CS 591.03 Introduction to Data Mining Instructor: Abdullah Mueen

LECTURE 3: DATA TRANSFORMATION AND DIMENSIONALITY REDUCTION



Chapter 3: Data Preprocessing

Data Preprocessing: An Overview

- Data Quality
- Major Tasks in Data Preprocessing

Data Cleaning

Data Integration

Data Reduction

Summary

Data Quality: Why Preprocess the Data?

Measures for data quality: A multidimensional view

- Accuracy: correct or wrong, accurate or not
- Completeness: not recorded, unavailable, ...
- Consistency: some modified but some not, dangling, ...
- Timeliness: timely update?
- Believability: how trustable the data are correct?
- Interpretability: how easily the data can be understood?

Major Tasks in Data Preprocessing

Data cleaning

 Fill in missing values, smooth noisy data, identify or remove outliers, and resolve inconsistencies

Data integration

Integration of multiple databases, data cubes, or files

Data reduction

- Dimensionality reduction
- Numerosity reduction
- Data compression

Data transformation and data discretization

- Normalization
- Concept hierarchy generation

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Data Cleaning

Data in the Real World Is Dirty: Lots of potentially incorrect data, e.g., instrument faulty, human or computer error, transmission error

- incomplete: lacking attribute values, lacking certain attributes of interest, or containing only aggregate data
 - e.g., Occupation = "" (missing data)
- noisy: containing noise, errors, or outliers
 - e.g., Salary = "-10" (an error)
- inconsistent: containing discrepancies in codes or names, e.g.,
 - Age = "42", Birthday = "03/07/2010"
 - Was rating "1, 2, 3", now rating "A, B, C"
 - discrepancy between duplicate records
- Intentional (e.g., disguised missing data)
 - Jan. 1 as everyone's birthday?

Incomplete (Missing) Data

Data is not always available

 E.g., many tuples have no recorded value for several attributes, such as customer income in sales data

Missing data may be due to

- equipment malfunction
- inconsistent with other recorded data and thus deleted
- data not entered due to misunderstanding
- certain data may not be considered important at the time of entry
- not register history or changes of the data

Missing data may need to be inferred

How to Handle Missing Data?

Ignore the tuple: usually done when class label is missing (when doing classification)—not effective when the % of missing values per attribute varies considerably

Fill in the missing value manually: tedious + infeasible?

Fill in it automatically with

- a global constant : e.g., "unknown", a new class?!
- the attribute mean
- the attribute mean for all samples belonging to the same class: smarter
- the most probable value: inference-based such as Bayesian formula or decision tree

Noisy Data

Noise: random error or variance in a measured variable

Incorrect attribute values may be due to

- faulty data collection instruments
- data entry problems
- data transmission problems
- technology limitation
- inconsistency in naming convention

Other data problems which require data cleaning

- duplicate records
- incomplete data
- inconsistent data

How to Handle Noisy Data?

Binning

- first sort data and partition into (equal-frequency) bins
- then one can smooth by bin means, smooth by bin median, smooth by bin boundaries, etc.

Regression

smooth by fitting the data into regression functions

Clustering

detect and remove outliers

Combined computer and human inspection

detect suspicious values and check by human (e.g., deal with possible outliers)

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Data Reduction Strategies

Data reduction: Obtain a reduced representation of the data set that is much smaller in volume but yet produces the same (or almost the same) analytical results

Why data reduction? — A database/data warehouse may store terabytes of data. Complex data analysis may take a very long time to run on the complete data set.

Data reduction strategies

- Dimensionality reduction, e.g., remove unimportant attributes
 - Wavelet transforms
 - Principal Components Analysis (PCA)
 - Feature subset selection, feature creation
- Numerosity reduction (some simply call it: Data Reduction)
 - Regression and Log-Linear Models
 - Histograms, clustering, sampling
- Data compression

Data Reduction 1: Dimensionality Reduction

Curse of dimensionality

- When dimensionality increases, data becomes increasingly sparse
- Density and distance between points, which is critical to clustering, outlier analysis, becomes less meaningful
- The possible combinations of subspaces will grow exponentially

