5110_Final_Project

Bindu Latha Banisetti

4/25/2022

```
library(tidyverse)
## -- Attaching packages ------ 1.3.1 --
## v ggplot2 3.3.5
                             0.3.4
                   v purrr
## v tibble 3.1.6
                   v dplyr 1.0.8
## v tidyr 1.1.4
                  v stringr 1.4.0
          2.1.2
## v readr
                    v forcats 0.5.1
## -- Conflicts ------ tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(modelr)
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
      combine
library(randomForest)
## randomForest 4.7-1
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:gridExtra':
##
##
      combine
## The following object is masked from 'package:dplyr':
##
      combine
##
```

```
## The following object is masked from 'package:ggplot2':
##
##
       margin
library(glmnet)
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
## Loaded glmnet 4.1-4
library(caret)
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
       lift
library(broom)
## Attaching package: 'broom'
## The following object is masked from 'package:modelr':
##
##
       bootstrap
dir1 <- file.path("winequality-red.csv")</pre>
dir2 <- file.path("winequality-white.csv")</pre>
red_wine_df <- read.csv(dir1, header = TRUE, sep = ";")</pre>
white_wine_df <- read.csv(dir2, header = TRUE, sep = ";")</pre>
which(is.na(red_wine_df))
## integer(0)
which(is.na(white_wine_df))
## integer(0)
```

Stepwise Model Selection for red wine

```
#Partition of data
red_wine_std <- data.frame(scale(red_wine_df[1:11]))</pre>
red_wine_std$quality <- red_wine_df$quality</pre>
set.seed(10)
partition_rw <- resample_partition(red_wine_std,</pre>
                                 p=c(train=0.5,
                                     valid=0.25,
                                     test=0.25))
#Function to calculate the RMSE of the predictors
step <- function(response, predictors, candidates, partition)</pre>
 rhs <- paste0(paste0(predictors, collapse="+"), "+", candidates)</pre>
  formulas <- lapply(paste0(response, "~", rhs), as.formula)</pre>
 rmses <- sapply(formulas,</pre>
                  function(fm) rmse(lm(fm, data=partition$train),
                                     data=partition$valid))
  names(rmses) <- candidates</pre>
 attr(rmses, "best") <- rmses[which.min(rmses)]</pre>
}
model_rw <- NULL
preds <- "1"
cands <- c("fixed.acidity","volatile.acidity","citric.acid","residual.sugar",</pre>
           "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
           "pH", "sulphates", "alcohol")
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
          fixed.acidity volatile.acidity
                                                      citric.acid
                           0.7855048
##
              0.8515544
                                                          0.8398467
                                  chlorides free.sulfur.dioxide
##
         residual.sugar
                                  0.8472211
              0.8578792
                                                 0.8532622
##
## total.sulfur.dioxide
                                                                 рΗ
                                     density
                                  0.8376948
                                                        0.8553145
##
              0.8401893
##
              sulphates
                                     alcohol
                               0.7346630
              0.8296731
## attr(,"best")
## alcohol
## 0.734663
preds <- "alcohol"</pre>
cands <- c("fixed.acidity","volatile.acidity","citric.acid","residual.sugar",</pre>
           "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
           "pH", "sulphates")
s1 <- step("quality", preds, cands, partition_rw)</pre>
```

```
model_rw <- c(model_rw, attr(s1, "best"))</pre>
##
          fixed.acidity
                              volatile.acidity
                                                         citric.acid
##
               0.7226665
                                     0.6902853
                                                           0.7215572
##
         residual.sugar
                                     chlorides free.sulfur.dioxide
               0.7347169
                                     0.7342695
                                                           0.7340596
##
## total.sulfur.dioxide
                                       density
                                                                   рΗ
               0.7308255
                                     0.7322296
                                                           0.7188688
##
##
               sulphates
##
               0.7190395
## attr(,"best")
## volatile.acidity
          0.6902853
preds <- c("alcohol","volatile.acidity")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
           "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
            "pH", "sulphates")
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
          fixed.acidity
                                                      residual.sugar
##
                                   citric.acid
##
               0.6878592
                                     0.6903075
                                                           0.6911506
               chlorides free.sulfur.dioxide total.sulfur.dioxide
##
##
               0.6902750
                                    0.6890341
                                                           0.6862892
##
                 density
                                                           sulphates
                                            рΗ
                                   0.6877442
##
               0.6892822
                                                           0.6848121
## attr(,"best")
## sulphates
## 0.6848121
preds <- c("alcohol","volatile.acidity","sulphates")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
            "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
            ("Ha"
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
##
          fixed.acidity
                                   citric.acid
                                                      residual.sugar
##
               0.6831365
                                     0.6846930
                                                           0.6857594
               chlorides free.sulfur.dioxide total.sulfur.dioxide
##
##
               0.6831365
                                     0.6830200
                                                           0.6794726
##
                 density
                                            рΗ
##
               0.6849305
                                   0.6831672
## attr(,"best")
## total.sulfur.dioxide
               0.6794726
##
```

```
preds <- c("alcohol","volatile.acidity","sulphates","total.sulfur.dioxide")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
            "chlorides", "free.sulfur.dioxide", "density",
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
                                                   residual.sugar
                                                                              chlorides
##
         fixed.acidity
                                citric.acid
             0.6784623
                                  0.6795727
                                                        0.6805401
                                                                              0.6774864
## free.sulfur.dioxide
                                     density
                                                                Нq
             0.6806207
                                  0.6796242
                                                        0.6776286
## attr(,"best")
## chlorides
## 0.6774864
preds <- c("alcohol","volatile.acidity", "sulphates", "total.sulfur.dioxide", "chlorides")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
           "free.sulfur.dioxide", "density",
            ("Ha"
s1 <- step("quality", preds, cands, partition rw)</pre>
model rw <- c(model rw, attr(s1, "best"))</pre>
##
         fixed.acidity
                                 citric.acid
                                                   residual.sugar free.sulfur.dioxide
##
             0.6760903
                                  0.6775808
                                                        0.6785556
                                                                              0.6780041
               density
                                          Нq
             0.6776890
                                  0.6740840
## attr(,"best")
##
         Нq
## 0.674084
preds <- c("alcohol", "volatile.acidity", "sulphates", "total.sulfur.dioxide", "chlorides", "pH")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
            "free.sulfur.dioxide", "density")
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
##
         fixed.acidity
                                 citric.acid
                                                   residual.sugar free.sulfur.dioxide
##
                                   0.6737470
                                                        0.6752222
                                                                              0.6748061
             0.6741904
##
                density
##
             0.6747926
## attr(,"best")
## citric.acid
##
      0.673747
```

```
preds <- c("alcohol","volatile.acidity","sulphates","total.sulfur.dioxide",</pre>
            "chlorides", "pH", "citric.acid")
cands <- c("fixed.acidity", "residual.sugar",</pre>
           "free.sulfur.dioxide", "density")
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
         fixed.acidity
##
                              residual.sugar free.sulfur.dioxide
                                                                                 density
                                   0.6750824
##
             0.6735421
                                                        0.6743678
                                                                              0.6738133
## attr(,"best")
## fixed.acidity
       0.6735421
##
preds <- c("alcohol", "volatile.acidity", "sulphates", "total.sulfur.dioxide",</pre>
            "chlorides", "pH", "citric.acid", "fixed.acidity")
cands <- c("residual.sugar", "free.sulfur.dioxide", "density")</pre>
s1 <- step("quality", preds, cands, partition_rw)</pre>
model_rw <- c(model_rw, attr(s1, "best"))</pre>
##
        residual.sugar free.sulfur.dioxide
                                                           density
             0.6749624
                              0.6741934
                                                         0.6742341
##
## attr(,"best")
## free.sulfur.dioxide
             0.6741934
```

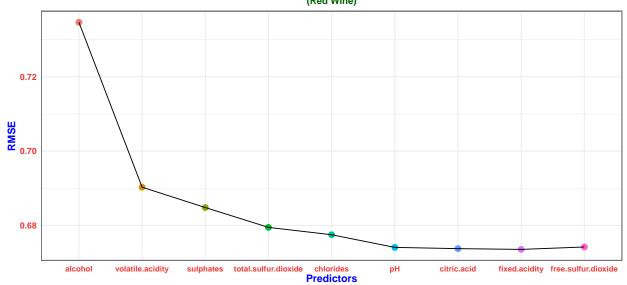
Model stopped improving at:

