

# PlaidML & Stripe

Model-guided Optimization & Polyhedral IR

**Brian Retford** 

## PlaidML: Tile DSL

#### **Tensor DSLs**

Compiler	Matrix Multiplication in Native DSL
PlaidML	C[i, j: I, J] = +(A[i, k] * B[k, j]);
(taco)	c(i, j) = a(i,k) * b(k,j)
TVM	tvm.sum(a[i, k] * b[j, k], axis=k)
Tensor Comprehensions	C(i, j) +=! A(i, k) * B(k, j)

#### Tile: Automatic Differentiation

```
... start with a dilated & strided convolution:
function (I[N, H, W, CI], K[KH, KW, CI, CO]) -> (O) {
   O[n, v, x, co: N, H/3, W/3, CO] =
    +(I[n, 3*y + 2*i, 3*x + 2*i, ci] * K[i, i, ci, co]);
... DI/DO is obtained by swapping the input I and the output O:
function (DO[N, OH, OW, CO], K[KH, KW, CI, CO]) -> (DI) {
   DI[n, 3*y + 2*i, 3*x + 2*i, ci: N, 3*OH, 3*OW, CI] =
    +(DO[n, y, x, co] * K[i, i, ci, co]);
```

## PlaidML v0

i.e., the currently available one

#### PlaidML v0.x: Summary

- https://github.com/plaidml/plaidml
- Open source, Apache 2 (new), supports training & inference
- Reasonable community starting to build on GitHub, 1600 stars
- Supports most popular frameworks (except training via pyTorch) via upcoming nGraph integration
- Performance portable for major GPU architectures
  - Fixed Optimization passes, Minimal hardware config
  - Between .5-1.5x as fast as AutoTVM
- Not well suited for deep learning accelerators or other architectures that benefit from micro-kernels



#### PlaidML v0: Optimization

Fixed passes, locally optimal, config driven

#### Vectorize

• Find a stride-1 dimension such that v = N^2 : v < vec size, constrain tiling to multiples of v

#### Tile

• For each index hill climb and use cost model to maximize reuse while fitting in cache & registers

#### Load

• Create a loading pattern designed to minimize bank conflicts for any number of parallel readers

#### Loop

Order loops using a topological ordering to maximize cache reuse

#### Thread

• Rollup as many inner loops into hardware threads as possible

"settings": {
 "threads": 256,
 "vec\_size": 1,
 "mem\_width": 128,
 "max\_mem": 32768,
 "max\_regs": 16384,
 "goal\_groups": 16,
 "goal\_flops\_per\_byte": 50

## PlaidML v1: Stripe

Extending PlaidML to encompass the modern accelerator landscape

#### PlaidML v1 / Stripe

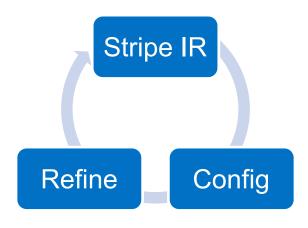
- Stripe enables:
  - Arbitrary tensorization
  - Complex vertical fusion
  - Arbitrarily complex memory hierarchies
  - Heterogenous compute topologies
  - Detailed performance / cost estimates
  - Software / hardware co-design

#### PlaidML v1 / Stripe: Polyhedral IR

PlaidML v1 introduces **Stripe**: a polyhedral IR that is highly amenable to optimization.

**Stripe** enables distinct passes that process stripe and emit more stripe

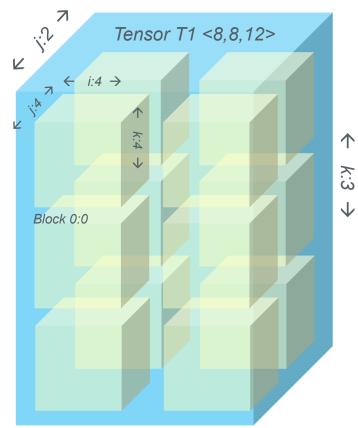
**Stripe** fundamentally represents operations over a polyhedral tensor space.