Dimensionality reduction

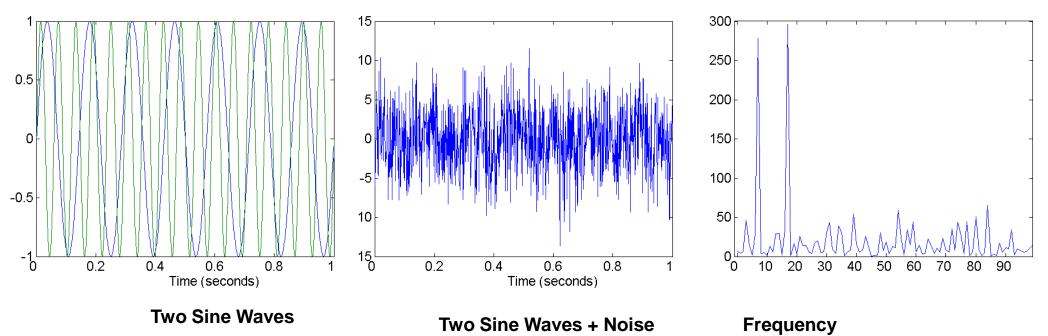
- Avoid the curse of dimensionality
- Help eliminate irrelevant features and reduce noise
- Reduce time and space required in data mining
- Allow easier visualization

Dimensionality reduction techniques

- Wavelet transforms
- Principal Component Analysis
- Supervised and nonlinear techniques (e.g., feature selection)

Mapping Data to a New Space

- Fourier transform
- Wavelet transform



What Is Wavelet Transform?

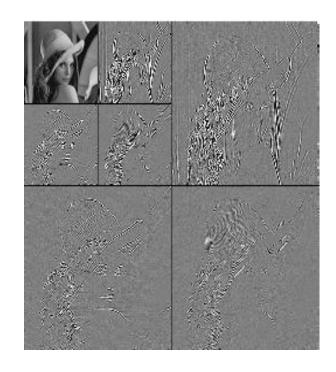
Decomposes a signal into different frequency subbands

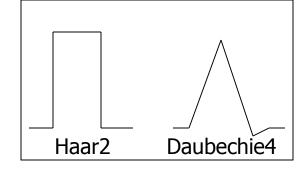
Applicable to n-dimensional signals

Data are transformed to preserve relative distance between objects at different levels of resolution

Allow natural clusters to become more distinguishable

Used for image compression





Wavelet Transformation

Discrete wavelet transform (DWT) for linear signal processing, multi-resolution analysis

Compressed approximation: store only a small fraction of the strongest of the wavelet coefficients

Similar to discrete Fourier transform (DFT), but better lossy compression, localized in space

Method:

- Length, L, must be an integer power of 2 (padding with 0's, when necessary)
- Each transform has 2 functions: smoothing, difference
- Applies to pairs of data, resulting in two set of data of length L/2
- Applies two functions recursively, until reaches the desired length

Wavelet Decomposition

Wavelets: A math tool for space-efficient hierarchical decomposition of functions

$$S = [2, 2, 0, 2, 3, 5, 4, 4]$$
 can be transformed to $S_{\wedge} = [2^{3}/_{4}, -1^{1}/_{4}, \frac{1}{2}, 0, 0, -1, -1, 0]$

Compression: many small detail coefficients can be replaced by 0's, and only the significant coefficients are retained

Resolution	Averages	Detail Coefficients
8	[2, 2, 0, 2, 3, 5, 4, 4]	
4	$[2,\ 1,\ 4,\ 4]$	[0,-1,-1,0]
2	$[1\frac{1}{2}, 4]$	$[\frac{1}{2}, 0]$
1	$[ilde{2}rac{3}{4}]$	$\left[-1\frac{1}{4}\right]$

Example Steps for Haar transform in MATLAB

```
N = [sqrt(8), sqrt(8), 2, 2, sqrt(2), sqrt(2), sqrt(2), sqrt(2)];

H_8 = [1 1 1 1 1 1 1 1; 1 1 1 1 -1 -1 -1 -1; 1 1 -1 -1 0 0 0 0; 0 0 0 0 1 1 -1 -1; 1 -1 0 0 0 0 0; 0 0 0 1 -1 0 0; 0 0 0 0 0 1 -1];

X = x*H_8'./N;

Y = y*H_8'./N;

sum((X-Y).^2)

sum((x-y).^2)
```

Why Wavelet Transform?