• fit = quality \sim alcohol + volatile acidity + sulphates + total sulfur dioxide + chlorides + pH + citric acid + fixed acidity

Visualizing how adding each variable affects the RMSE

```
color = "darkgreen",
                          face = "bold"),
axis.title = element text(color = "blue",
                          face = "bold",
                          size = 12),
axis.text.x = element_text(hjust = 0.5,
                          vjust = 0.5,
                           color = "brown2",
                          face = "bold",
                          size = 9),
axis.text.y = element_text(color = "brown2",
                           face = "bold",
                          size = 10),
panel.border = element_rect(colour = "grey45",
                           fill=NA, size=1),
legend.position = "none")
```

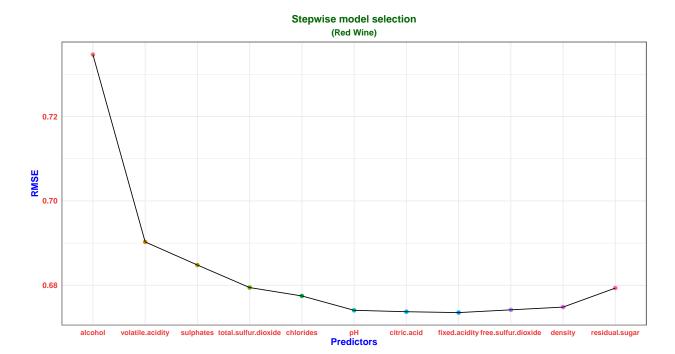
Stepwise model selection (Red Wine)



visualizing how each variable(including the predictors) affects the RMSE for Red wine

residual.sugar density

```
0.6748470
##
        0.6754391
## attr(,"best")
## density
## 0.674847
preds <- c("alcohol","volatile.acidity","sulphates","total.sulfur.dioxide",</pre>
           "chlorides", "pH", "citric.acid", "fixed.acidity", "free.sulfur.dioxide",
           "density")
cands <- c("residual.sugar")</pre>
s1 <- step("quality", preds, cands, partition_rw)</pre>
temp_model_rw <- c(temp_model_rw, attr(s1, "best"))</pre>
## residual.sugar
        0.6793522
## attr(,"best")
## residual.sugar
##
        0.6793522
#Representation of RMSE for all the variables
step_model_temp <- tibble(index=seq_along(temp_model_rw),</pre>
                     variable=factor(names(temp_model_rw), levels=names(temp_model_rw)),
                     RMSE=temp_model_rw)
ggplot(step_model_temp, aes(y=RMSE)) +
 geom_point(aes(x=variable, color = variable), size = 2) +
  geom_line(aes(x=index)) +
  theme_minimal()+
  labs(title = "Stepwise model selection",
               subtitle = "(Red Wine)",
               x = "Predictors",
               y = "RMSE") +
        theme(plot.title = element_text(hjust = 0.5,
                                          color = "darkgreen",
                                          face = "bold"),
              plot.subtitle = element_text(hjust = 0.5,
                                          color = "darkgreen",
                                          face = "bold"),
              axis.title = element_text(color = "blue",
                                          face = "bold",
                                         size = 12),
              axis.text.x = element text(hjust = 0.5,
                                         vjust = 0.5,
                                         color = "brown2",
                                         face = "bold",
                                          size = 9),
              axis.text.y = element_text(color = "brown2",
                                          face = "bold",
                                          size = 10),
              panel.border = element_rect(colour = "grey45",
                                          fill=NA, size=1),
              legend.position = "none")
```



Consider the following fits and extract the best fit model:

- fit1 <- quality ~ alcohol + volatile acidity + sulphates + total sulfur dioxide + chlorides + pH
- fit2 <- quality \sim alcohol + volatile acidity + sulphates + total sulfur dioxide + chlorides + pH + citric acid
- fit 3 <- quality \sim alcohol + volatile acidity + sulphates + total sulfur dioxide + chlorides + pH + citric acid + fixed acidity

Cross Validation

```
set.seed(2020)
#partition_rw_train <- red_wine_std[-partition_rw$test$idx,]
#redwine_cv <- crossv_kfold(partition_rw_train, 5)
#redwine_cv
redwine_cv <- crossv_kfold(red_wine_std, 5)
redwine_cv</pre>
```

```
## # A tibble: 5 x 3
## train test .id
## <named list> <named list> <chr>
## 1 <resample [1,279 x 12]> <resample [320 x 12]> 1
## 2 <resample [1,279 x 12]> <resample [320 x 12]> 2
## 3 <resample [1,279 x 12]> <resample [320 x 12]> 3
## 4 <resample [1,279 x 12]> <resample [320 x 12]> 4
## 5 <resample [1,280 x 12]> <resample [319 x 12]> 5
```

```
#Calculating RMSE for each fold of data
cv_rw <- redwine_cv %>%
 mutate(fit = purrr::map(train,
                   ~ lm(quality ~ alcohol + volatile.acidity + sulphates +
                          total.sulfur.dioxide + chlorides + pH, data = .)),
         rmse = purrr::map2_dbl(fit, test, ~ rmse(.x, .y)))
cv_rw
## # A tibble: 5 x 5
##
    train
                                                    .id
                                                          fit
                             test
                                                                        rmse
     <named list>
                             <named list>
                                                    <chr> <named list> <dbl>
## 1 <resample [1,279 x 12] > <resample [320 x 12] > 1
                                                          <lm>
                                                                       0.673
## 2 <resample [1,279 x 12] > <resample [320 x 12] > 2
                                                          <1m>
                                                                       0.659
## 3 <resample [1,279 x 12] > <resample [320 x 12] > 3
                                                          <1m>
                                                                       0.587
## 4 <resample [1,279 x 12]> <resample [320 x 12]> 4
                                                          <1m>
                                                                       0.670
## 5 <resample [1,280 x 12] > <resample [319 x 12] > 5
                                                          <lm>
                                                                       0.666
#Average of RMSEs
mean(cv_rw$rmse)
```

Comparing models using CV

[1] 0.650961

Calling the function

```
## # A tibble: 1 x 3
## cv_rmse cv_rsq cv_mae
      <dbl> <dbl> <dbl>
## 1 0.651 0.349 0.506
fit2_rmse
## # A tibble: 1 x 3
   cv_rmse cv_rsq cv_mae
      <dbl> <dbl> <dbl>
## 1 0.651 0.349 0.506
fit3_rmse
## # A tibble: 1 x 3
## cv_rmse cv_rsq cv_mae
     <dbl> <dbl> <dbl>
## 1 0.651 0.348 0.507
#Goodness of fit
gof_fs_rw <- lm( quality ~ alcohol + volatile.acidity + sulphates +</pre>
              total.sulfur.dioxide + chlorides + pH , red_wine_df)
glance(gof_fs_rw)
## # A tibble: 1 x 12
## r.squared adj.r.squared sigma statistic
                                         p.value
                                                   df logLik
                                                              AIC
                                                                   BIC
       <dbl>
                   <dbl> <dbl>
                               <dbl>
                                         <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                   147. 7.12e-149
       0.357
                    0.355 0.649
                                                    6 -1573. 3163. 3206.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
summary(gof_fs_rw)
##
## lm(formula = quality ~ alcohol + volatile.acidity + sulphates +
##
      total.sulfur.dioxide + chlorides + pH, data = red_wine_df)
##
## Residuals:
       Min
               1Q Median
                                3Q
## -2.60575 -0.35883 -0.04806 0.46079 1.95643
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
                     4.2957316  0.3995603  10.751  < 2e-16 ***
## (Intercept)
## alcohol
                    -1.0381945 0.1004270 -10.338 < 2e-16 ***
## volatile.acidity
## sulphates
                      ## total.sulfur.dioxide -0.0023721  0.0005064  -4.684  3.05e-06 ***
## chlorides -2.0022839 0.3980757 -5.030 5.46e-07 ***
                     ## pH
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.6487 on 1592 degrees of freedom
## Multiple R-squared: 0.3572, Adjusted R-squared: 0.3548
## F-statistic: 147.4 on 6 and 1592 DF, p-value: < 2.2e-16</pre>
```

