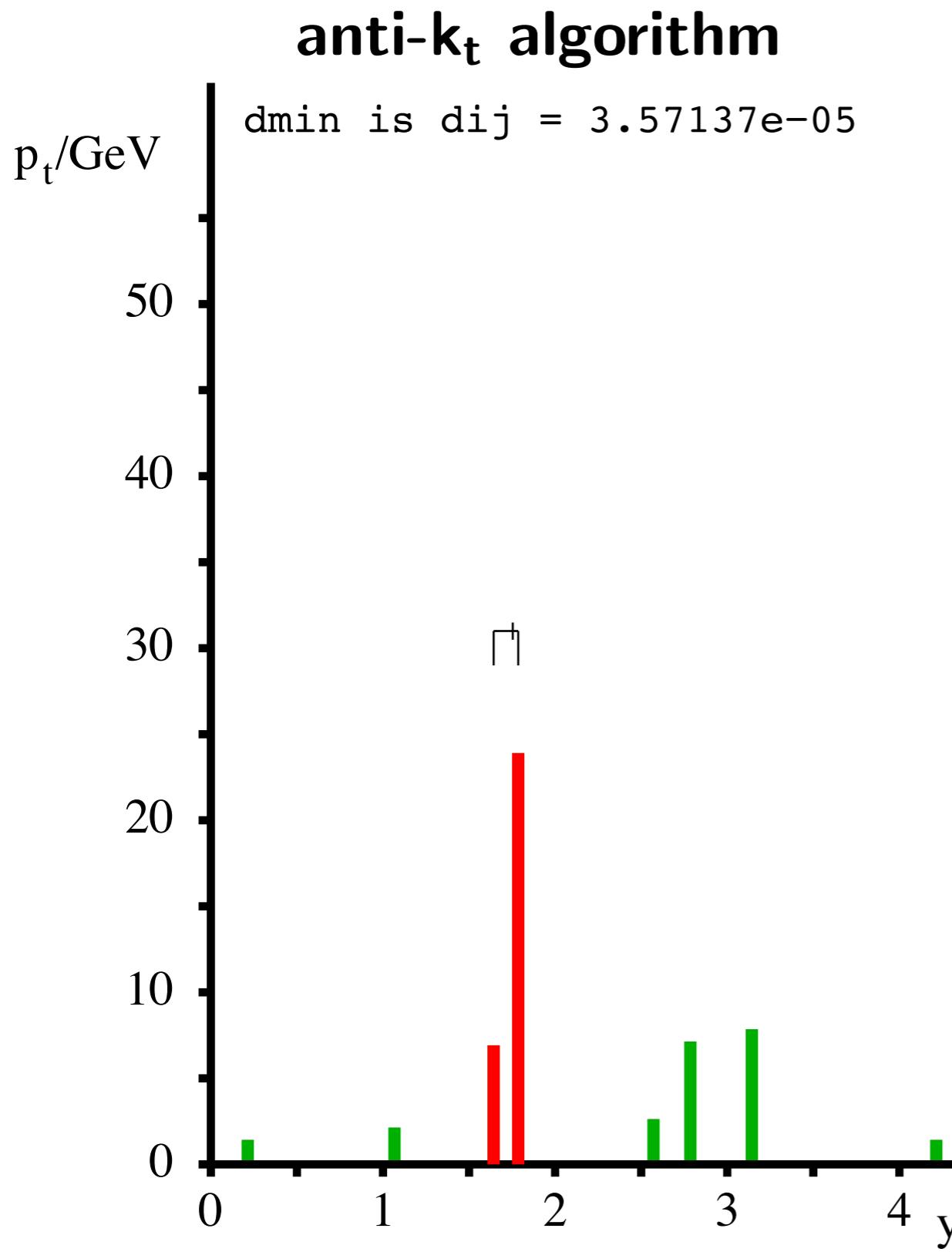
## anti- $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out anti- $k_t$

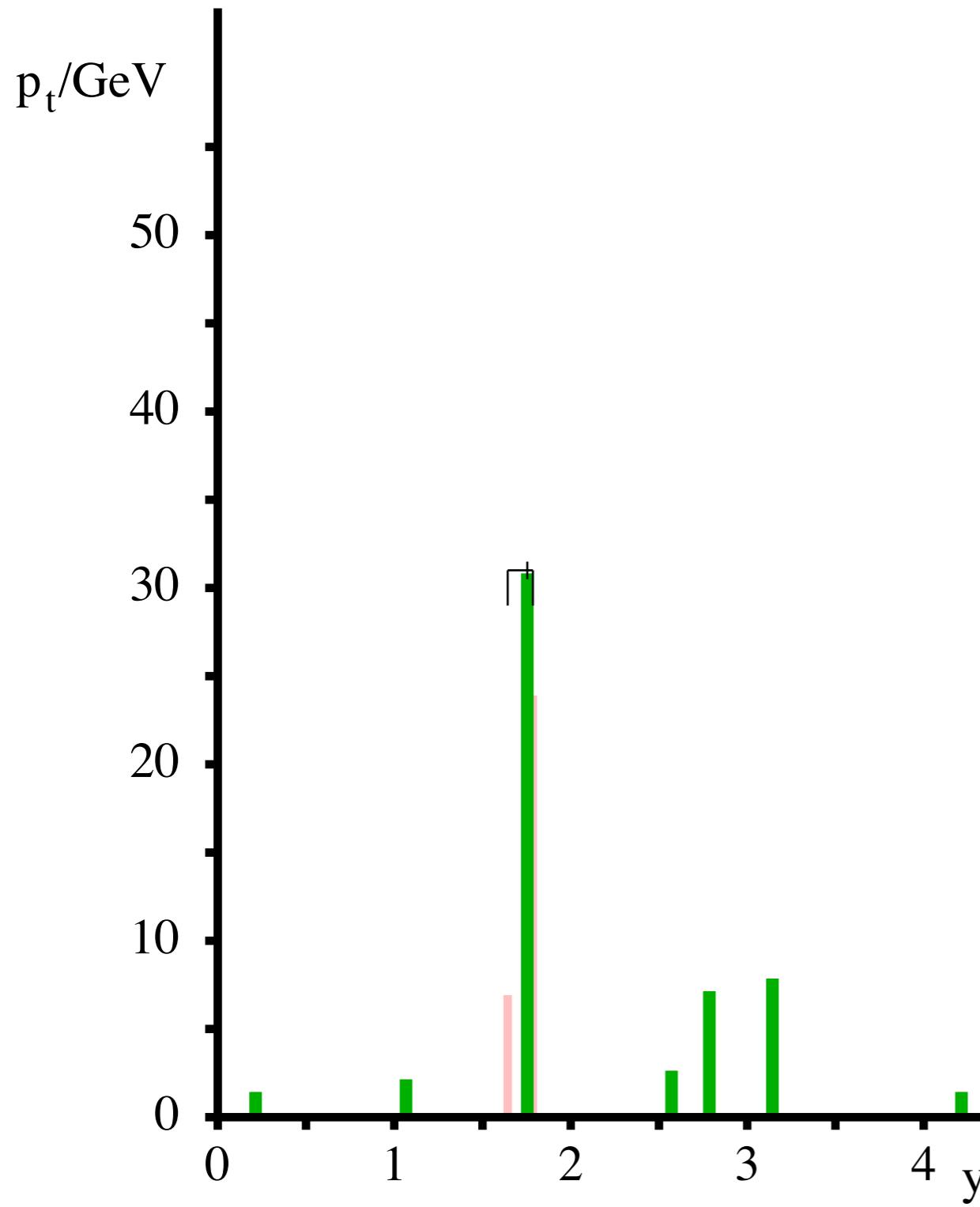


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out anti- $k_t$

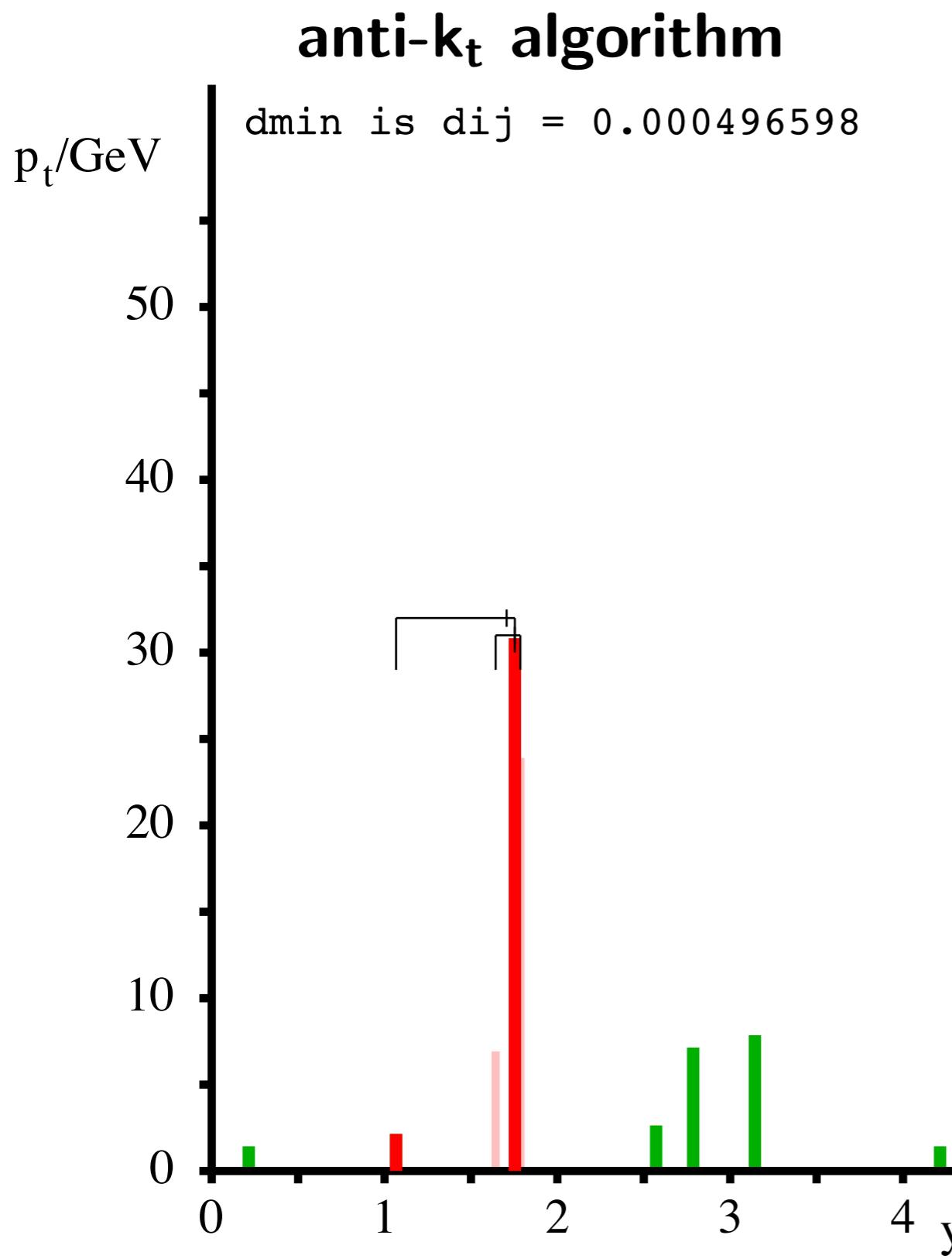
## anti- $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out anti- $k_t$

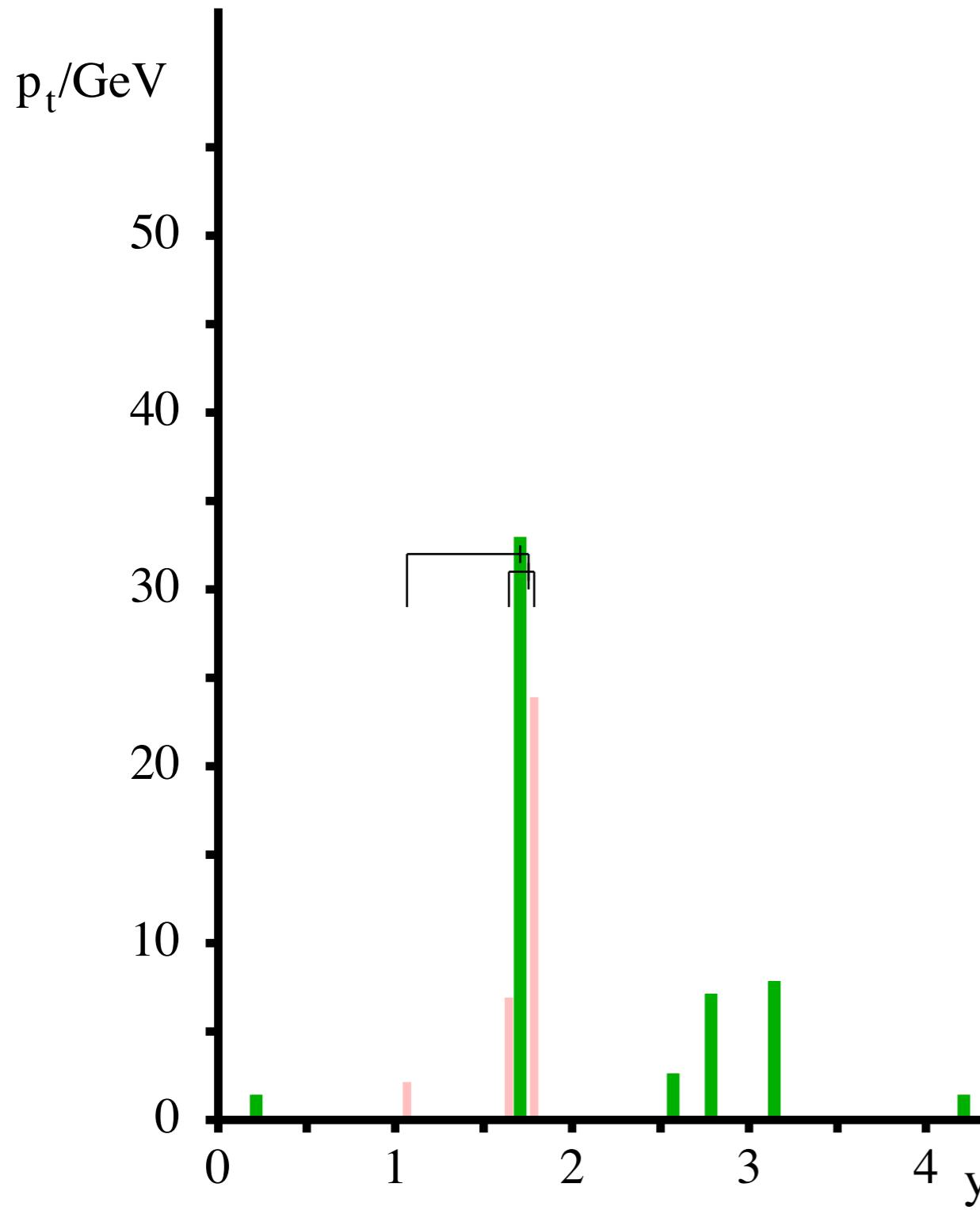


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out anti- $k_t$

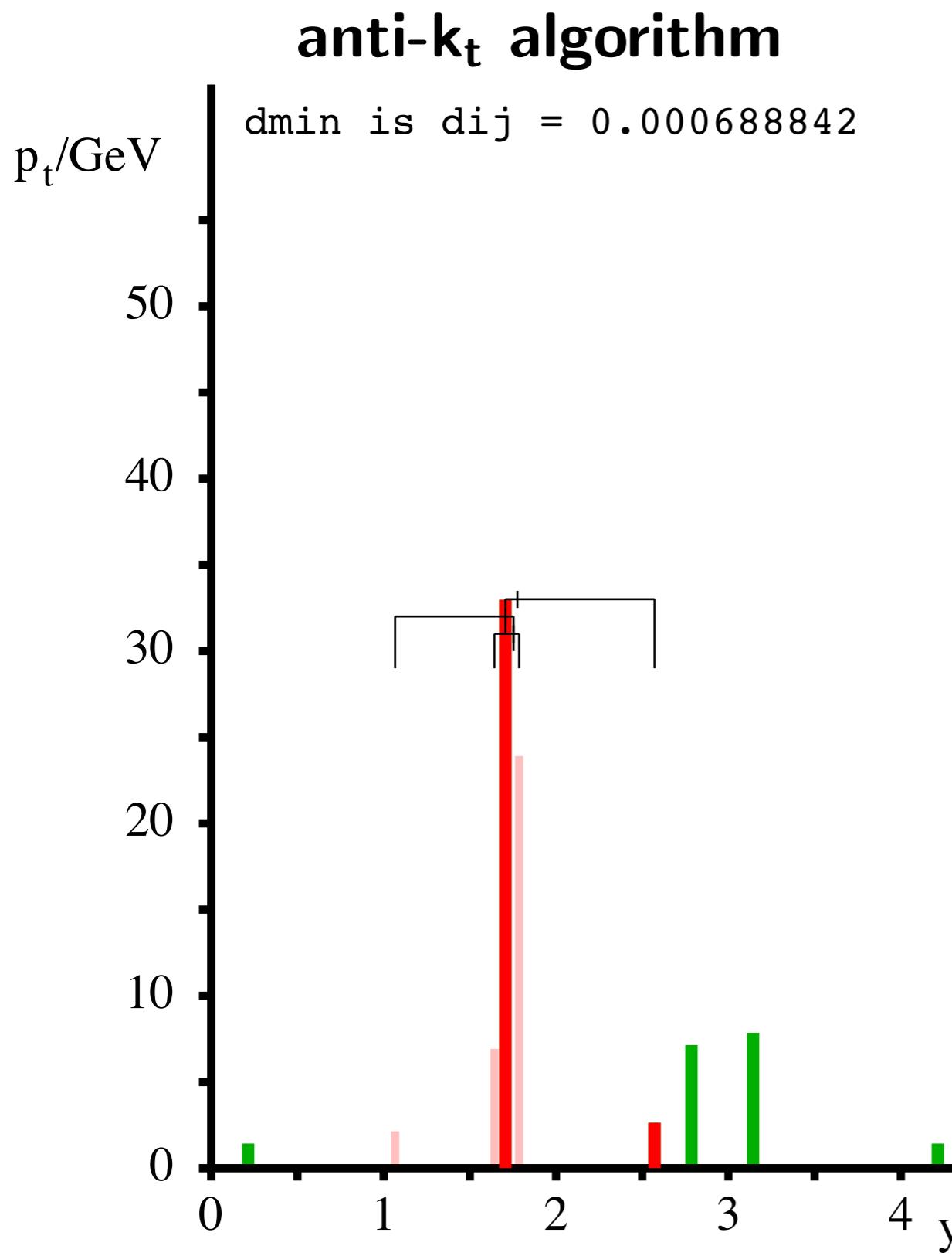
## anti- $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out anti- $k_t$

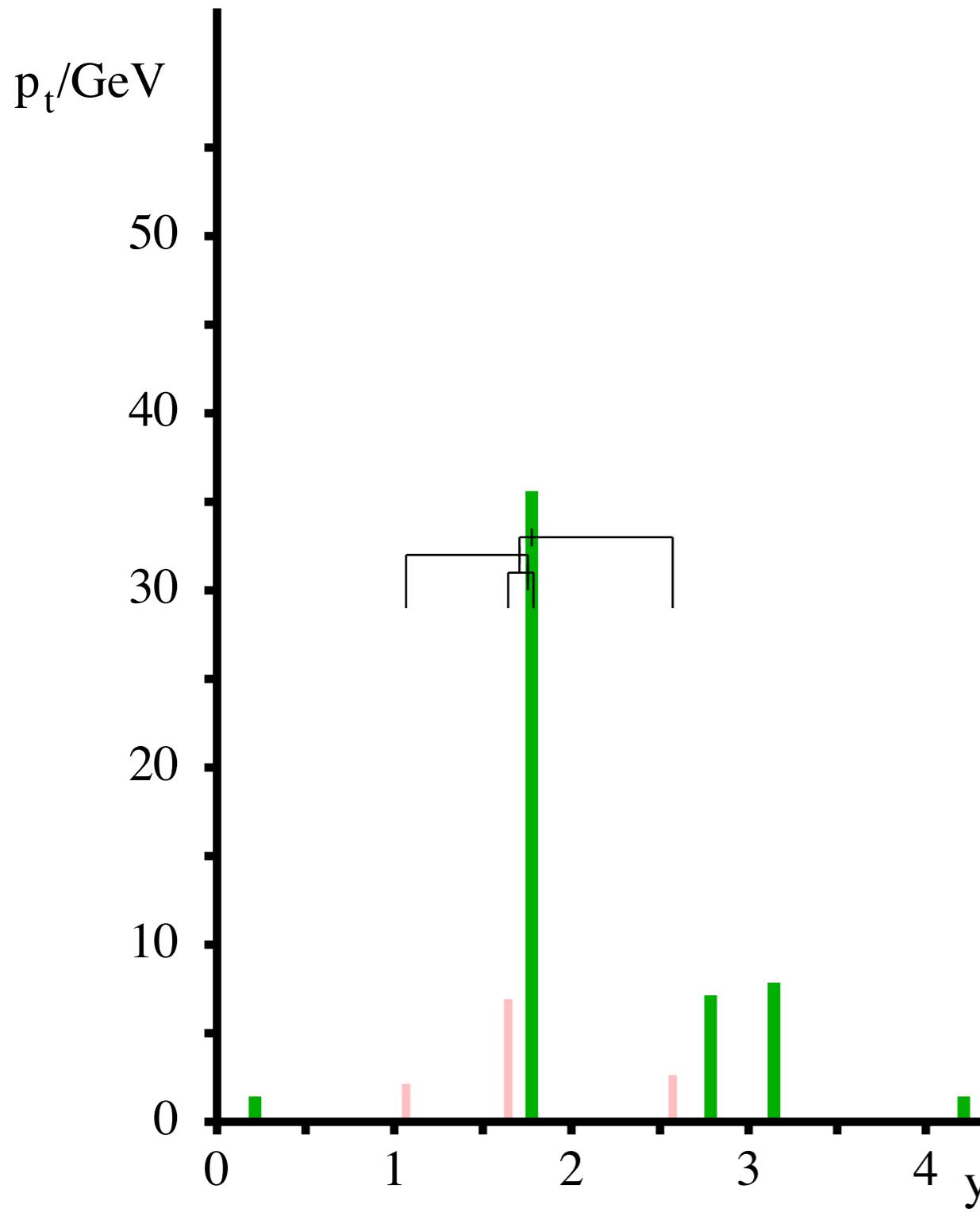


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out anti- $k_t$

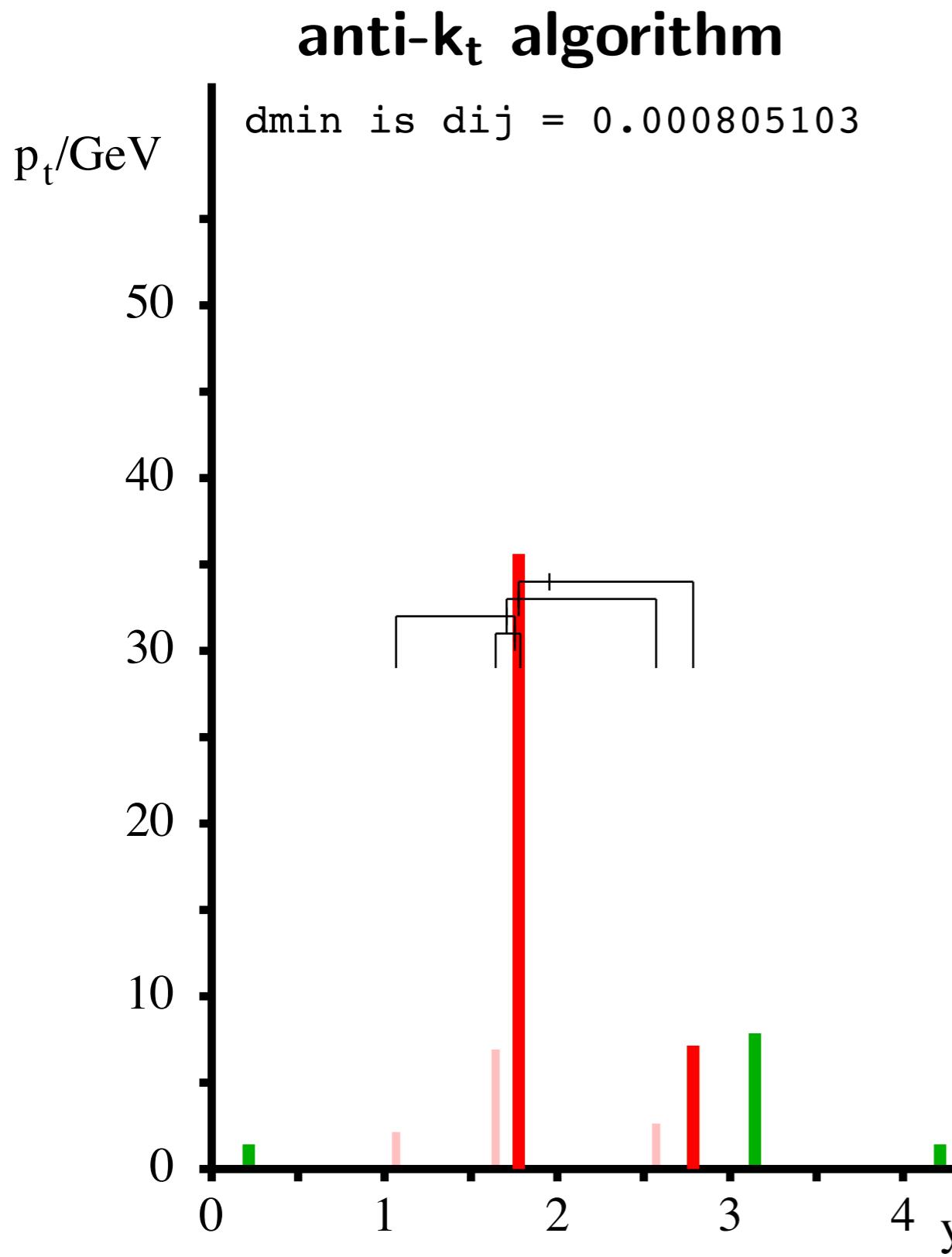
## anti- $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out anti- $k_t$



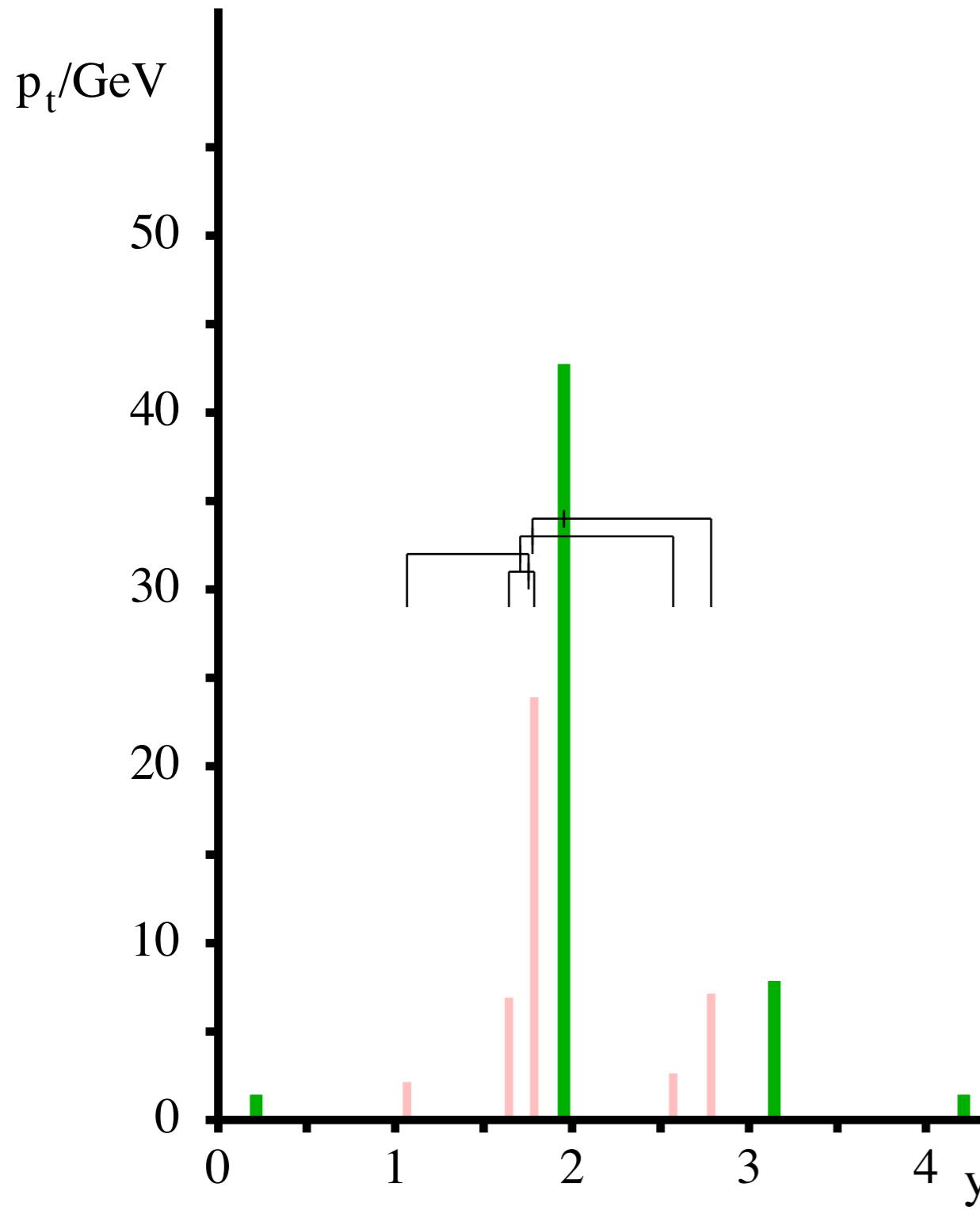
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$

## anti- $k_t$ algorithm

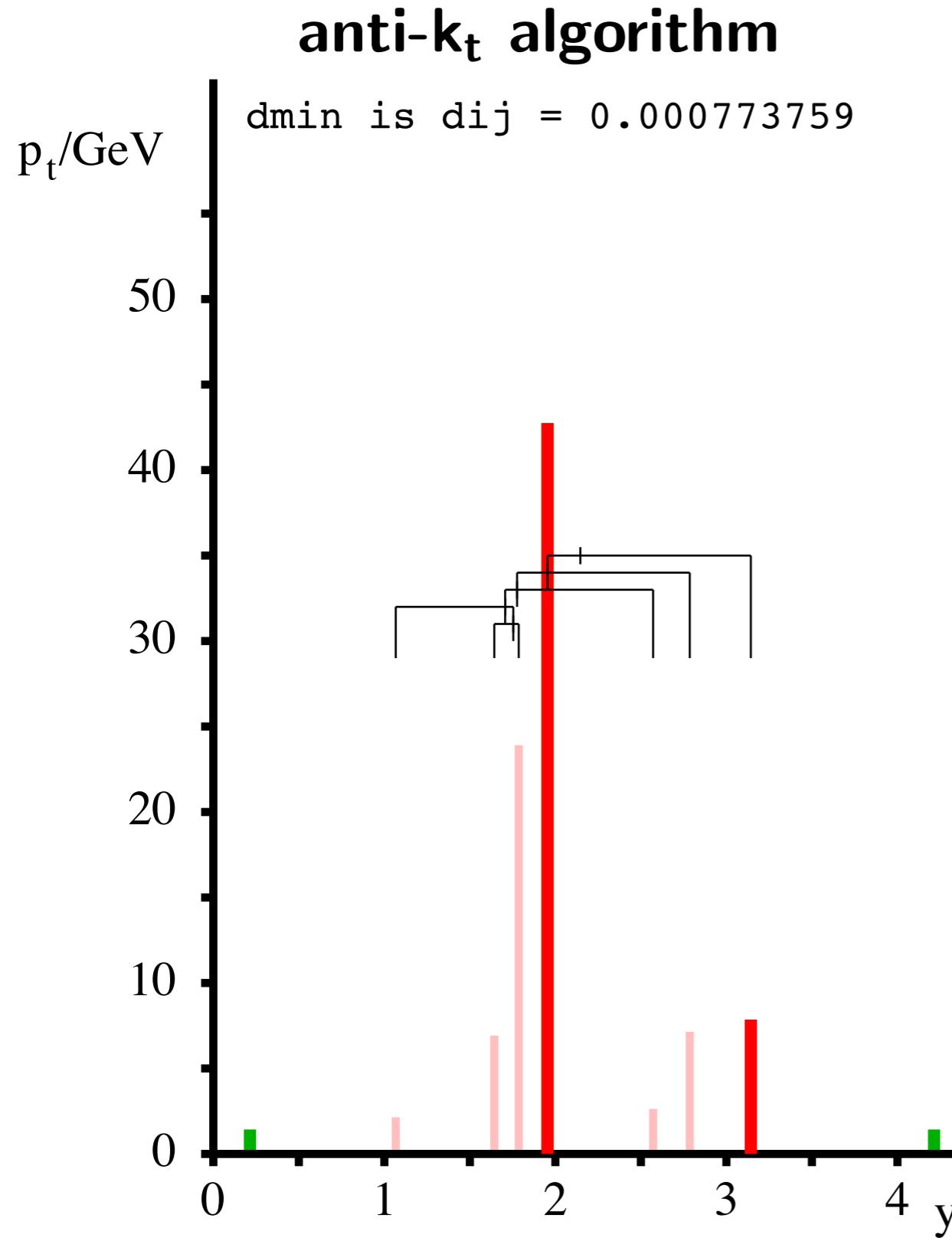


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$



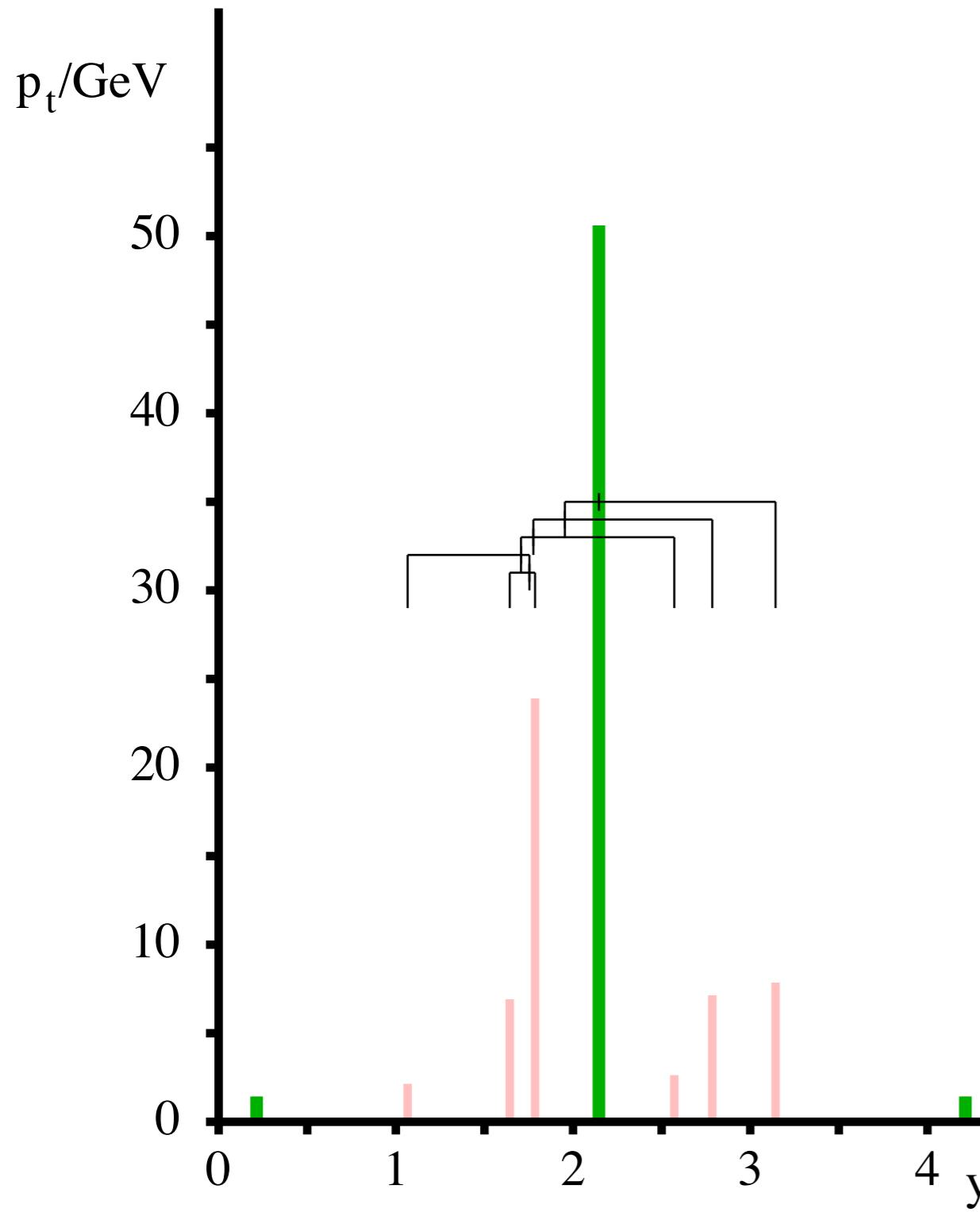
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$

