EVAdoption Code

December 7, 2023

1 Imports

```
import numpy as np
import matplotlib.pyplot as plt
from scipy.integrate import odeint, solve_ivp, solve_bvp
from scipy.optimize import minimize
import pandas as pd
import scipy.linalg as la

# setup the print and display options to make displaying easier
np.set_printoptions(precision=5, suppress=True)
pd.set_option("display.precision", 15)
np.set_printoptions(formatter={'float': lambda x: "{0:0.7f}".format(x)})
pd.set_option('display.float_format', lambda x: "{0:0.7f}".format(x))
pd.set_option('display.max_columns', None)
```

2 Base Model

2.1 Create the base model and plot real data to show trends

```
E = 0.0008
# time points
t0 = 0
tf = 50
# constants
ch = 0.15 # rate from combustion to hybrid
he = 0.1 # rate from hybrid to electric
ec = 0.01 # rate from electric to combustion
hc = 0.1 # rate from hybrid to combustion
eh = 0.01 # rate from electric to hybrid
ce = 0.1 # rate from combustion to electric
c = 0.0 # rate of new combustion
h = 0.0 # rate of new hybrid
e = 0.0 # rate of new electric
# solve ODE
sol = solve_ivp(model, [t0, tf], [C, H, E], args=(ch, he, ec, hc, eh, ce, c, h, __
 ⇒e), t_eval=np.linspace(t0, tf, 1000))
# plot actual data
plt.subplot(121)
dot_size = 10
plt.scatter(rel_sales_df['Year'], rel_sales_df['Hybrid_ratio'], color="r",__
 ⇒s=dot_size)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Combustion_ratio'], color="k",_
 ⇔s=dot_size)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Electric_ratio'], color="b",u
 ⇒s=dot size)
plt.plot(sol.t + 2010, sol.y[0], label="Combustion", c="k")
plt.plot(sol.t + 2010, sol.y[1], label="Hybrid", c="r")
plt.plot(sol.t + 2010, sol.y[2], label="Electric", c="b")
plt.title("Conservative Model")
plt.xlabel("Year")
plt.ylabel("Proportion of Car Purchases")
plt.legend()
#### PROGRESSIVE MODEL ####
# constants for progressive model
ch = 0.19 # rate from combustion to hybrid
he = 0.2 # rate from hybrid to electric
ec = 0.01 # rate from electric to combustion
hc = 0.1 # rate from hybrid to combustion
eh = 0.18 # rate from electric to hybrid
```

```
ce = 0.1 # rate from combustion to electric
c = 0.0  # rate of new combustion
h = 0.0 # rate of new hybrid
e = 0.0007 # rate of new electric
# solve ode
sol2 = solve_ivp(model, [t0, tf], [C, H, E], args=(ch, he, ec, hc, eh, ce, c, u)
 \rightarrowh, e), t_eval=np.linspace(t0, tf, 1000))
# plot
plt.subplot(122)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Hybrid_ratio'], color="r",_
 ⇔s=dot size)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Combustion_ratio'], color="k",u
 ⇒s=dot_size)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Electric_ratio'], color="b", __
 ⇔s=dot_size)
plt.plot(sol2.t + 2010, sol2.y[0], label="Combustion", c="k")
plt.plot(sol2.t + 2010, sol2.y[1], label="Hybrid", c="r")
plt.plot(sol2.t + 2010, sol2.y[2], label="Electric", c="b")
plt.title("Progressive Model")
plt.xlabel("Year")
plt.ylabel("Proportion of Car Purchases")
plt.legend()
# save figure
plt.savefig('original_model.png', dpi=200, bbox_inches='tight')
plt.show()
```

3 California Regulation

3.1 Showing real data trends in the california car sale market

```
[]: # real data
eh = [0,.075,.12,.18,.254, .36, 1]
c = [1, 1-.075, 1-.12, 1-.18,1-.254, 1-.36, 0]
t = [2010,2018,2021,2022,2023,2026,2035]

# plot
plt.plot(t,eh, label = "Electric/Hybrid")
plt.scatter(t,eh)
plt.plot(t,c, label = "Combustion")
plt.scatter(t,c)
plt.xlabel("Years")
```

```
plt.ylabel("Proportion of Car Purchases")
plt.legend()
plt.show()
```

3.2 Create model and fit it to California data

```
[]: # build model
     def model(t, cars, ec, ce, c, e):
         return np.array([(ec)*cars[0]*cars[1] + c*cars[0],
                          (ce)*cars[0]*cars[1] + e*cars[1]])
     # constants
     ec = -0.4 # rate from electric to combustion
     ce = .3 # rate from combustion to electric
     c = -0.023 \# rate of new combustion
     e = 0.1 # rate of new electric
     # initial conditions
     C = 0.9792
     E = 0.0008
     # time points
     t0 = 0
     tf = 25
     # solve ODE
     sol = solve_ivp(model, [t0, tf], [C,E], args=(ec, ce, c,e), t_eval=np.
      ⇔linspace(t0, tf, 1000))
     # plot
     plt.plot(sol.t, sol.y[0], label="Combustion")
     plt.plot(sol.t, sol.y[1], label="Electric/Hybrid")
     plt.xlabel("Years Since 2010")
     plt.ylabel("Proportion of Car Purchases")
     plt.legend()
     plt.show()
     # print values at t=10
     print(len(sol.y[0]))
     year = 2020
     time = int((year - 2010) * 1000 / tf)
     print(time)
     print("Combustion: ", sol.y[0][time])
     print("Electric: ", sol.y[1][time])
```