Best fit model:

• quality ~ alcohol + volatile.acidity + sulphates + total.sulfur.dioxide + chlorides + pH

Stepwise Model Selection for white wine

```
##
        fixed.acidity
                         volatile.acidity
                                                 citric.acid
##
            0.9046956
                              0.9040842
                                                   0.9115613
##
        residual.sugar
                               chlorides free.sulfur.dioxide
##
            0.9083983
                              0.8910796
                                                  0.9115526
## total.sulfur.dioxide
                                                          рΗ
                                 density
                                                  0.9066175
##
            0.8967295
                              0.8741188
##
            sulphates
                                 alcohol
##
            0.9097914
                              0.8153880
## attr(,"best")
## alcohol
## 0.815388
```

```
model_ww <- c(model_ww, attr(s2, "best"))</pre>
##
          fixed.acidity
                              volatile.acidity
                                                         citric.acid
##
               0.8129728
                                     0.8013749
                                                            0.8146745
##
         residual.sugar
                                     chlorides free.sulfur.dioxide
               0.8095793
                                     0.8142981
                                                           0.8090157
##
## total.sulfur.dioxide
                                       density
                                                                   pН
               0.8153080
                                     0.8141830
                                                           0.8140691
##
##
               sulphates
##
               0.8129943
## attr(,"best")
## volatile.acidity
          0.8013749
preds <- c("alcohol","volatile.acidity")</pre>
cands <- c("fixed.acidity","citric.acid","residual.sugar",</pre>
            "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
            "pH", "sulphates")
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
          fixed.acidity
                                                      residual.sugar
##
                                   citric.acid
##
               0.7986474
                                     0.8022197
                                                            0.7901090
               chlorides free.sulfur.dioxide total.sulfur.dioxide
##
##
               0.8008642
                                     0.7956051
                                                           0.8001968
##
                 density
                                                           sulphates
                                            рΗ
##
               0.7969973
                                   0.8006140
                                                           0.7994550
## attr(,"best")
## residual.sugar
         0.790109
preds <- c("alcohol","volatile.acidity","residual.sugar")</pre>
cands <- c("fixed.acidity", "citric.acid",</pre>
            "chlorides", "free.sulfur.dioxide", "total.sulfur.dioxide", "density",
            "pH", "sulphates")
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
##
          fixed.acidity
                                   citric.acid
                                                            chlorides
##
               0.7866903
                                     0.7912216
                                                            0.7899837
    free.sulfur.dioxide total.sulfur.dioxide
##
                                                              density
##
               0.7870588
                                     0.7900478
                                                            0.7885526
##
                      рΗ
                                     sulphates
##
               0.7880903
                                     0.7879418
## attr(,"best")
## fixed.acidity
       0.7866903
##
```

```
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity")</pre>
cands <- c("citric.acid", "chlorides", "free.sulfur.dioxide",</pre>
           "total.sulfur.dioxide", "density", "pH", "sulphates")
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
##
            citric.acid
                                     chlorides free.sulfur.dioxide
##
              0.7875729
                                     0.7865390
                                                   0.7842173
## total.sulfur.dioxide
                                       density
                                                                  рH
              0.7865822
                                    0.7873280
                                                         0.7861562
##
              sulphates
              0.7845328
##
## attr(,"best")
## free.sulfur.dioxide
##
             0.7842173
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide")
cands <- c("citric.acid", "chlorides",</pre>
           "total.sulfur.dioxide", "density", "pH", "sulphates")
s2 <- step("quality", preds, cands, partition ww)
model ww <- c(model ww, attr(s2, "best"))</pre>
##
            citric.acid
                                     chlorides total.sulfur.dioxide
##
              0.7850955
                                    0.7840036
                                                         0.7837253
                                                          sulphates
##
                 density
                                            Нq
              0.7851699
##
                                   0.7837374
                                                          0.7822481
## attr(,"best")
## sulphates
## 0.7822481
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide", "sulphates")
cands <- c("citric.acid", "chlorides",</pre>
           "total.sulfur.dioxide", "density", "pH")
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
##
            citric.acid
                                     chlorides total.sulfur.dioxide
##
              0.7831977
                                    0.7820405
                                                           0.7813755
##
                 density
                                    0.7820393
              0.7827787
## attr(,"best")
## total.sulfur.dioxide
              0.7813755
##
```

```
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide", "sulphates", "total.sulfur.dioxide")
cands <- c("citric.acid", "chlorides",</pre>
           "density", "pH")
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
## citric.acid chlorides
                                 density
   0.7822786
                  0.7811962 0.7824629
                                          0.7810240
## attr(,"best")
         рΗ
##
## 0.781024
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide", "sulphates", "total.sulfur.dioxide", "pH")
cands <- c("citric.acid","chlorides","density")</pre>
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
s2
## citric.acid chlorides
                                 density
## 0.7819109
                  0.7808872
                              0.7861522
## attr(,"best")
## chlorides
## 0.7808872
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide", "sulphates", "total.sulfur.dioxide",
            "pH", "chlorides")
cands <- c("citric.acid", "density")</pre>
s2 <- step("quality", preds, cands, partition_ww)</pre>
model_ww <- c(model_ww, attr(s2, "best"))</pre>
## citric.acid
                    density
    0.7817750
                  0.7866456
## attr(,"best")
## citric.acid
##
      0.781775
```

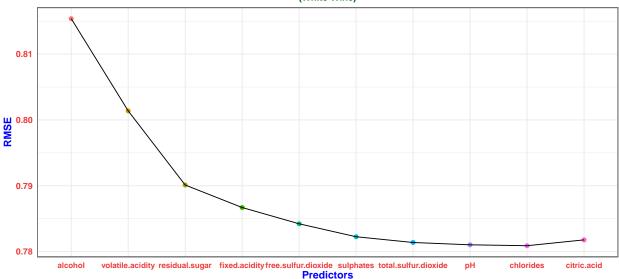
Model stopped improving at:

• fit = quality \sim alcohol + volatile acidity + residual sugar + fixed acidity + free sulfur dioxide + sulphates + total sulfur dioxide + pH + chlorides

Visualizing how adding each variable affects the RMSE.

```
step_model_ww <- tibble(index=seq_along(model_ww),</pre>
                     variable=factor(names(model_ww), levels=names(model_ww)),
                     RMSE=model_ww)
ggplot(step_model_ww, aes(y=RMSE)) +
  geom_point(aes(x=variable, color = variable), size = 2) +
  geom_line(aes(x=index)) +
 theme minimal()+
  labs(title = "Stepwise model selection",
               subtitle = "(White Wine)",
               x = "Predictors",
               y = "RMSE") +
        theme(plot.title = element_text(hjust = 0.5,
                                         color = "darkgreen",
                                         face = "bold"),
              plot.subtitle = element_text(hjust = 0.5,
                                         color = "darkgreen",
                                         face = "bold"),
              axis.title = element_text(color = "blue",
                                         face = "bold",
                                         size = 12),
              axis.text.x = element_text(hjust = 0.5,
                                         vjust = 0.5,
                                         color = "brown2",
                                         face = "bold",
                                         size = 9),
              axis.text.y = element_text(color = "brown2",
                                         face = "bold",
                                         size = 10),
              panel.border = element_rect(colour = "grey45",
                                         fill=NA, size=1),
              legend.position = "none")
```

