More Fun With Automata Homework 2, CS500, Fall 2014

Aaron Gonzales, group 16

January 26, 2015

Ex 7

Show that if L is regular then L is regular. Why does it not suffice to use the fact that the regular languages are closed under concatenation and union?

Answer:

Ex 8

Given a string w , let w^R denote w written in reverse. Given a language L, let $L^R=\{w^R|w\in L\}$. Prove that L is regular if and only if L^R is regular. Why is this harder to prove with DFAs?

Answer:

Ex 12

Given a language L, let L1/2 denote the set of words that can appear as first halves of words in L:

$$L_{1/2} = \{x | \exists y : |x| = |y| \text{ and } xy \in L\}$$

where |w| denotes the length of a word w. Prove that if L is regular, then $L_{1/2}$ is regular. Generalize this to $L_{1/3}$, the set of words that can appear as middle thirds of words in L:

$$L_{1/3} = \{ y | \exists x, z : |x| = |y| = |z| \text{ and } xyz \in L \}$$

nswer:	
x 9	
A for-all NFA is one such that $L(M)$ is the set of strings where every computation path ends in a accepting state. Show how to simulate an for-all NFA with a DFA, and thus prove that a language recognized by some for-all NFA if and only if it is regular.	n s
nswer:	
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Answer:	
Ex 14	
Describe the equivalence classes of the three languages from Exercise 2. Use them to give the minimal DFA for each language, or prove that the DFA you designed before is minimal.	
Answer:	
Ex 20	
$ ext{Ex } ext{20}$ Consider the language	

What are its equivalence classes? What does its minimal infinite-state machine look like?

Answer:		