4 Disaster Effect

4.1 Showing historical car sales and marking recessions

```
[]: # read car sales data
     car_sales = pd.read_csv('TOTALSA.csv')
     car_sales['DATE'] = pd.to_datetime(car_sales['DATE']) # convert to datetime__
      \hookrightarrow format
     # read recession dates
     recession = pd.read_csv('recession_dates.csv')[['Peaks', 'Troughs']]
     # convert to datetime format
     recession['Peaks'] = pd.to_datetime(recession['Peaks'])
     recession['Troughs'] = pd.to_datetime(recession['Troughs'])
     # create figure and plot car sales
     fig, ax = plt.subplots(1,1,figsize=(12,3))
     car_sales.plot(x='DATE', y='TOTALSA', ax=ax, c='#1f77b4')
     # gray out the recession areas
     for i in range(recession.shape[0]):
         ax.axvspan(recession.loc[i, 'Peaks'], recession.loc[i, 'Troughs'], alpha=0.

¬3, color='gray')

     # label plot
     ax.set_title('Total Vehicle Sales')
     ax.set vlabel('Millions of Units')
     ax.legend(['Sales', 'Recessions'])
     ax.set_xlabel('Year')
     plt.tight_layout()
     plt.savefig('Total Vehicle Sales')
     plt.show()
```

5 Charging Ports

5.1 Setup the data

```
# save the charging data to a csv in the data folder
charging_df.to_csv("data/charging.csv", index=False)
```

```
[]: # load the charging data
     charging_df = pd.read_csv("data/charging.csv")
     # load the sales data
     sales_df = pd.read_csv("data/vehicle_sales_2000_2023.csv")
     # combine the charging stations data to the vehicle sales data based
     # on the year column
     sales_df = sales_df.merge(charging_df, on='Year', how='left')
     # since charging ports did not exist in the early years of sales, fill these
      ⇔with zeros
     sales_df['Charging Ports'] = sales_df['Charging Ports'].fillna(0).astype(float)_u
      →/ 1000
     sales_df['Station Locations'] = sales_df['Station Locations'].fillna(0).
      ⇒astype(float) / 1000
     # compute the station locations ratio
     sales_df['Station Locations Ratio'] = sales_df['Station Locations'] /__
      ⇔sales_df['Total']
     # only consider years where there were electric vehicle sales and charging \Box
      \hookrightarrowstations
     rel_sales_df = sales_df.loc[sales_df['Year'] >= 2011, :].copy()
```

5.2 Find a best fit exponential for charging stations

```
plt.plot(ts + 2000, np.exp(a * ts + b), color='orange', label="Exponential")
plt.xlabel("Year")
plt.ylabel("Number of Charging Stations (thousands)")
plt.title("Number of US Charging Stations over Time")
plt.legend()
plt.show()
```