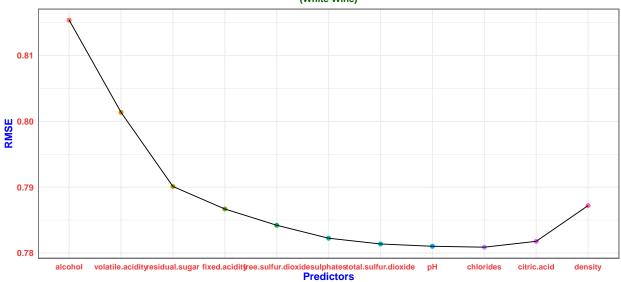
Stepwise model selection (White Wine)



visualizing how each variable(including the predictors) affects the RMSE for Red wine

```
temp model ww <- model ww
preds <- c("alcohol","volatile.acidity","residual.sugar","fixed.acidity",</pre>
           "free.sulfur.dioxide", "sulphates", "total.sulfur.dioxide",
           "pH", "chlorides", "citric.acid")
cands <- c("density")</pre>
s2 <- step("quality", preds, cands, partition_ww)</pre>
temp_model_ww <- c(temp_model_ww, attr(s2, "best"))</pre>
##
     density
## 0.7872114
## attr(,"best")
    density
## 0.7872114
step_model_ww_temp <- tibble(index=seq_along(temp_model_ww),</pre>
                     variable=factor(names(temp model ww), levels=names(temp model ww)),
                     RMSE=temp_model_ww)
ggplot(step_model_ww_temp, aes(y=RMSE)) +
  geom_point(aes(x=variable, color = variable), size = 2) +
  geom_line(aes(x=index)) +
  theme_minimal()+
  labs(title = "Stepwise model selection",
               subtitle = "(White Wine)",
               x = "Predictors",
               y = "RMSE") +
        theme(plot.title = element_text(hjust = 0.5,
                                         color = "darkgreen",
                                         face = "bold"),
              plot.subtitle = element_text(hjust = 0.5,
                                         color = "darkgreen",
                                         face = "bold"),
              axis.title = element_text(color = "blue",
                                         face = "bold",
                                         size = 12),
              axis.text.x = element_text(hjust = 0.5,
                                         vjust = 0.5,
                                          color = "brown2",
                                         face = "bold",
                                          size = 9),
              axis.text.y = element_text(color = "brown2",
                                          face = "bold",
                                         size = 10),
              panel.border = element_rect(colour = "grey45",
                                          fill=NA, size=1),
              legend.position = "none")
```





Consider the following fits and extract the best fit model:

- fit1 <- quality \sim alcohol + volatile.acidity + residual.sugar + fixed.acidity + free.sulfur.dioxide + sulphates + total.sulfur.dioxide + pH
- fit2 <- quality \sim alcohol + volatile.acidity + residual.sugar + fixed.acidity + free.sulfur.dioxide + sulphates + total.sulfur.dioxide + pH + chlorides

Cross Validation

```
set.seed(2020)
#partition_ww_train <- white_wine_std[-partition_ww$test$idx,]</pre>
#whitewine_cv <- crossv_kfold(partition_ww_train, 5)</pre>
#whitewine_cv
whitewine_cv <- crossv_kfold(white_wine_std, 5)</pre>
whitewine_cv
## # A tibble: 5 x 3
                                                      .id
##
     train
                              test
     <named list>
                               <named list>
## 1 <resample [3,918 x 12] > <resample [980 x 12] > 1
## 2 <resample [3,918 x 12] > <resample [980 x 12] > 2
## 3 <resample [3,918 x 12] > <resample [980 x 12] > 3
## 4 <resample [3,919 x 12] > <resample [979 x 12] > 4
## 5 <resample [3,919 x 12] > <resample [979 x 12] > 5
#Calculating RMSE for each fold of data
cv_rw <- whitewine_cv %>%
 mutate(fit = purrr::map(train,
```

~ lm(quality ~ alcohol + volatile.acidity + residual.sugar +

```
fixed.acidity + free.sulfur.dioxide +
                              sulphates + total.sulfur.dioxide + pH, data = .)),
         rmse = purrr::map2_dbl(fit, test, ~ rmse(.x, .y)))
cv_rw
## # A tibble: 5 x 5
##
    train
                                                    .id
                                                          fit
                             test
                                                                         rmse
                              <named list>
##
     <named list>
                                                    <chr> <named list> <dbl>
## 1 <resample [3,918 x 12] > <resample [980 x 12] > 1
                                                          <1m>
                                                                        0.747
## 2 <resample [3,918 x 12] > <resample [980 x 12] > 2
                                                          <1m>
                                                                        0.806
## 3 <resample [3,918 x 12] > <resample [980 x 12] > 3
                                                          <1m>
                                                                        0.743
## 4 <resample [3,919 x 12] > <resample [979 x 12] > 4
                                                          <1m>
                                                                        0.727
## 5 <resample [3,919 x 12] > <resample [979 x 12] > 5
                                                          <1m>
                                                                        0.762
#Average of RMSEs
mean(cv_rw$rmse)
```

Comparing models using CV

[1] 0.7568375

Calling the function

```
## # A tibble: 1 x 3
## cv_rmse cv_rsq cv_mae
## <dbl> <dbl> <dbl> <dbl> ## 1 0.757 0.269 0.588
```

```
fit2_rmse_ww
## # A tibble: 1 x 3
     cv_rmse cv_rsq cv_mae
##
      <dbl> <dbl> <dbl>
      0.757 0.269 0.588
## 1
Best fit Model
  • quality ~ alcohol + volatile.acidity + residual.sugar + fixed.acidity + free.sulfur.dioxide + sulphates
    + total.sulfur.dioxide + pH
fit_rw <- lm(quality ~ alcohol + volatile.acidity + sulphates + total.sulfur.dioxide + chlorides + pH,
summary(fit_rw)
##
## Call:
## lm(formula = quality ~ alcohol + volatile.acidity + sulphates +
       total.sulfur.dioxide + chlorides + pH, data = red_wine_std)
##
## Residuals:
##
       Min
                  1Q
                      Median
## -2.60575 -0.35883 -0.04806 0.46079 1.95643
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
                                    0.01622 347.419 < 2e-16 ***
## (Intercept)
                        5.63602
## alcohol
                         0.30976
                                    0.01791 17.291 < 2e-16 ***
## volatile.acidity
                        -0.18590 0.01798 -10.338 < 2e-16 ***
## sulphates
                                    0.01865
                                            8.076 1.31e-15 ***
                         0.15064
## total.sulfur.dioxide -0.07803
                                    0.01666 -4.684 3.05e-06 ***
## chlorides
                        -0.09424
                                    0.01874 -5.030 5.46e-07 ***
                                    0.01791 -3.750 0.000183 ***
## pH
                        -0.06719
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.6487 on 1592 degrees of freedom
## Multiple R-squared: 0.3572, Adjusted R-squared: 0.3548
## F-statistic: 147.4 on 6 and 1592 DF, p-value: < 2.2e-16
fit_ww <- lm(quality ~ alcohol + volatile.acidity + residual.sugar + fixed.acidity + free.sulfur.dioxid
summary(fit_ww)
##
## Call:
## lm(formula = quality ~ alcohol + volatile.acidity + residual.sugar +
##
       fixed.acidity + free.sulfur.dioxide + sulphates + total.sulfur.dioxide +
      pH, data = white_wine_std)
##
##
```

```
## Residuals:
##
      Min
                               30
               1Q Median
                                      Max
## -3.8931 -0.4982 -0.0358 0.4644 3.1821
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                        5.87791 0.01080 544.038 < 2e-16 ***
                                   0.01304 34.834 < 2e-16 ***
## alcohol
                        0.45433
## volatile.acidity
                       -0.19887
                                   0.01126 -17.665 < 2e-16 ***
## residual.sugar
                        0.13274
                                   0.01283 10.349 < 2e-16 ***
## fixed.acidity
                       -0.04222
                                   0.01220 -3.461 0.000542 ***
## free.sulfur.dioxide 0.08078
                                   0.01427
                                            5.662 1.58e-08 ***
                                   0.01108 4.273 1.97e-05 ***
## sulphates
                        0.04736
## total.sulfur.dioxide -0.03866
                                   0.01581 -2.445 0.014529 *
## pH
                        0.02708
                                   0.01240 2.184 0.029034 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.7561 on 4889 degrees of freedom
## Multiple R-squared: 0.2722, Adjusted R-squared: 0.2711
## F-statistic: 228.6 on 8 and 4889 DF, p-value: < 2.2e-16
#Data partition
#Redwine
set.seed(1)
train <- createDataPartition(red_wine_std$quality, p=0.6, list=FALSE)
table(red_wine_std$quality[train])
##
##
     3
        4
            5 6 7
##
     5 35 407 383 119 12
reddf_train <- red_wine_std[as.integer(train),]</pre>
reddf_test <- red_wine_std[-as.integer(train),]</pre>
#Whitewine
set.seed(1)
train_w <- createDataPartition(white_wine_std$quality, p=0.6, list=FALSE)
table(white_wine_std$quality[train_w])
##
##
     3
          4
             5
                    6
                         7
                              8
##
     14 101 869 1319 518 113
                                   5
whitedf_train <- white_wine_std[as.integer(train_w),]</pre>
whitedf_test <- white_wine_std[-as.integer(train_w),]</pre>
```