## Stripe in Depth

#### Stripe Conceptual Model

- Describes nested and repeated computational BLOCKS, each BLOCK represents a set of parallelizable computations
- BLOCKS are described by INDEXES and CONSTRAINTS that create polyhedral bounds over views of tensors called REFINEMENTS
- Nested BLOCKS have their own INDEXES
- Nested BLOCKS can create polyhedral sub regions of REFINEMENTS in the parent block by creating more REFINEMENTS which are automatically offset.
- The interior of a **BLOCK** nest contains code that is executed for every valid value of every **INDEX** of every containing **BLOCK**.



Block 0:

```
-0: #program block [] ( // layer test7
    none new@0x00000000<[0]>I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
    none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
      out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
         1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                     Tile Code
        out<[0]>01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
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       0: \$I = load(I)
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   0: #main block [] ( // main
       in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
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Tags

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                                                                                                      Indexes
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, xx/1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
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        out<[0]> 01[x, y, co]:add i8(1:65536, 1.01)
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  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
      out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
        1024 - kx - x >= 0
        -1 + ky + y >= 0
        1024 - ky - y >= 0
         out<[0]>01[x, v, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: K1 = load(K1)
       2: $01 = mul($I, $K1)
       3: 01 = store(\$01)
```

```
-0: #program block [] ( // layer test7
    none new@0x00000000<[0]>I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
    none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
      out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
         1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                     Tile Code
        out<[0]>01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: K1 = load(K1)
       2: $01 = mul($I, $K1)
       3: 01 = store($01)
```

```
-0: #program block [] ( // laver test7
     none new@0x00000000<[0]> I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
     none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
       out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new@0x00000000<[0]>01[0, 0, 0] i8(1024:65536, 1024:64, 64:1)
     0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
        1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                    Tile Code
        out<[0]> 01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1+kx+x,-1+ky+y,ci] i8(1:32768, 1:32, 1:1)
        in<[0]> K1[kx, ky, ci, co i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: $K1 = load(K1)
                                    Aggregators
       2: $01 = mul($I, $K1)
       3: 01 = store($01)
```

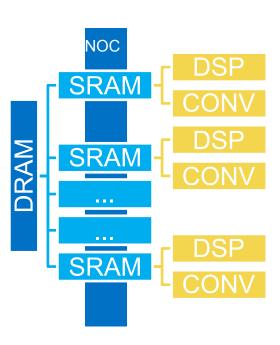
```
-0: #program block [] ( // layer test7
    none new@0x00000000<[0]>I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
    none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
      out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
         1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                     Tile Code
        out<[0]>01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: K1 = load(K1)
       2: $01 = mul($I, $K1)
       3: 01 = store($01)
```

```
-0: #program block [] ( // layer test7
    none new@0x00000000<[0]>I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
    none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
       out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
        1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                     Tile Code
        out<[0]>01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: K1 = load(K1)
      2: $01 = mul($I, $K1)
       3: 01 = store($01)
                      SSA IL
```

```
-0: #program block [] ( // layer test7
    none new@0x00000000<[0]>I[\overline{0}, 0, 0] i8(1024:32768, 1024:32, 32:1)
    none new@0x00000000<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
    none new(0x00000000<[0]>03[0, 0, 0] is (1024:65536, 1024:64, 64:1)
  0: #main block [] ( // main
      in<[0]>I[0, 0, 0] i8(1024:32768, 1024:32, 32:1)
      in<[0]> K1[0, 0, 0, 0] i8(3:6144, 3:2048, 32:64, 64:1)
      out<[0]> 01[0, 0, 0]:assign i8(1024:65536, 1024:64, 64:1)
      none new(0x00000000<[0]>01[0, 0, 0] is (1024:65536, 1024:64, 64:1)
    0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, ky:3, x:1024, y:1024] (
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
         -1 + kx + x >= 0
         1024 - kx - x >= 0
         -1 + ky + y >= 0
        1024 - ky - y >= 0
                                                                                     Tile Code
        out<[0]>01[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
       0: \$I = load(I)
       1: K1 = load(K1)
       2: $01 = mul($I, $K1)
       3: 01 = store($01)
```