Use hat-shape filters

- Emphasize region where points cluster
- Suppress weaker information in their boundaries

Effective removal of outliers

Insensitive to noise, insensitive to input order

Multi-resolution

Detect arbitrary shaped clusters at different scales

Efficient

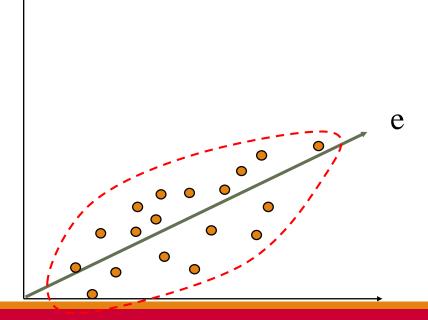
Complexity O(N)

Only applicable to low dimensional data

Principal Component Analysis (PCA)

Find a projection that captures the largest amount of variation in data

The original data are projected onto a much smaller space, resulting in dimensionality reduction. We find the eigenvectors of the covariance matrix, and these eigenvectors define the new space †



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Example: Steps for PCA in Matlab

```
X(1,:) = round(sin(0:2*pi+1)*1000) + rand(1,8)*100
X(2,:) = round(sin(0:2*pi+1)*1000) + rand(1,8)*100
X(3,:) = round(sin(0:2*pi+1)*1000) + rand(1,8)*100
X(4,:) = round(sin(0:2*pi+1)*1000) + rand(1,8)*100
X(5,:) = round(sin(0:5/2:(5*pi+4))*200) + rand(1,8)*100
X(6,:) = round(sin(0:5/2:(5*pi+4))*200) + rand(1,8)*100
X(7,:) = round(sin(0:5/2:(5*pi+4))*200) + rand(1,8)*100
X(8,:) = round(sin(0:5/2:(5*pi+4))*200) + rand(1,8)*100
plot(X')
for i = 1:8
          X(i.:) = zNorm(X(i.:)):
end
C = (X*X')
[V,D] = eig(C);
V(:,7)
X*V(:,7)
plot(X*V(:,7),X*V(:,8),'*')
```

```
function y = zNorm(x)

y = (x-mean(x))./std(x,1);
```

Principal Component Analysis (Steps)

Given N data vectors from n-dimensions, find $k \le n$ orthogonal vectors (principal components) that can be best used to represent data

- Normalize input data: Each attribute falls within the same range
- Compute k orthonormal (unit) vectors, i.e., principal components
- Each input data (vector) is a linear combination of the k principal component vectors
- The principal components are sorted in order of decreasing "significance" or strength
- Since the components are sorted, the size of the data can be reduced by eliminating the *weak* components, i.e., those with low variance (i.e., using the strongest principal components, it is possible to reconstruct a good approximation of the original data)

Works for numeric data only

Attribute Subset Selection

Another way to reduce dimensionality of data

Redundant attributes

- Duplicate much or all of the information contained in one or more other attributes
- E.g., purchase price of a product and the amount of sales tax paid

Irrelevant attributes

- Contain no information that is useful for the data mining task at hand
- E.g., students' ID is often irrelevant to the task of predicting students' GPA

Heuristic Search in Attribute Selection

There are 2^d possible attribute combinations of d attributes

Typical heuristic attribute selection methods:

- Best single attribute under the attribute independence assumption: choose by significance tests
- Best step-wise feature selection:
 - The best single-attribute is picked first
 - Then next best attribute condition to the first, ...
- Step-wise attribute elimination:
 - Repeatedly eliminate the worst attribute
- Best combined attribute selection and elimination
- Optimal branch and bound:
 - Use attribute elimination and backtracking

Attribute Creation (Feature Generation)

Create new attributes (features) that can capture the important information in a data set more effectively than the original ones