Random Forest Regression

#Red wine

```
fit_rw_rf <- randomForest(quality ~ alcohol + volatile.acidity +</pre>
                           sulphates + total.sulfur.dioxide +
                           chlorides + pH, reddf_train,
                         mtry = 3,
                         importance = TRUE,
                         na.action = na.omit)
summary(fit_rw_rf)
##
                  Length Class Mode
## call
                       -none- call
## type
                   1
                         -none- character
## predicted
                  961
                       -none- numeric
## mse
                  500 -none- numeric
## rsq
                  500 -none- numeric
## local*
                 961 -none- numeric
## localImportance 0 -none- NULL
                    O -none- NULL
## proximity
## ntree
                    1
                        -none- numeric
## mtry
                   1 -none- numeric
## forest
                  11 -none- list
                  0
## coefs
                         -none- NULL
                  961 -none- numeric
## y
## test
                  O -none- NULL
                  O -none- NULL
## inbag
## terms
                         terms call
fit_rw_rf_prediction<-predict(fit_rw_rf,newdata=reddf_test)</pre>
rf_rw_results<-as.data.frame(cbind(fit_rw_rf_prediction,reddf_test$quality))
colnames(rf_rw_results)<-c("prediction", "real")</pre>
{\it \#White\ Wine\ -\ Random\ forest\ regression}
fit_ww_rf <- randomForest(quality ~ alcohol + volatile.acidity +</pre>
                           residual.sugar + fixed.acidity +
                           free.sulfur.dioxide + sulphates +
                           total.sulfur.dioxide + pH, whitedf_train,
                         mtry = 3,
                         importance = TRUE,
                         na.action = na.omit)
fit_ww_rf
##
## randomForest(formula = quality ~ alcohol + volatile.acidity + residual.sugar + fixed.acidity +
##
                 Type of random forest: regression
                       Number of trees: 500
## No. of variables tried at each split: 3
##
```

```
## Mean of squared residuals: 0.4264972
## % Var explained: 47.14

fit_ww_rf_prediction<-predict(fit_ww_rf,newdata=whitedf_test)
rf_ww_results<-as.data.frame(cbind(fit_ww_rf_prediction,whitedf_test$quality))
colnames(rf_ww_results)<-c("prediction","real")</pre>
```

Ridge Regression

##

##

##

```
#Ridge regression for red wine
ctrl <- trainControl(method="repeatedcv", number=10, repeats=10)</pre>
grd <- expand.grid(lambda=exp(seq(from=-7, to=-2, length.out=20)),</pre>
             alpha=0)
set.seed(1)
fit_rw_ridge <- train(quality ~ alcohol + volatile.acidity +</pre>
                   sulphates + total.sulfur.dioxide +
                   chlorides + pH, data=reddf_train,
         method="glmnet",
         preProcess=c("center", "scale"),
         trControl=ctrl, tuneGrid=grd)
fit_rw_ridge
## glmnet
##
## 961 samples
##
   6 predictor
## Pre-processing: centered (6), scaled (6)
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 866, 865, 865, 865, 865, 865, ...
## Resampling results across tuning parameters:
##
##
   lambda
            RMSE
                    Rsquared
                           MAE
##
   ##
   ##
   ##
   ##
##
   0.003399216  0.6608113  0.3426984  0.5170648
##
   ##
   0.005753800 0.6608113 0.3426984 0.5170648
   ##
##
   ##
```

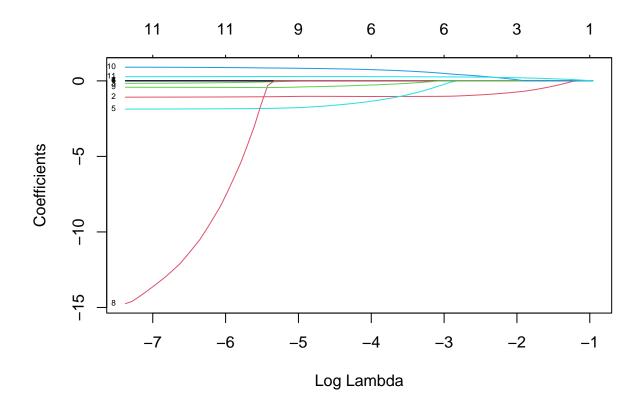
0.016485680 0.6608113 0.3426984 0.5170648

```
##
    ##
    ##
    ##
    0.079953042  0.6612124  0.3428183  0.5188810
##
    0.5199677
    ##
## Tuning parameter 'alpha' was held constant at a value of 0
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were alpha = 0 and lambda = 0.02790506.
#Ridge regression for white wine
ctrl <- trainControl(method="repeatedcv", number=10, repeats=10)</pre>
grd <- expand.grid(lambda=exp(seq(from=-7, to=-2, length.out=20)),</pre>
                 alpha=0)
set.seed(1)
fit_ww_ridge <- train(quality ~ alcohol + volatile.acidity +</pre>
                         residual.sugar + fixed.acidity +
                         free.sulfur.dioxide + sulphates +
                         total.sulfur.dioxide + pH, data=whitedf_train,
            method="glmnet",
            preProcess=c("center", "scale"),
            trControl=ctrl, tuneGrid=grd)
fit_ww_ridge
## glmnet
##
## 2939 samples
##
     8 predictor
## Pre-processing: centered (8), scaled (8)
## Resampling: Cross-Validated (10 fold, repeated 10 times)
## Summary of sample sizes: 2646, 2645, 2644, 2644, 2645, 2645, ...
## Resampling results across tuning parameters:
##
##
    lambda
               RMSE
                         Rsquared
                                   MAE
##
    0.000911882 0.7713956 0.2644750 0.5963063
##
    0.001186388 0.7713956 0.2644750 0.5963063
    0.001543529 0.7713956 0.2644750 0.5963063
##
##
    0.002008180 0.7713956 0.2644750 0.5963063
##
    0.002612707 0.7713956 0.2644750 0.5963063
##
    0.003399216 0.7713956 0.2644750 0.5963063
##
    0.004422489 0.7713956 0.2644750 0.5963063
##
    0.005753800 0.7713956 0.2644750 0.5963063
    0.007485879 0.7713956 0.2644750 0.5963063
##
    0.009739369 0.7713956 0.2644750 0.5963063
##
##
    0.012671232  0.7713956  0.2644750  0.5963063
##
    0.016485680 0.7713956 0.2644750 0.5963063
    0.021448399 0.7713956 0.2644750 0.5963063
##
    0.027905057 0.7713956 0.2644750 0.5963063
##
```

```
## 0.036305375 0.7713956 0.2644750 0.5963063
## 0.047234459 0.7715800 0.2644133 0.5964922
## 0.061453549 0.7719637 0.2642660 0.5968524
## 0.079953042 0.7725760 0.2640283 0.5973675
## 0.104021477 0.7735260 0.2636500 0.5981261
## 0.135335283 0.7749544 0.2630627 0.5992021
##
## Tuning parameter 'alpha' was held constant at a value of 0
## RMSE was used to select the optimal model using the smallest value.
## The final values used for the model were alpha = 0 and lambda = 0.03630538.
```

Lasso Regression

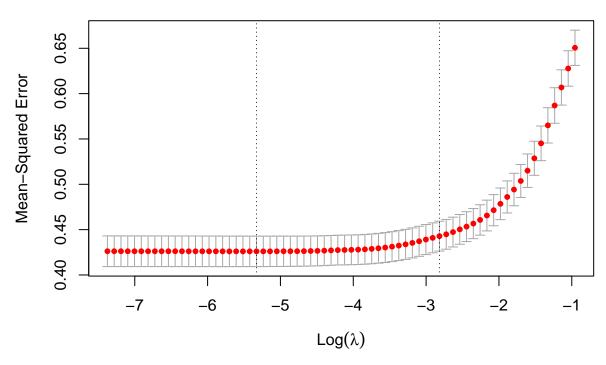
Lasso Regression



```
# Using k-fold cv to get best optimal lambda value
red_cv_ls_model<-cv.glmnet(predictors_rw,response_rw,alpha=1)

#produce plot of MSE values for each lambda
plot(red_cv_ls_model)</pre>
```