## anti- $k_t$ algorithm

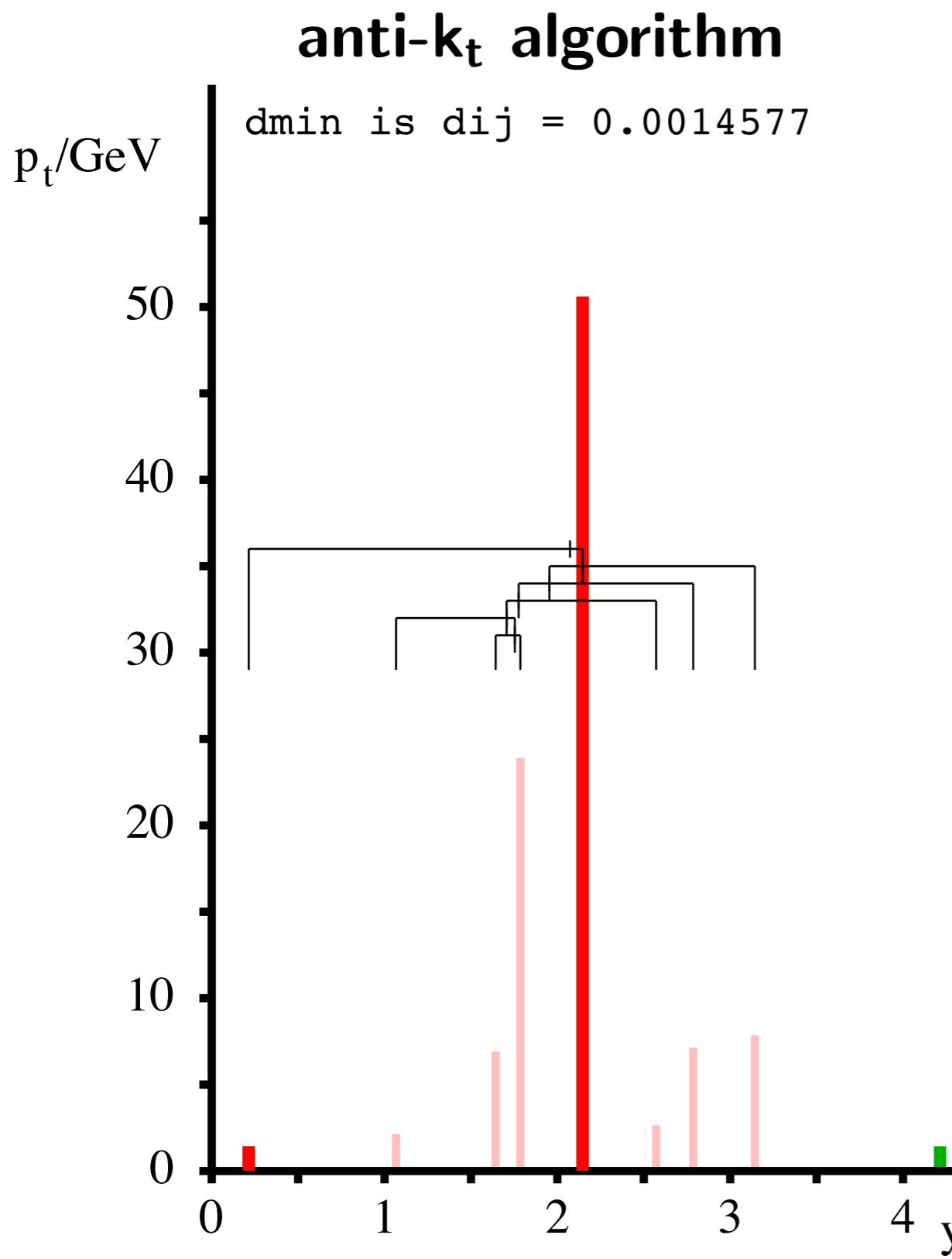


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob → no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$



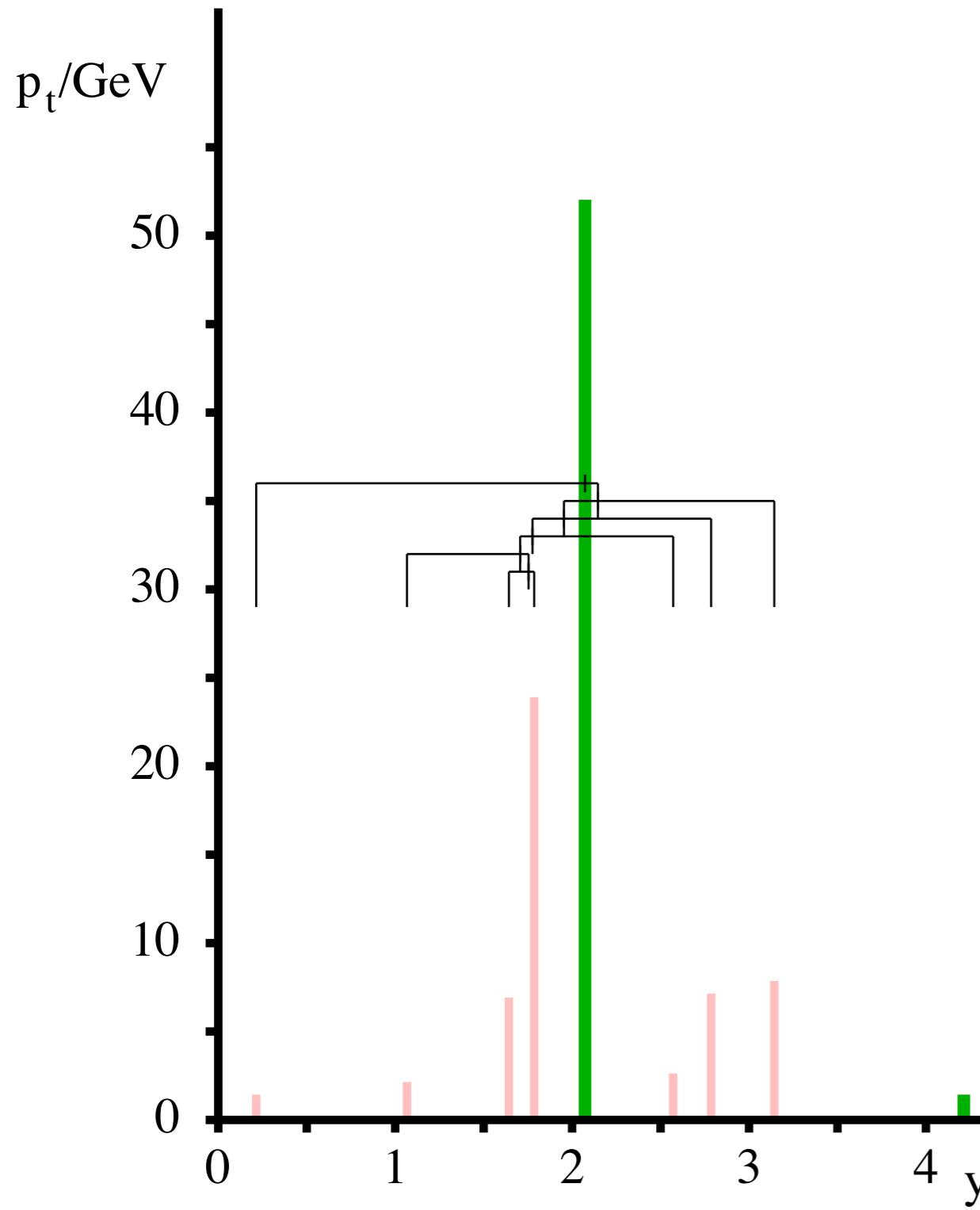
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

*Anti- $k_t$  gradually makes its way through the secondary blob → no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$

## anti- $k_t$ algorithm

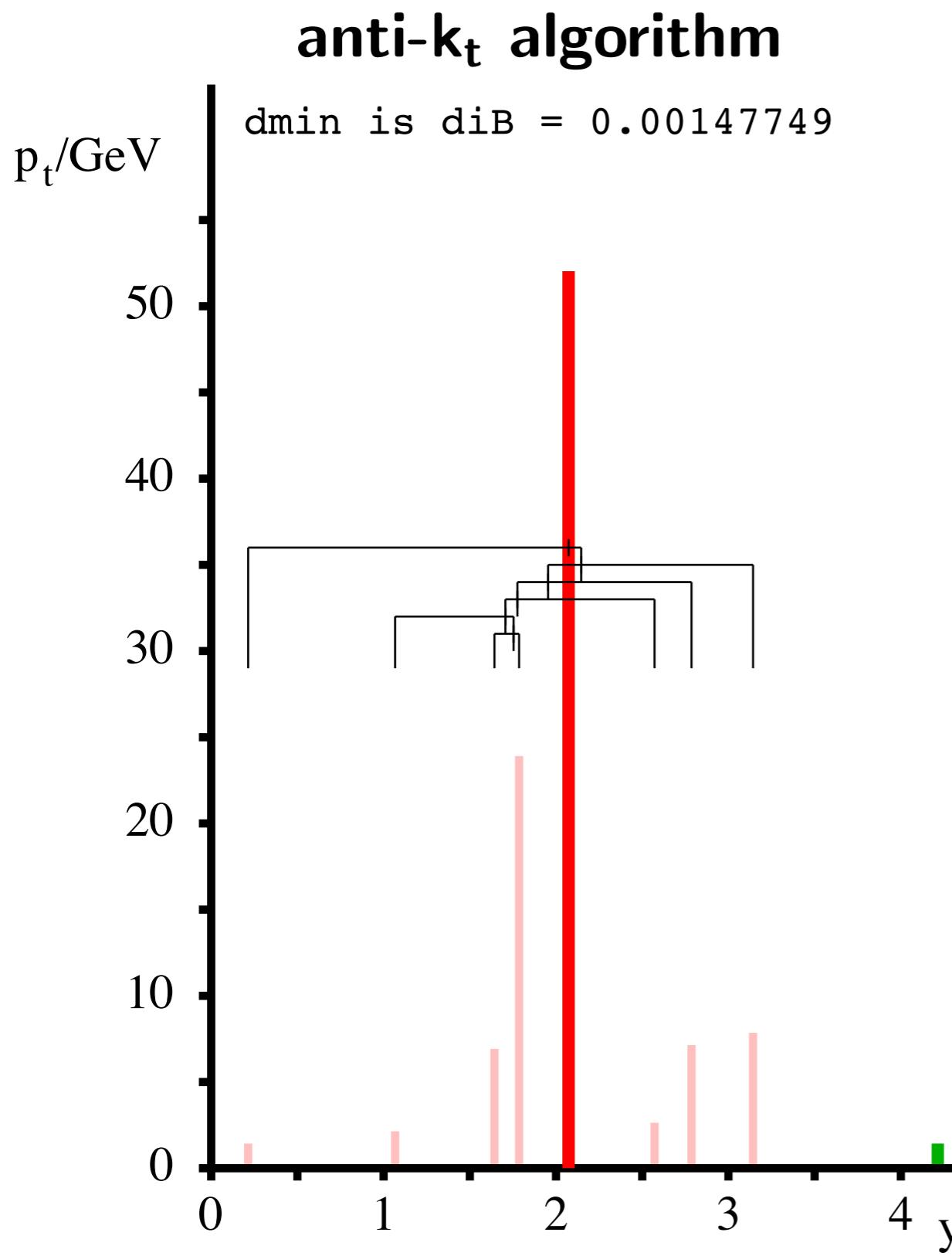


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$



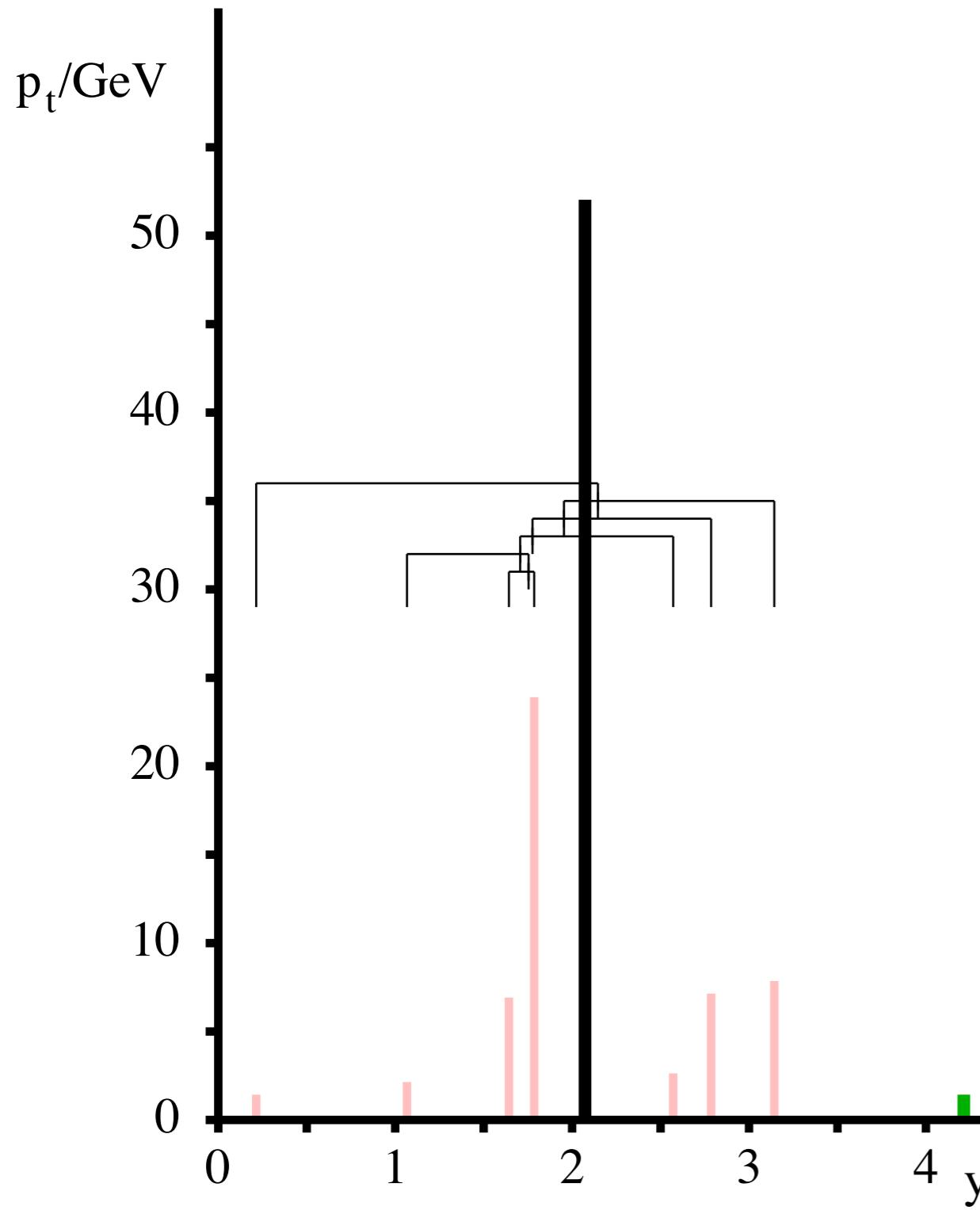
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

*Anti- $k_t$  gradually makes its way through the secondary blob → no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$

## anti- $k_t$ algorithm

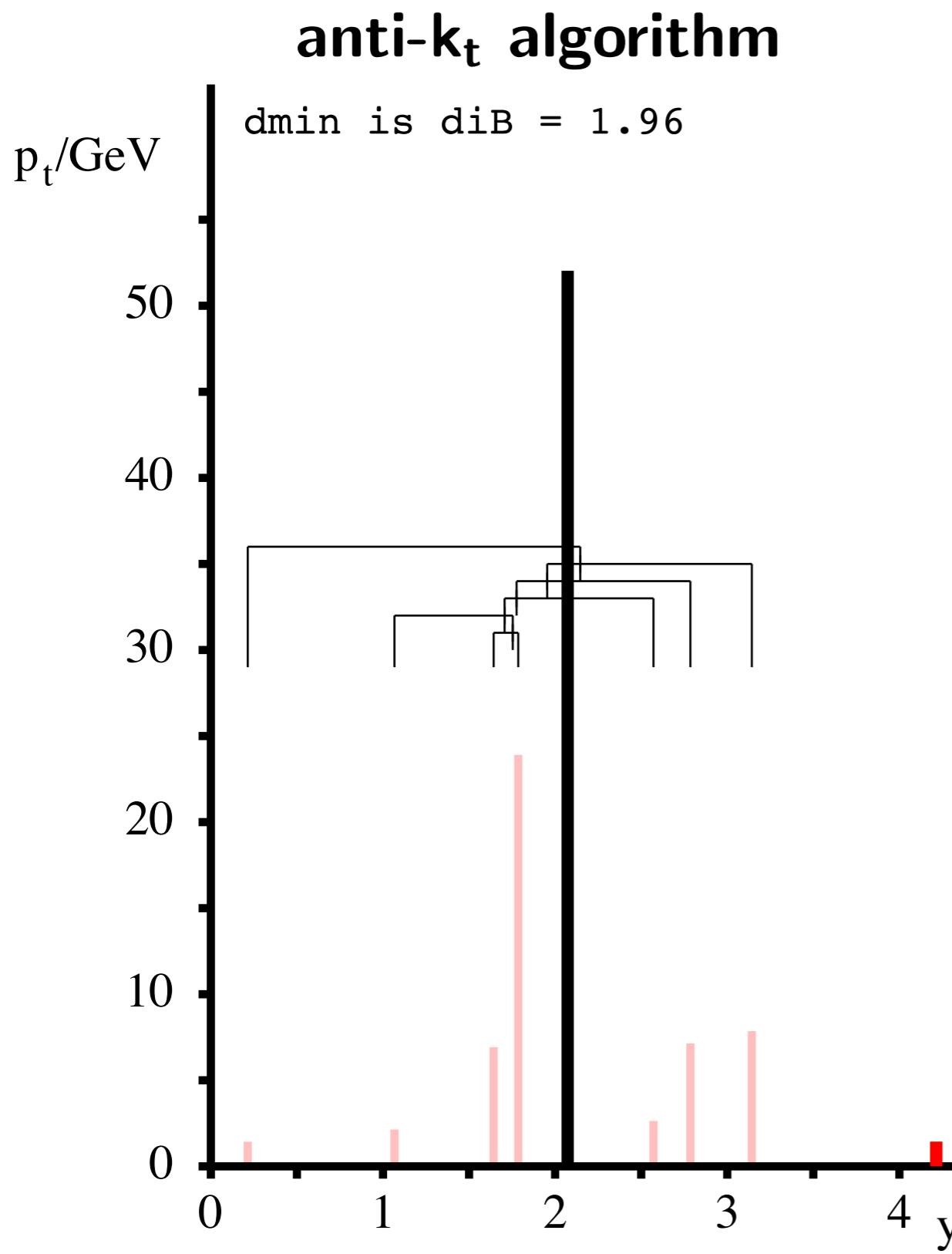


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$



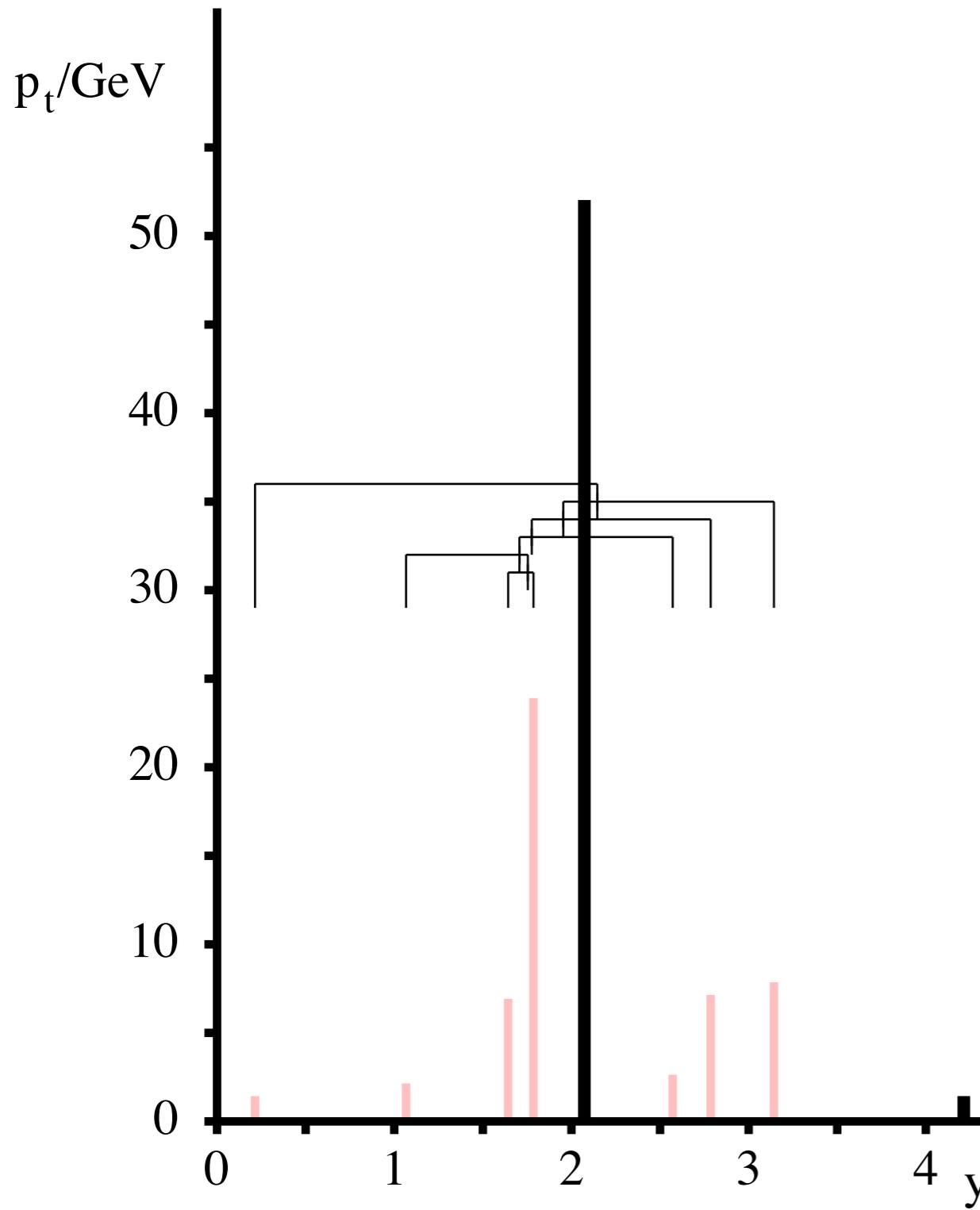
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out anti- $k_t$

## anti- $k_t$ algorithm



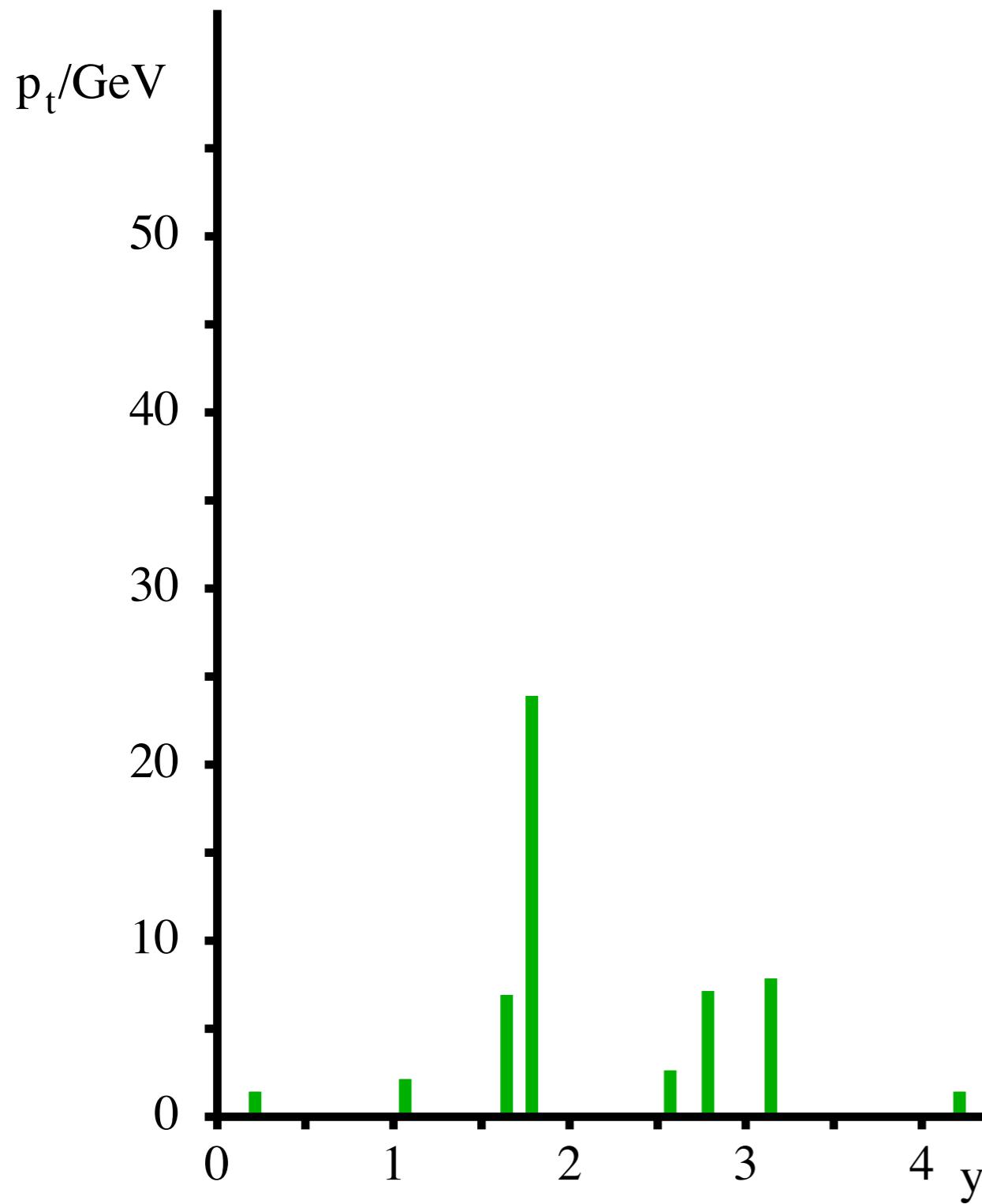
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*Anti- $k_t$  gradually makes its way through the secondary blob  $\rightarrow$  no clear identification of substructure associated with 2nd parton.*

# Identifying jet substructure: try out $k_t$

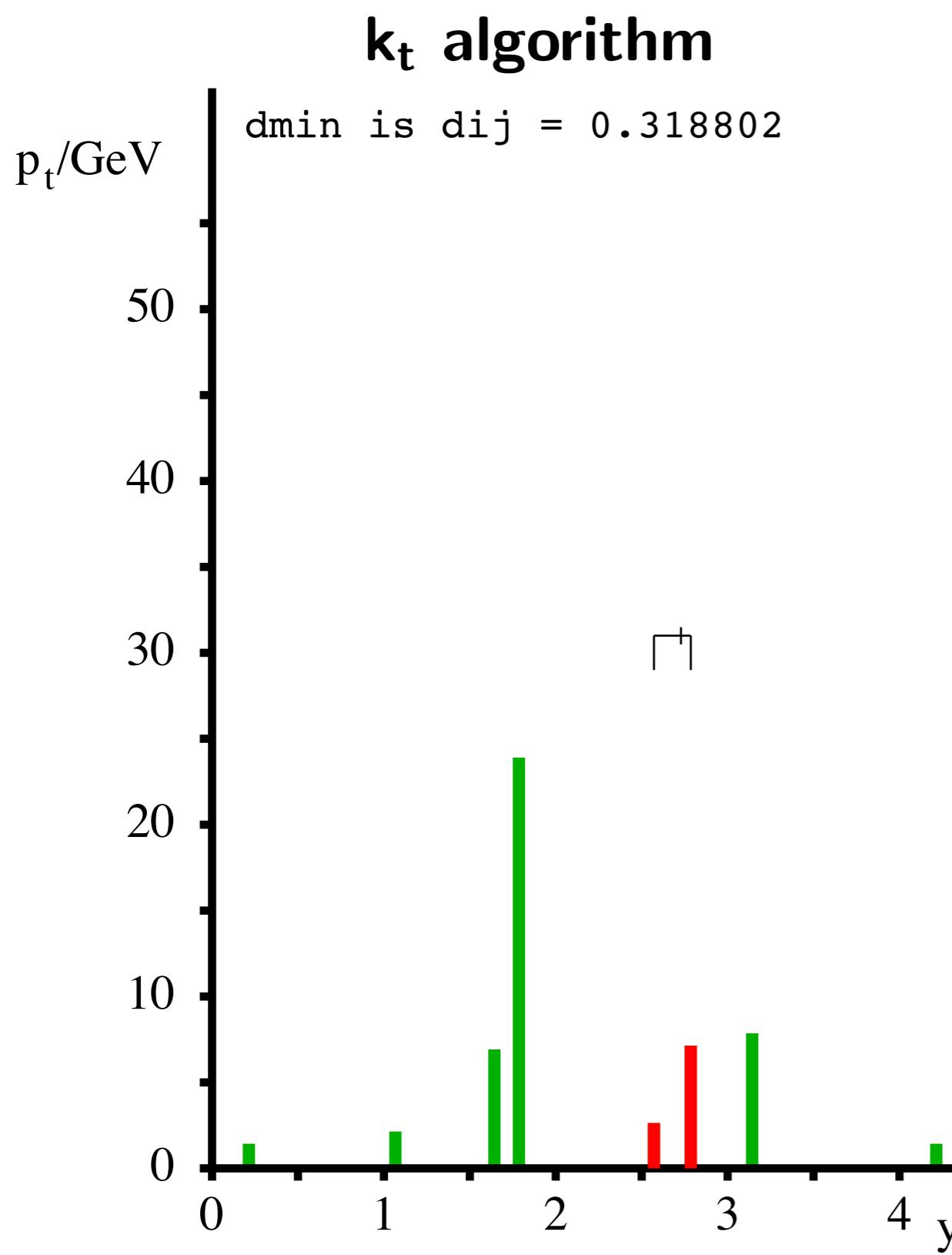
## $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out $k_t$

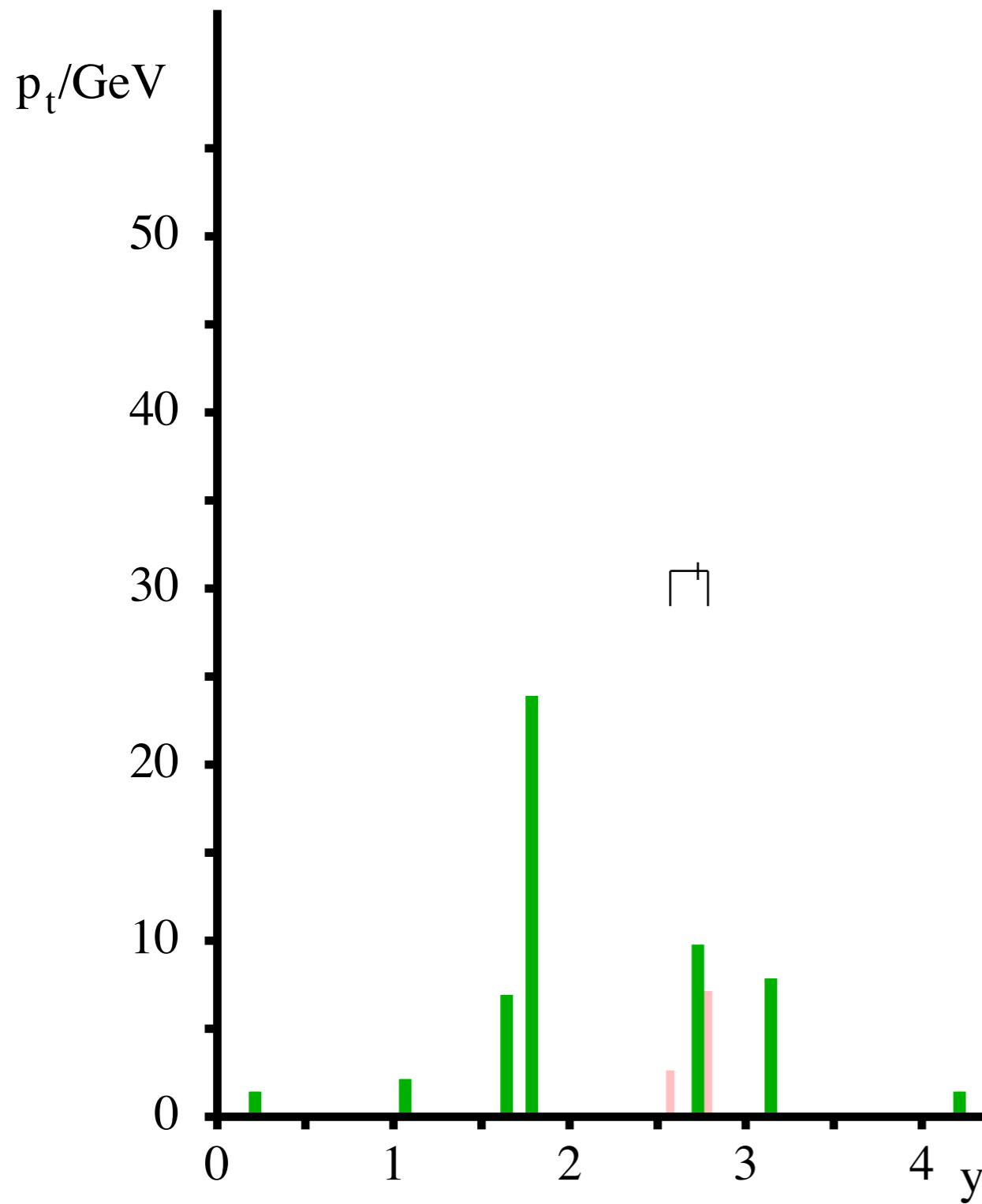


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out $k_t$

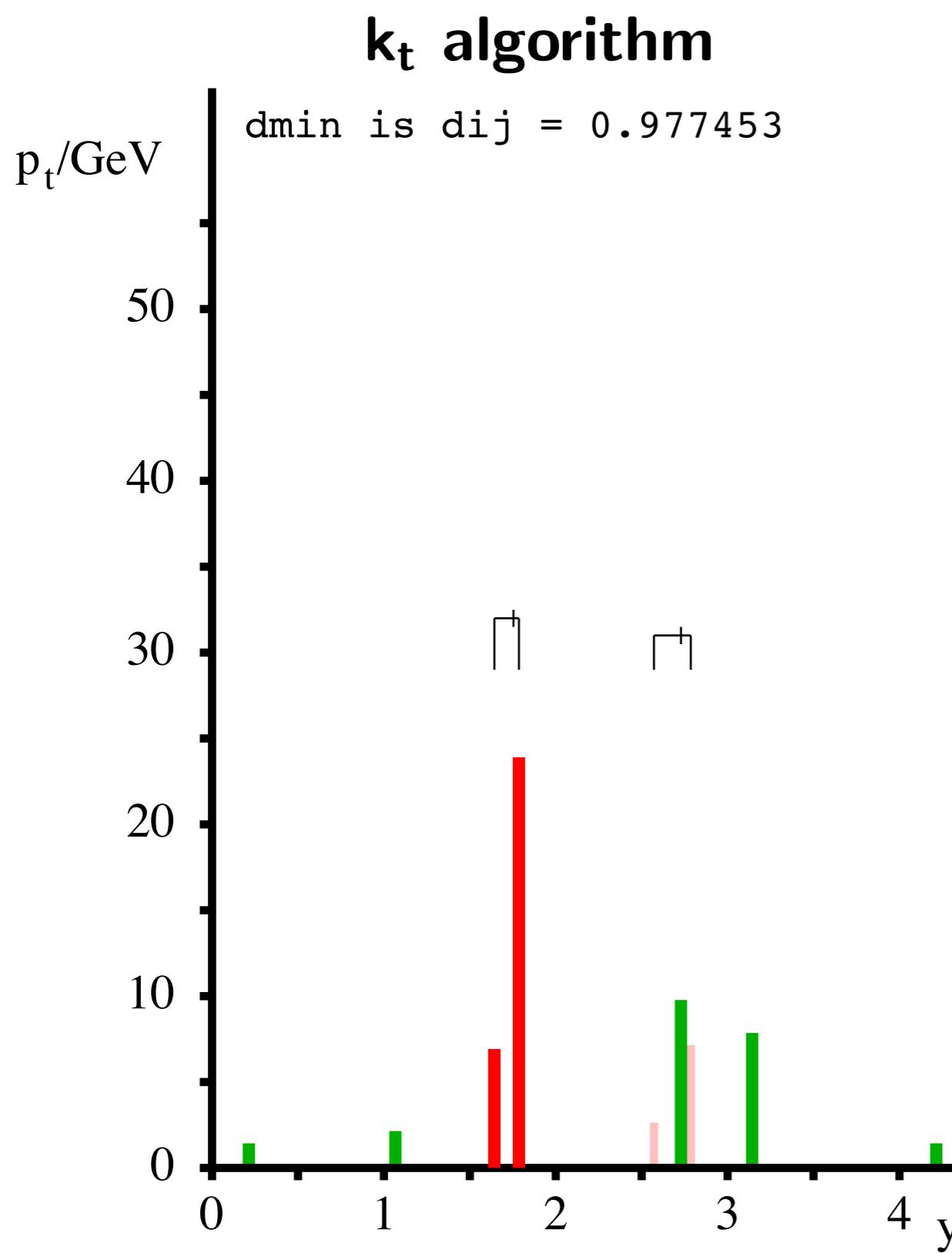
## $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