Three general methodologies

- Attribute extraction
 - Domain-specific
- Mapping data to new space (see: data reduction)
 - E.g., Fourier transformation, wavelet transformation, manifold approaches (not covered)
- Attribute construction
 - Combining features (see: discriminative frequent patterns in Chapter on "Advanced Classification")
 - Data discretization

Data Reduction 2: Numerosity Reduction

Reduce data volume by choosing alternative, *smaller forms* of data representation

Parametric methods (e.g., regression)

- Assume the data fits some model, estimate model parameters, store only the parameters, and discard the data (except possible outliers)
- Ex.: Log-linear models—obtain value at a point in m-D space as the product on appropriate marginal subspaces

Non-parametric methods

- Do not assume models
- Major families: histograms, clustering, sampling, ...

Parametric Data Reduction: Regression and Log-Linear Models

Linear regression

- Data modeled to fit a straight line
- Often uses the least-square method to fit the line

Multiple regression

 Allows a response variable Y to be modeled as a linear function of multidimensional feature vector

Log-linear model

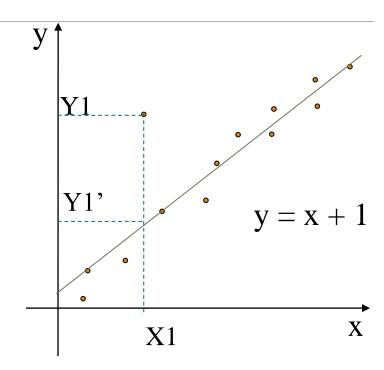
Approximates discrete multidimensional probability distributions

Regression Analysis

Regression analysis: A collective name for techniques for the modeling and analysis of numerical data consisting of values of a *dependent variable* (also called *response variable* or *measurement*) and of one or more *independent variables* (aka. *explanatory variables* or *predictors*)

The parameters are estimated so as to give a "best fit" of the data

Most commonly the best fit is evaluated by using the *least* squares method, but other criteria have also been used



Used for prediction (including forecasting of time-series data), inference, hypothesis testing, and modeling of causal relationships

Regress Analysis and Log-Linear Models

Linear regression: Y = w X + b

- Two regression coefficients, w and b, specify the line and are to be estimated by using the data at hand
- Using the least squares criterion to the known values of Y_1 , Y_2 , ..., X_1 , X_2 ,

Multiple regression: $Y = b_0 + b_1 X_1 + b_2 X_2$

Many nonlinear functions can be transformed into the above

Log-linear models:

- Approximate discrete multidimensional probability distributions
- Estimate the probability of each point (tuple) in a multi-dimensional space for a set of discretized attributes,
 based on a smaller subset of dimensional combinations
- Useful for dimensionality reduction and data smoothing

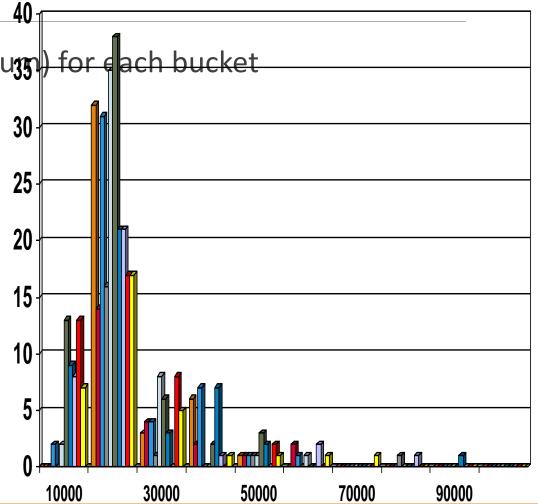
Histogram Analysis

Divide data into buckets and store average (sum) for each bucket

Partitioning rules:

Equal-width: equal bucket range

Equal-frequency (or equal-depth)



Clustering

Partition data set into clusters based on similarity, and store cluster representation (e.g., centroid and diameter) only

Can be very effective if data is clustered but not if data is "smeared"

Can have hierarchical clustering and be stored in multi-dimensional index tree structures