#### Stripe: Hardware Model

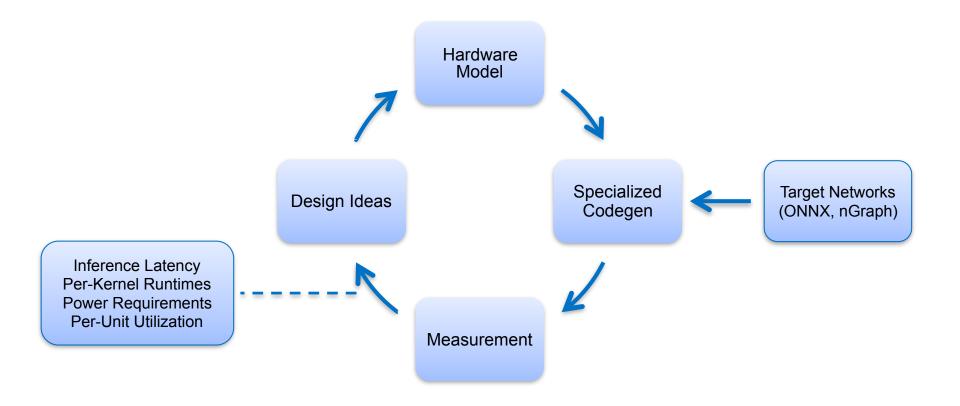
```
"clock mhz": {{ CLOCK MHZ }},
"mem units": {
   "DRAM": { "count": 1, "size KiB": 1048576 },
   "SRAM": { "count": {{ NUM SRAM }}, "size KiB": {{ SRAM SIZE KIB }} },
},
"exec units": {
   "DSP": { "count": {{NUM_DSP}}, "ops per cycle": 64 },
   "CONV": { "count": {{NUM CONV}}, "ops per cycle": 512, "pipeline depth": 2 }
},
"tx units": {
   "DMA": { "count": 1 },
   "NOC": { "count": 1 },
},
"buses": [
    { "sources": ["DRAM[0]"], "sinks": ["DMA[0]"], "bytes per cycle": 64 },
     "sources": ["DMA[0]"], "sinks": ["DRAM[0]"], "bytes per cycle": 64 },
        "sources": ["DMA[0]"],
        "sinks": [{% for i in range(NUM SRAM) %} "SRAM[{{i}}]"{endfor %}],
        "bytes per cycle": 64
   },
        "sources": ["NOC[0]"],
        "sinks": [{% for i in range(NUM SRAM) %} "SRAM[{{i}}}]"{% endfor %}],
        "bytes per cycle": 512
   },
```