# Identifying jet substructure: try out $k_t$

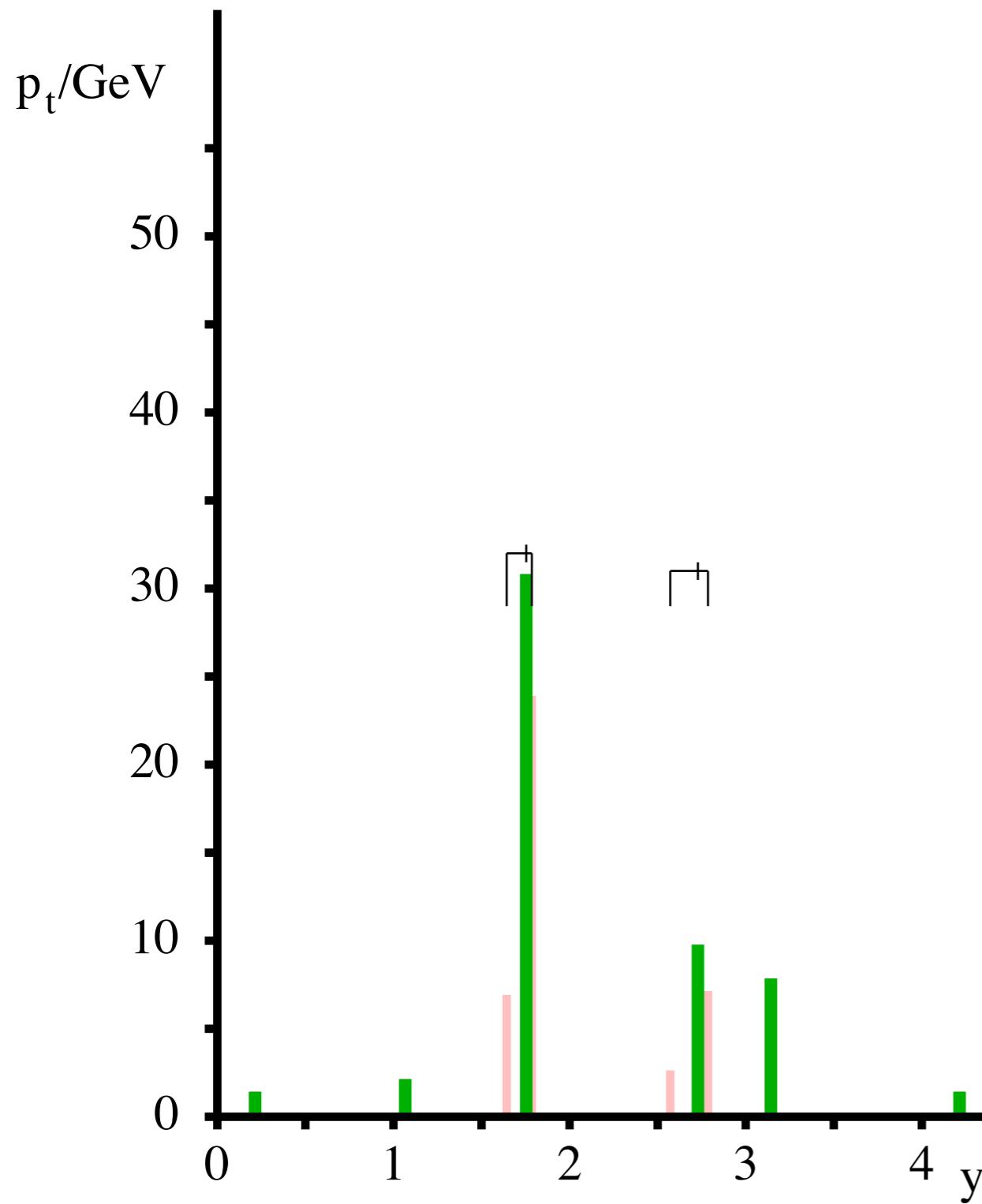


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out $k_t$

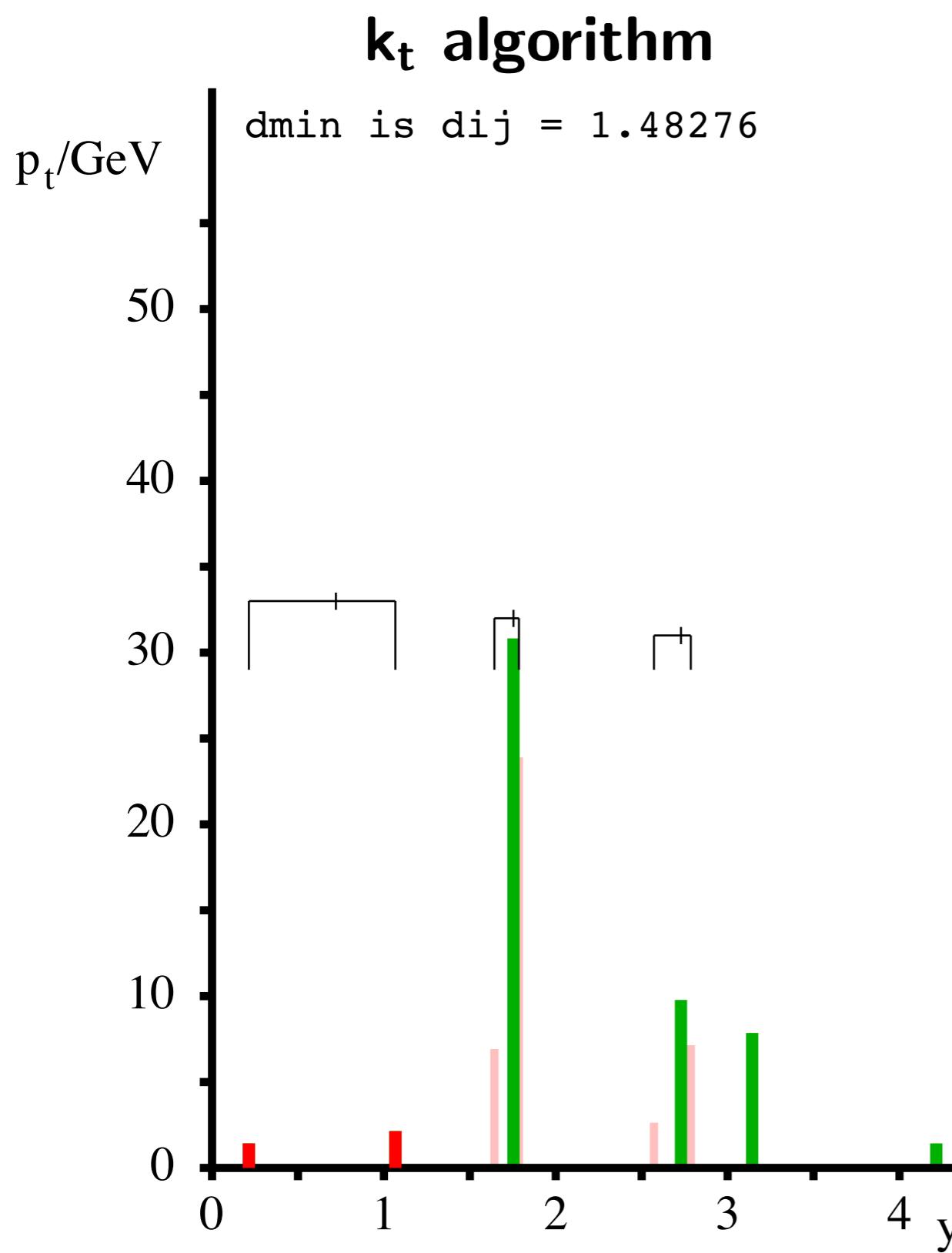
## $k_t$ algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

# Identifying jet substructure: try out $k_t$



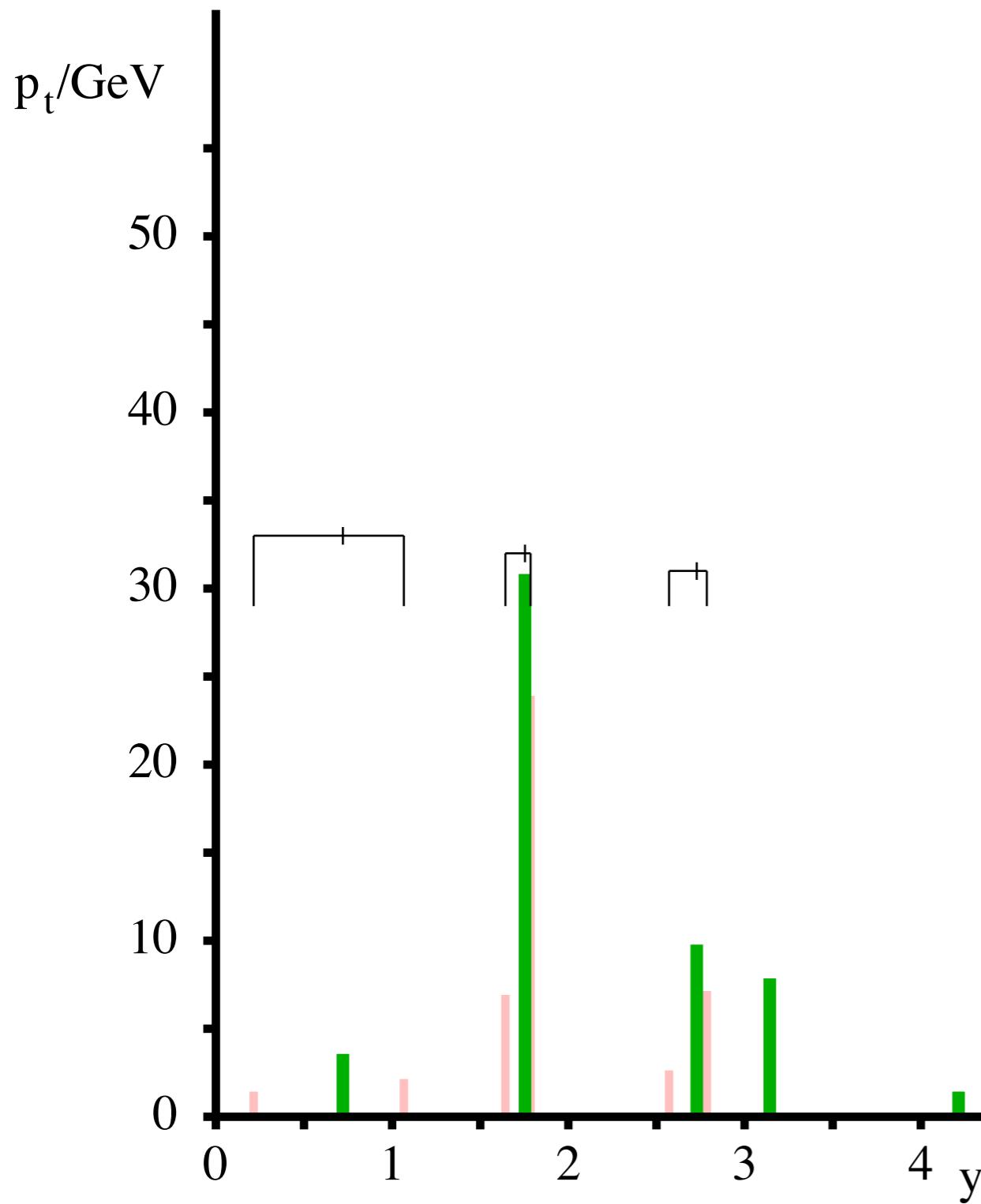
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

*$k_t$  clusters soft “junk” early on in the clustering*

# Identifying jet substructure: try out $k_t$

## $k_t$ algorithm

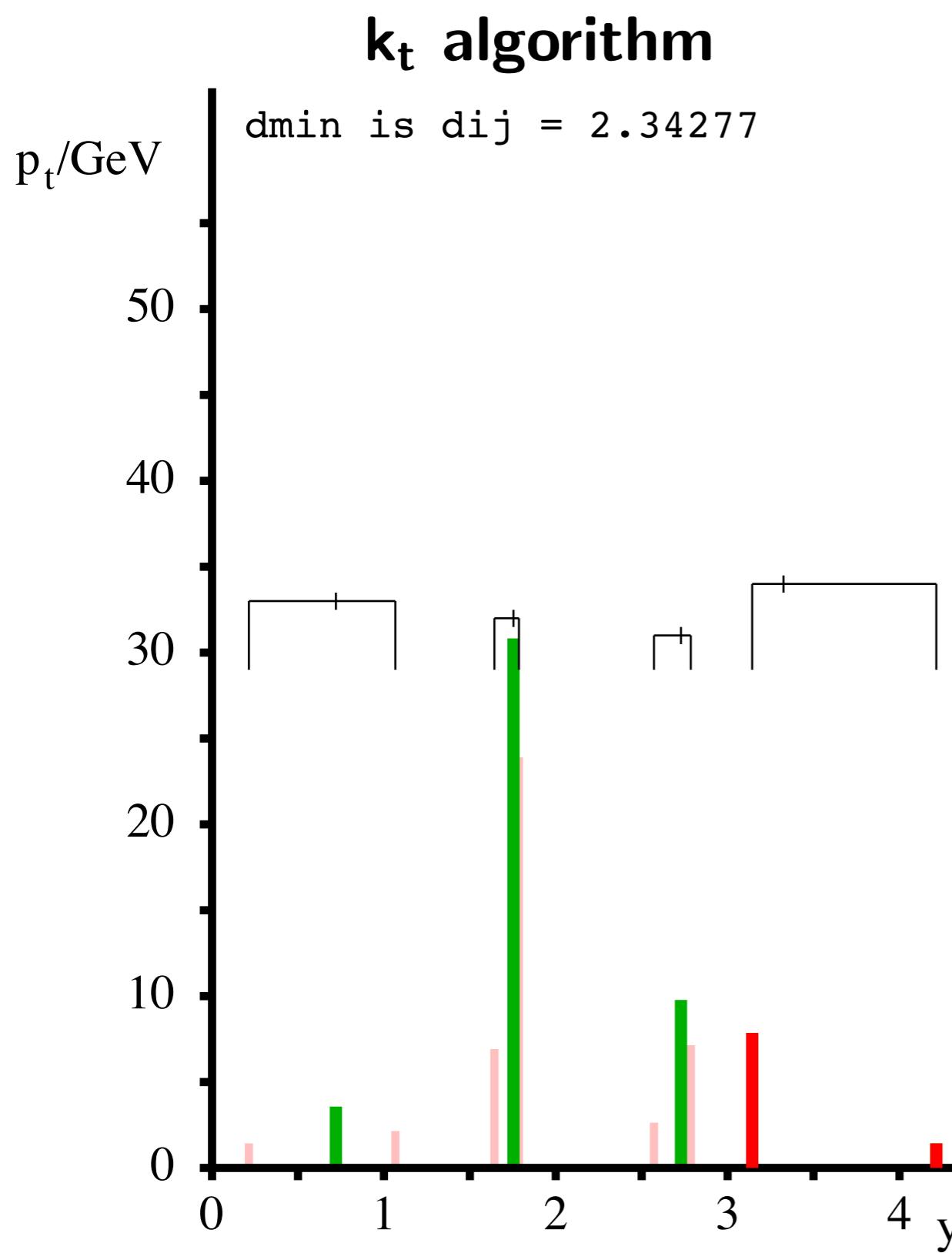


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*$k_t$  clusters soft “junk” early on in the clustering*

# Identifying jet substructure: try out $k_t$



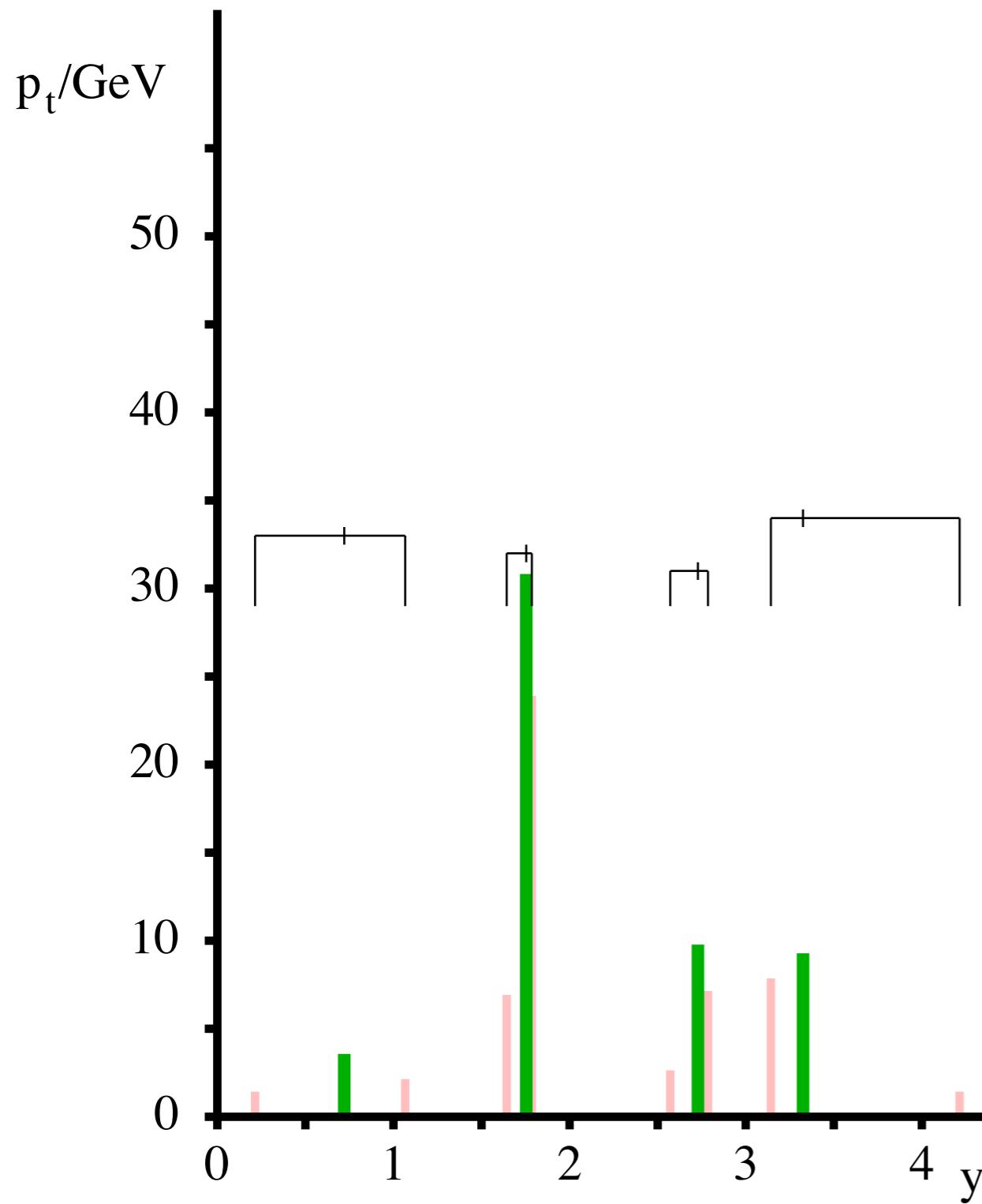
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*$k_t$  clusters soft “junk” early on in the clustering*

# Identifying jet substructure: try out $k_t$

## $k_t$ algorithm

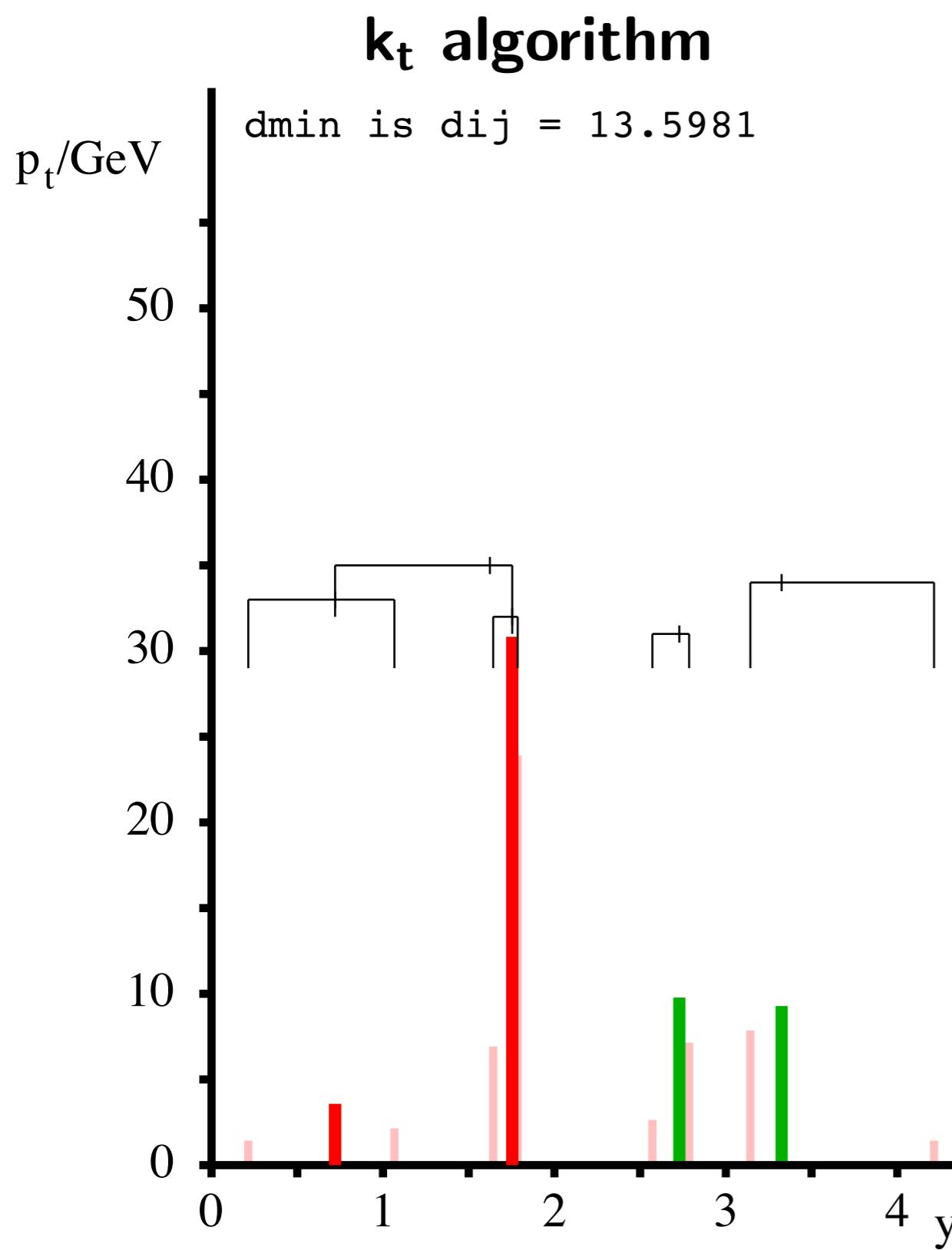


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

*$k_t$  clusters soft “junk” early on in the clustering*

# Identifying jet substructure: try out $k_t$



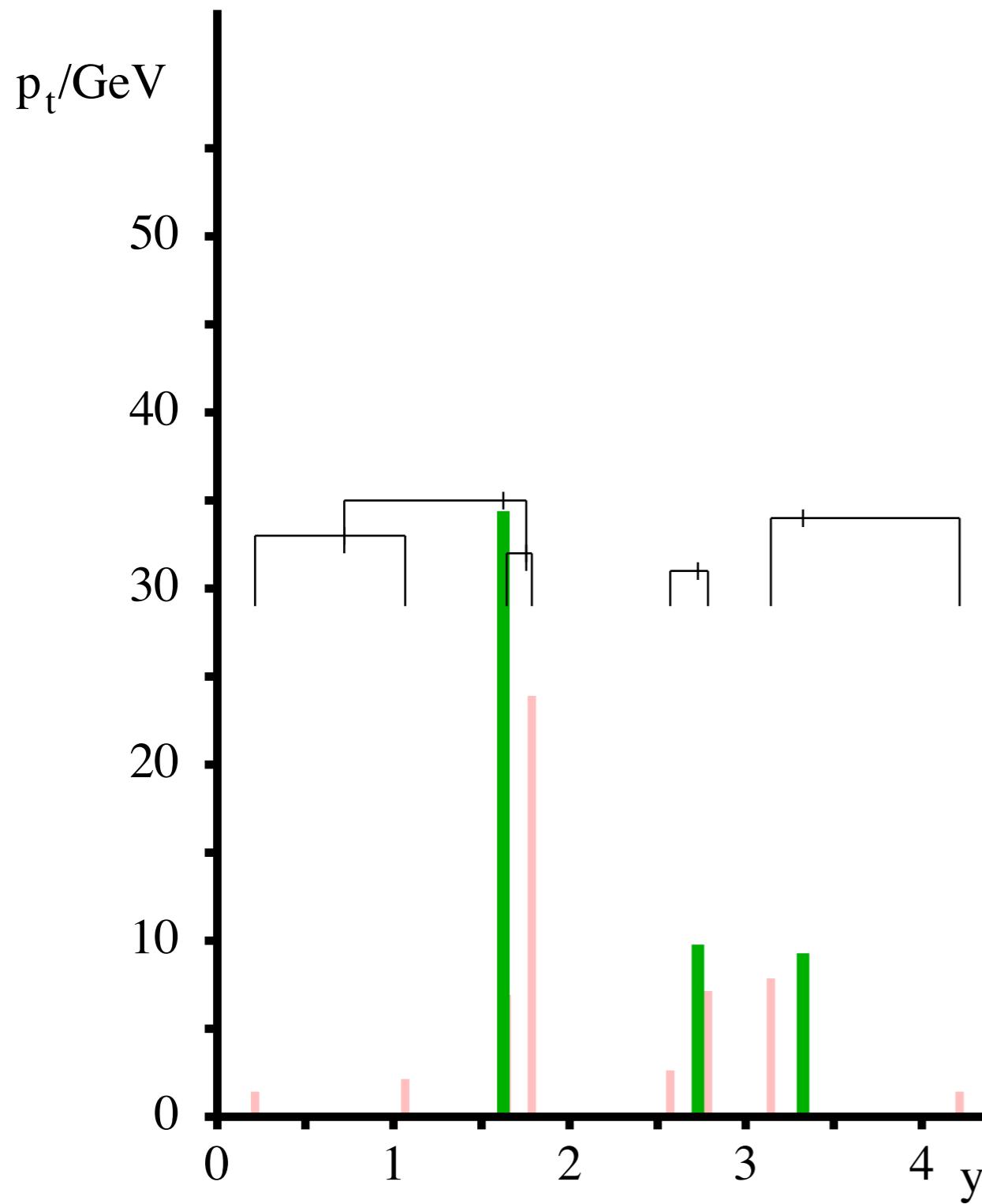
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

# Identifying jet substructure: try out $k_t$

## $k_t$ algorithm

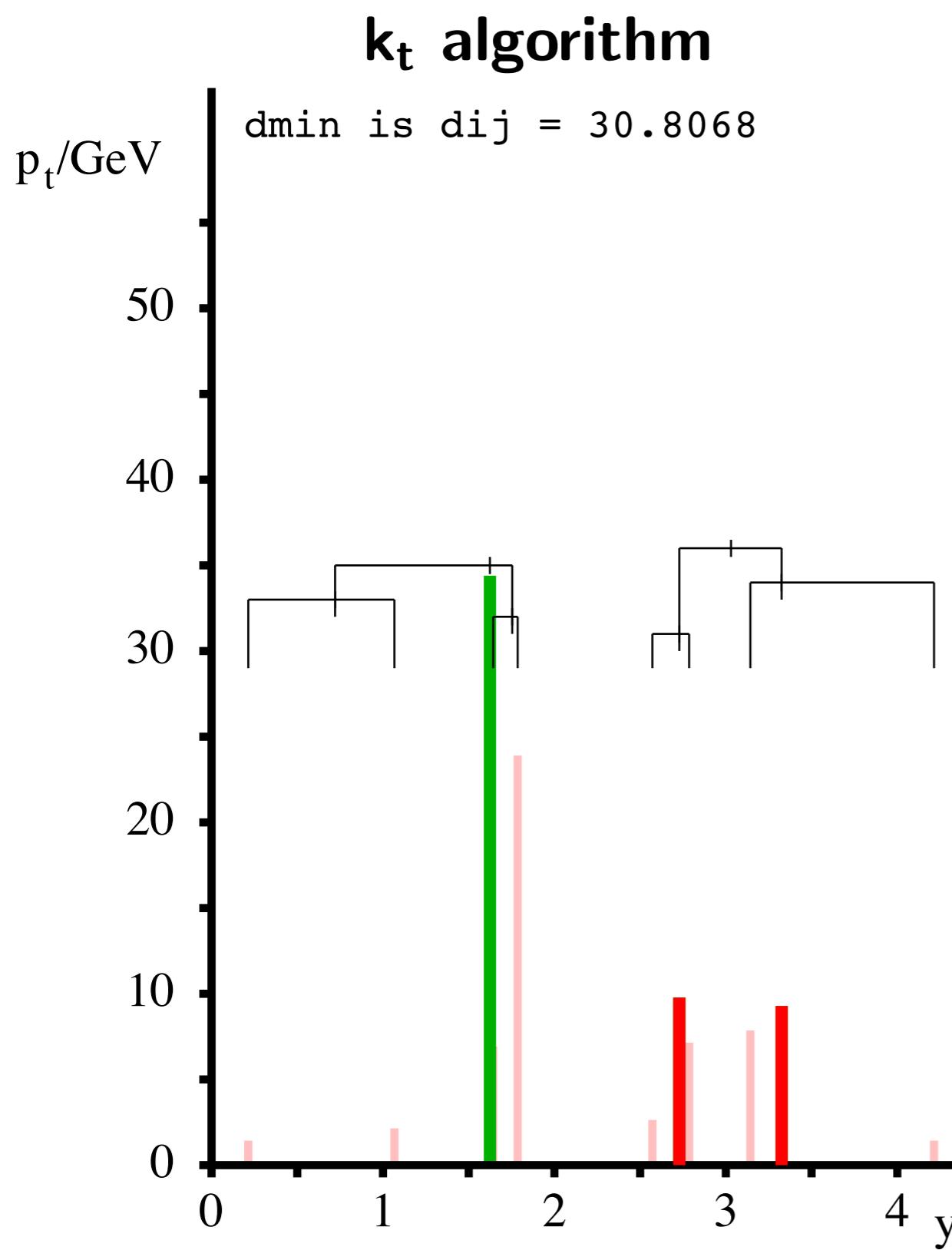


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

# Identifying jet substructure: try out $k_t$



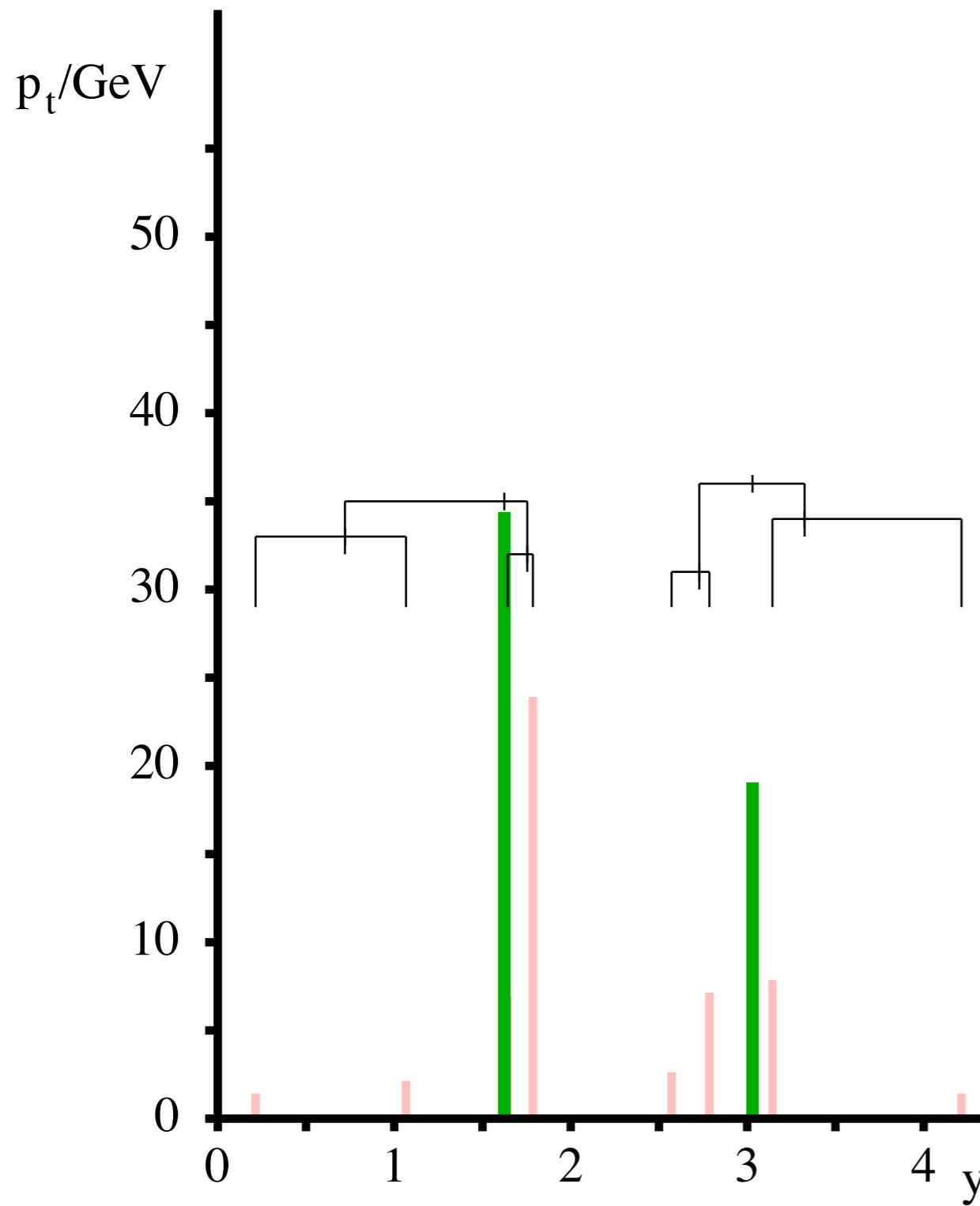
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