5.3 Run the charging station ODE to make future predictions

```
# SOLVING THE CHARGING STATION IVP #
    # define the altered charing station base model
    def ces(t, y, K_ch, K_ce, K_he, alpha, beta, C_s):
        #print(y[0], y[1], y[2], y[3], C_s, y[3] / C_s)
        return (
            -K_{ch} * y[0] * y[1] - K_{ce} * y[0] * y[2],
            K_{ch} * y[0] * y[1] - K_{he} * y[1] * y[2],
            (K_ce * y[0] * y[2] + K_he * y[1] * y[2] + alpha * y[3]) * (1-y[2]),
            beta * y[3] * (1 - y[3] / C_s)
        )
    # go from 2011 to 2050
    t_span = (0, 50-11)
    ts = np.linspace(*t_span, 500)
    # create a clean version of the years as integers
    ts_int = ts.astype(int)
    ts_yr_inds = np.where(ts_int[1:] != ts_int[:-1])[0] + 1
    ts_yr_inds = np.concatenate([[0], ts_yr_inds])
    # find which years are using historical data and which years involve future data
    mn yr, mx yr = rel sales df['Year'].min(), rel sales df['Year'].max()
    ts_2011 = (ts[ts_yr_inds] + 2011).astype(int)
    inner_years = (ts_2011 >= mn_yr) & (ts_2011 <= mx_yr)
    inner_ts_yr_inds = ts_yr_inds[inner_years]
    # setup y0 based on the actual ratios at the start of 2011
    y0 = np.array([
        rel_sales_df['Combustion_ratio'].values[0],
        rel_sales_df['Hybrid_ratio'].values[0],
        rel_sales_df['Electric_ratio'].values[0],
        rel_sales_df['Station Locations Ratio'].values[0]
    ])
    # set constants to make the trends match the data from 2011 through 2022
```

```
K_ch = 0.10
K ce = 0.11
K_he = 0.01
alpha = 1.7
beta = 0.28
C_s = 0.15
# solve the modified ivp
solution = solve_ivp(ces, t_span, y0, t_eval=ts, args=(K_ch, K_ce, K_he, alpha,_
⇔beta, C_s))
# extract the true values
C = rel_sales_df['Combustion_ratio'].values
H = rel_sales_df['Hybrid_ratio'].values
E = rel_sales_df['Electric_ratio'].values
S = rel_sales_df['Station Locations Ratio'].values
# find the predicted values in the future
model yrs = ts + 2011
model_C = solution.y[0]
model H = solution.y[1]
model_E = solution.y[2]
model_S = solution.y[3]
# define a color map that maps the default colors to
# our specified uniform colors
color_map = {
    'blue': 'black', # combustion
   'orange': 'red', # hybrid
   'green': 'blue', # electric
    'red': 'green' # charqing stations
}
# PLOTTING THE SOLUTION'S FIT TO THE ACTUAL DATA #
# since the combustion ratios are a lot higher than the other ratios, plot the
# combustion fit separate from the other fits
plt.subplot(1,2,1)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Combustion_ratio'],_

color=color_map['blue'], label='Combustion Actual')

plt.plot(rel_sales_df['Year'], model_C[inner_ts_yr_inds],__
 ⇔color=color_map['blue'], label='Combustion Model')
plt.vlines(2022, rel_sales_df['Combustion_ratio'].min(), 1,__
 ⇔linestyles='dashed', color='black')
plt.legend(loc='lower left')
```

```
plt.ylabel("Percentage of Total Sales")
plt.xlabel("Year")
# plot the hybrid, electric and station location fits
plt.subplot(1,2,2)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Hybrid_ratio'],__

¬color=color_map['orange'], label='Hybrid Actual')
plt.plot(rel_sales_df['Year'], model_H[inner_ts_yr_inds],__

¬color=color_map['orange'], label='Hybrid Fit')

plt.scatter(rel_sales_df['Year'], rel_sales_df['Electric_ratio'],__

¬color=color_map['green'], label='Electric Actual')

plt.plot(rel_sales_df['Year'], model_E[inner_ts_yr_inds],__

¬color=color_map['green'], label='Electric Fit')
plt.scatter(rel_sales_df['Year'], rel_sales_df['Station Locations Ratio'], u
 ⇔color=color_map['red'], label='Charging Stations Actual')
plt.plot(rel_sales_df['Year'], model_S[inner_ts_yr_inds],__

¬color=color_map['red'], label='Charging Stations Fit')

plt.vlines(2022, 0, rel_sales_df['Hybrid_ratio'].max(), linestyles='dashed', u
 ⇔color='black')
plt.legend()
plt.xlabel("Year")
plt.ylabel("Percentage of Total Sales")
# show the fitting plot
plt.suptitle("Fitting Model Parameters to the Data")
plt.gcf().set_size_inches(12, 4)
plt.show()
###################################
# PLOT FUTURE PREDICTIONS #
###################################
dot_size = 10
# plot the actual data from 2011 to 2022
plt.scatter(rel sales df['Year'], rel sales df['Combustion ratio'],

color=color_map['blue'], s=dot_size)

plt.scatter(rel_sales_df['Year'], rel_sales_df['Hybrid_ratio'],__
 plt.scatter(rel_sales_df['Year'], rel_sales_df['Electric_ratio'],__

¬color=color_map['green'], s=dot_size)
plt.scatter(rel_sales_df['Year'], rel_sales_df['Station Locations Ratio'], u

¬color=color_map['red'], s=dot_size)
# plot the future predictions
plt.plot(model_yrs, model_C, label='Combustion Model', color=color_map['blue'])
```

```
plt.plot(model_yrs, model_H, label='Hybrid Model', color=color_map['orange'])
plt.plot(model_yrs, model_E, label='Electric Model', color=color_map['green'])
plt.plot(model_yrs, model_S, label='Charging Stations Model', u
 # plot a vertical line to demonstrate where the future predictions start
plt.vlines(2022, 0, 1, linestyles='dashed', color='black', label='2022')
# set other model parameters
plt.xlabel("Year")
plt.ylabel("Percentage of Total Sales")
plt.legend()
plt.title("Model Predictions from 2022 to 2050")
plt.show()
# print how accurate the model fits the data as of 2022
ind_2022 = np.argsort(np.abs(ts + 2011 - 2022))[0]
print("model_C in 2022:", model_C[ind_2022])
print("actualC in 2022:", C[-1])
print("model_H in 2022:", model_H[ind_2022])
print("actualH in 2022:", H[-1])
print("model_E in 2022:", model_E[ind_2022])
print("actualE in 2022:", E[-1])
print("model_S in 2022:", model_S[ind_2022])
print("actualS in 2022:", S[-1])
```