11 11 11 11 9 8 7 7 7 7 4 3 3 2 2 0



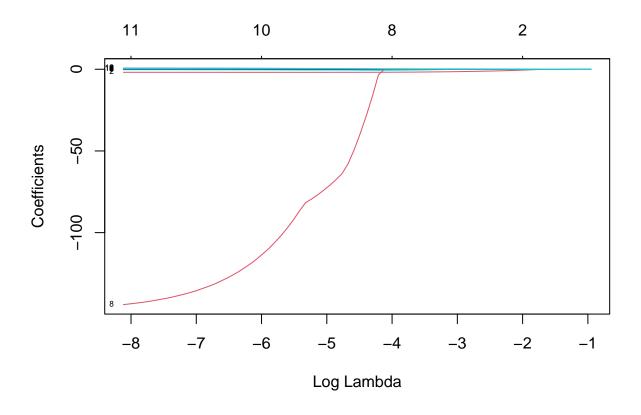
```
#find optimal lambda value that minimizes the MSE
best_lambda_rw<-red_cv_ls_model$lambda.min
best_lambda_rw</pre>
```

[1] 0.004850794

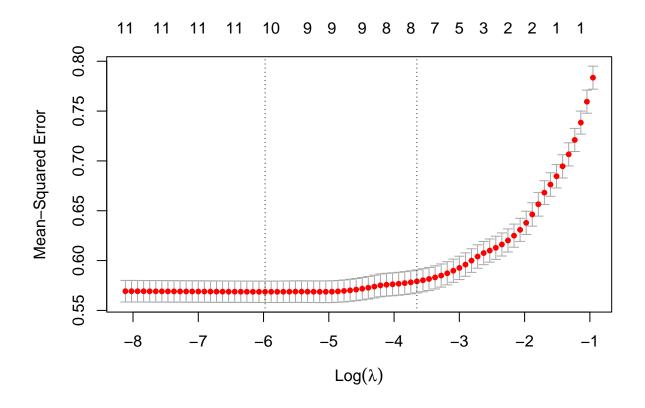
best_model_ls_rw<-glmnet(predictors_rw,response_rw,alpha=1,lambda=best_lambda_rw)
coef(best_model_ls_rw)</pre>

```
## 12 x 1 sparse Matrix of class "dgCMatrix"
##
                                   s0
## (Intercept)
                         4.311058572
## fixed.acidity
                         0.001590786
## volatile.acidity
                        -1.045885442
## citric.acid
                        -0.056043048
## residual.sugar
                         0.004545097
## chlorides
                        -1.812127522
## free.sulfur.dioxide
                         0.003379133
## total.sulfur.dioxide -0.002981089
## density
                        -0.437661346
## pH
## sulphates
                         0.850821345
## alcohol
                         0.287823262
```

```
# To find the rsquare of our best model
#To obtain predicted values
predicted_quality_rw<-predict(best_model_ls_rw, s=best_lambda_rw, newx=predictors_rw)</pre>
#Finding the SST and SSE and Rsquare
sst_rw<-sum((actual_quality_rw-mean(actual_quality_rw))^2)</pre>
sse_rw<-sum((actual_quality_rw-predicted_quality_rw)^2)</pre>
rsq_ls_rw<-1-(sse_rw/sst_rw)
rsq_ls_rw
## [1] 0.3595207
#Finding the RMSE and MAE
n_rw<-nrow(red_wine_df)</pre>
rmse_ls_rw<-sqrt(sum((actual_quality_rw-predicted_quality_rw)^2)/n_rw)</pre>
rmse_ls_rw
## [1] 0.6460953
mae_ls_rw<-sum(abs(actual_quality_rw-predicted_quality_rw))/n_rw</pre>
mae_ls_rw
## [1] 0.5020461
view(data.frame(RMSE=rmse_ls_rw,MAE=mae_ls_rw,R_Square=rsq_ls_rw))
# Lasso Regression on White wine
response_ww<-white_wine_df$quality
actual_quality_ww<-white_wine_df$quality</pre>
predictors_ww<-data.matrix(white_wine_df[,c("fixed.acidity","volatile.acidity","citric.acid",</pre>
                              "residual.sugar", "chlorides", "free.sulfur.dioxide",
                              "total.sulfur.dioxide", "density", "pH", "sulphates",
                              "alcohol")])
white_ls_model<-glmnet(predictors_ww,response_ww,alpha=1)</pre>
coef_ww<-plot(white_ls_model,xvar="lambda",label=TRUE)</pre>
```



```
# Using k-fold cv to get best optimal lambda value
library("glmnet")
white_cv_ls_model<-cv.glmnet(predictors_ww,response_ww,alpha=1)
plot(white_cv_ls_model)</pre>
```



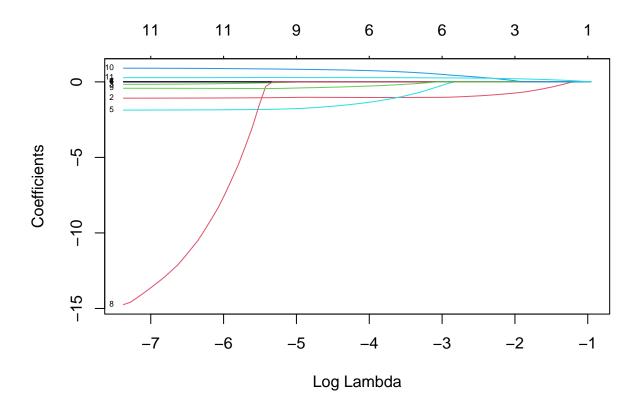
```
#find optimal lambda value that minimizes the MSE
best_lambda_ww<-white_cv_ls_model$lambda.min
best_lambda_ww</pre>
```

[1] 0.002537796

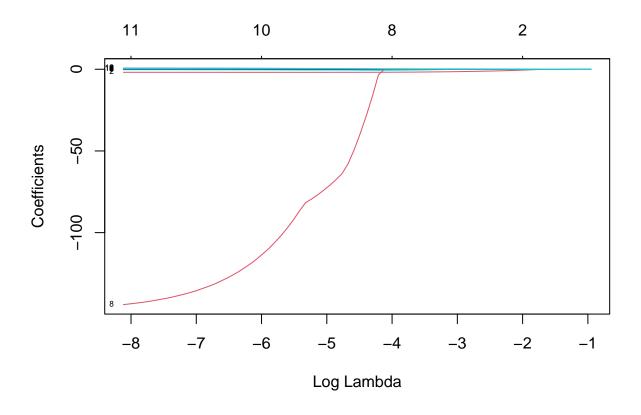
best_model_ls_ww<-glmnet(predictors_ww,response_ww,alpha=1,lambda=best_lambda_ww)
coef(best_model_ls_ww)</pre>

```
## 12 x 1 sparse Matrix of class "dgCMatrix"
##
                                    s0
## (Intercept)
                         1.135530e+02
## fixed.acidity
                         3.015296e-02
## volatile.acidity
                         -1.875380e+00
## citric.acid
## residual.sugar
                         6.637850e-02
## chlorides
                         -3.934651e-01
## free.sulfur.dioxide
                         3.599613e-03
## total.sulfur.dioxide -2.344057e-04
## density
                        -1.129171e+02
## pH
                         5.208469e-01
## sulphates
                         5.556340e-01
## alcohol
                         2.329256e-01
```

```
# To find the rsquare of our best model
#To obtain predicted values
predicted_quality_ww<-predict(best_model_ls_ww, s=best_lambda_ww, newx=predictors_ww)</pre>
#find the SST and SSE
sst_ww<-sum((actual_quality_ww-mean(actual_quality_ww))^2)</pre>
sse_ww<-sum((actual_quality_ww-predicted_quality_ww)^2)</pre>
rsq_ls_ww<-1-(sse_ww/sst_ww)</pre>
rsq_ls_ww
## [1] 0.2811733
n_ww<-nrow(white_wine_df)</pre>
rmse_ls_ww<-sqrt(sum((actual_quality_ww-predicted_quality_ww)^2)/n_ww)</pre>
rmse_ls_ww
## [1] 0.7508001
mae_ls_ww<-sum(abs(actual_quality_ww-predicted_quality_ww))/n_ww</pre>
mae_ls_ww
## [1] 0.5843081
ls_results_df <- tibble(wine_type = c("Red Wine","White wine"),</pre>
                              rmse = c(rmse_ls_rw,rmse_ls_ww),
                              mae = c(mae_ls_rw,rmse_ls_rw),
                              rsquare = c(rsq_ls_rw,rsq_ls_ww))
view(ls_results_df)
plot(red_ls_model,xvar="lambda",label=TRUE)
```



plot(white_ls_model,xvar="lambda",label=TRUE)