$k_t$  clusters soft “junk” early on in the clustering

# Identifying jet substructure: try out $k_t$

## $k_t$ algorithm

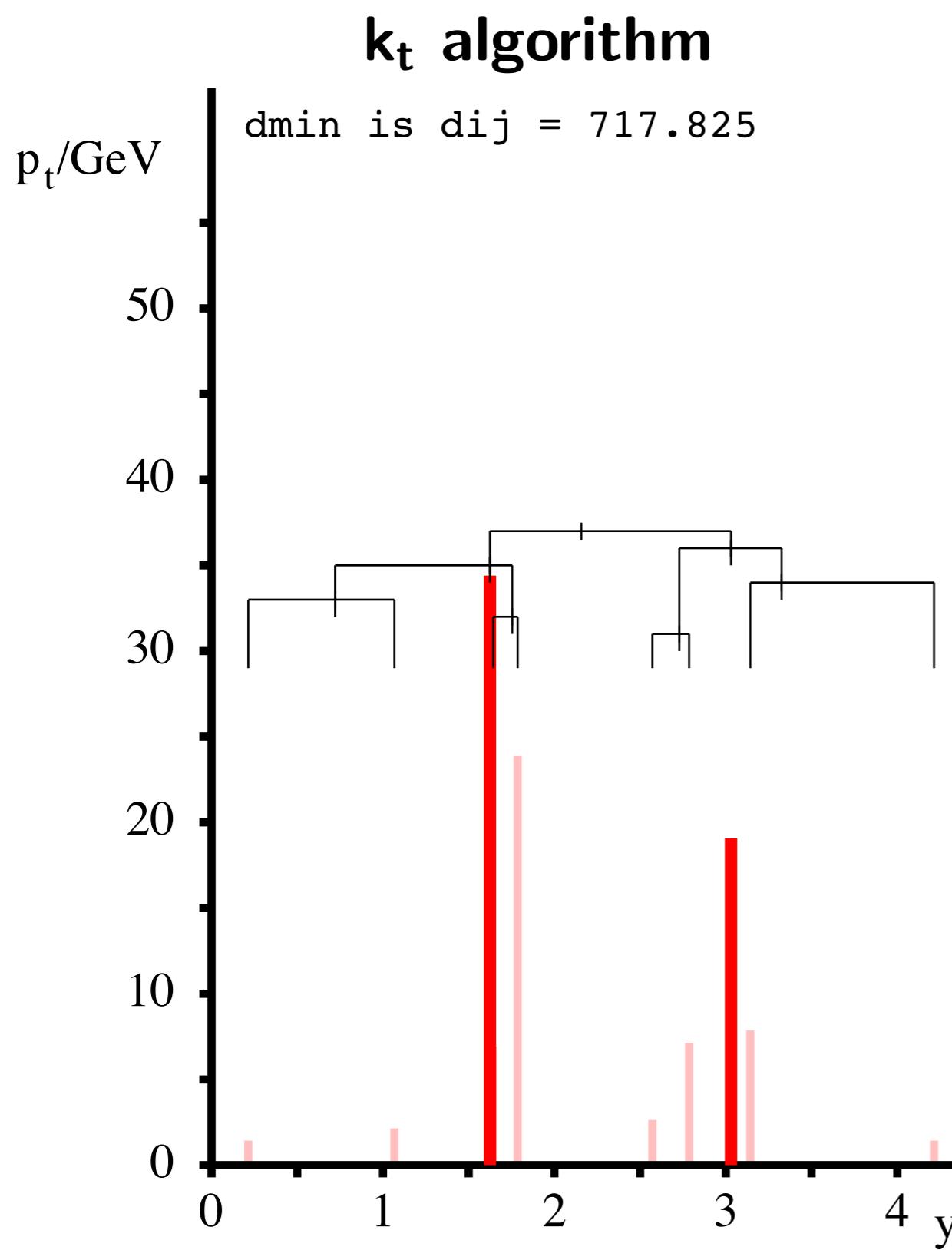


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

# Identifying jet substructure: try out $k_t$



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

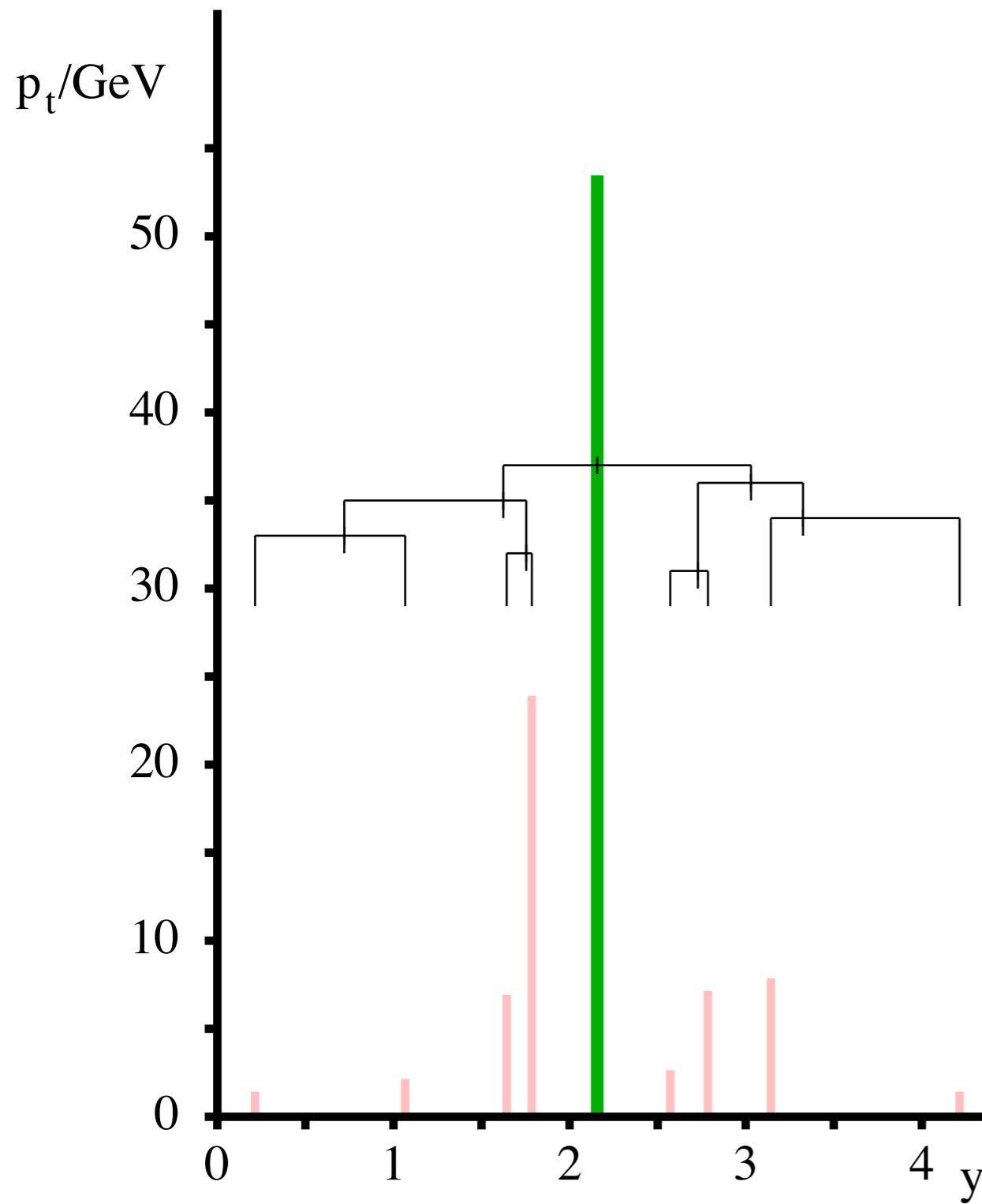
This is crucial for identifying the kinematic variables of the partons in the jet (e.g. z).

$k_t$  clusters soft “junk” early on in the clustering

*Its last step is to merge two hard pieces. Easily undone to identify underlying kinematics*

# Identifying jet substructure: try out $k_t$

## $k_t$ algorithm



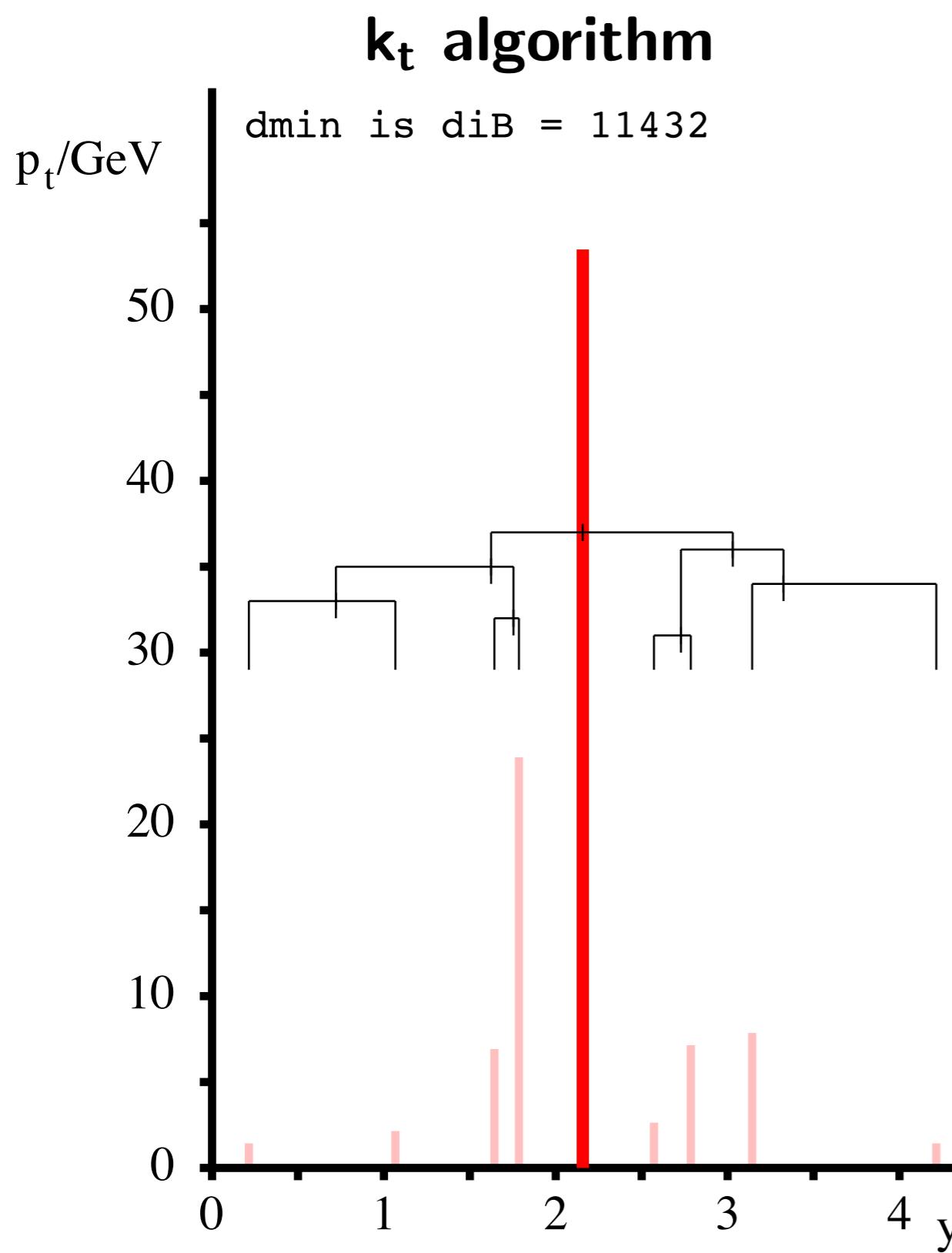
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

*Its last step is to merge two hard pieces. Easily undone to identify underlying kinematics*

# Identifying jet substructure: try out $k_t$



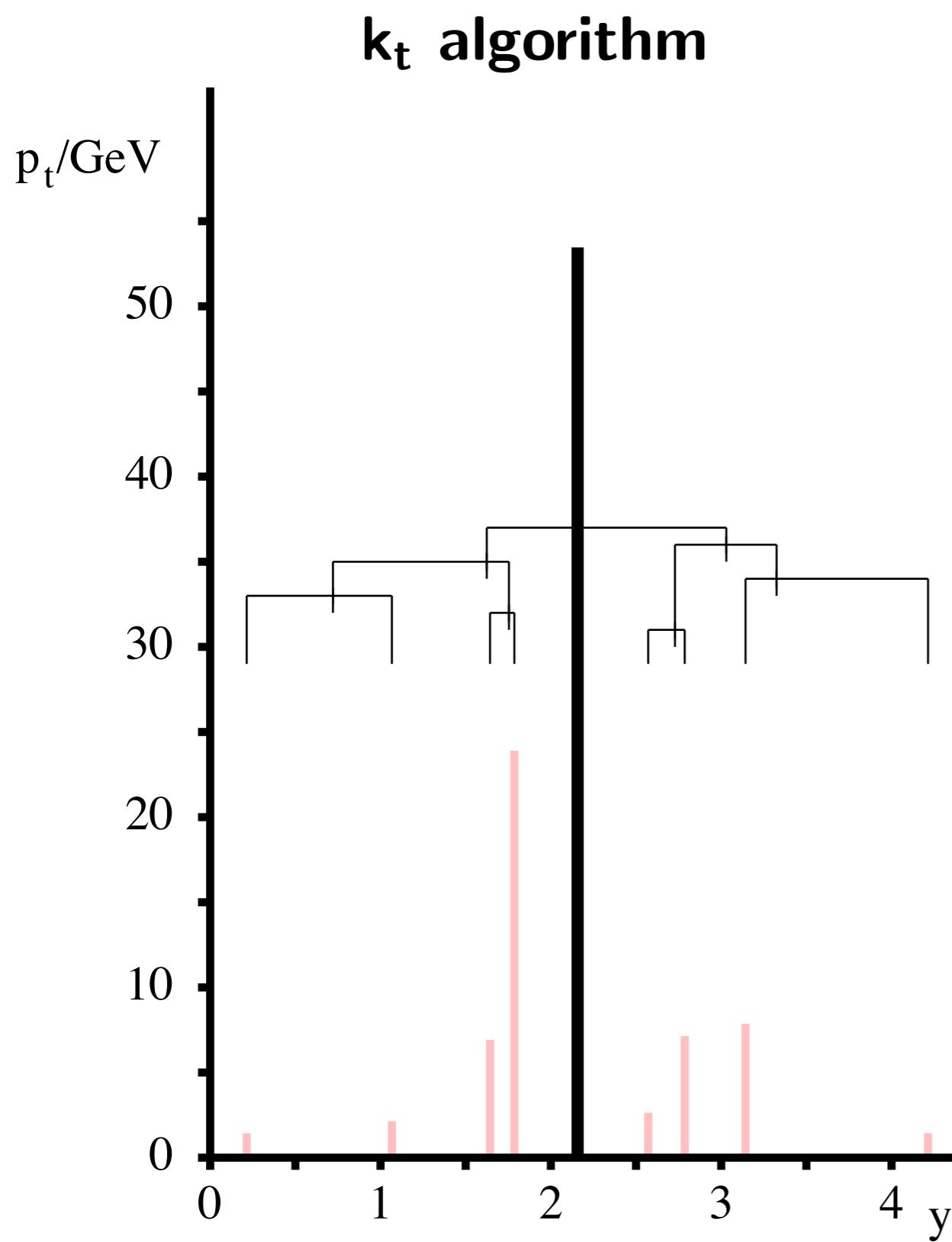
How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

*Its last step is to merge two hard pieces. Easily undone to identify underlying kinematics*

# Identifying jet substructure: try out $k_t$



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

This is crucial for identifying the kinematic variables of the partons in the jet (e.g.  $z$ ).

$k_t$  clusters soft “junk” early on in the clustering

*Its last step is to merge two hard pieces. Easily undone to identify underlying kinematics*

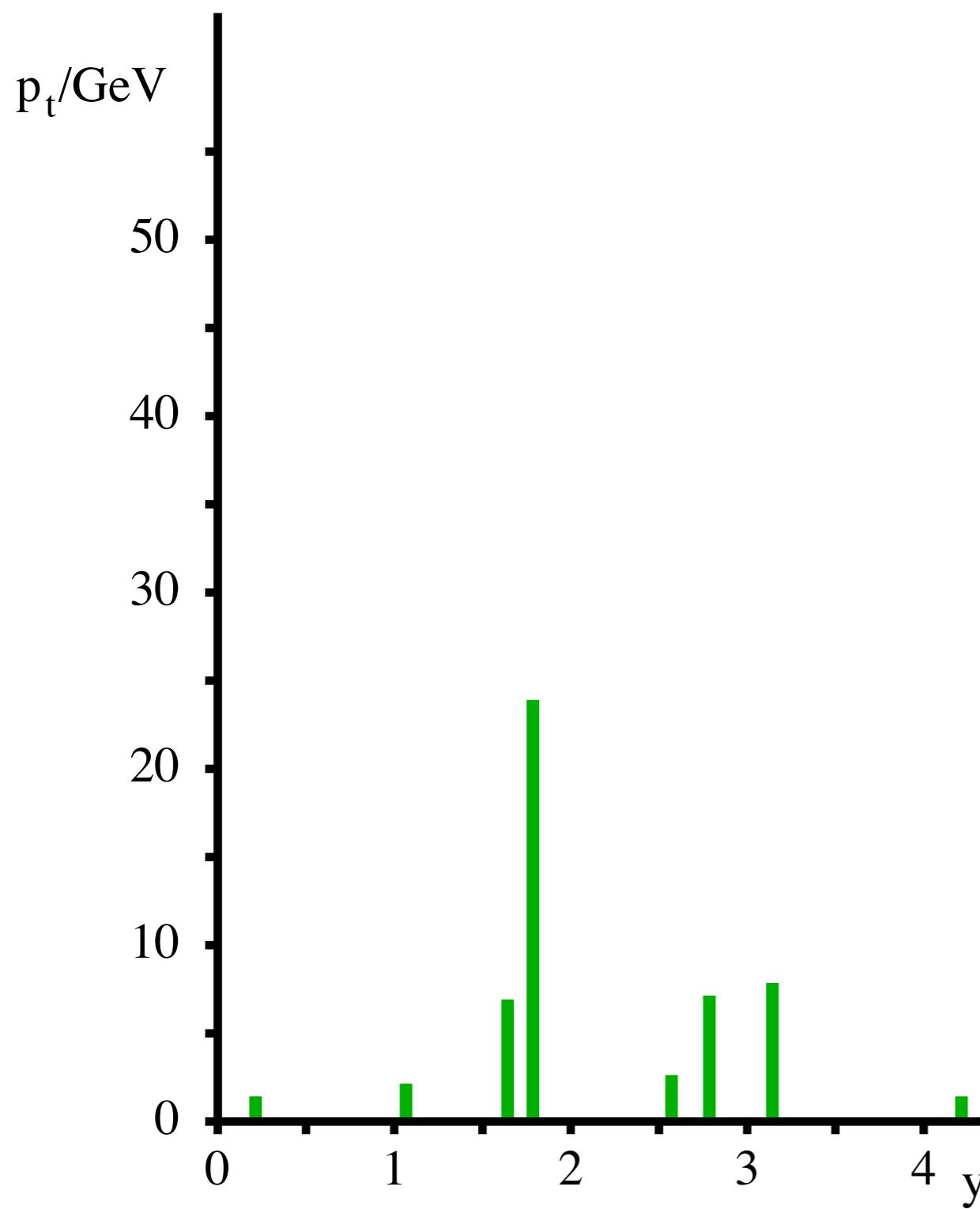
This meant it was the first algorithm to be used for jet substructure.

Seymour '93

Butterworth, Cox & Forshaw '02

# Identifying jet substructure: Cam/Aachen

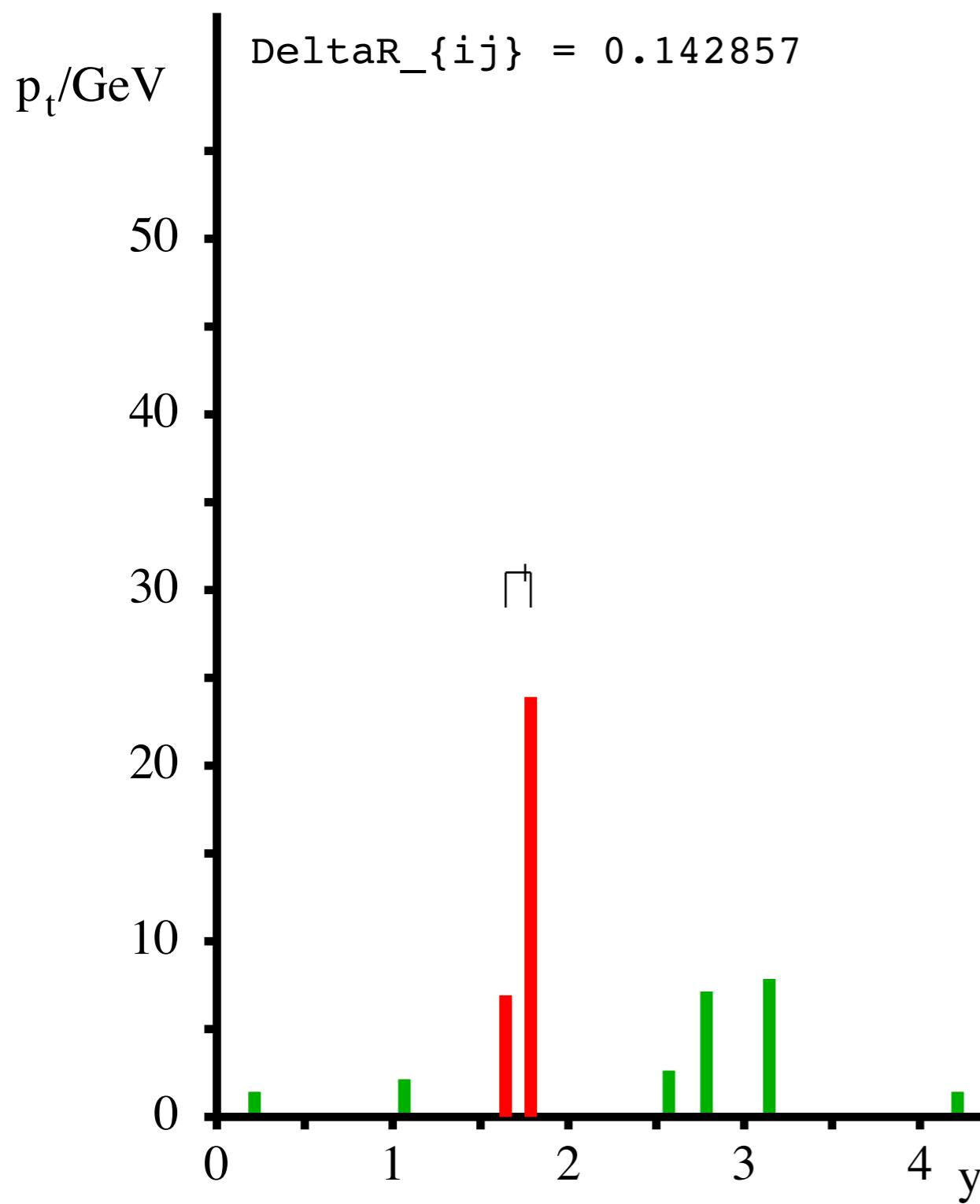
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

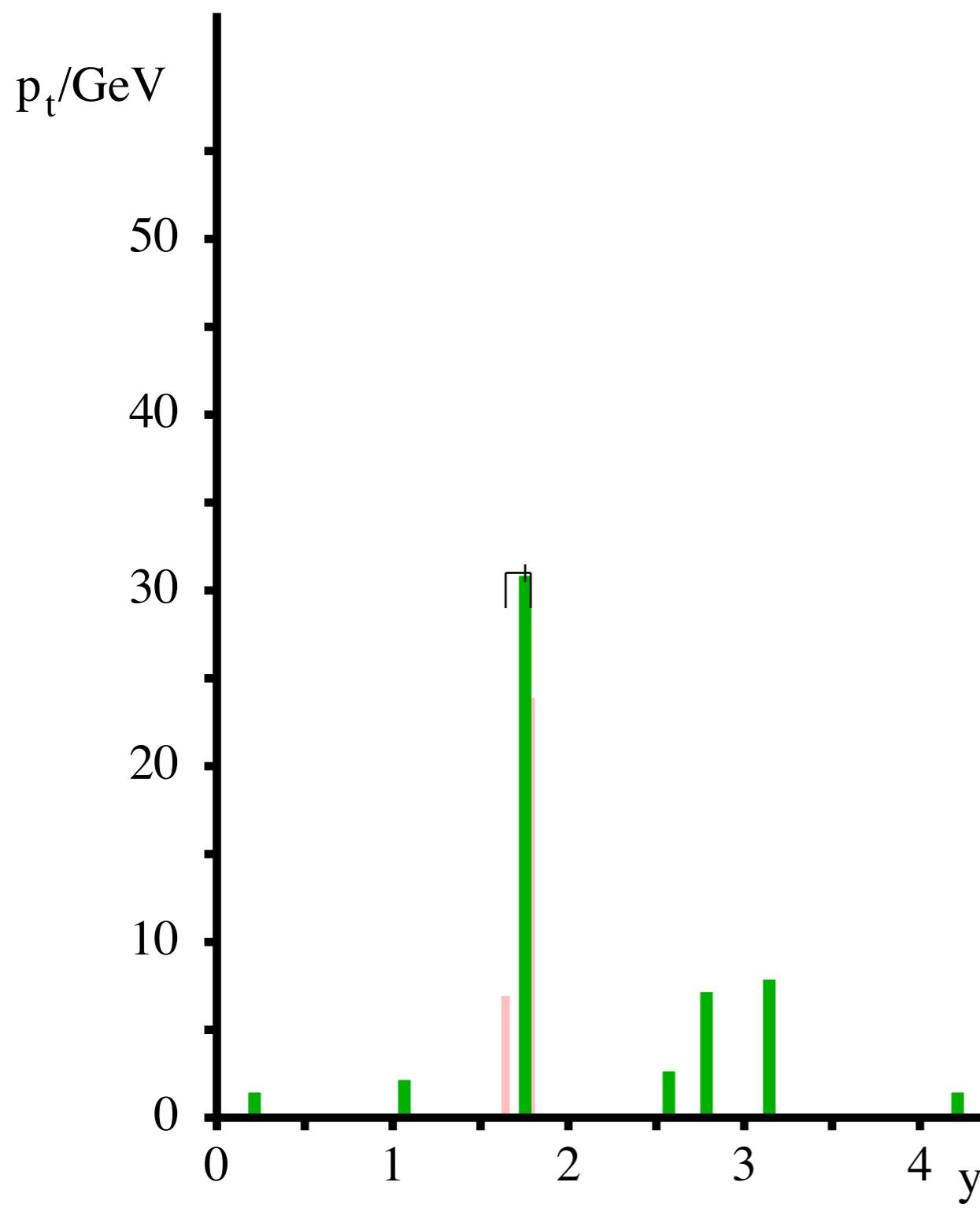
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

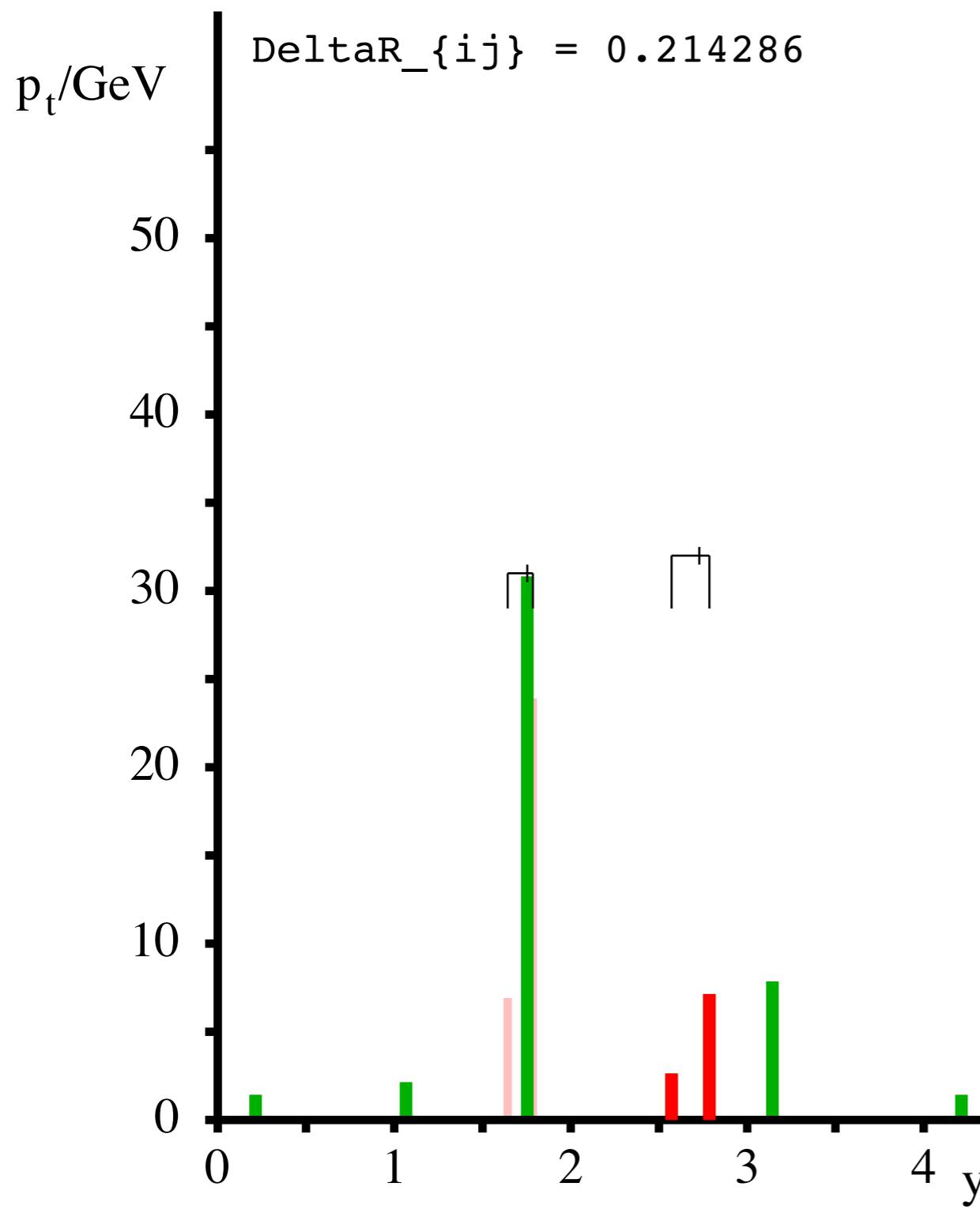
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

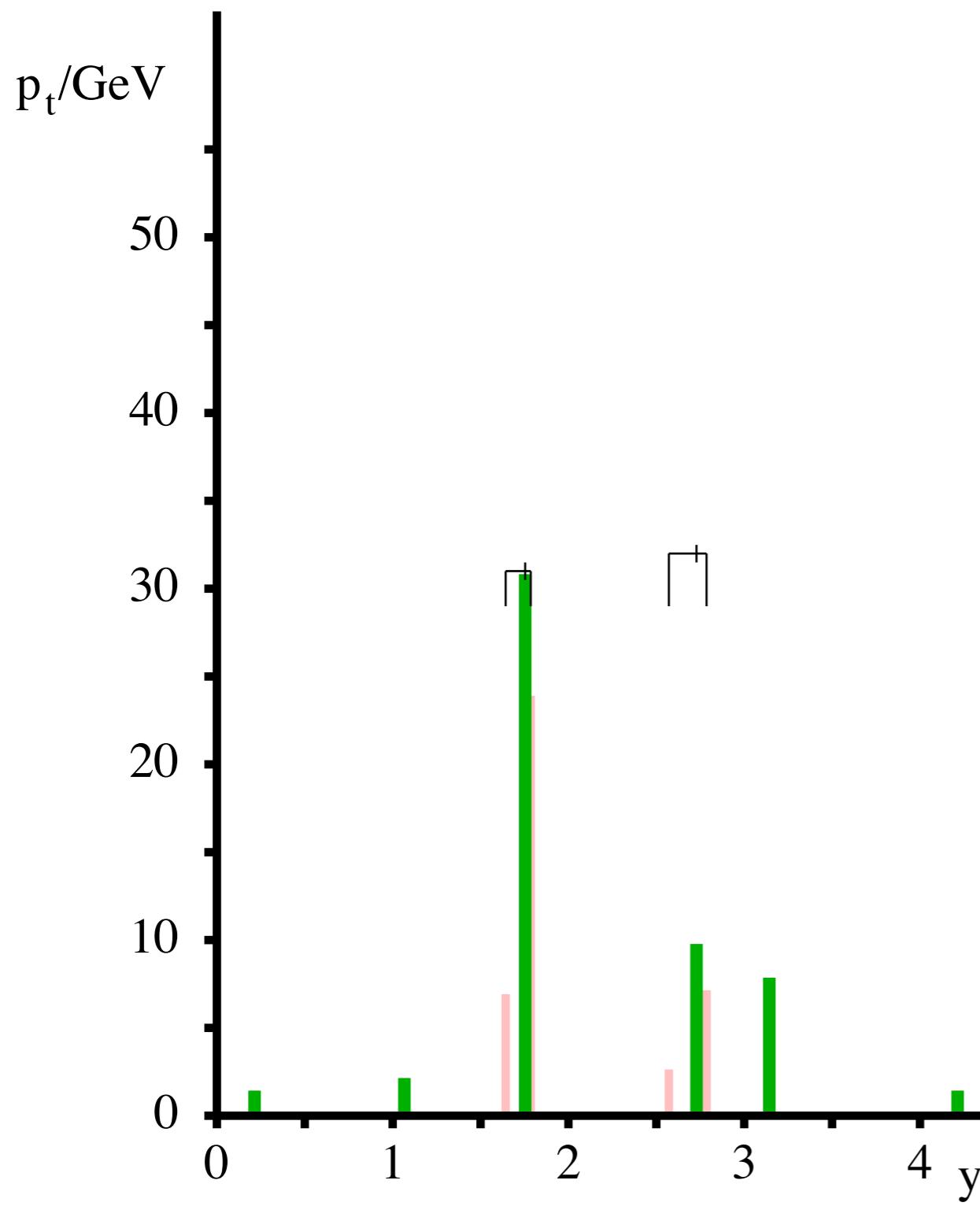
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

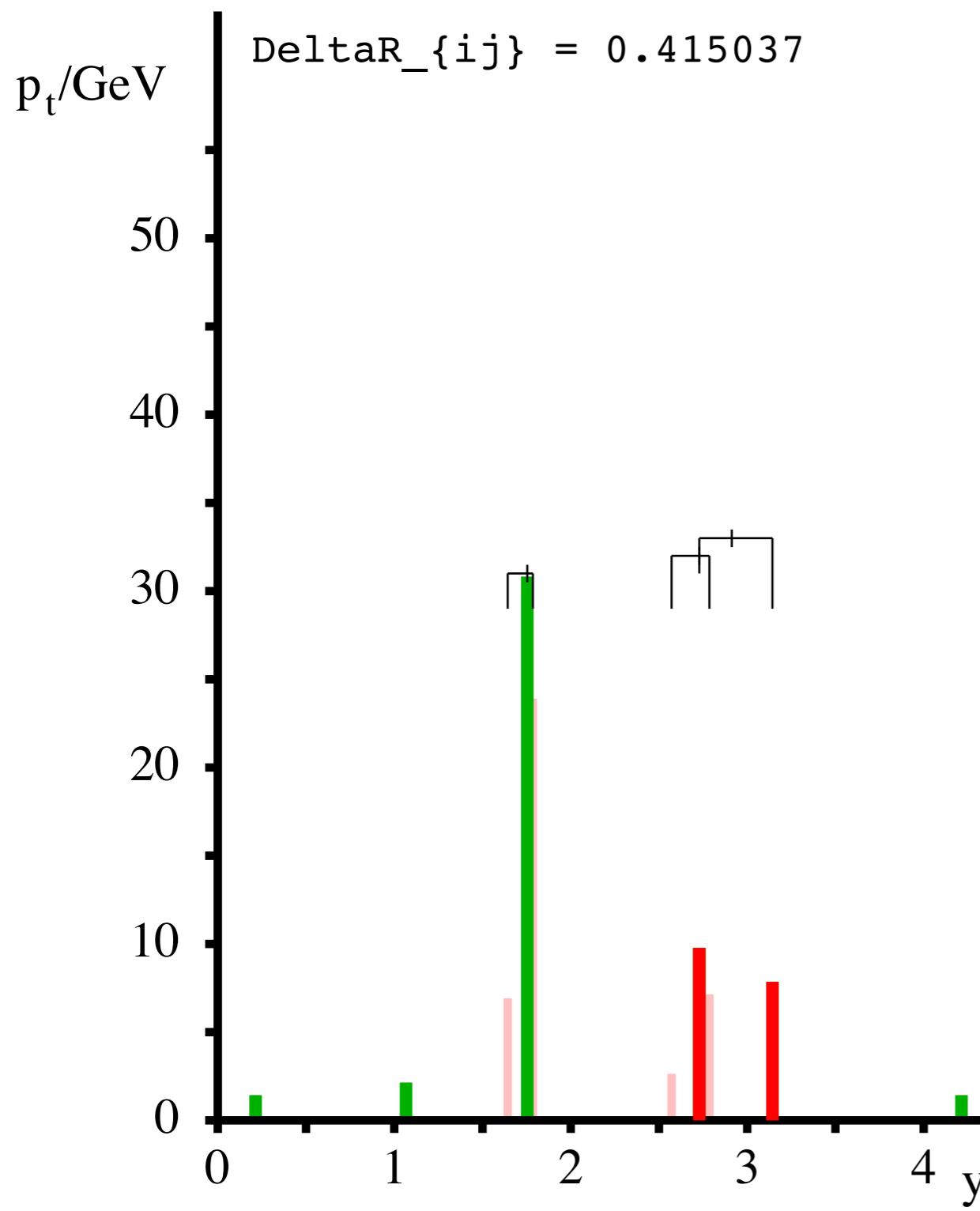
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