There are many choices of clustering definitions and clustering algorithms

Cluster analysis will be studied in depth in Chapter 10

Sampling

Sampling: obtaining a small sample s to represent the whole data set N

Allow a mining algorithm to run in complexity that is potentially sub-linear to the size of the data

Key principle: Choose a representative subset of the data

- Simple random sampling may have very poor performance in the presence of skew
- Develop adaptive sampling methods, e.g., stratified sampling:

Note: Sampling may not reduce database I/Os (page at a time)

Types of Sampling

Simple random sampling

There is an equal probability of selecting any particular item

Sampling without replacement

Once an object is selected, it is removed from the population

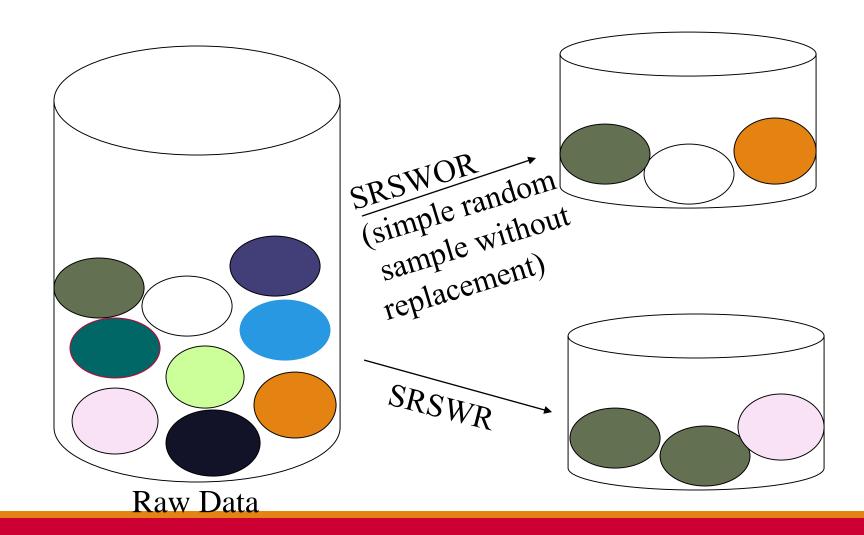
Sampling with replacement

A selected object is not removed from the population

Stratified sampling:

- Partition the data set, and draw samples from each partition (proportionally, i.e., approximately the same percentage of the data)
- Used in conjunction with skewed data

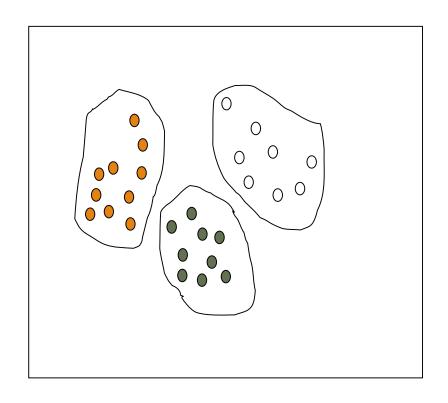
Sampling: With or without Replacement

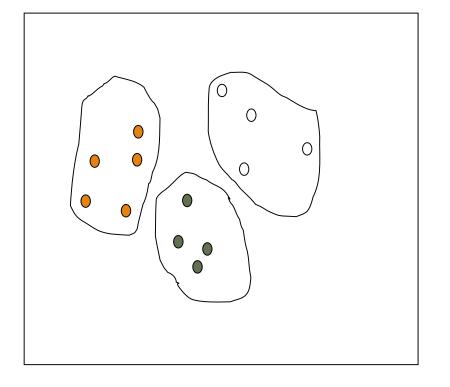


Sampling: Cluster or Stratified Sampling

Raw Data

Cluster/Stratified Sample





Data Reduction 3: Data Compression

String compression

- There are extensive theories and well-tuned algorithms
- Typically lossless, but only limited manipulation is possible without expansion

Audio/video compression

- Typically lossy compression, with progressive refinement
- Sometimes small fragments of signal can be reconstructed without reconstructing the whole

Time sequence is not audio

Typically short and vary slowly with time

Dimensionality and numerosity reduction may also be considered as forms of data compression

Data Compression