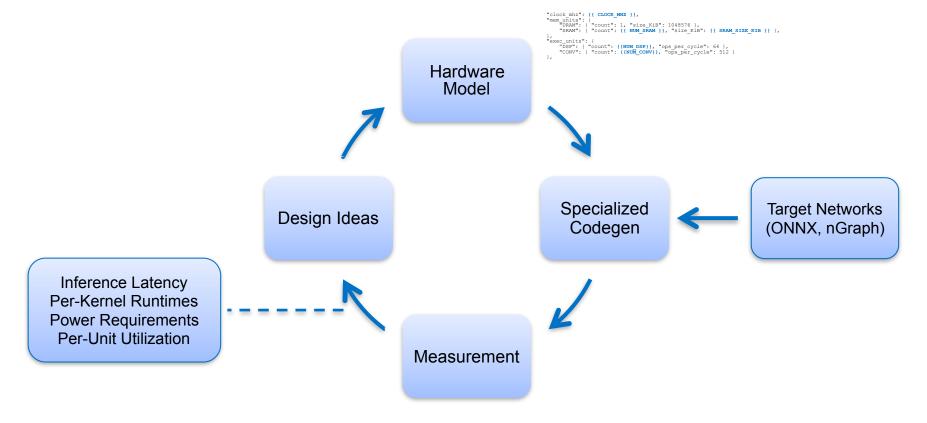
#### Stripe: Optimizer Config

```
"name": "fuse CONV add", "fusion": { "a reqs": ["CONV"], "b reqs": ["eltwise add"], "fused set": ["CONV"] } },
 "name": "fuse CONV zelu", "fusion": { "a reqs": ["CONV"], "b reqs": ["eltwise zelu"], "fused set": ["CONV"] } },
 "name": "fuse CONV", "fusion": { "parent reqs": ["CONV"], "fused set": ["CONV inner"] } },
 "name": "localize main", "localize": { "reqs": ["main"] } },
{ "name": "scalarize main", "scalarize": { "reqs": ["main"] } },
{ "name": "loc CONV", "locate block": { "reqs": ["CONV"], "loc": { "name": "CONV" } } },
 "name": "loc pool", "locate block": { "reqs": ["agg op max"], "loc": { "name": "DSP" } } },
 "name": "loc eltwise", "locate block": { "reqs": ["eltwise"], "loc": { "name": "DSP" } } },
  "name": "deps main", "compute deps": { "reqs": ["main"] } },
    "name": "schedule main",
    "schedule": {
        "regs": ["main"],
        "mem loc": { "name": "SRAM" },
        "mem KiB": {{ SRAM SIZE KIB / NUM SRAM }},
        "alignment": 16,
        "xfer loc": { "name": "DMA" },
        "allow out of range accesses": true,
        "num banks": {{ NUM SRAM }}
},
{ "name": "place program", "memory placement": { "reqs": ["program"], "locs": [{ "name": "DRAM" }], "alignment": 4 } }
```

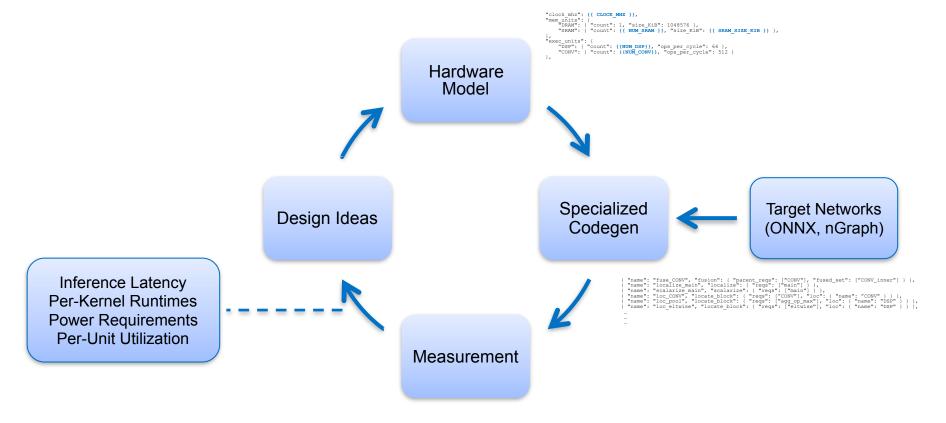
#### Stripe: Enabling Hardware / Software Co-Design



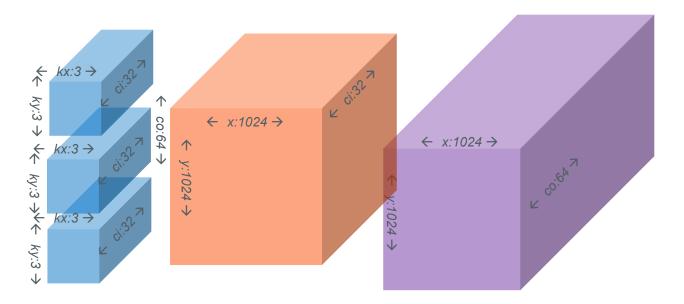
#### Stripe: Enabling Hardware / Software Co-Design