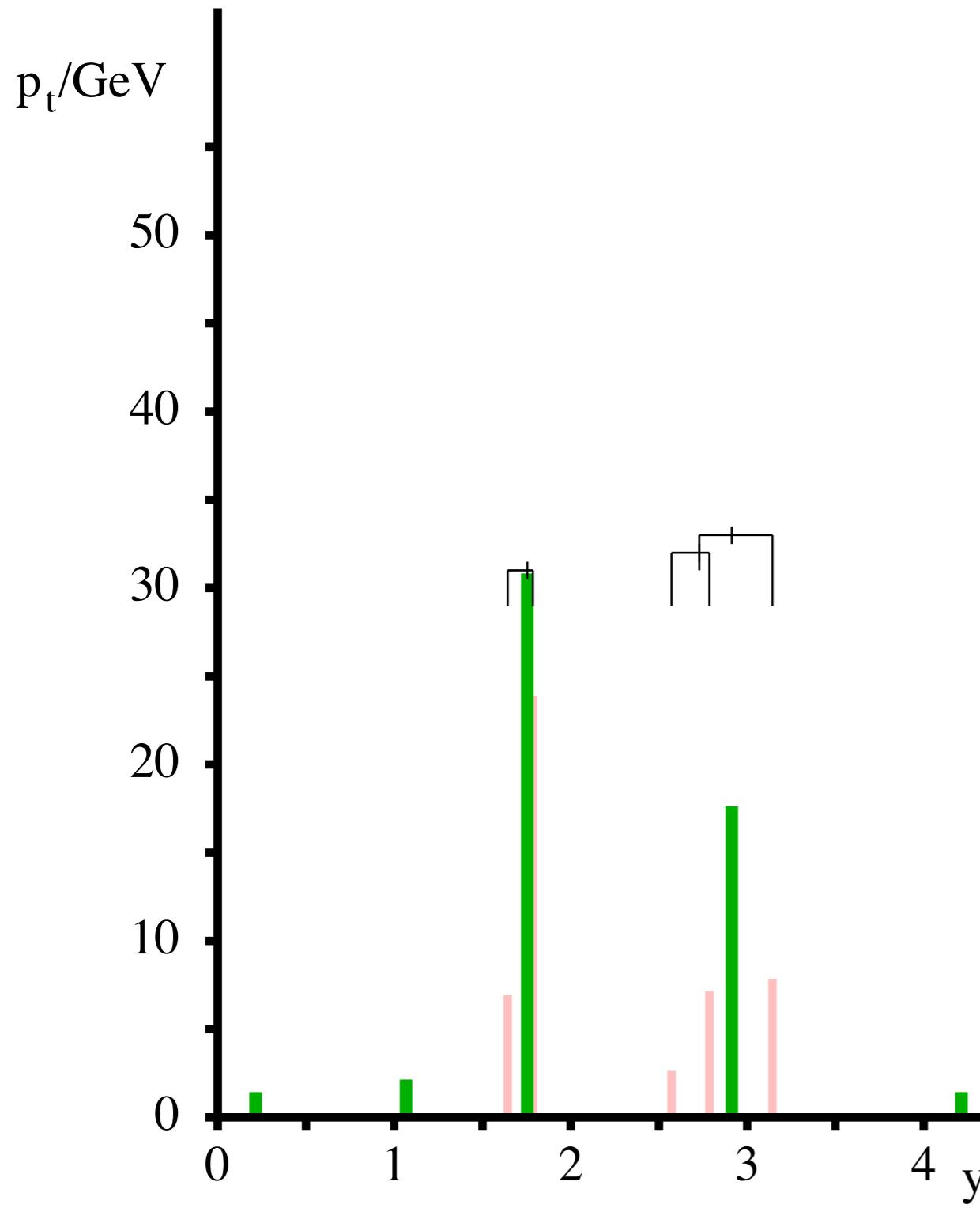
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

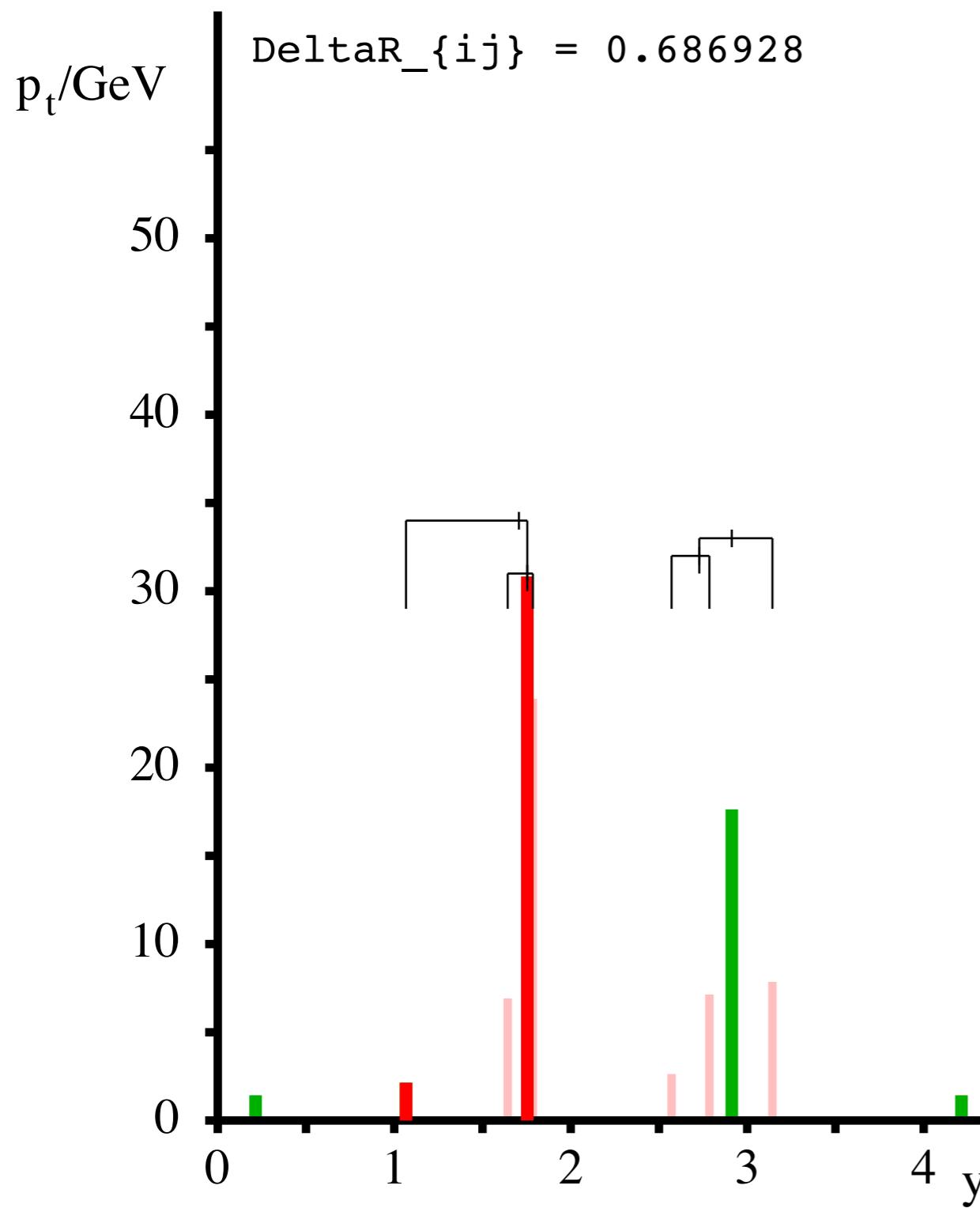
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

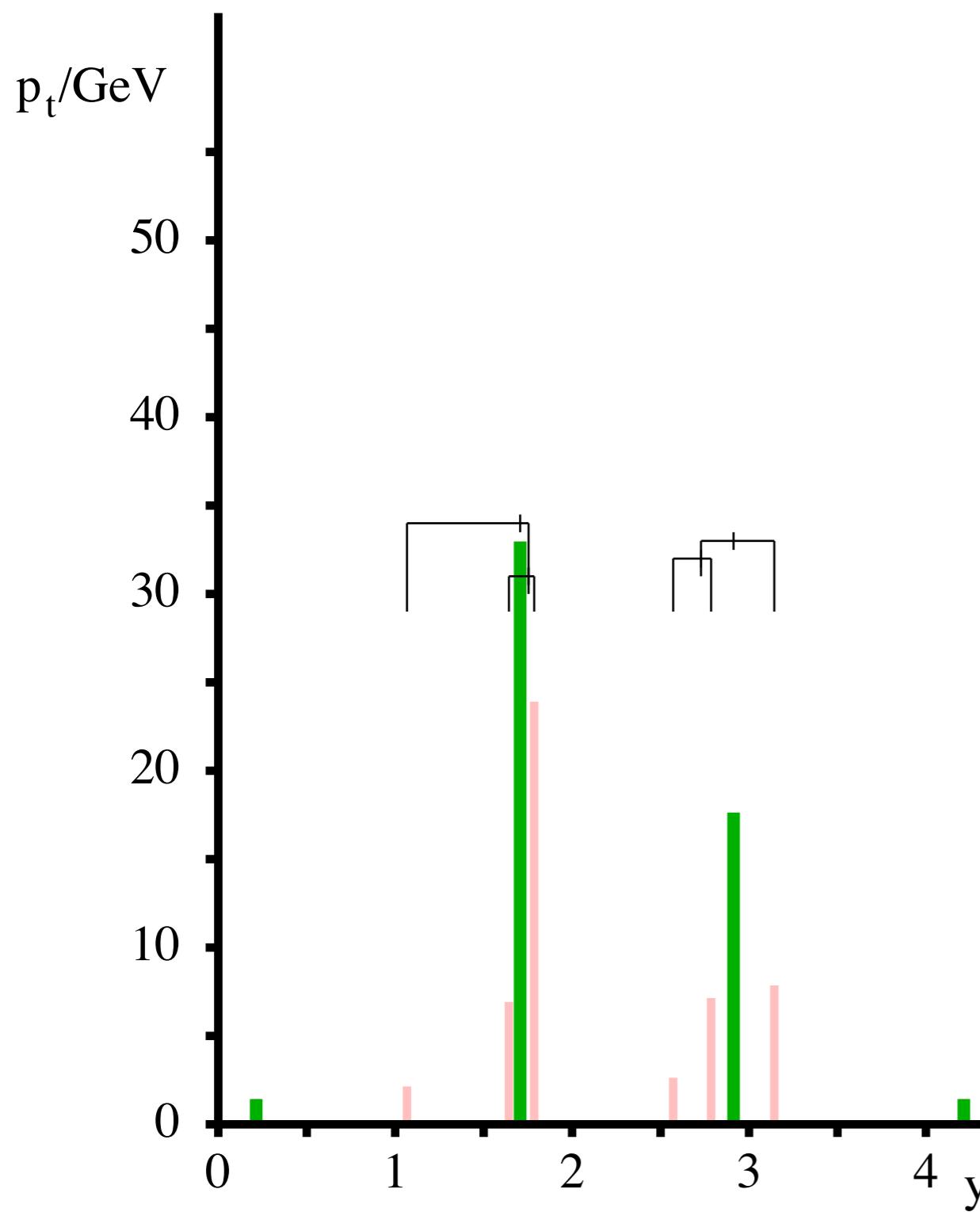
## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