#grid.arrange(coef_rw, coef_ww, nrow=1)

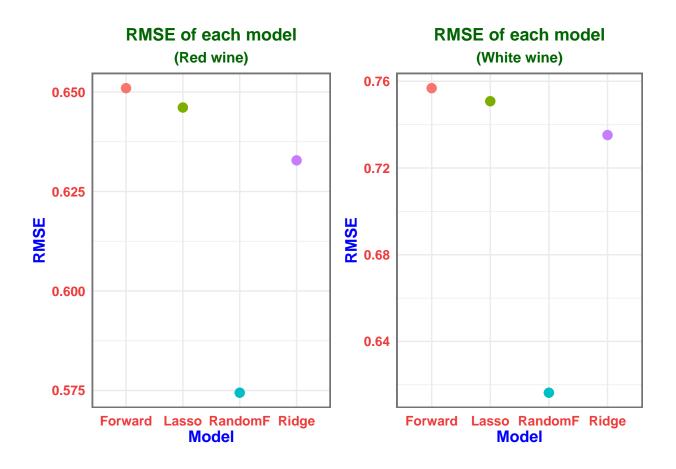
```
fit_fs_rmse_rw<-as.numeric(fit1_rmse["cv_rmse"])</pre>
fit_fs_rsq_rw<-as.numeric(fit1_rmse["cv_rsq"])</pre>
fit_fs_rmse_ww<-as.numeric(fit1_rmse_ww["cv_rmse"])</pre>
fit_fs_rsq_ww<-as.numeric(fit1_rmse_ww["cv_rsq"])</pre>
fit_fs_mae_rw<-as.numeric(fit1_rmse["cv_mae"])</pre>
fit_fs_mae_ww<-as.numeric(fit1_rmse_ww["cv_mae"])</pre>
fit_rd_rmse_rw<-rmse(fit_rw_ridge,reddf_test)</pre>
fit_rd_rsq_rw<-rsquare(fit_rw_ridge,reddf_test)</pre>
fit_rd_rmse_ww<-rmse(fit_ww_ridge,whitedf_test)</pre>
fit_rd_rsq_ww<-rsquare(fit_ww_ridge,whitedf_test)</pre>
fit_rd_mae_rw<-mae(fit_rw_ridge,reddf_test)</pre>
fit_rd_mae_ww<-mae(fit_ww_ridge,whitedf_test)</pre>
fit_ls_rmse_rw<-rmse_ls_rw</pre>
fit_ls_rsq_rw<-rsq_ls_rw</pre>
fit_ls_rmse_ww<-rmse_ls_ww</pre>
fit_ls_rsq_ww<-rsq_ls_ww
fit_ls_mae_rw<-mae_ls_rw</pre>
fit_ls_mae_ww<-mae_ls_ww
fit_rf_rmse_rw<-rmse(fit_rw_rf,reddf_test)</pre>
fit_rf_rsq_rw<- rsquare(fit_rw_rf,reddf_test)</pre>
```

```
fit_rf_rmse_ww<-rmse(fit_ww_rf,whitedf_test)</pre>
fit_rf_rsq_ww<- rsquare(fit_ww_rf,whitedf_test)</pre>
fit_rf_mae_rw<-mae(fit_rw_rf,reddf_test)</pre>
fit_rf_mae_ww<-mae(fit_ww_rf,whitedf_test)</pre>
fs_results_df <- tibble(wine_type = c("Red Wine","White wine"),</pre>
                            rmse = c(fit_fs_rmse_rw,fit_fs_rmse_ww),
                            mae = c(fit_fs_mae_rw,fit_fs_mae_ww),
                             rsquare = c(fit_fs_rsq_rw,fit_fs_rsq_ww))
view(fs_results_df)
rd_results_df <- tibble(wine_type = c("Red Wine","White wine"),</pre>
                             rmse = c(fit_rd_rmse_rw,fit_rd_rmse_ww),
                            mae = c(fit_rd_mae_rw,fit_rd_mae_ww),
                             rsquare = c(fit_rd_rsq_rw,fit_rd_rsq_ww))
view(rd_results_df)
ls_results_df <- tibble(wine_type = c("Red Wine","White wine"),</pre>
                             rmse = c(fit_ls_rmse_rw,fit_ls_rmse_ww),
                             mae = c(fit_ls_mae_rw,fit_ls_mae_ww),
                             rsquare = c(fit_ls_rsq_rw,fit_ls_rsq_ww))
view(ls_results_df)
rf_results_df <- tibble(wine_type = c("Red Wine","White wine"),</pre>
                             rmse = c(fit_rf_rmse_rw,fit_rf_rmse_ww),
                             mae = c(fit_rf_mae_rw,fit_rf_mae_ww),
                             rsquare = c(fit_rf_rsq_rw,fit_rf_rsq_ww))
view(rf_results_df)
rmse_of_plots_rw<-data.frame(rmse_value=c(fit_fs_rmse_rw,fit_rd_rmse_rw,fit_ls_rmse_rw,fit_rf_rmse_rw),
rmse_of_plots_ww<-data.frame(rmse_value=c(fit_fs_rmse_ww,fit_rd_rmse_ww,fit_ls_rmse_ww,fit_rf_rmse_ww),
rsq_of_plots_rw<-data.frame(rsq_value=c(fit_fs_rsq_rw,fit_rd_rsq_rw,fit_ls_rsq_rw,fit_rf_rsq_rw),model=
rsq_of_plots_ww<-data.frame(rsq_value=c(fit_fs_rsq_ww,fit_rd_rsq_ww,fit_ls_rsq_ww,fit_rf_rsq_ww),model=
mae_of_plots_rw<-data.frame(mae_value=c(fit_fs_mae_rw,fit_rd_mae_rw,fit_ls_mae_rw,fit_rf_mae_rw),model=
mae_of_plots_ww<-data.frame(mae_value=c(fit_fs_mae_ww,fit_rd_mae_ww,fit_ls_mae_ww,fit_rf_mae_ww),model=
rmse_plot_rw<-ggplot(data=rmse_of_plots_rw)+</pre>
  geom_point(aes(x=model,y=rmse_value,color=model),size=3)+
  theme_minimal()+
  labs(x="Model",
       y="RMSE",
       title="RMSE of each model",
       subtitle="(Red wine)")+
  theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
```