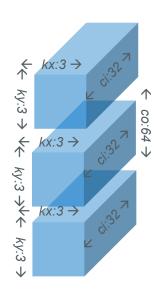


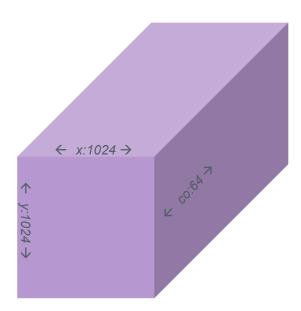
#### Stripe: Enabling Hardware / Software Co-Design

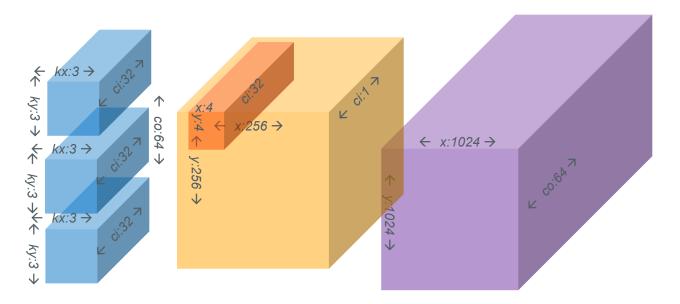


#### Stripe: Tensorization





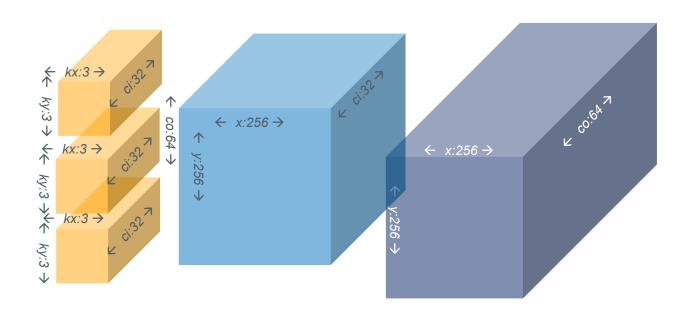




```
"tensorize": {
"regs": [ "agg op add", "comb op mul" ], "outer set": [ "CONV" ], "inner set": [ "CONV inner" ],
"stencils": [
 {"idxs": [{ "name": "i1", "size": 32, "outs": [-1], "ins": [-1, 0] }, { "name": "c", "size": -1, "outs": [0], "ins": [-1, -1] }]},
 {"idxs": [{ "name": "i1", "size": \frac{4}{4}, "outs": [-1], "ins": [-1, 0] }, { "name": "i2", "size": \frac{4}{4}, "outs": [-1], "ins": [0, -1] },
BEFORE:
0: #agg op add #comb op mul #contraction #kernel block [ci:32, co:64, kx:3, kv:3, x:1024, v:1024] ( // kernel 0
        // O1[x, y, co: X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
        out<[0]> O1[x, y, co]:add i8(1:65536, 1:64, 1:1)
        in<[0]>I[-1+kx+x,-1+ky+y,ci] i8(1:32768, 1:32, 1:1)
        in<[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:64, 1:1)
   ) {
     0: \$I = load(I); 1: \$K1 = load(K1); 2: \$01 = mul(\$I, \$K1); 3: \$01 = store(\$01)
AFTER:
0: #agg op add #comb op mul #contraction #CONV #kernel block [ci:1, co:1, kx:1, ky:1, x:256, y:256] ( // kernel 0
        // O1[x, y, co : X, Y, C2] = +(I[-1 + kx + x, -1 + ky + y, ci] * K1[kx, ky, ci, co])
        out<DRAM[0]> 01[4*x, 4*v, 16*col:add i8(4:65536, 4:64, 16:1)
        in < DRAM[0] > I[kx + 4*x, ky + 4*y, 32*ci] i8(4:32768, 4:32, 32:1)
        in<DRAM[0]> K1[kx, ky, 32*ci, 16*col i8(1:6144, 1:2048, 32:1, 16:32)
      0: #CONV inner block [ci:32, co:64, kx:3, ky:3, x:4, y:4] ( // kernel 0
          out<DRAM[0]> 01[x, y, co]:add i8(1:65536, 1:64, 1:1)
         in < DRAM[0] > I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 1:1)
         in<DRAM[0] > K1[kx, ky, ci, co] i8(1:6144, 1:2048, 1:1, 1:32)
     ) {
     0: \$I = load(I); 1: \$K1 = load(K1); 2: \$01 = mul(\$I, \$K1); 3: \$01 = store(\$01)
    } }
```