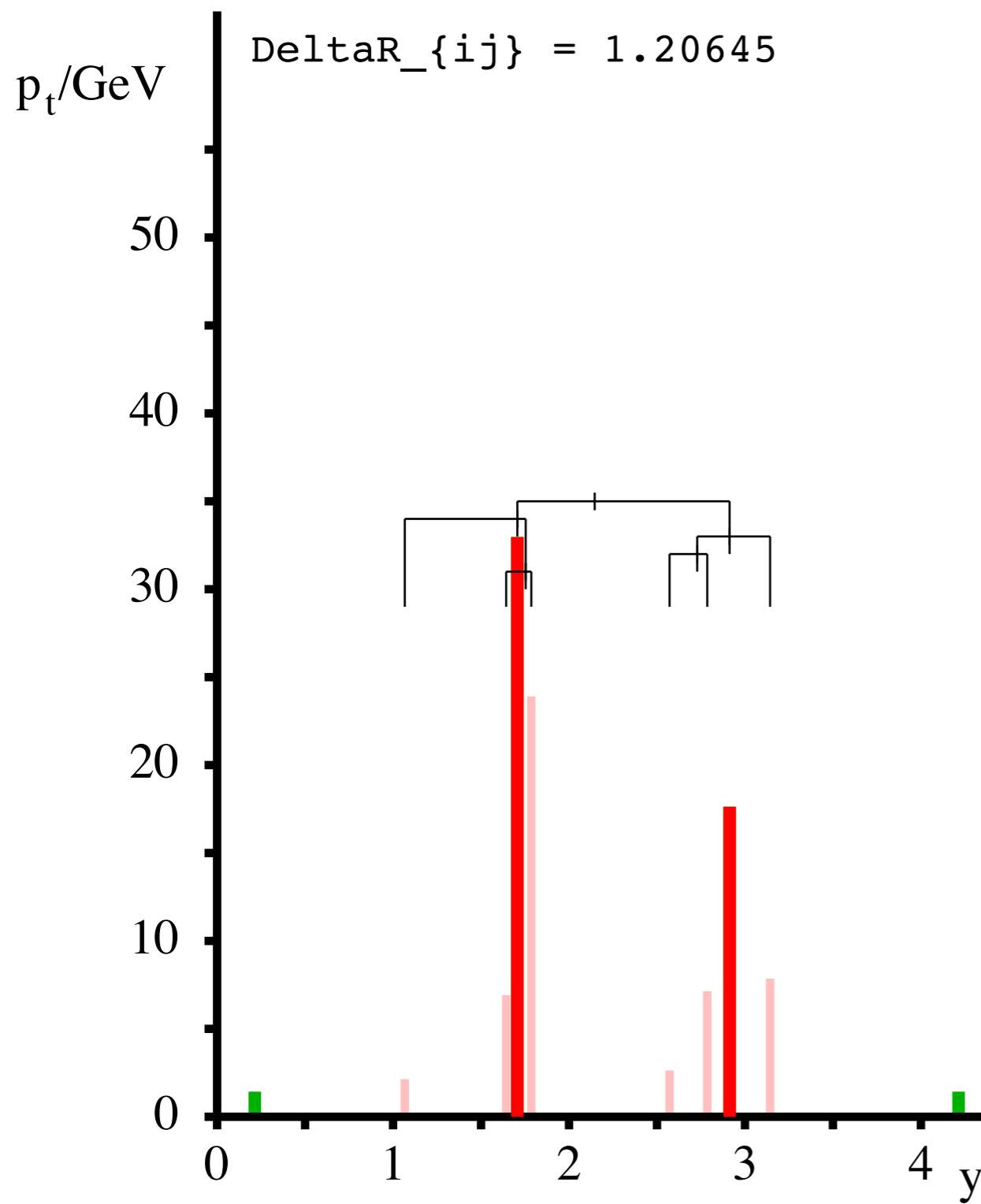


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

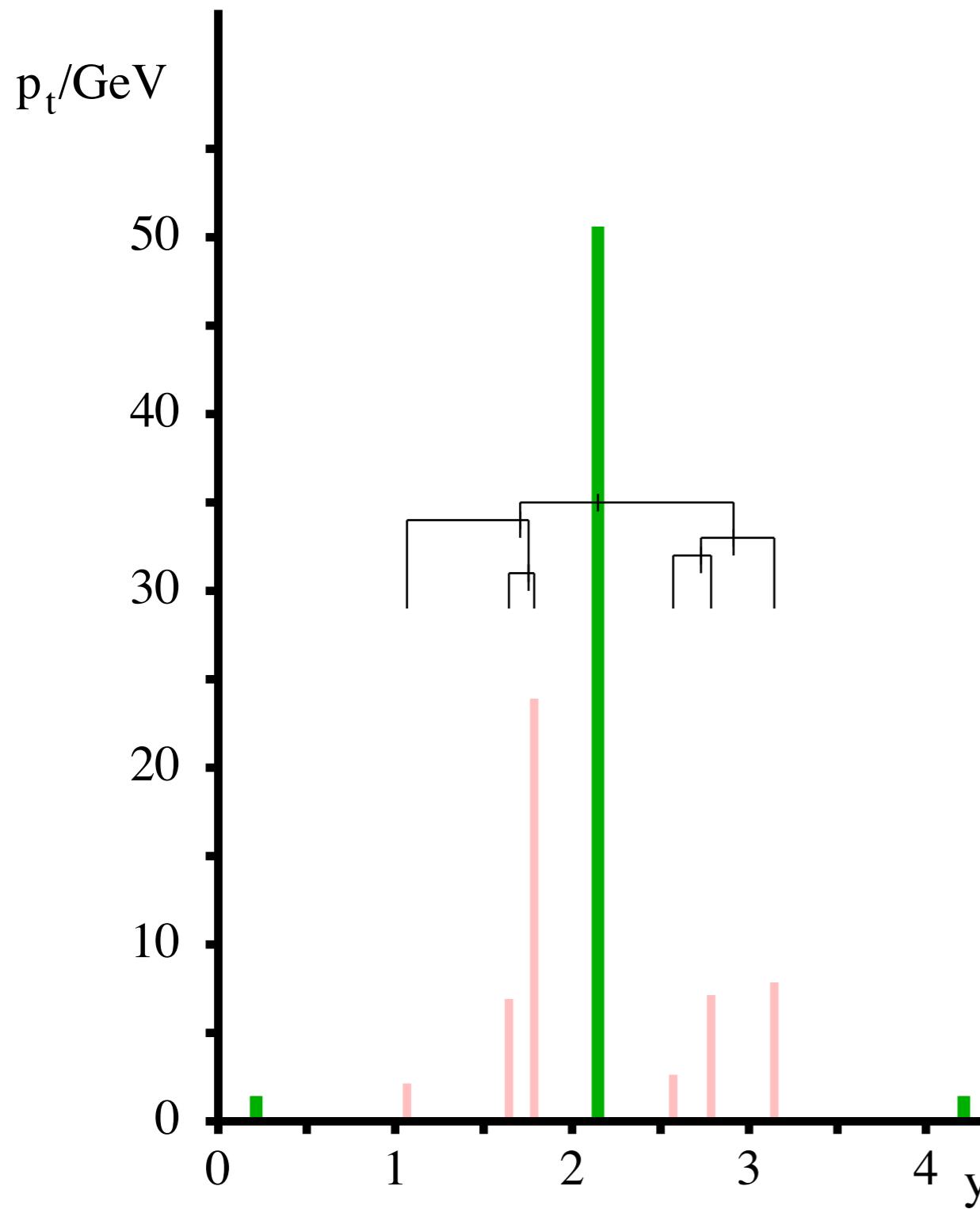


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, **joins them**

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

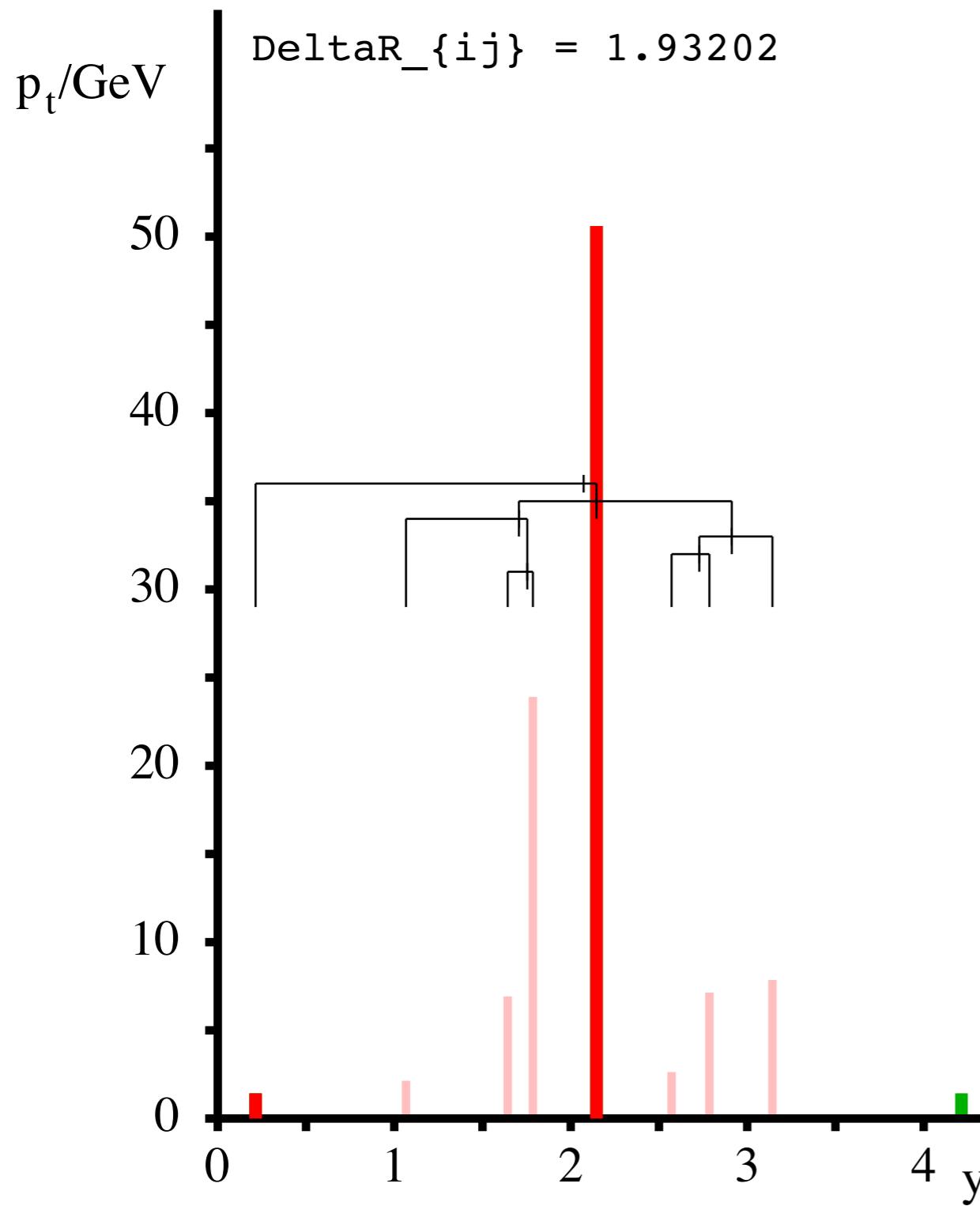


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

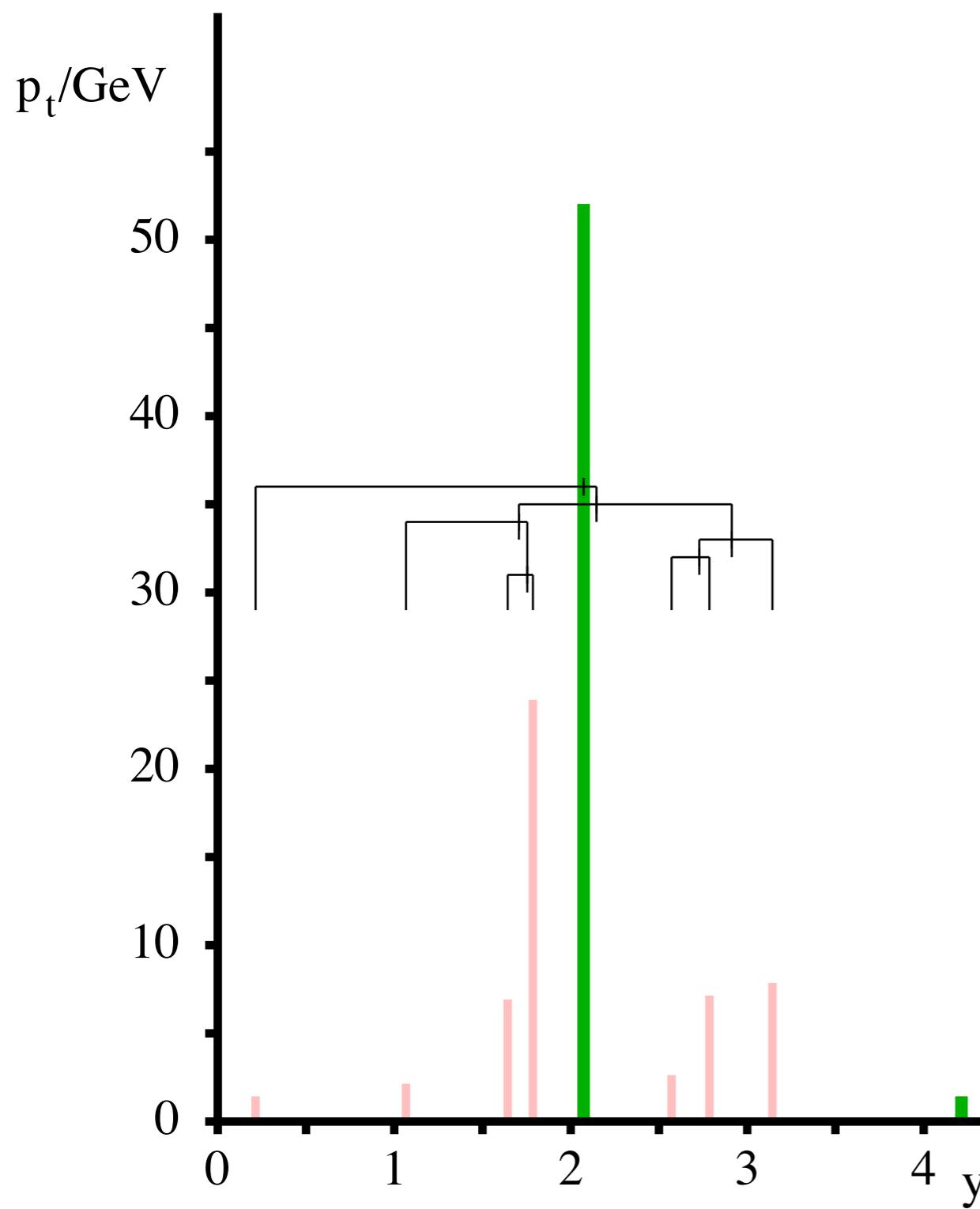


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

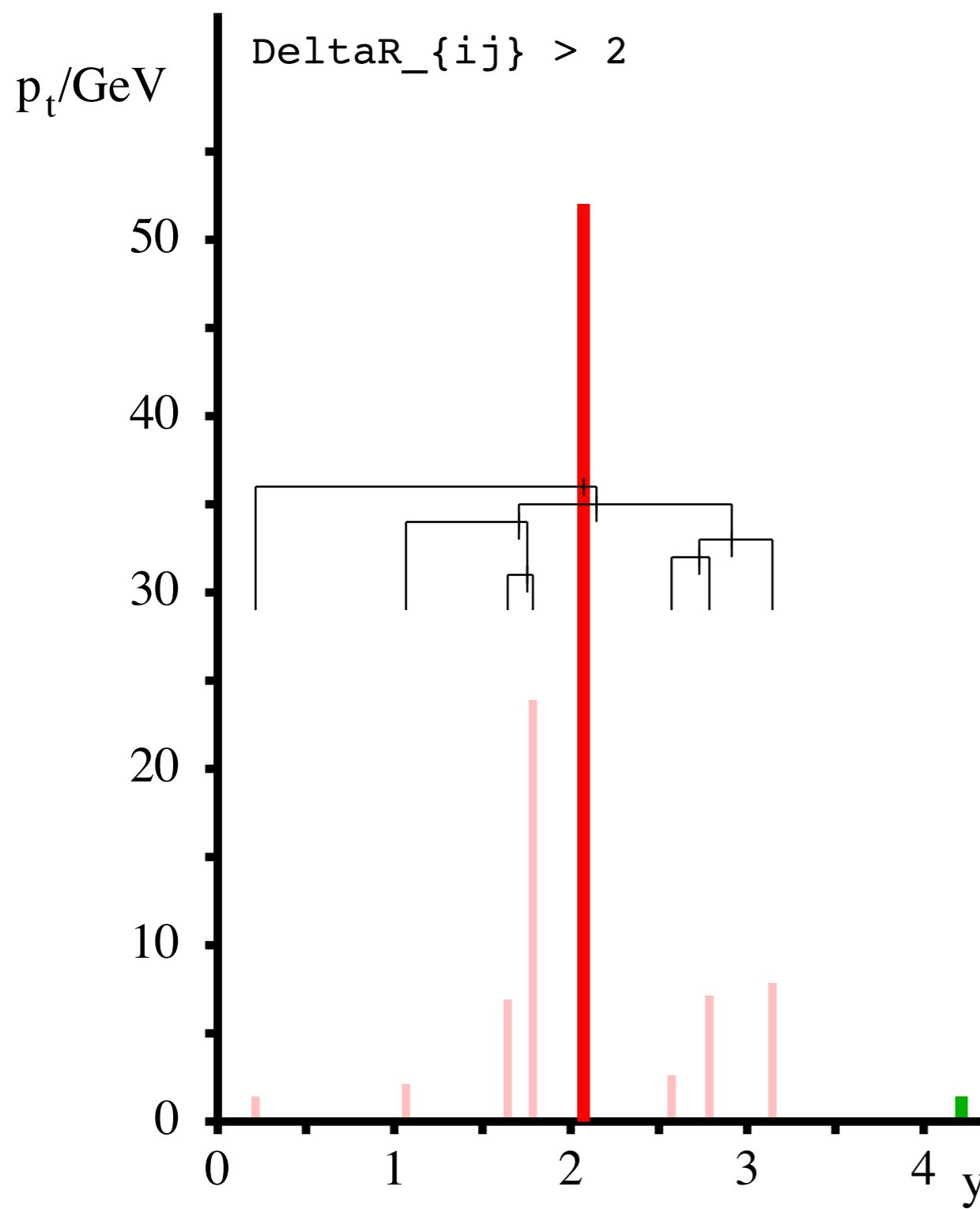


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

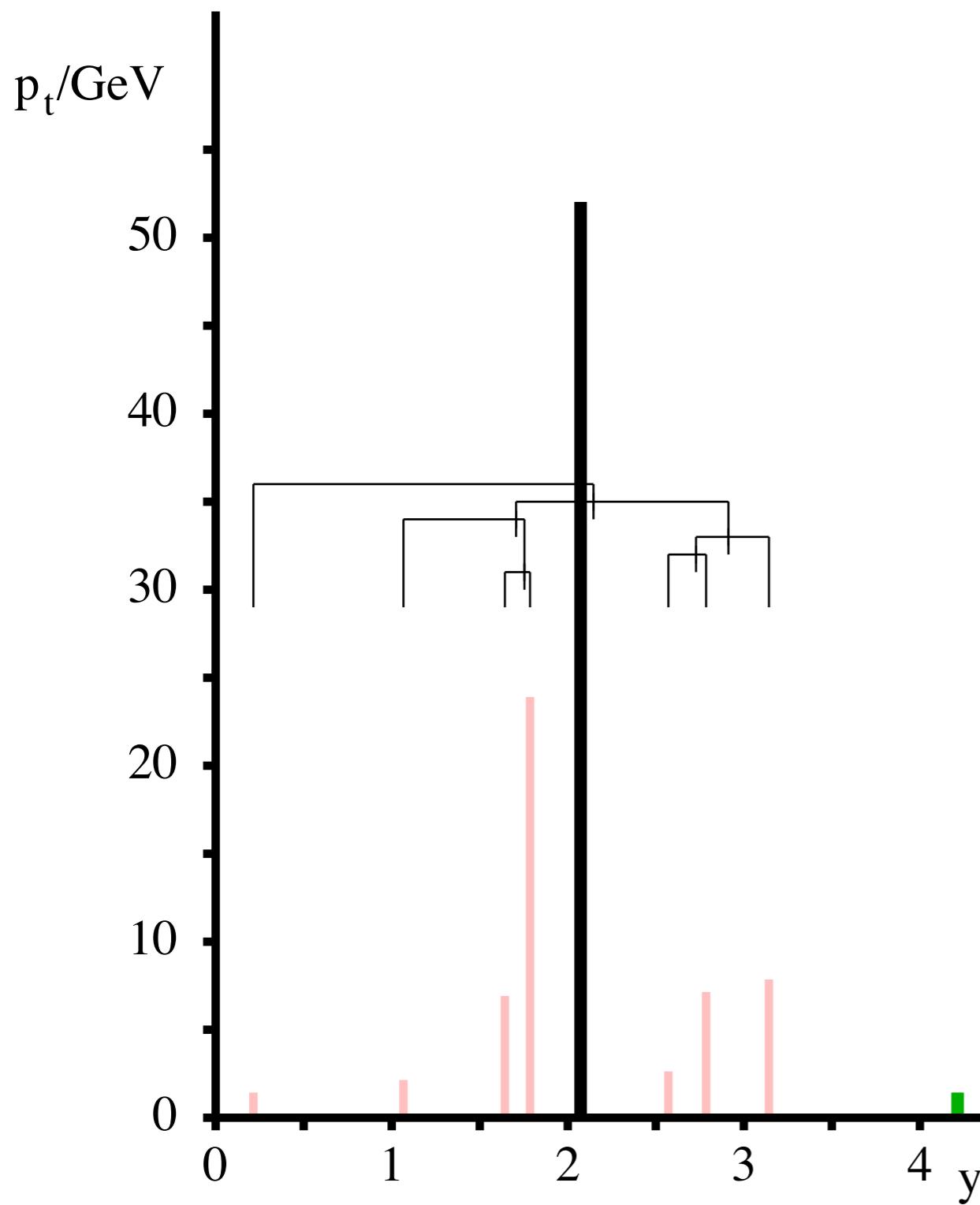


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

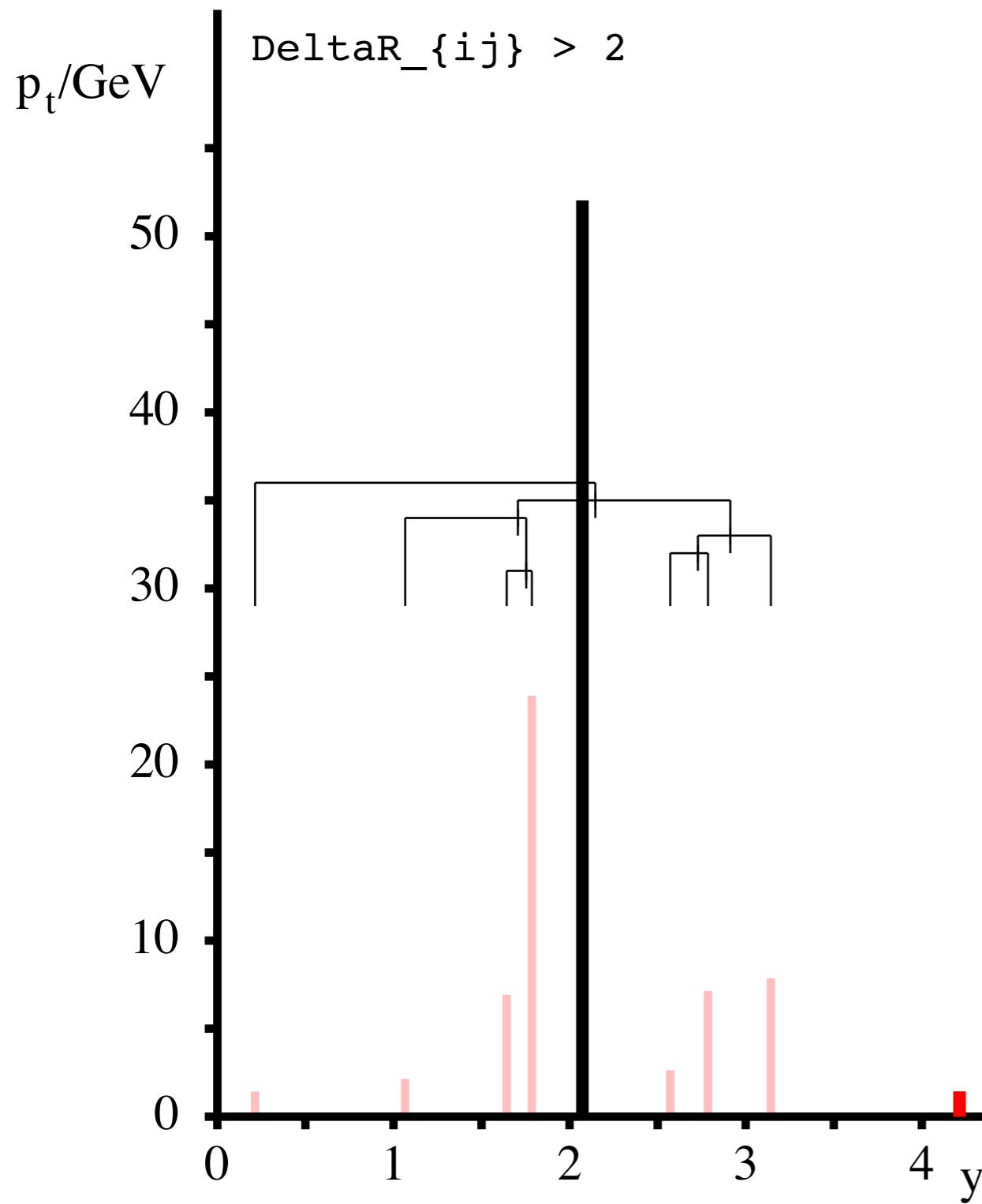


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm

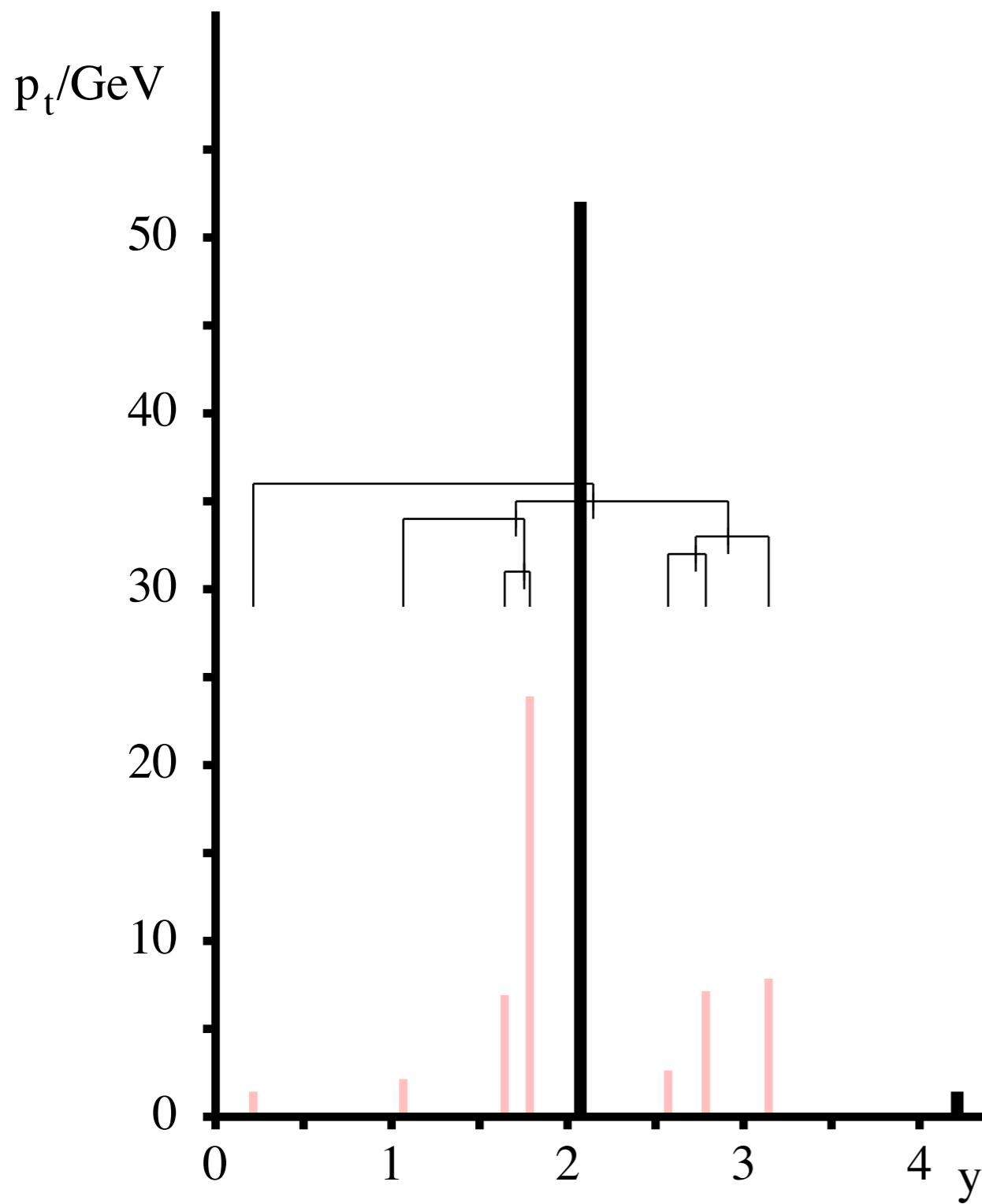


How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

# Identifying jet substructure: Cam/Aachen

## Cambridge/Aachen algorithm



How well can an algorithm identify the “blobs” of energy inside a jet that come from different partons?

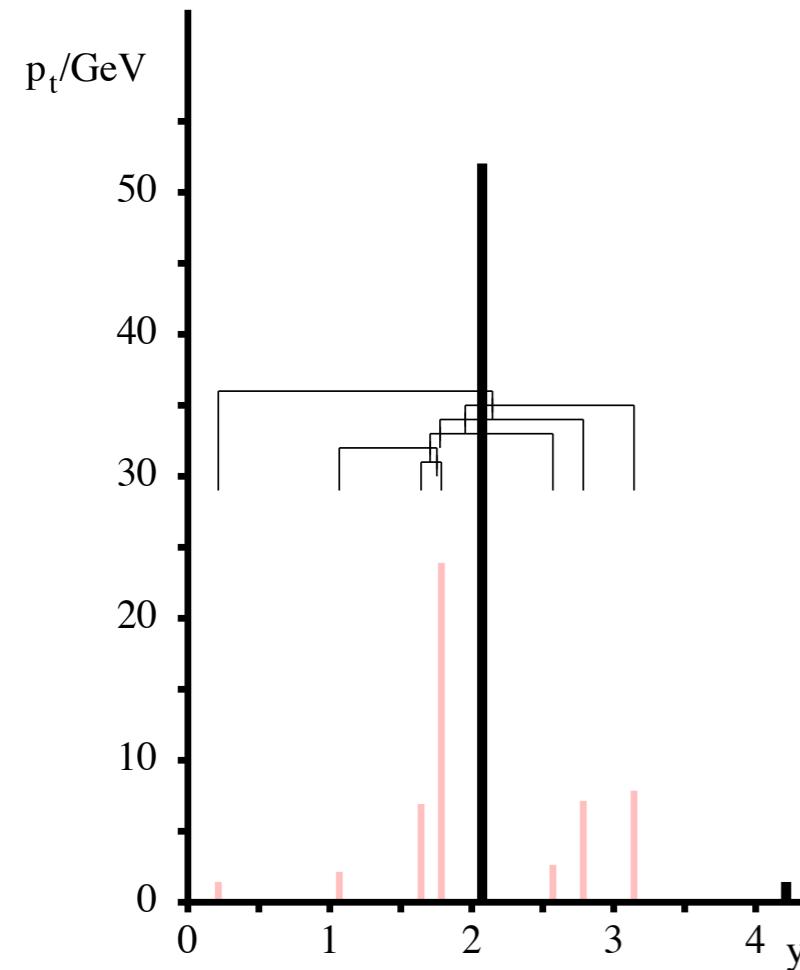
C/A identifies two hard blobs with limited soft contamination, joins them, and then adds in remaining soft junk

The interesting substructure is buried inside the clustering sequence — it's less contaminated by soft junk, but needs to be pulled out with special techniques

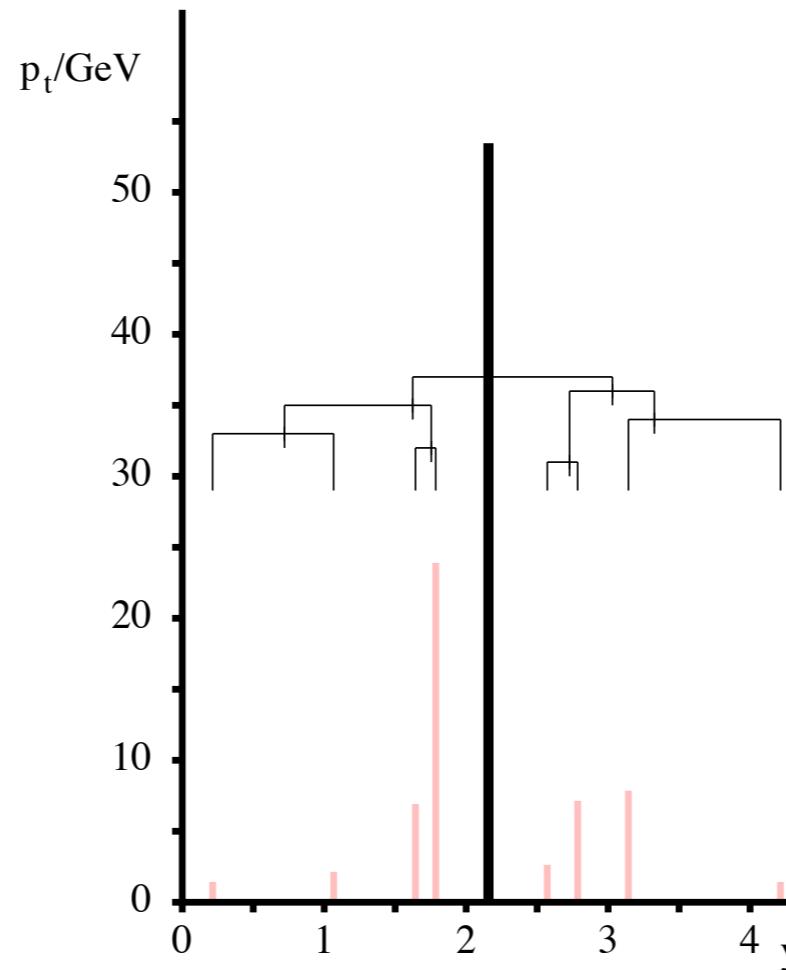
Butterworth, Davison, Rubin & GPS '08  
Kaplan, Schwartz, Reherman & Tweedie '08

Butterworth, Ellis, Rubin & GPS '09  
Ellis, Vermilion & Walsh '09

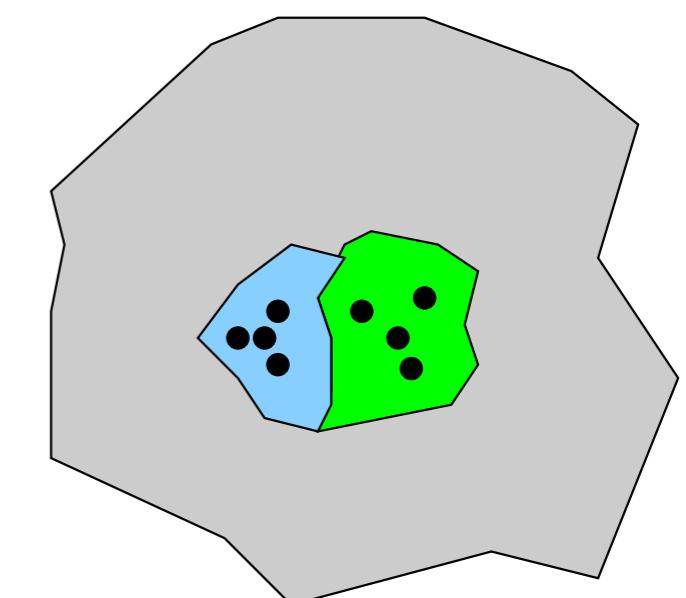
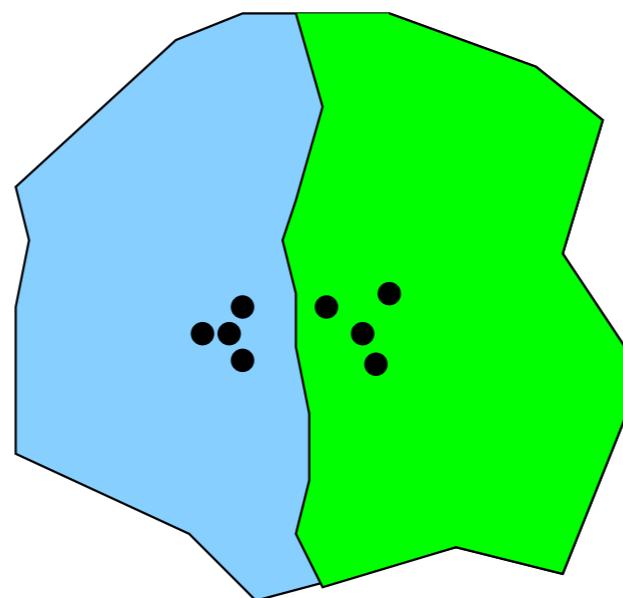
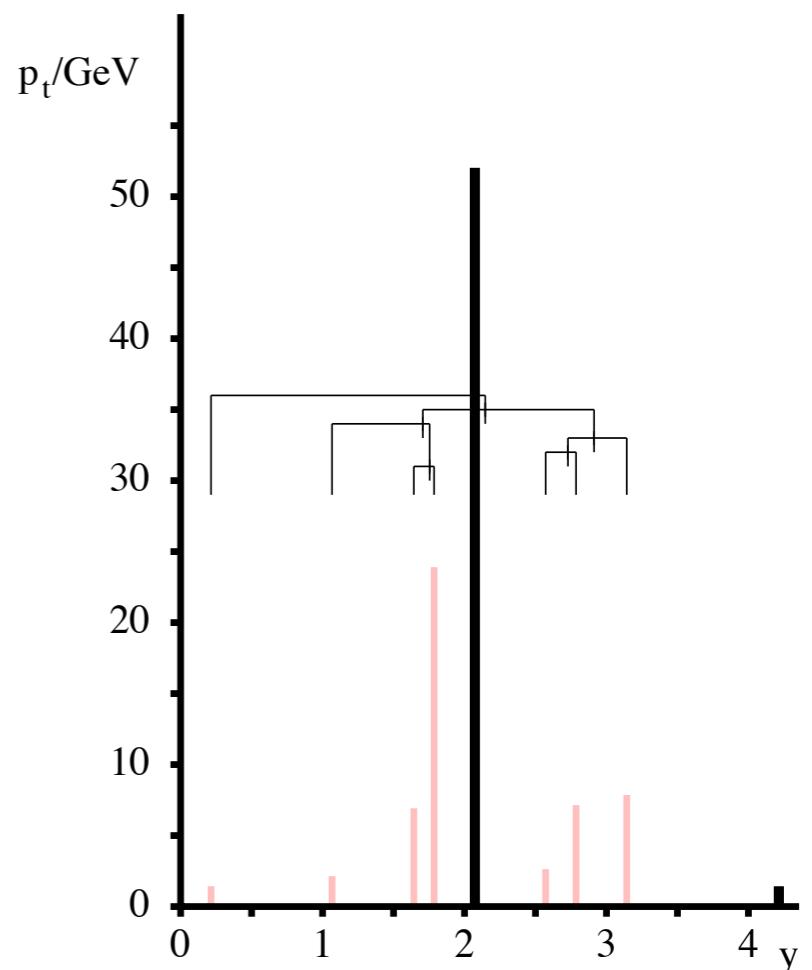
## anti- $k_t$ algorithm



## $k_t$ algorithm



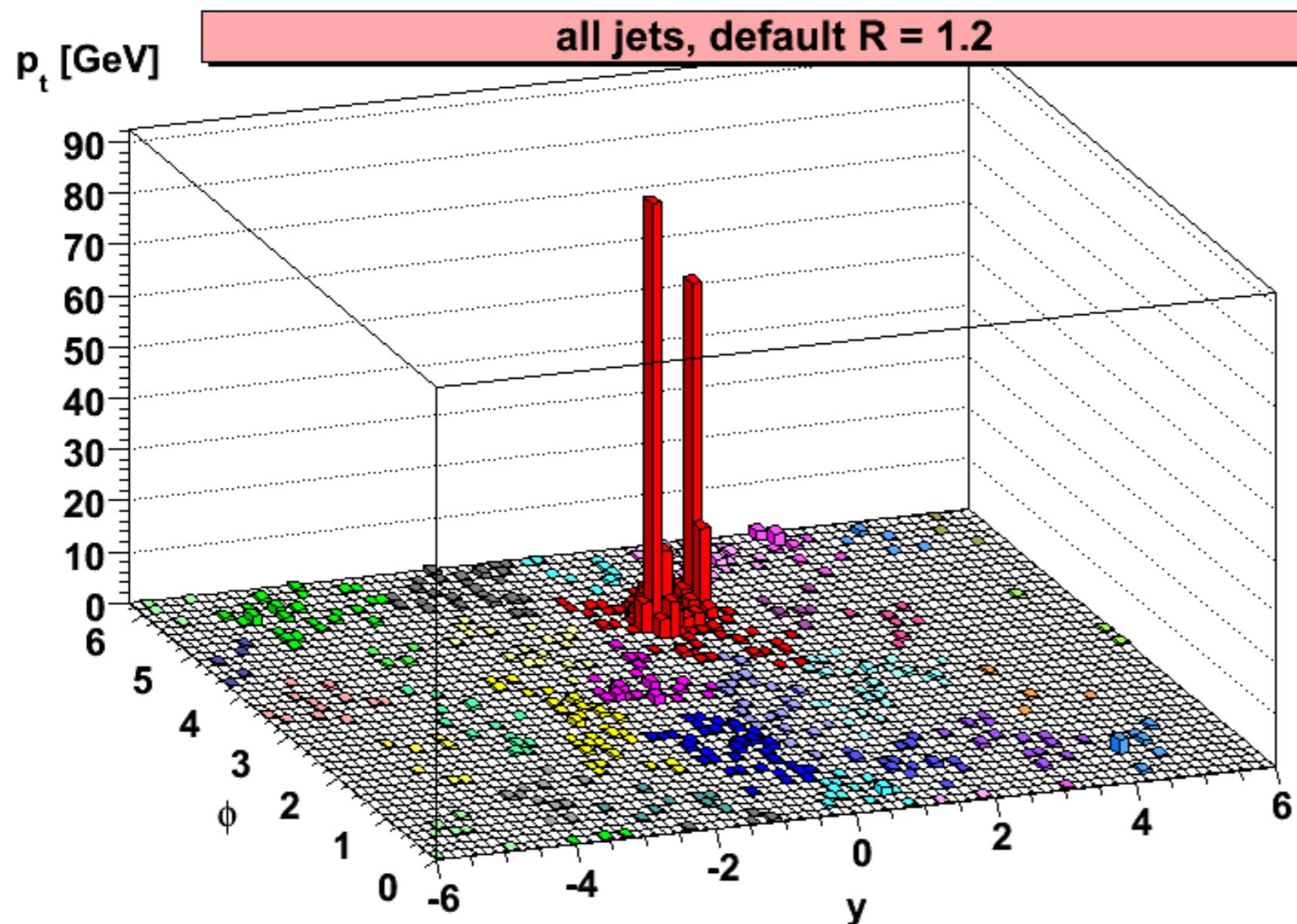
## Cambridge/Aachen



$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

SIGNAL



Zbb BACKGROUND

Cluster event, C/A, R=1.2

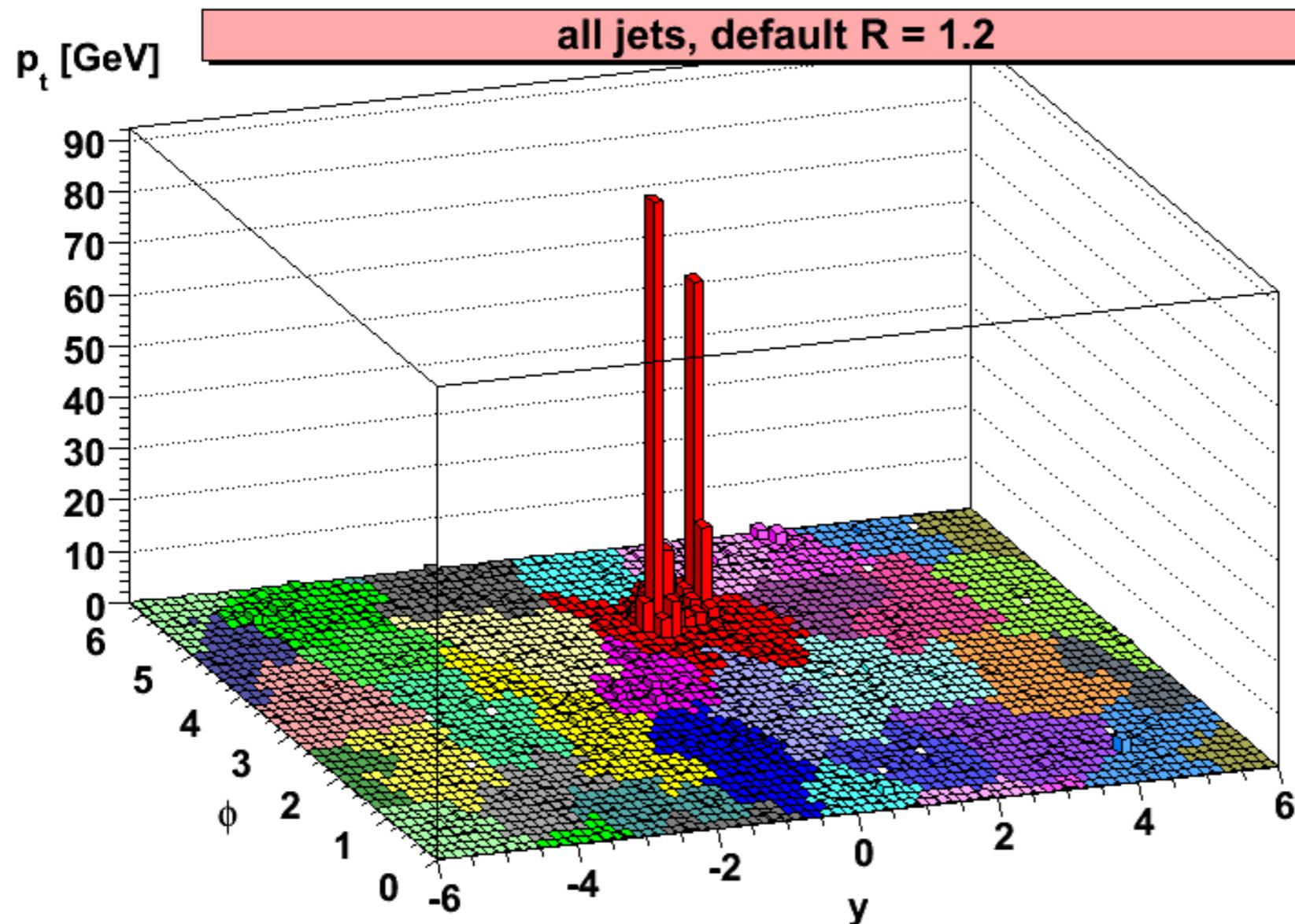
Butterworth, Davison, Rubin & GPS '08

arbitrary norm.

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

SIGNAL



Zbb BACKGROUND

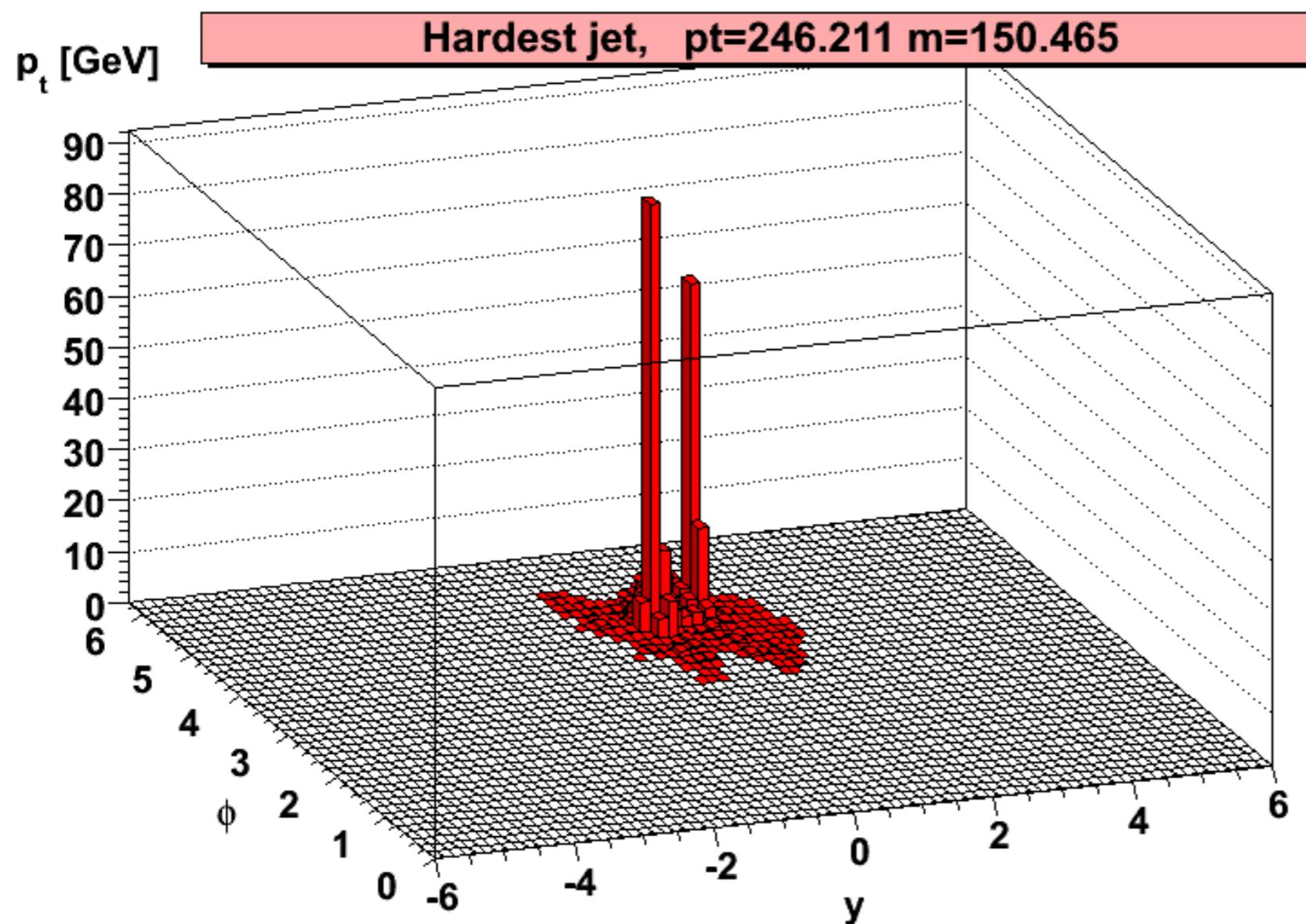
Fill it in,  $\rightarrow$  show jets more clearly

Butterworth, Davison, Rubin & GPS '08

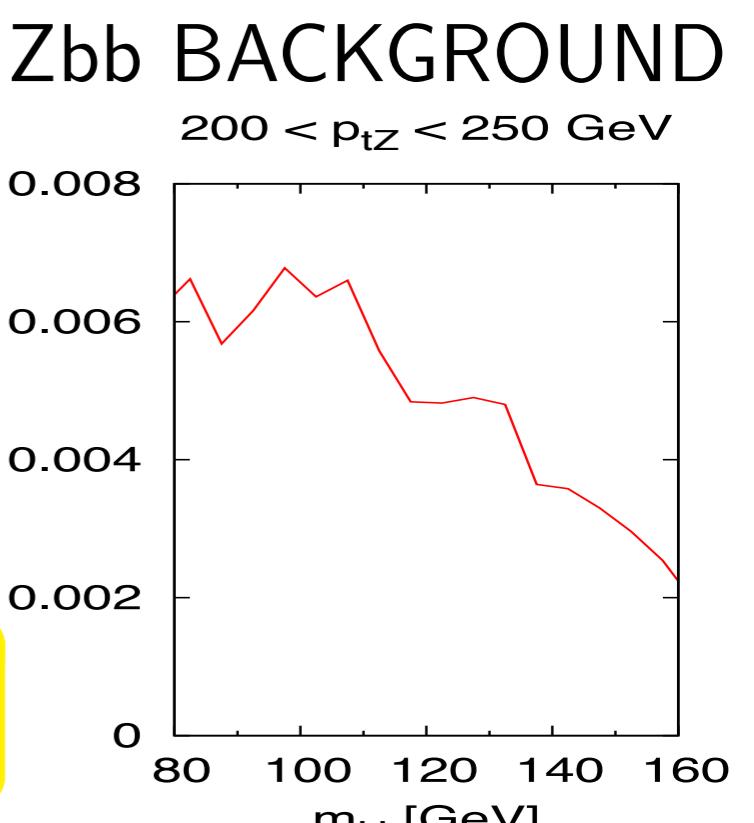
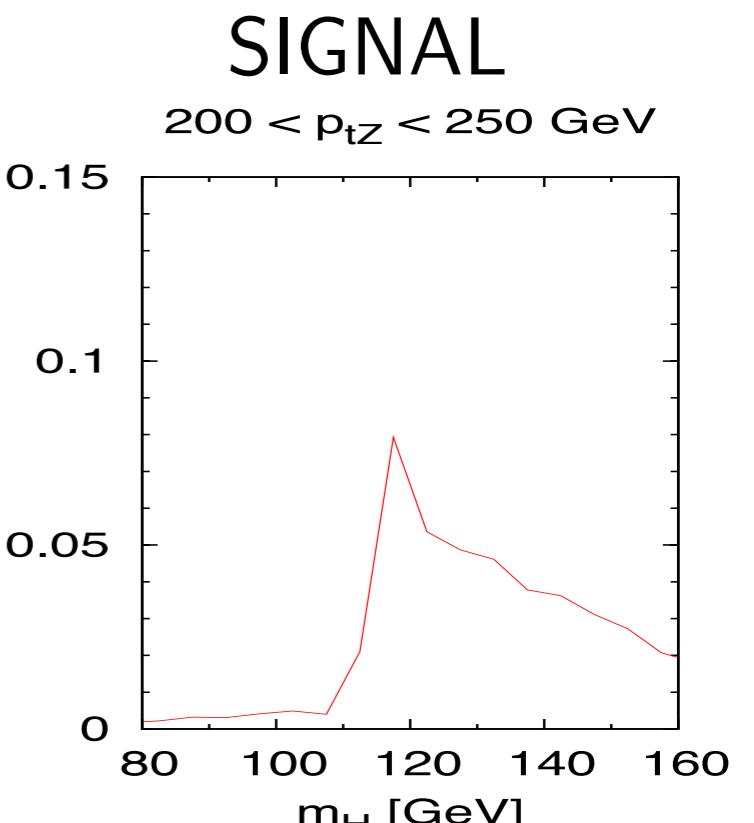
arbitrary norm.

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Consider hardest jet,  $m = 150$  GeV

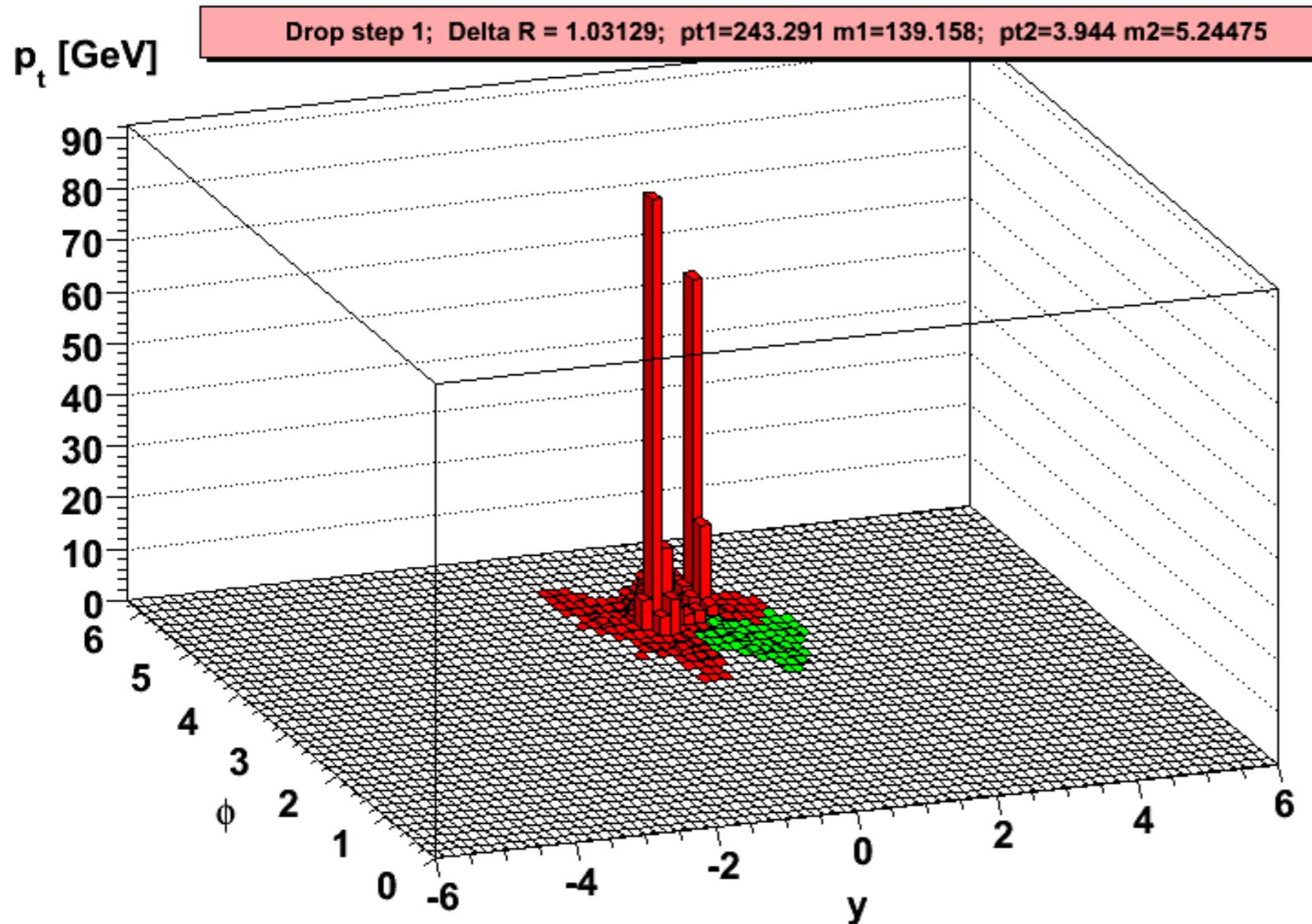


arbitrary norm.