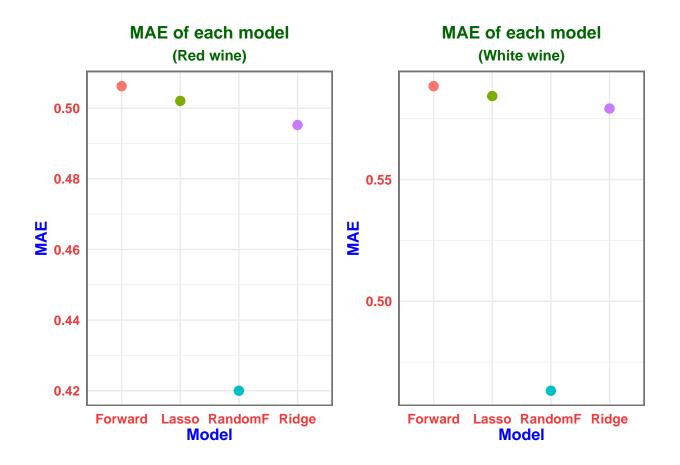
```
face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
rmse_plot_ww<-ggplot(data=rmse_of_plots_ww)+</pre>
  geom_point(aes(x=model,y=rmse_value,color=model),size=3)+
  theme_minimal()+
  labs(x="Model",
       y="RMSE",
       title="RMSE of each model",
       subtitle="(White wine)")+
  theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
rsq_plot_rw<-ggplot(data=rsq_of_plots_rw)+
  geom_point(aes(x=model,y=rsq_value,color=model),size=3)+
  theme_minimal()+
  labs(x="Model",
       y="RSquared Value",
       title="RSquared of each model",
       subtitle="(Red wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
```

```
face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
rsq_plot_ww<-ggplot(data=rsq_of_plots_ww)+
  geom_point(aes(x=model,y=rsq_value,color=model),size=3)+
  theme_minimal()+
  labs(x="Model",
       y="RSquared Value",
       title="RSquare of each model",
       subtitle="(White wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
mae_plot_rw<-ggplot(data=mae_of_plots_rw)+</pre>
  geom_point(aes(x=model,y=mae_value,color=model),size=3)+
  theme_minimal()+
  labs(x="Model",
       y="MAE",
       title="MAE of each model",
```

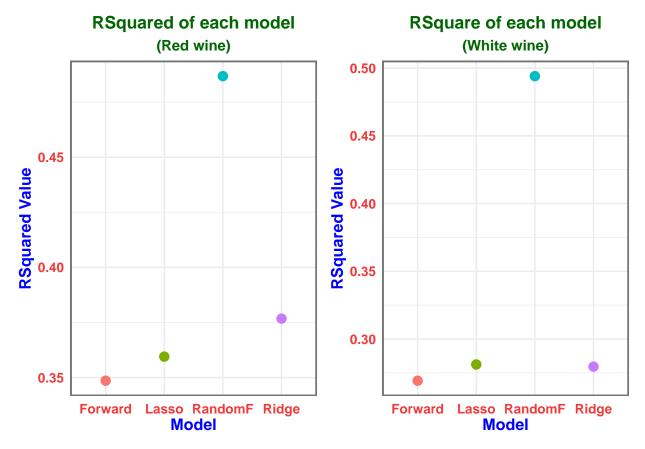
```
subtitle="(Red wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
mae_plot_ww<-ggplot(data=mae_of_plots_ww)+</pre>
  geom_point(aes(x=model,y=mae_value,color=model),size=3)+
  theme minimal()+
 labs(x="Model",
       y="MAE",
       title="MAE of each model",
       subtitle="(White wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
grid.arrange(rmse_plot_rw,rmse_plot_ww,nrow = 1)
```



grid.arrange(mae_plot_rw,mae_plot_ww,nrow = 1)



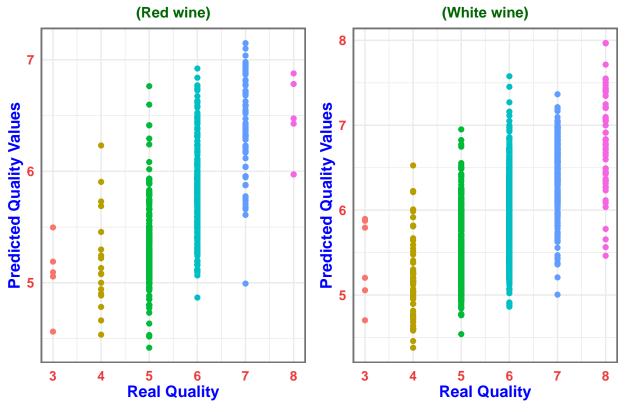
grid.arrange(rsq_plot_rw,rsq_plot_ww,nrow = 1)



```
red_rf_results<-ggplot(data=rf_rw_results)+</pre>
  geom_point(aes(x=real,y=prediction,color=factor(real)))+
  theme_minimal()+
  labs(x="Real Quality",
       y="Predicted Quality Values",
       title="Real Vs Predicted Response Variable",
       subtitle="(Red wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
```

```
legend.position = "none")
white_rf_results<-ggplot(data=rf_ww_results)+</pre>
  geom_point(aes(x=real,y=prediction,color=factor(real)))+
 theme_minimal()+
 labs(x="Real Quality",
       y="Predicted Quality Values",
       title="Real Vs Predicted Response Variable",
       subtitle="(White wine)")+
  theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                plot.subtitle = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
                axis.title = element_text(color = "blue",
                                           face = "bold",
                                           size = 12),
                axis.text.x = element_text(hjust = 0.5,
                                           vjust = 0.5,
                                           color = "brown2",
                                           face = "bold",
                                           size = 10),
                axis.text.y = element_text(color = "brown2",
                                           face = "bold",
                                           size = 10),
                panel.border = element_rect(colour = "grey45",
                                           fill=NA, size=1),
         legend.position = "none")
grid.arrange(red_rf_results, white_rf_results, nrow=1)
```

Real Vs Predicted Response Variable Real Vs Predicted Response Variable

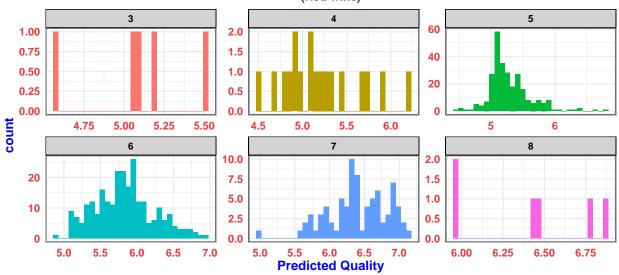


```
red_rf_plot<-ggplot(data=rf_rw_results)+</pre>
  geom_histogram(aes(x= prediction,fill=factor(real)))+
  facet_wrap(~ factor(real), scales="free")+
  theme_minimal()+
  labs(x="Predicted Quality",
       title="Real Vs Predicted Response Variable",
       subtitle="(Red wine)")+
   theme(plot.title = element_text(hjust = 0.5,
                                           color = "darkgreen",
                                           face = "bold"),
          plot.subtitle = element_text(hjust = 0.5,
                                     color = "darkgreen",
                                     face = "bold"),
          axis.title = element_text(color = "blue",
                                     face = "bold",
                                     size = 12),
          axis.text.x = element_text(hjust = 0.5,
                                     vjust = 0.5,
                                     color = "brown2",
                                     face = "bold",
                                     size = 10),
          axis.text.y = element_text(color = "brown2",
                                     face = "bold",
                                     size = 10),
          panel.border = element_rect(colour = "grey45",
                                     fill=NA, size=1),
```

```
strip.background = element_rect(fill = "lightgrey"),
         strip.text = element_text(color = "black", face = "bold"),
         legend.position = "none")
white_rf_plot<-ggplot(data=rf_ww_results)+</pre>
  geom_histogram(aes(x= prediction,fill=factor(real)))+
  facet_wrap(~ factor(real), scales="free")+
 theme minimal()+
  labs(x="Predicted Quality",
       title="Real Vs Predicted Response Variable",
       subtitle="(white wine)")+
  theme(plot.title = element_text(hjust = 0.5,
                                          color = "darkgreen",
                                          face = "bold"),
          plot.subtitle = element_text(hjust = 0.5,
                                    color = "darkgreen",
                                    face = "bold"),
          axis.title = element_text(color = "blue",
                                    face = "bold",
                                    size = 12),
          axis.text.x = element_text(hjust = 0.5,
                                    vjust = 0.5,
                                    color = "brown2",
                                    face = "bold",
                                    size = 10),
          axis.text.y = element_text(color = "brown2",
                                    face = "bold",
                                    size = 10),
          panel.border = element_rect(colour = "grey45",
                                    fill=NA, size=1),
         strip.background = element_rect(fill = "lightgrey"),
         strip.text = element_text(color = "black", face = "bold"),
         legend.position = "none")
grid.arrange(red_rf_plot, white_rf_plot, nrow = 2)
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```

Real Vs Predicted Response Variable

(Red wine)



Real Vs Predicted Response Variable