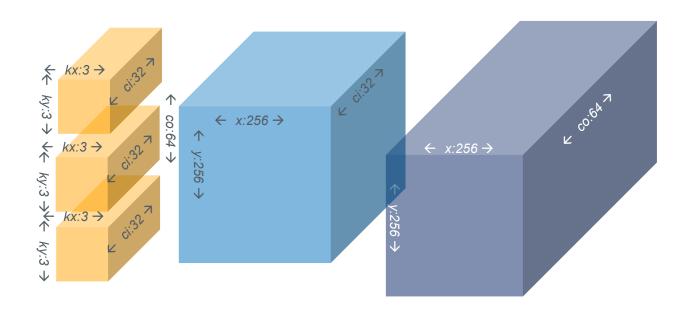
```
"autotile": {
   "reqs" : ["conv"], "outer_set" : ["conv"], "inner_set" : ["conv_inner"],
   "only_po2" : false,
   "memory" : "SRAM" // "pipeline_depth" : 2
}
```

```
"autotile": {
   "reqs" : ["conv"], "outer_set" : ["conv"], "inner_set" : ["conv_inner"],
   "only_po2" : false,
   "memory" : "SRAM" // "pipeline_depth" : 2
}
```



```
"autotile": {
   "reqs" : ["conv"], "outer_set" : ["conv"], "inner_set" : ["conv_inner"],
   "only_po2" : false,
   "memory" : "SRAM" // "pipeline_depth" : 2
}
```

kx	ky	ci	со	х	у	cost
1	1	32	4	8	8	120
1	1	16	8	8	8	140
1	1	32	5	4	4	270
3	3	32	1	6	6	310
3	3	16	1	9	9	340

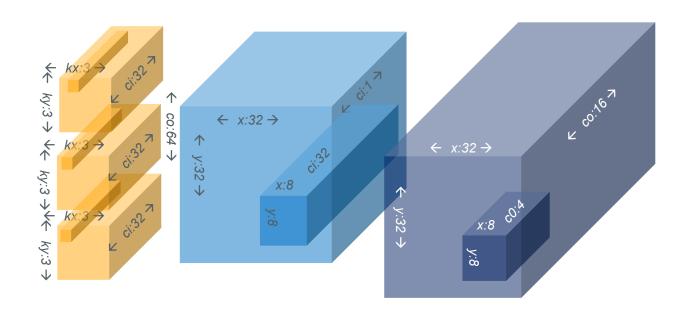


```
"autotile": {
   "reqs" : ["conv"], "outer_set" : ["conv"], "inner_set" : ["conv_inner"],
   "only_po2" : false,
   "memory" : "SRAM" // "pipeline_depth" : 2
```

kx	ky	ci	со	x	у	cost
1	1	32	4	8	8	120
1	1	16	8	8	8	140
1	1	32	5	4	4	270
3	3	32	1	6	6	310
3	3	16	1	9	9	340