Butterworth, Davison, Rubin & GPS '08

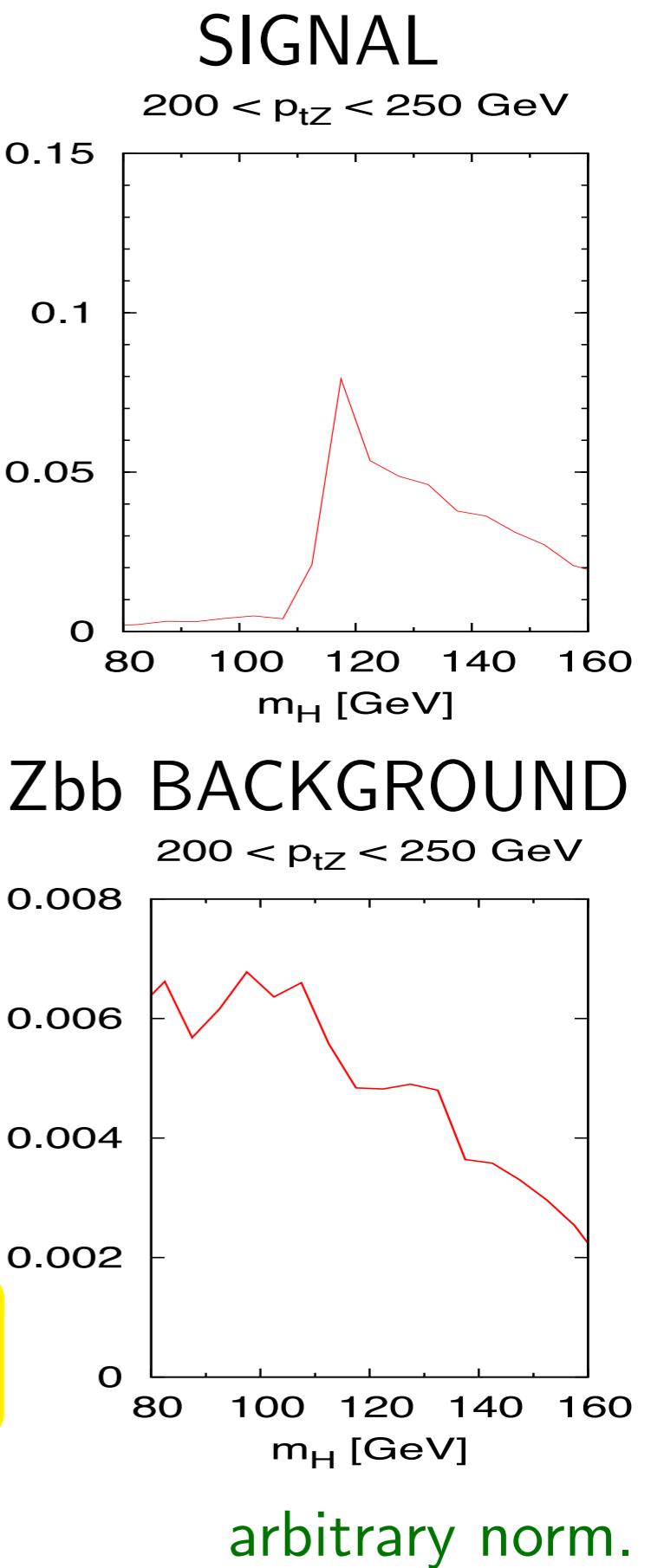
$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



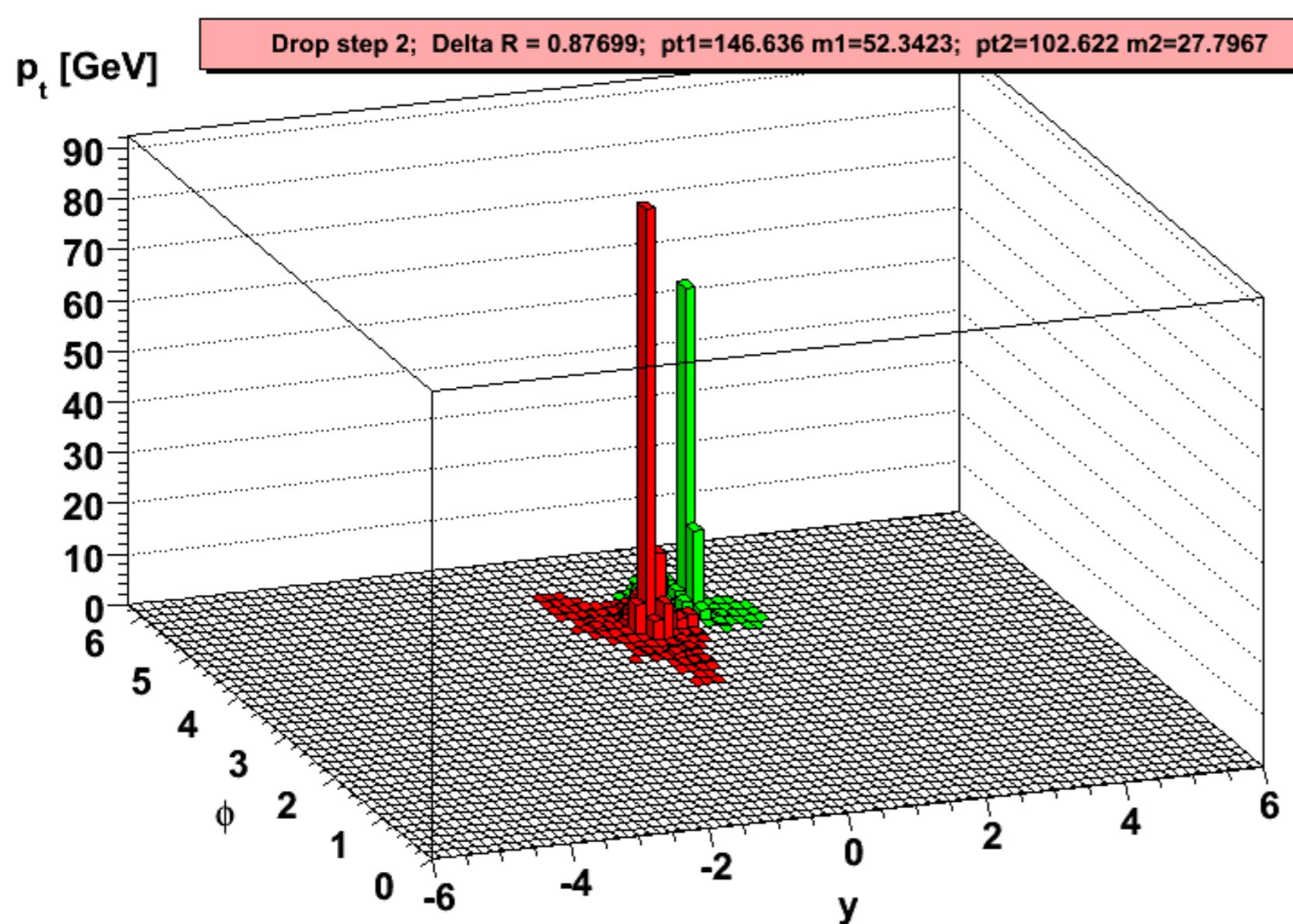
split:  $m = 150$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.92 \rightarrow$  repeat

Butterworth, Davison, Rubin & GPS '08



$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

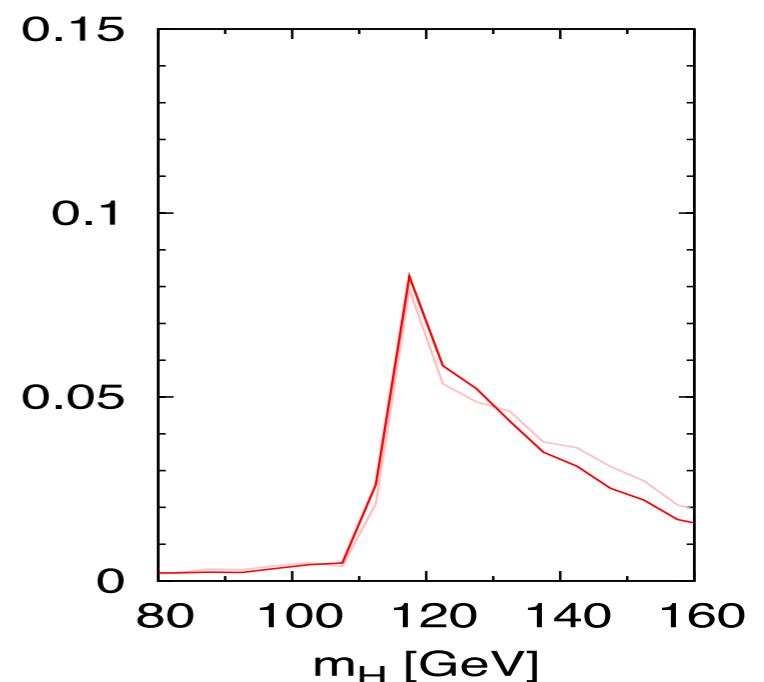
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



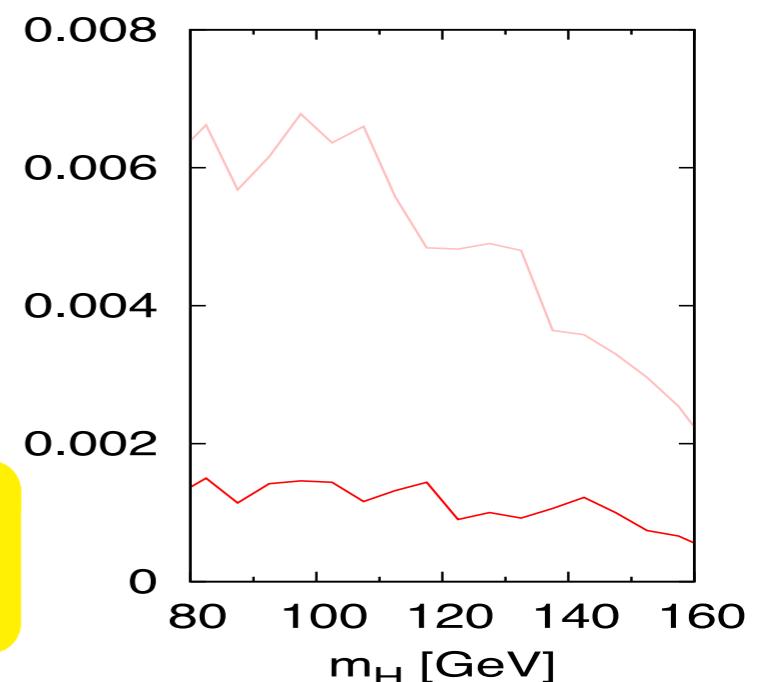
split:  $m = 139$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow$  mass drop

Butterworth, Davison, Rubin & GPS '08

SIGNAL  
 $200 < p_{tZ} < 250$  GeV



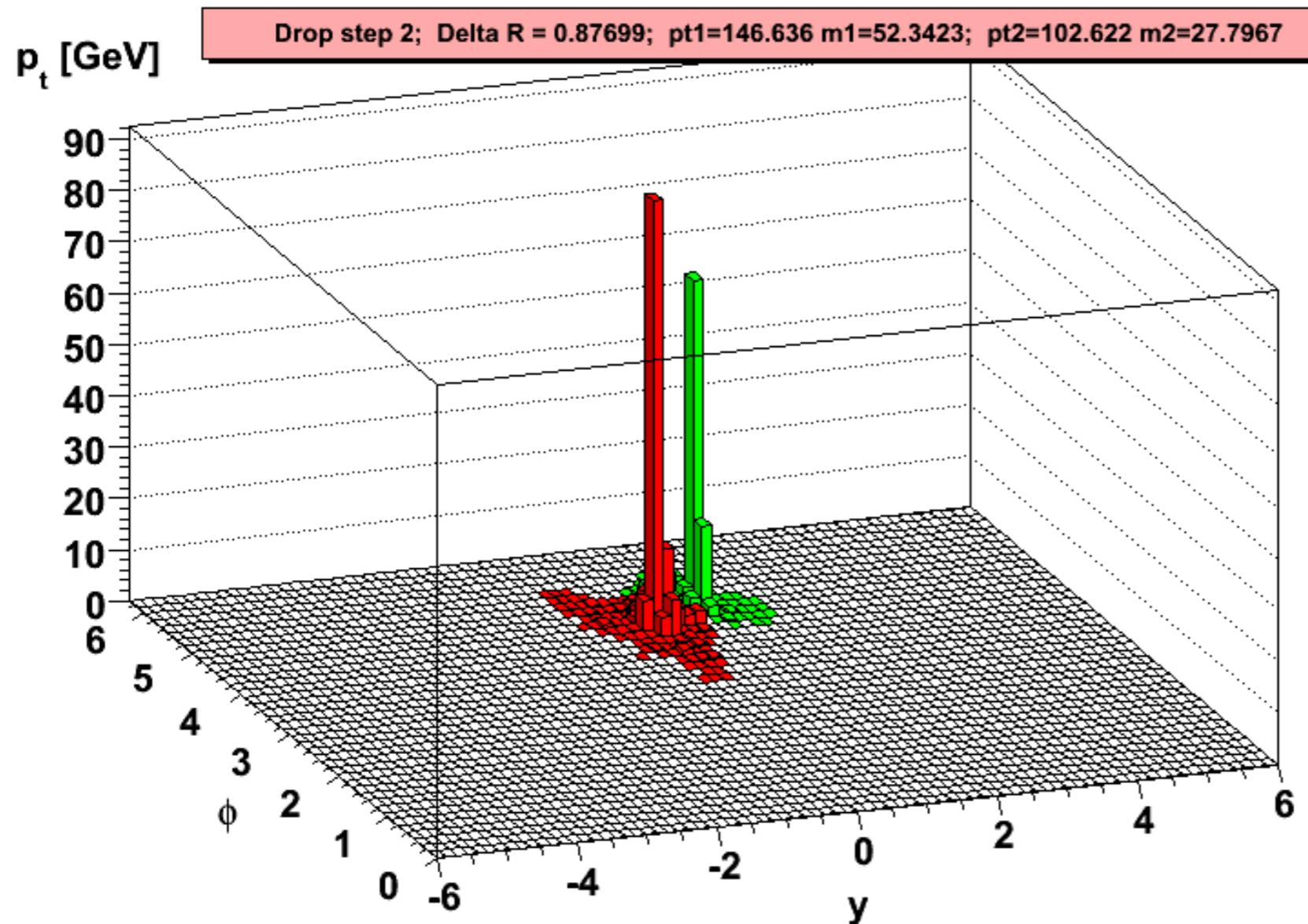
Zbb BACKGROUND  
 $200 < p_{tZ} < 250$  GeV



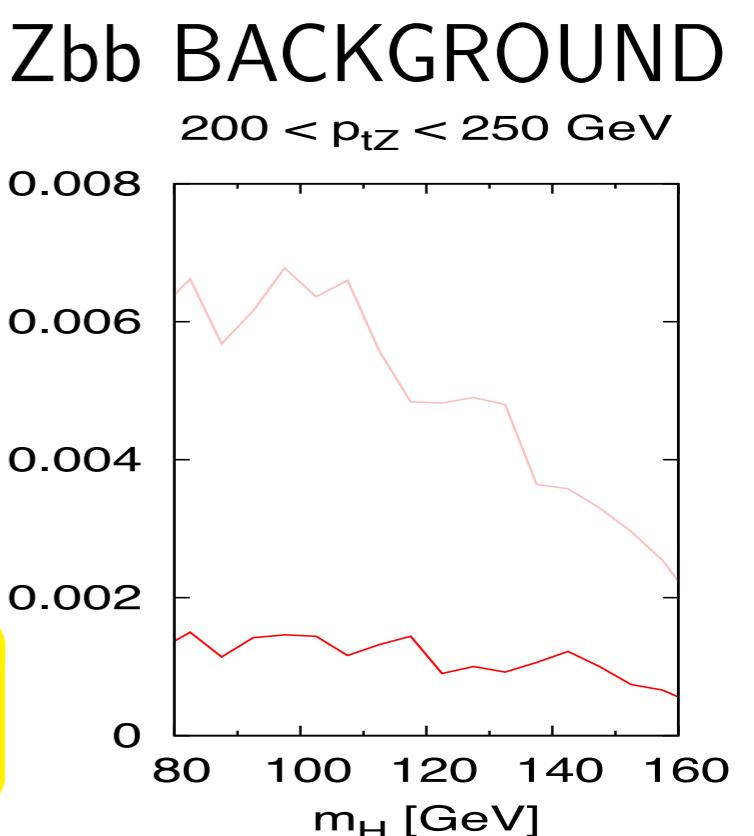
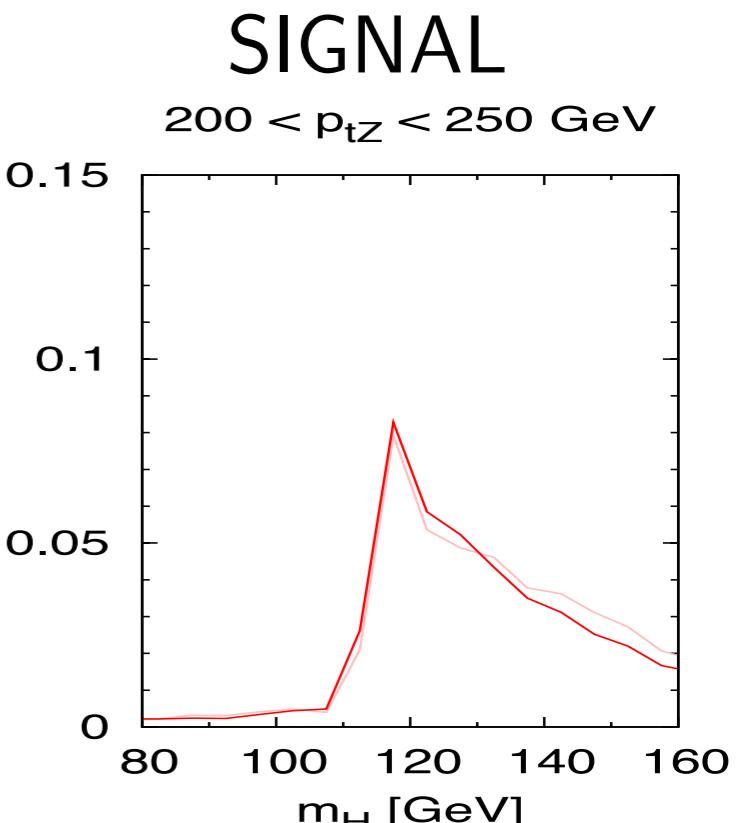
arbitrary norm.

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



check:  $y_{12} \simeq \frac{p_{t2}}{p_{t1}} \simeq 0.7 \rightarrow$  OK + 2  $b$ -tags (anti-QCD)

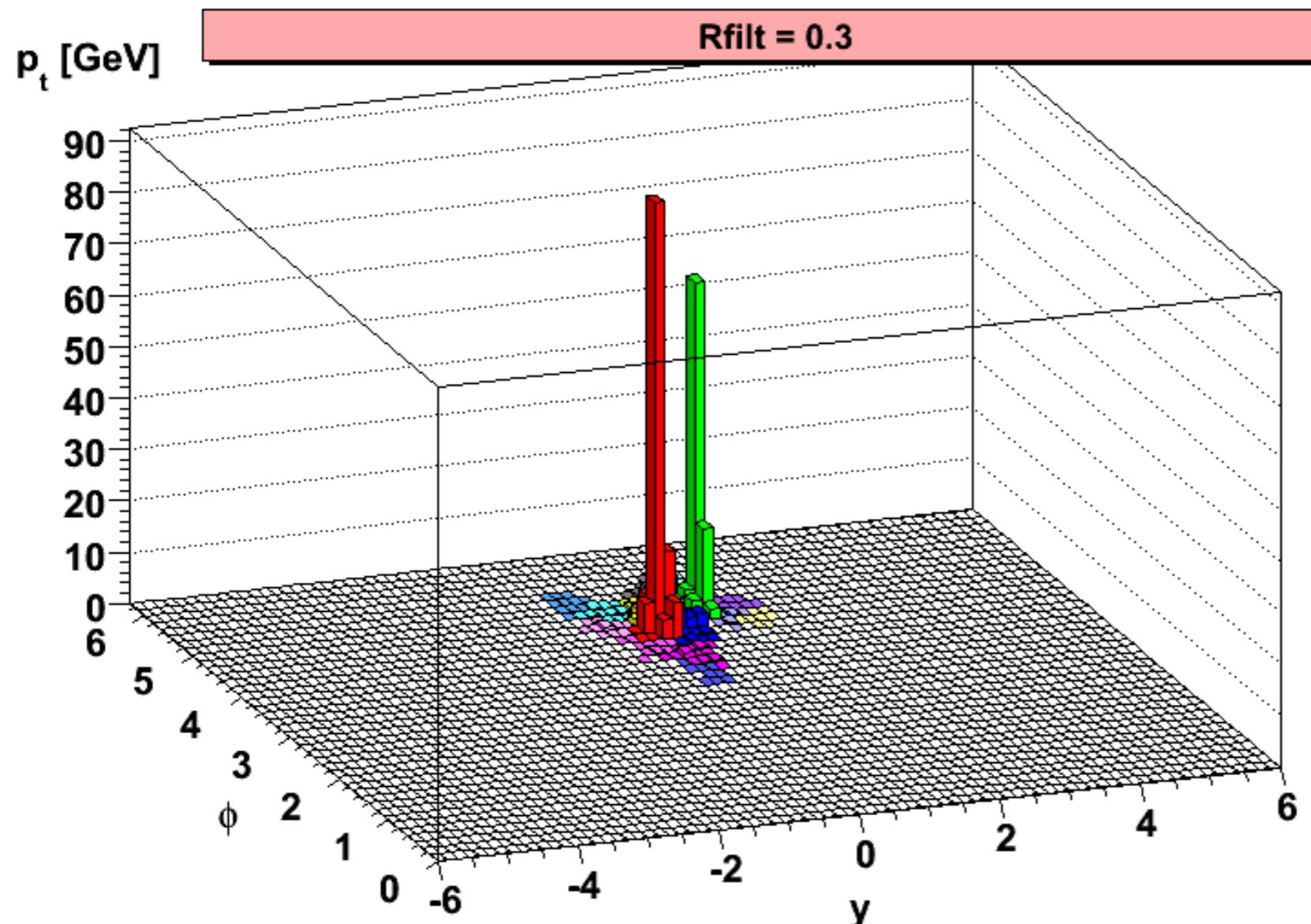


arbitrary norm.

Butterworth, Davison, Rubin & GPS '08

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

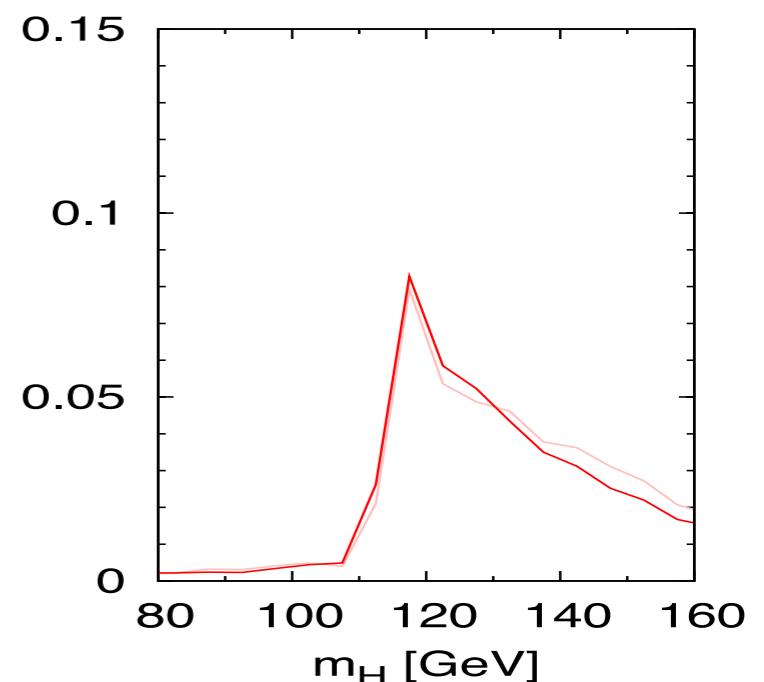
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



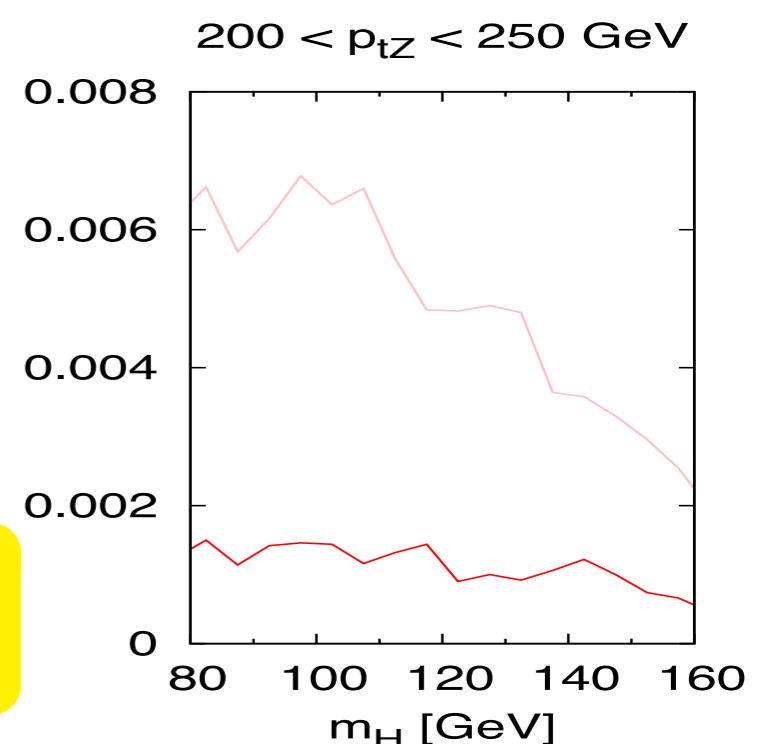
$R_{filt} = 0.3$

Butterworth, Davison, Rubin & GPS '08

**SIGNAL**  
 $200 < p_{tZ} < 250$  GeV



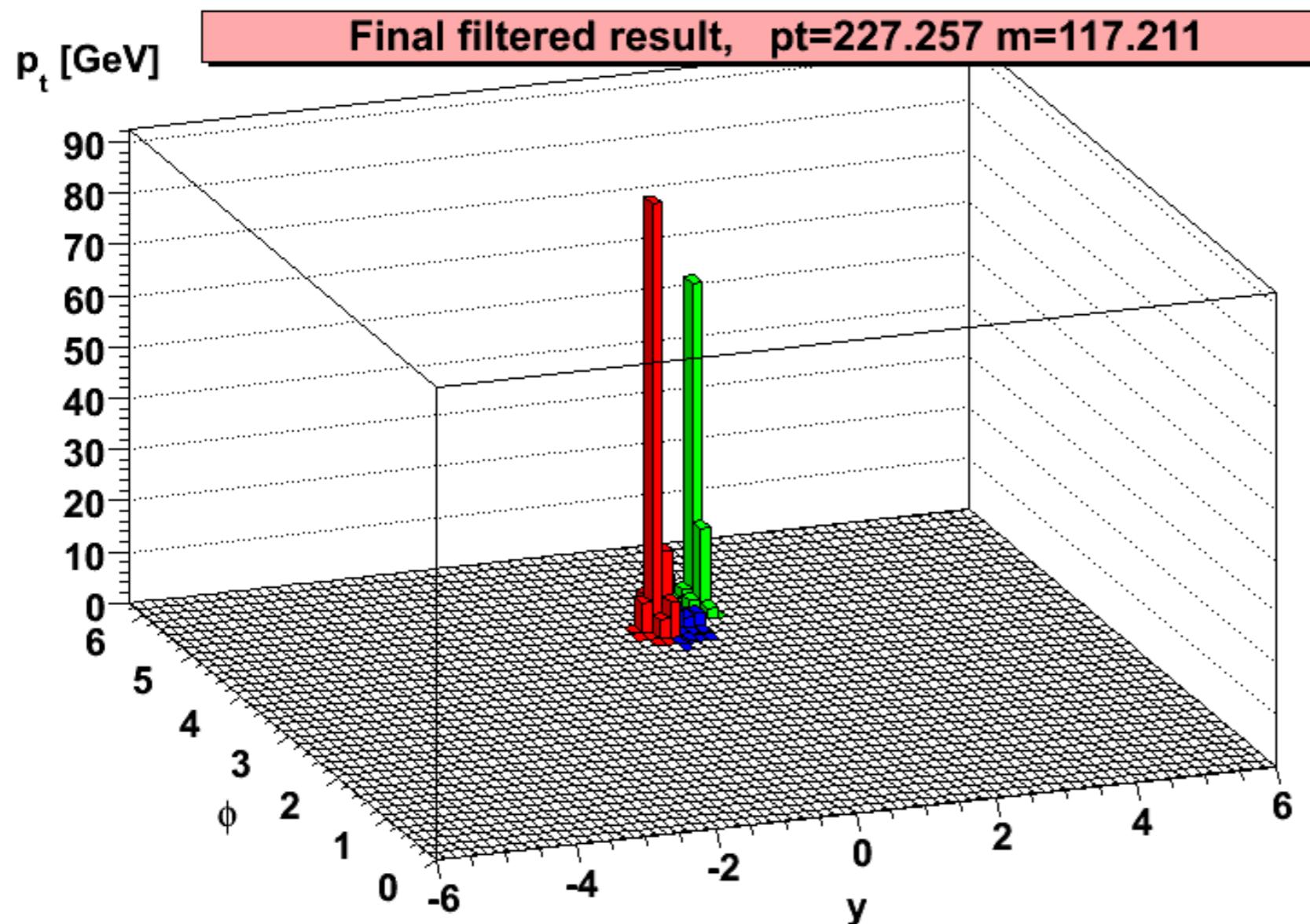
**Zbb BACKGROUND**



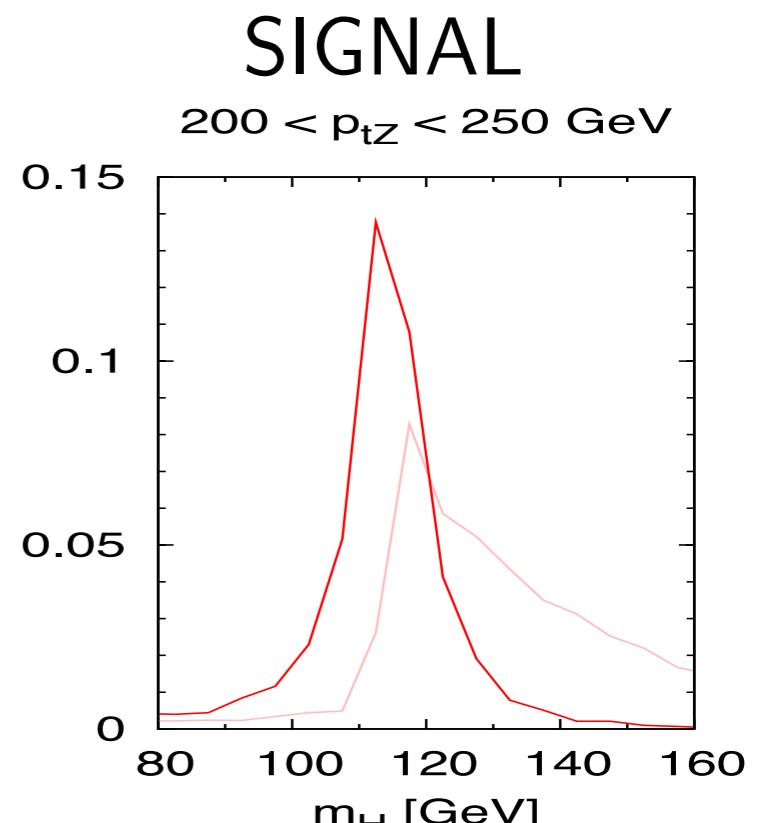
arbitrary norm.

$pp \rightarrow ZH \rightarrow \nu\bar{\nu}bb$ , @14 TeV,  $m_H = 115$  GeV

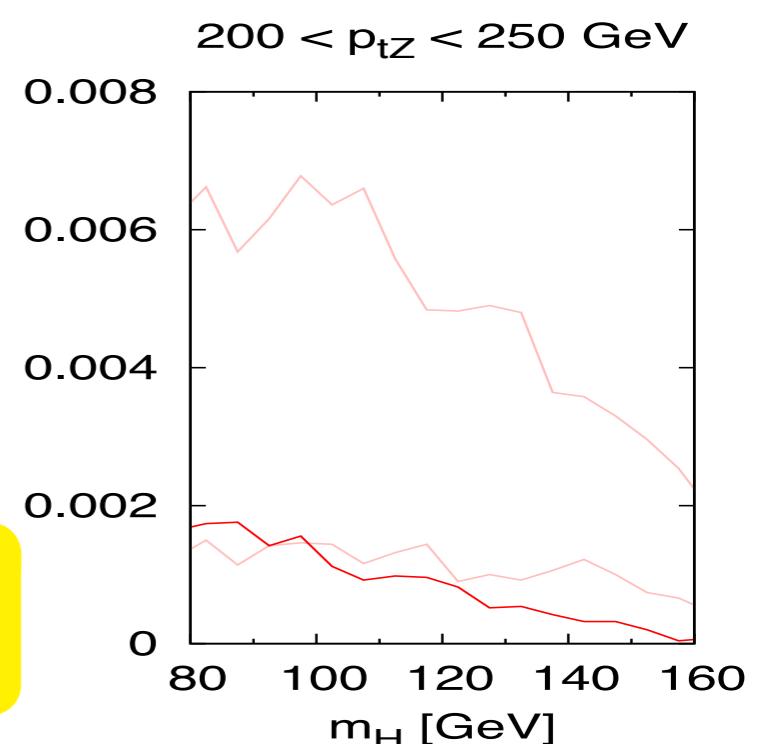
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



$R_{filt} = 0.3$ : take 3 hardest,  $m = 117$  GeV



Zbb BACKGROUND

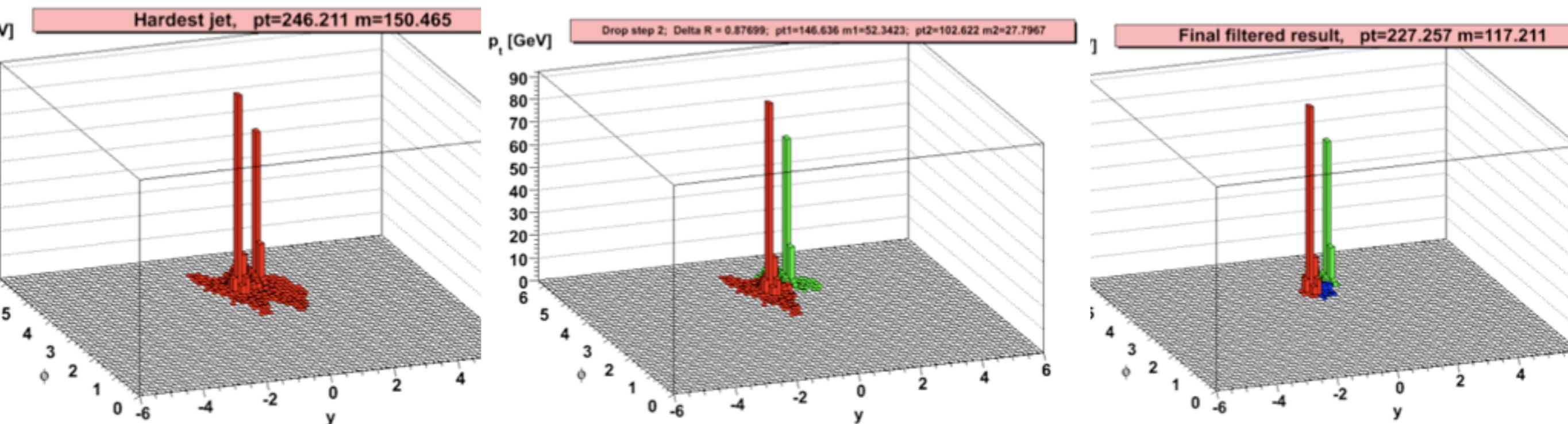
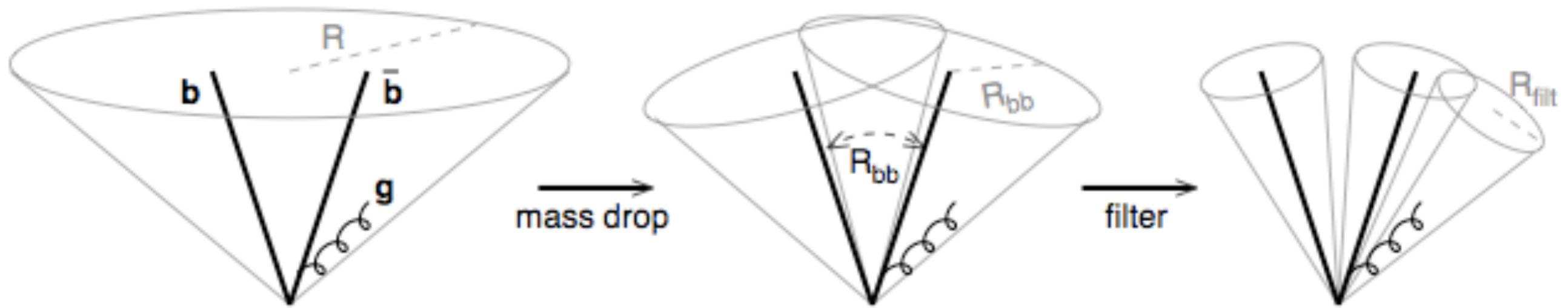


Butterworth, Davison, Rubin & GPS '08

arbitrary norm.

# Boosted Higgs analysis

$pp \rightarrow ZH \rightarrow vvb\bar{b}$



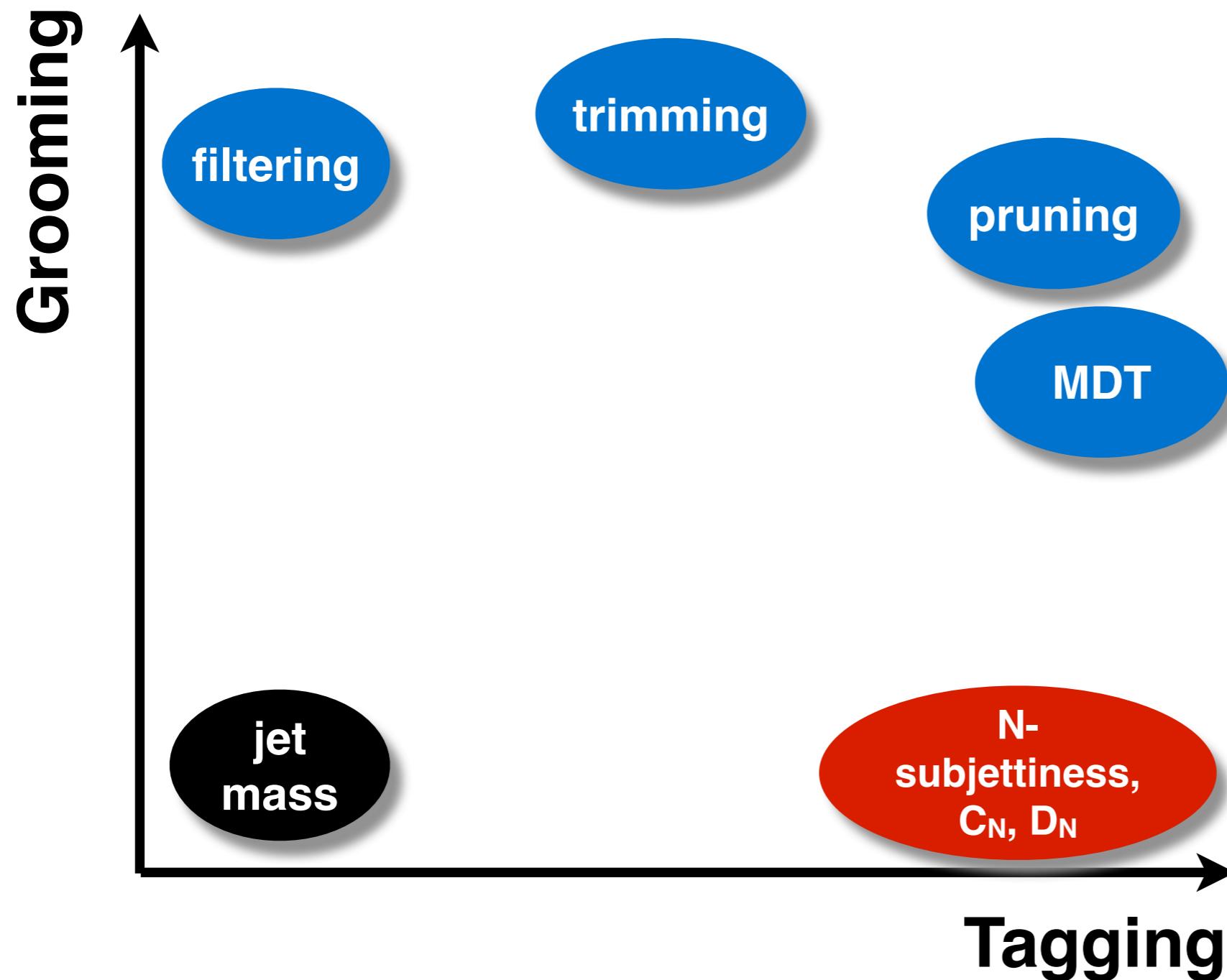
Cluster with a large  $R$

Undo the clustering into subjets,  
until a large mass drop  
is observed

Re-cluster with smaller  
 $R$ , and keep only 3  
hardest jets

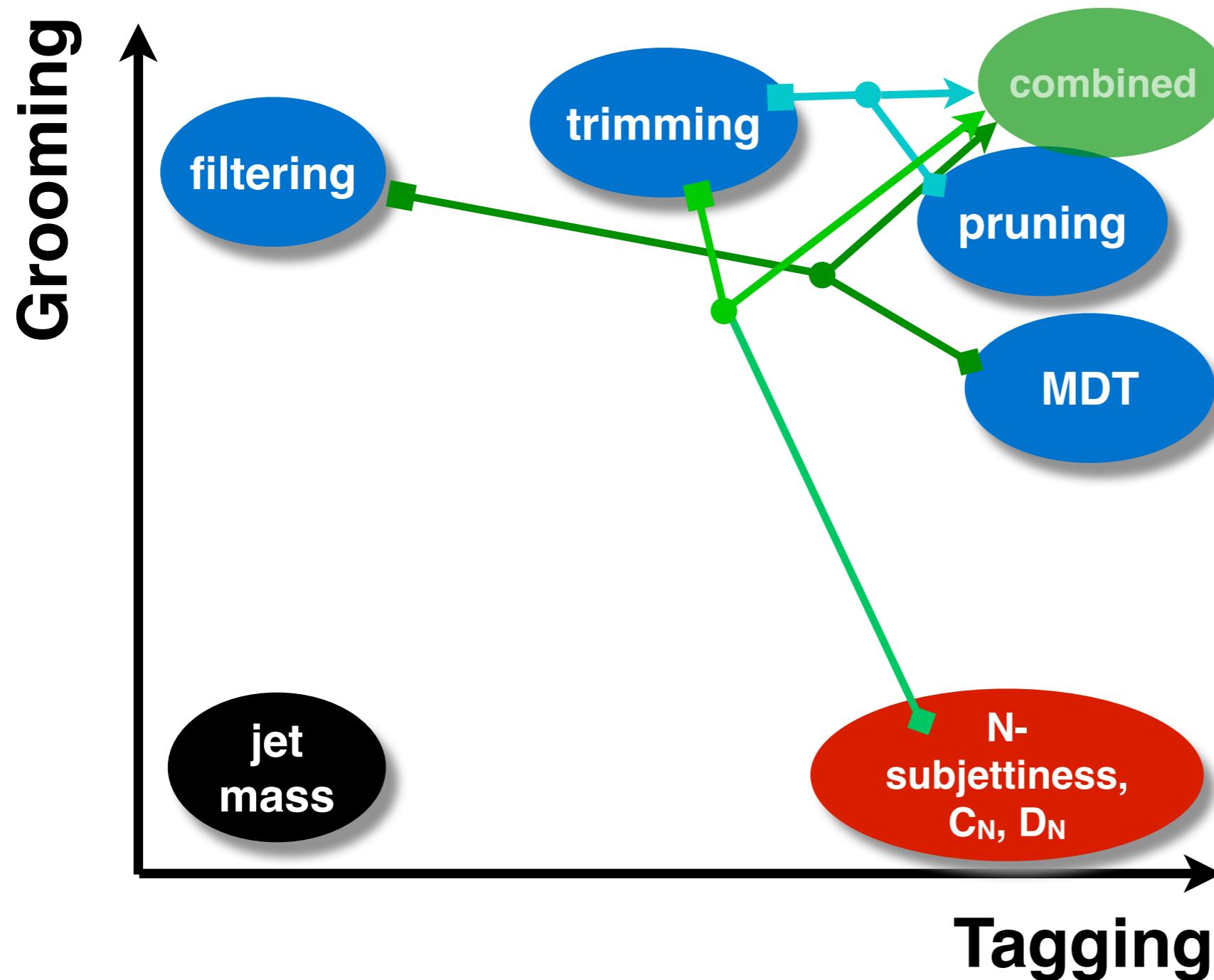
# different (2-body) substructure tools

Detailed relative positions depend on physics context  
(and are possibly contentious!)



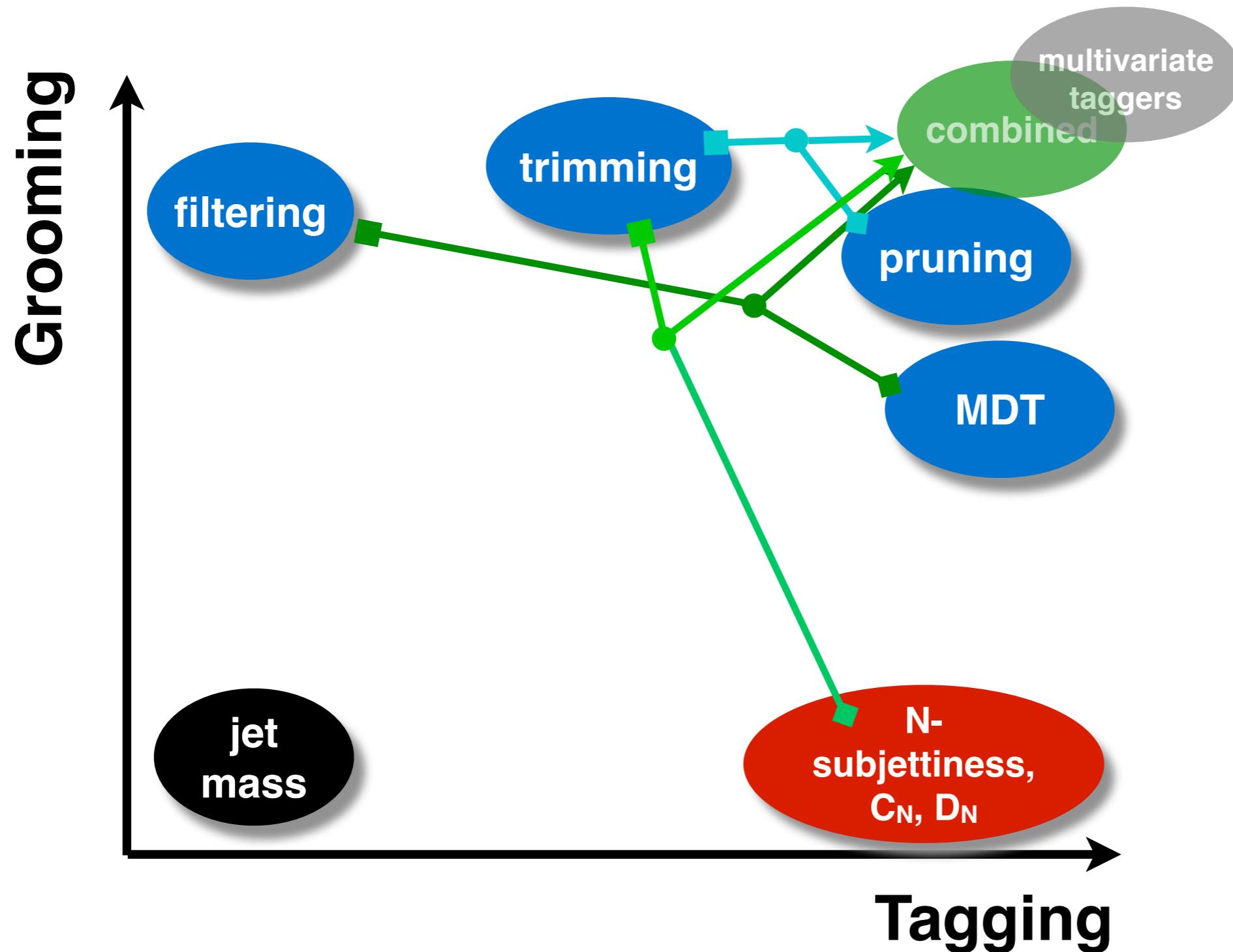
# different (2-body) substructure tools

Detailed relative positions depend on physics context  
(and are possibly contentious!)



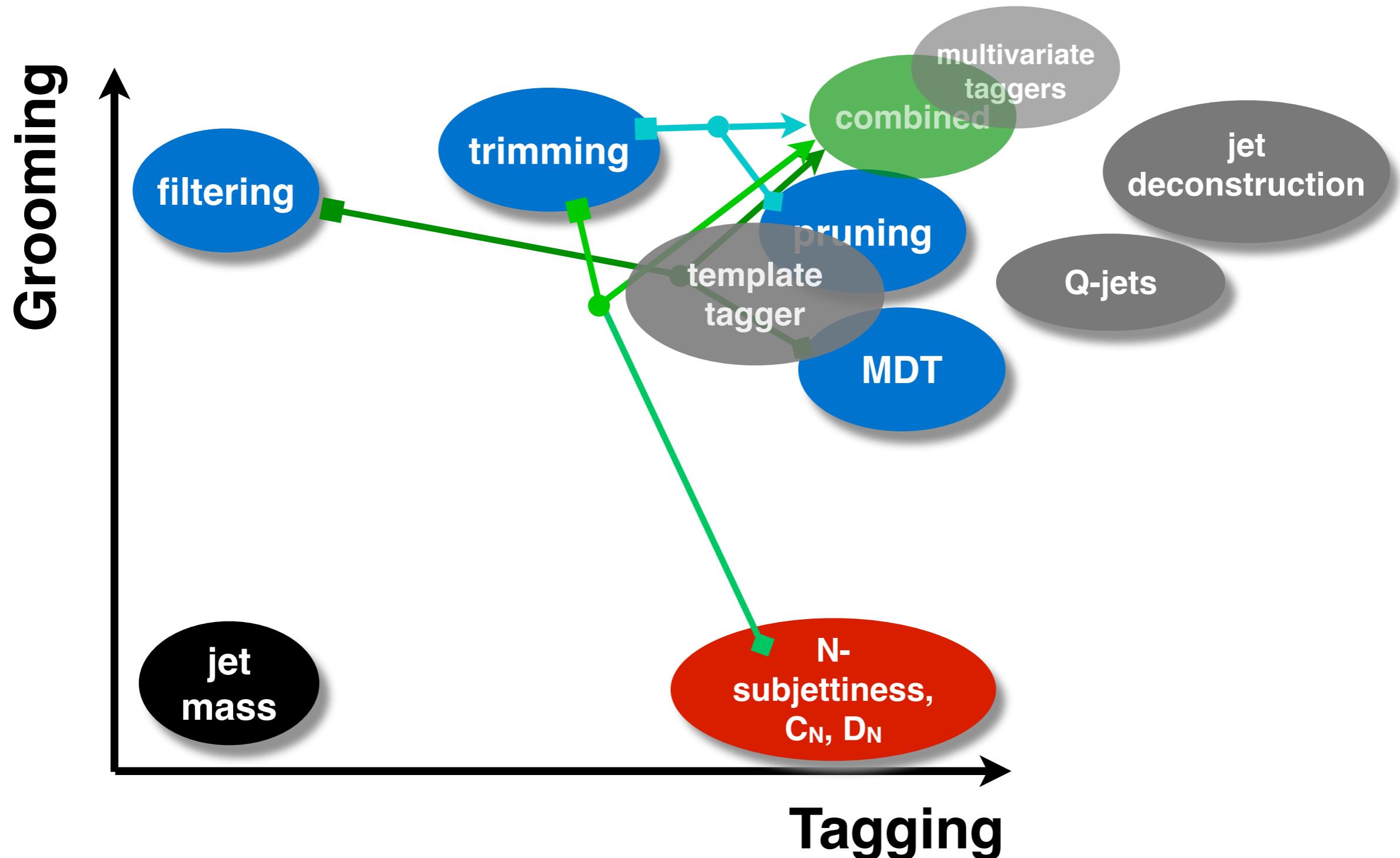
# different (2-body) substructure tools

Detailed relative positions depend on physics context  
(and are possibly contentious!)



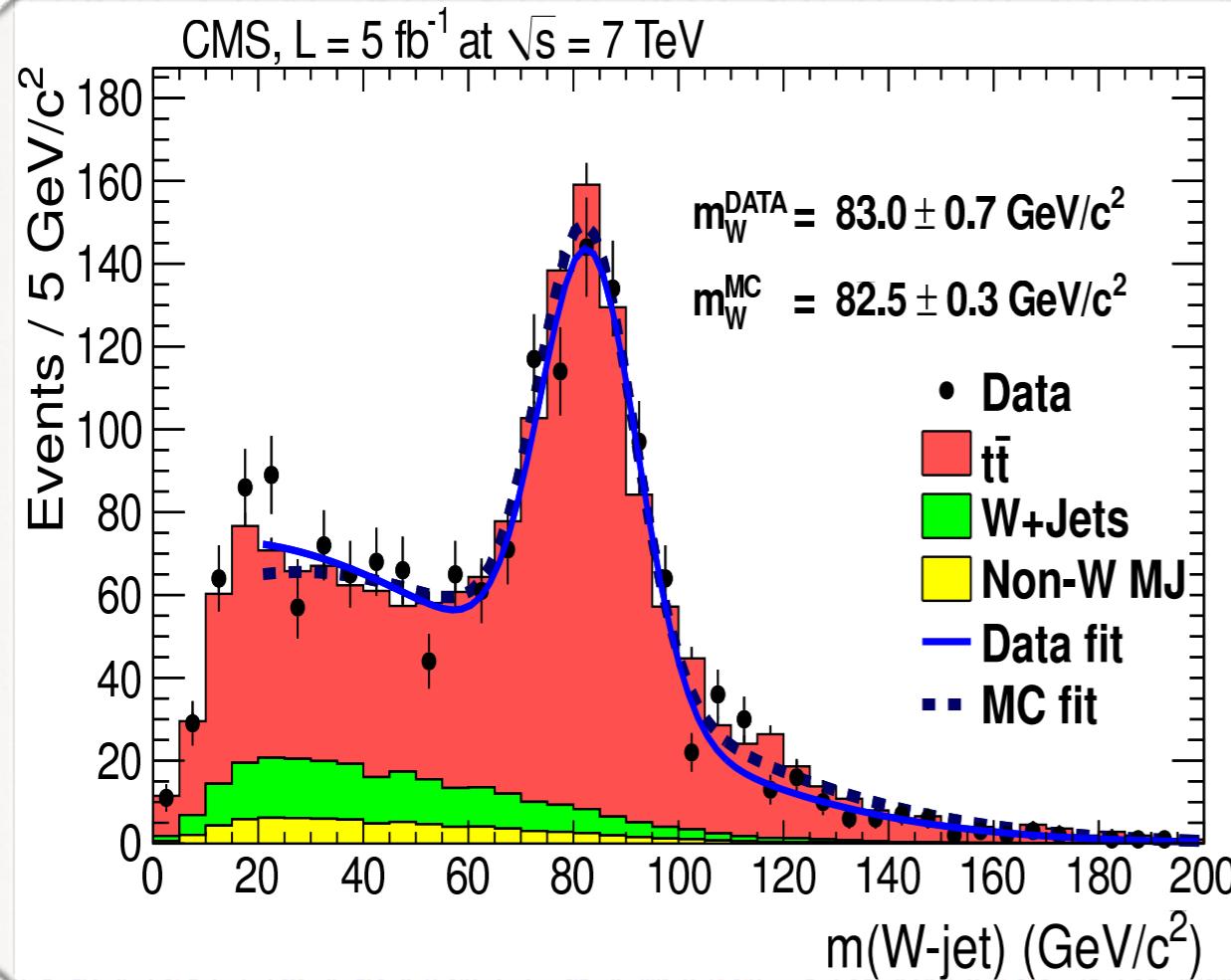
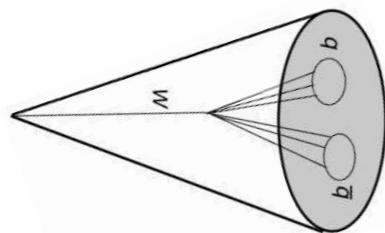
# different (2-body) substructure tools

Detailed relative positions depend on physics context  
(and are possibly contentious!)

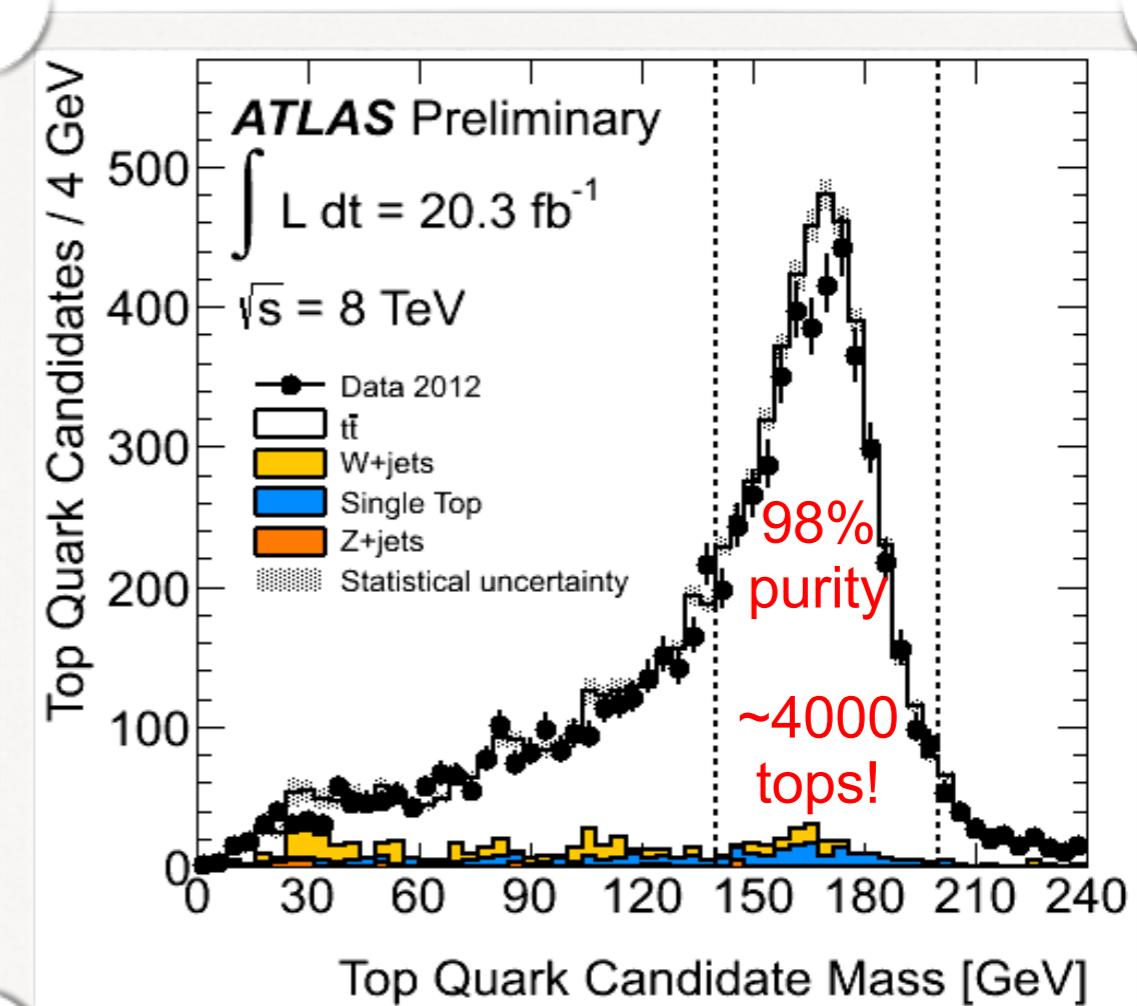
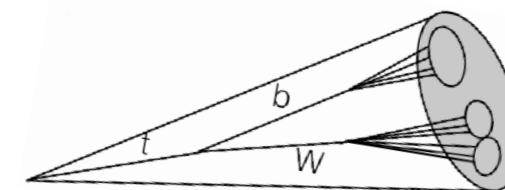


# Seeing W's and tops in a single jet

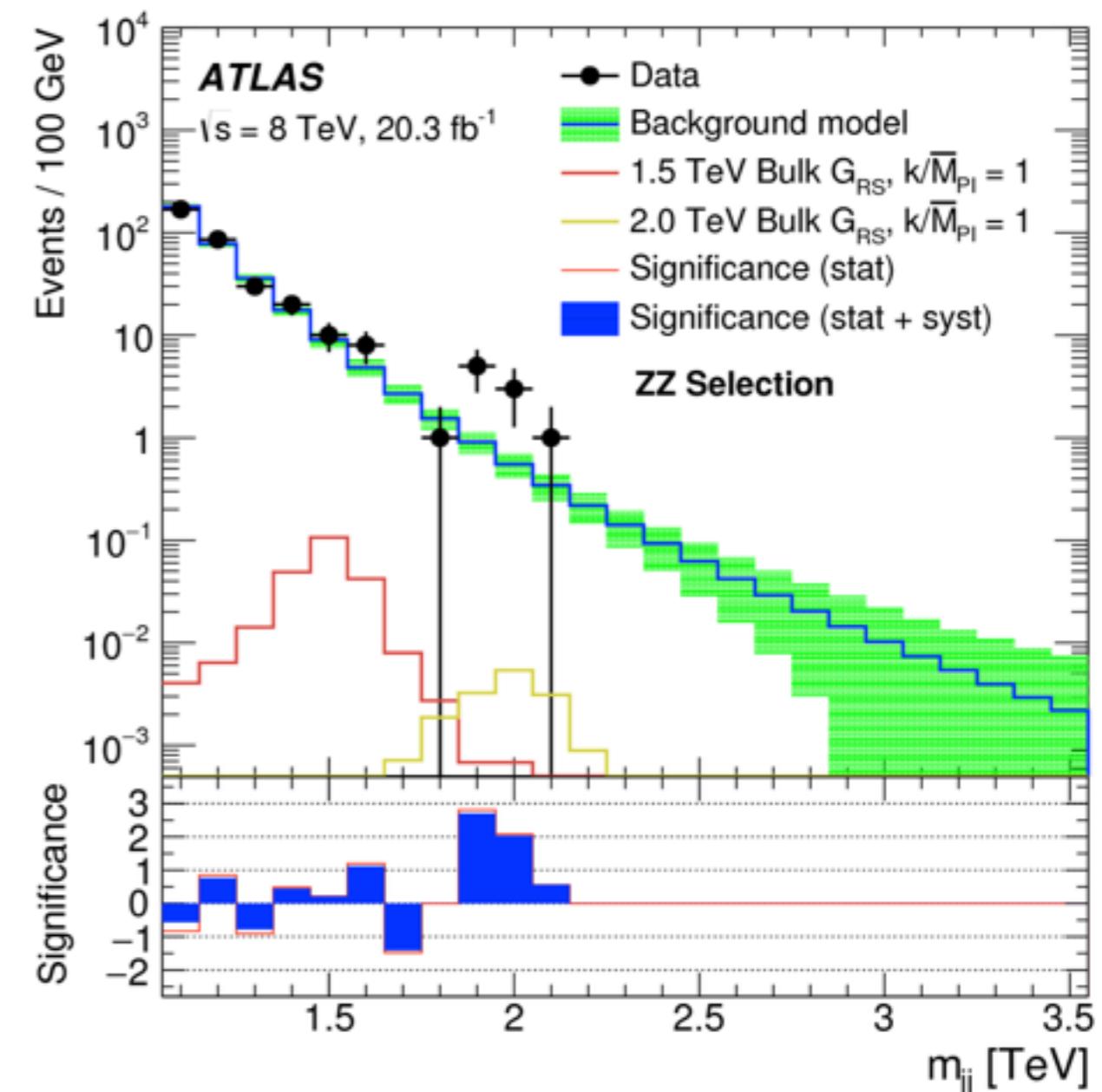
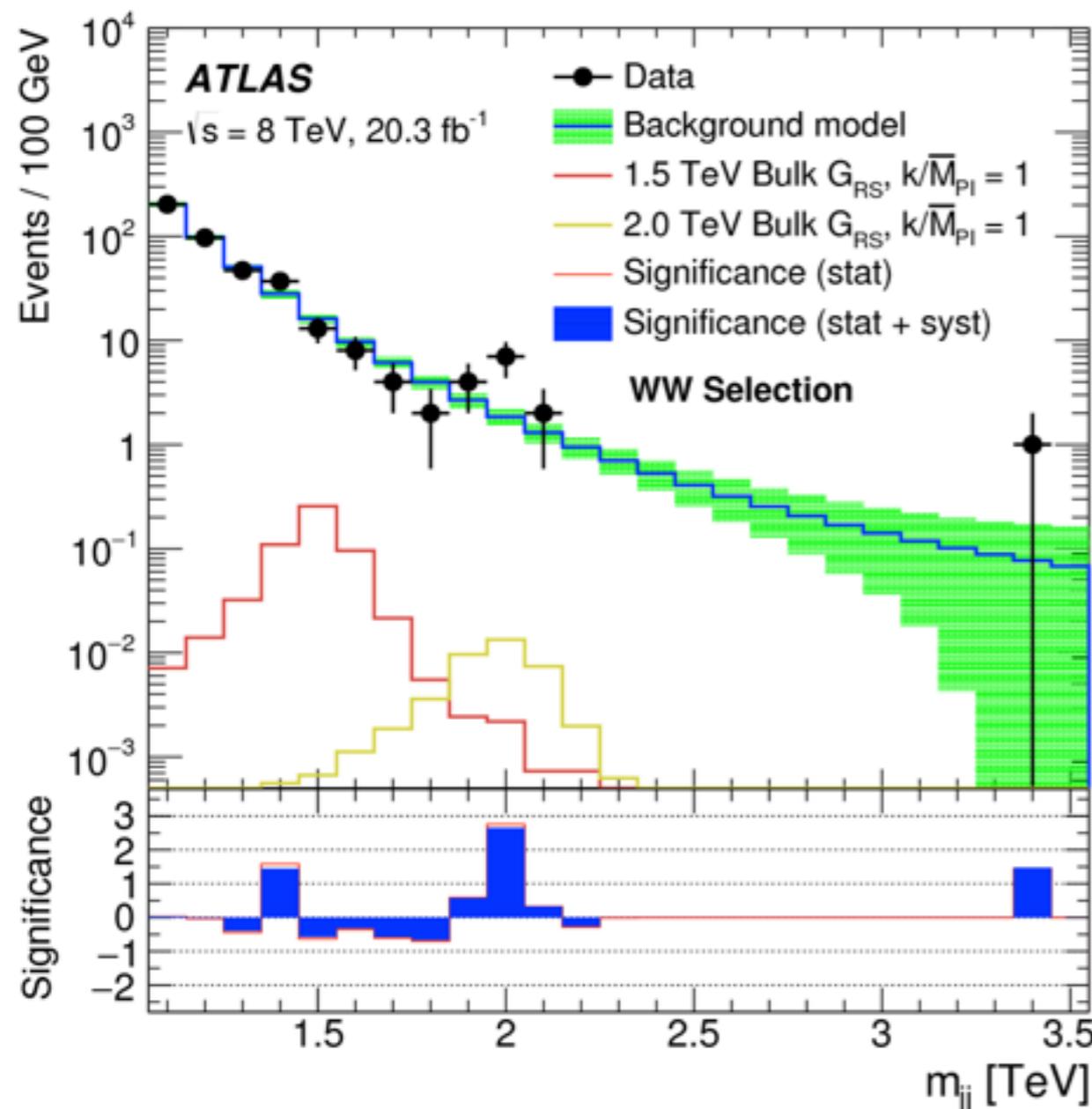
## W's in a single jet



## tops in a single jet



# ATLAS di-boson excess



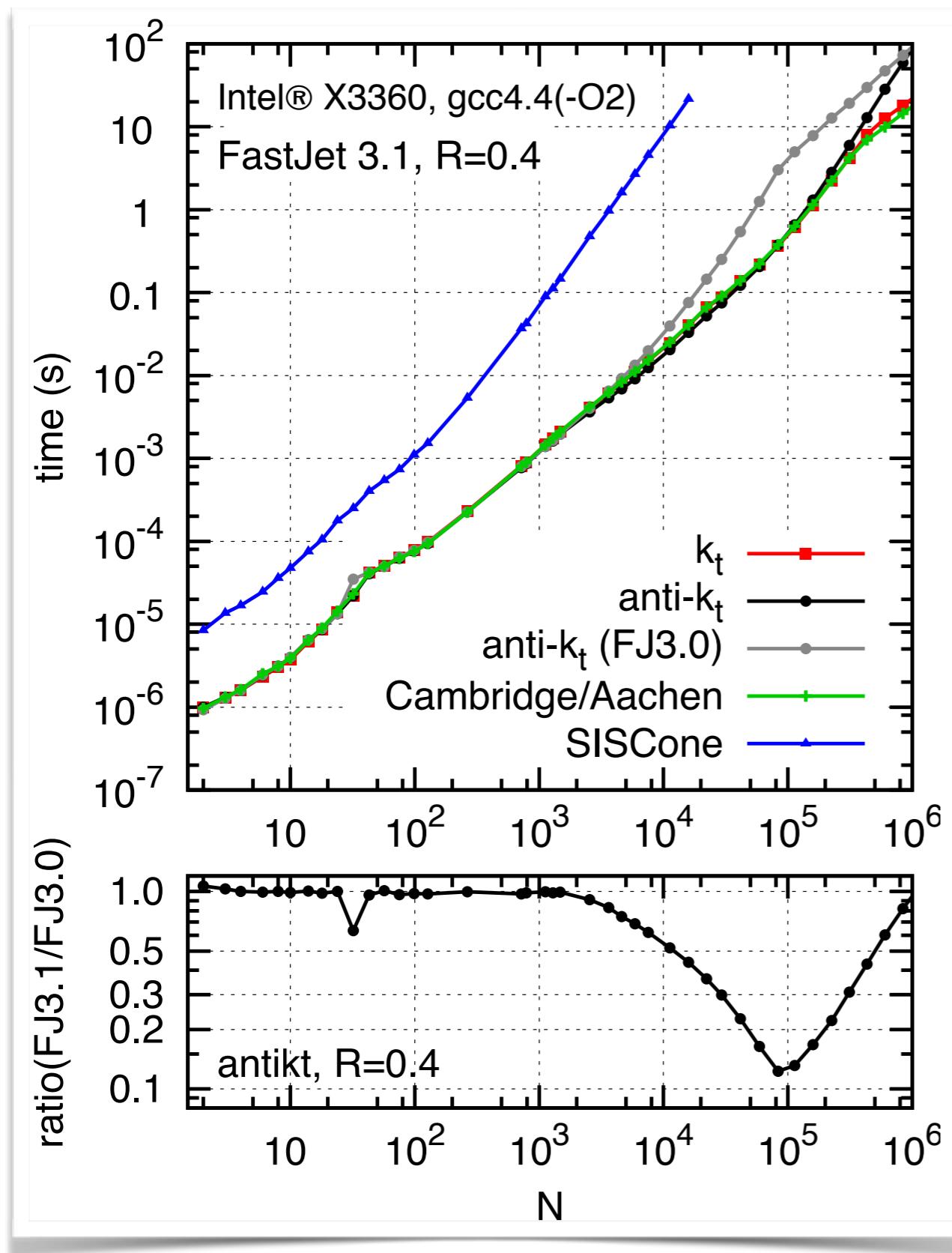
About 30 interpretations on arXiv so far!

# Points to remember from these lectures

- Major difference relative to QED: quarks and gluons both emit gluons
- Non-perturbative physics lurks in many places; limiting its impact (jets), factorising unavoidable non-perturbative parts (PDFs), are both key to our successful use of perturbative QCD
- Tightly connected with infrared and collinear divergences, which are ubiquitous in QCD

# EXTRAS

# Time to cluster N particles in FastJet



Time to cluster N  
particles

Improvement  
wrt FJ 3.0.x,  
**factor of 2 for 10k**

Version 1.017 of FastJet Contrib is distributed with the following packages

Package	Version	Information
ClusteringVetoPlugin	1.0.0	README NEWS
ConstituentSubtractor	1.0.0	README NEWS
EnergyCorrelator	1.1.0	README NEWS
GenericSubtractor	1.2.0	README NEWS
JetCleanser	1.0.1	README NEWS
JetFFMoments	1.0.0	README NEWS
JetsWithoutJets	1.0.0	README NEWS
Nsubjettiness	2.1.0	README NEWS
RecursiveTools	1.0.0	README NEWS
ScJet	1.1.0	README NEWS
SoftKiller	1.0.0	README NEWS
SubjetCounting	1.0.1	README NEWS
ValenciaPlugin	2.0.0	README NEWS
VariableR	1.1.1	README NEWS