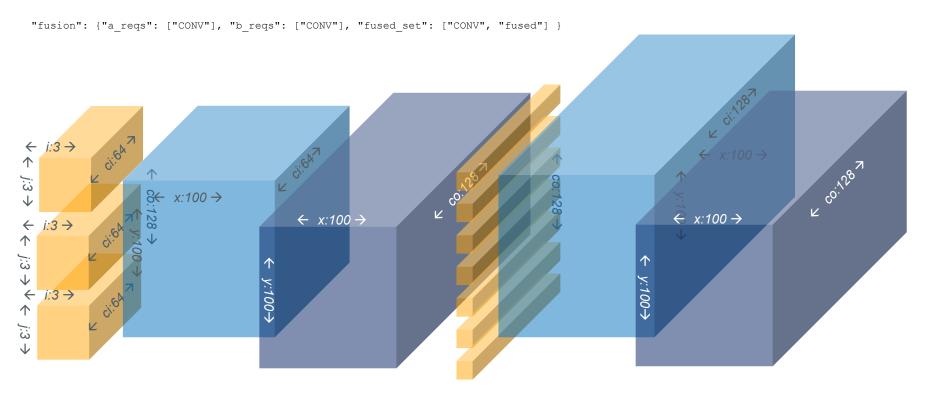
```
"autotile": {
   "reqs" : ["conv"], "outer_set" : ["conv"], "inner_set" : ["conv_inner"],
   "only_po2" : false,
   "memory" : "SRAM" // "pipeline_depth" : 2
}
```

kx	ky	ci	со	x	У	cost
1	1	32	4	8	8	120
1	1	16	8	8	8	140
1	1	32	5	4	4	270
3	3	32	1	6	6	310
3	3	16	1	9	9	340

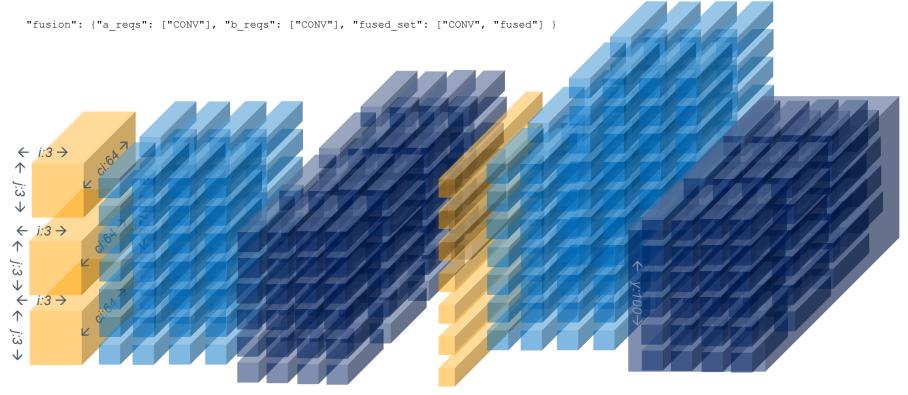


```
"autotile": {
  "reqs" : ["conv"], "outer set" : ["conv"], "inner set" : ["conv inner"],
  "only po2" : true,
  "memory": "SRAM" // "pipeline depth": 2
BEFORE:
0: #conv block<CONV[0]> [ci:32, co:64, kx:3, ky:3, x:256, y:256] (
       out<DRAM[0]> O1[co, x, y]:add i8(64:65536, 4:64, 4:1)
       in < DRAM[0] > I[kx + x - 1, ky + y - 1, ci] i8(4:32768, 4:32, 32:1)
       in<DRAM[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 32:1, 64:32)
) {
   0: \$I = load(I); 1: \$K1 = load(K1); 2: \$01 = mul(\$I, \$K1); 3: \$01 = store(\$01)
AFTER:
0: #conv block<CONV[0]> [ci:1, co:16, kx:3, ky:3, x:32, y:32] ( // kernel 0
    out<DRAM[0]> 01[8*x, 8*v, 4*co]:add i8(16:65536, 16:64, 64:1)
    in<DRAM[0]>I[kx + 8*x, ky + 8*y, ci] i8(16:32768, 16:32, 32:1)
    in<DRAM[0]> K1[kx, ky, ci, 4*co] i8(1:6144, 1:2048, 32:1, 64:32)
) {
   0: <Elided memory xfers>
    1: #conv inner block<CONV[0]> [ci:32, co:4, kx:1, ky:1, x:8, y:8] ( // No halos as the tiling makes lots of 1x1 convolutions
        out<SRAM[0]> 01[co, x, y]:add i8(4:65536, 8:64, 8:1)
        in < SRAM[0] > I[-1 + kx + x, -1 + ky + y, ci] i8(1:32768, 1:32, 32:1)
        in<SRAM[0]> K1[kx, ky, ci, co] i8(1:6144, 1:2048, 32:1, 4:32)
      0: \$I = load(I); 1: \$K1 = load(K1); 2: \$01 = mul(\$I, \$K1); 3: \$01 = store(\$01)
```

```
"fusion": {"a_reqs": ["CONV"], "b_reqs": ["CONV"], "fused_set": ["CONV", "fused"] }
```



```
"fusion": {"a_reqs": ["CONV"], "b_reqs": ["CONV"], "fused_set": ["CONV", "fused"] }
```



```
"fusion": {"a reqs": ["CONV"], "b reqs": ["CONV"], "fused set": ["CONV", "fused"] }
BEFORE:
0: #agg op add #comb op mul #CONV #contraction #kernel block [ci:64, co:128, i:3, j:3 x:100, y:100] ( // kernel 0
 // O1[x, y, co : X, Y, CO1] = +(In[-1 + i + x, -1 + j + y, ci] * K1[i, j, ci, co])
 ) {
    0: \sin = \operatorname{load}(\operatorname{In}); 1: K1 = \operatorname{load}(K1); 2: O1 = \operatorname{mul}(\operatorname{SIn}, K1); 3: O1 = \operatorname{store}(\operatorname{O1})
1: #agg op add #comb op mul #CONV #contraction #kernel block [ci:128, co:128, x:100, y:100] ( // kernel 1
  // O2[x, y, co : X, Y, CO2] = +(O1[i + x, j + y, ci] * K2[i, j, ci, co])
 ) {
    0: \$01 = 10ad(01); 1: \$K2 = 10ad(K2); 2: \$02 = mul(\$01, \$K2); 3: 02 = store(\$02)
AFTER:
0: #fused block [co:8, x:100, y:100] ( // kernel 0+kernel 1 ... ) {
  0: block [ci:64, co:16, i:3, j:3, x:1, v:1] (...) {
    out < SRAM[0] > 01[x, y, co]: add fp32(1:16, 1:16, 1:16, 1:1)
    in<[0]>In[-1+i+x,-1+j+y,ci] fp32(1:640000, 1:6400, 1:64, 1:1)
    in<[0]> K1[i, j, ci, co] fp32(1:24576, 1:8192, 1:128, 1:1)
    0: \sin = \operatorname{load}(\operatorname{In}); 1: K1 = \operatorname{load}(K1); 2: O1 = \operatorname{mul}(\operatorname{SIn}, K1); 3: O1 = \operatorname{store}(\operatorname{O1})
  1: block [ci:64, co:16, x:1, y:1] (...) {
    out<[0]> O2[x, y, co]:add fp32(1:1280000, 1:12800, 1:128, 1:1)
    in<SRAM[0]> 01[x, y, ci] fp32(1:16, 1:16, 1:16, 1:1)
    in<[0]> K2[0, 0, ci, co] fp32(1:16384, 1:16384, 1:128, 1:1)
    0: \$01 = 10ad(01); 1: \$K2 = 10ad(K2); 2: \$02 = mul(\$01, \$K2); 3: 02 = store(\$02)
```

### PlaidML v1.x / Stripe : Status

- Initial code upstreamed to public as of 0.5
  - Available at <a href="https://github.com/plaidml/plaidml">https://github.com/plaidml/plaidml</a>, inside the tile/stripe and tile/codegen directories
- Configurations for GPUs, CPUs & porting v0 to Stripe in progress
- Extensions for conditionals, loops, and indirection (scatter / gather) coming in v1
- Paper coming out early next year
- Specification available on request to: <u>tim.zerrell@intel.com</u>