

Computer Graphics

Discussion 3

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Part I: Some Special Matrices

Camera, Projection, and Viewport

Matrix Review

- All the objects you draw on screen are drawn one vertex at a time, by starting with the vertex's xyz coordinate and then multiplying by a matrix to get the final xy coordinate on the screen.

$$\begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & ? & ? \end{bmatrix} * \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

M P

Transforms

$$\begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ \mathbf{0} & \mathbf{0} & ? & ? \end{bmatrix} \quad * \quad \begin{bmatrix} x \\ y \\ z \\ \mathbf{1} \end{bmatrix}$$

M P

- Before that matrix, the xyz coordinate is always some trivial value like (.5, .5, .5)
 - In the reference system of the shape itself
 - For example, a cube's own coordinates for its corners
- After that matrix, it's some different xy pixel coordinate denoting where that vertex will show up on the screen.
 - And z for depth, and a fourth number for translations / perspective effects
- That mapping is all that the transform does.

Transform Process

- The transform is always just one 4x4 matrix.
- But calculating what it should be involves multiplying out a big chain of intermediate special matrices. That chain is always:

$$\begin{bmatrix} ? & 0 & 0 & ? \\ 0 & ? & 0 & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Viewport} * \begin{bmatrix} ? & 0 & ? & ? \\ 0 & ? & ? & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & ? & ? \end{bmatrix} \textit{Projection} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Camera} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Model} * \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Transform Process

$$\begin{bmatrix} ? & 0 & 0 & ? \\ 0 & ? & 0 & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Viewport} * \begin{bmatrix} ? & 0 & ? & ? \\ 0 & ? & ? & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & ? & ? \end{bmatrix} \textit{Projection} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Camera} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Model} * \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- Note: We never actually see the viewport matrix.
 - The viewport matrix happens out of sight at the end of the vertex shader.
 - Set up by JavaScript's call to `gl.viewport(x,y,width,height)`
- All the other special matrices you do manage.

Transform Process

$$\begin{bmatrix} ? & 0 & 0 & ? \\ 0 & ? & 0 & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Viewport} * \begin{bmatrix} ? & 0 & ? & ? \\ 0 & ? & ? & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & ? & ? \end{bmatrix} \textit{Projection} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Camera} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Model} * \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- The camera matrix is very much like the model transform matrix for placing shapes. But:
 - The shape being placed is the scene's observer
 - You actually use the **inverse matrix** of what you would have done to a 3D model of an actual camera

Projections

- So, there are two choices for how the view frustum is shaped: Perspective or Orthographic (parallel)
- The frustum has six planes, and the closest to the camera is called the “near plane”
- The projection matrix maps all 3D points that fall inside a frustum onto the near plane of that frustum, thereby reducing all shapes to 2D, for screen display.

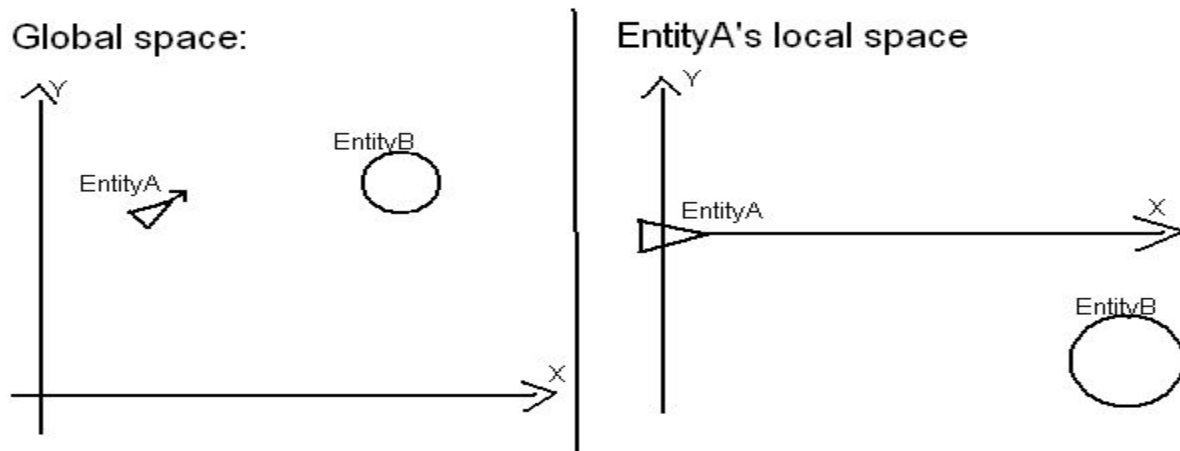
Projections: Online Demos

- http://threejs.org/examples/#webgl_camera
 - Perspective vs orthographic - the difference between the two projection frustums (and what they see) -- press O and P to switch between the two.
 - Clipping planes
 - Tons of other informative examples are linked there, like the demo of flat vs smooth shading:
http://threejs.org/examples/#webgl_morphnormals

Part II: Coordinate spaces

World Coordinates

- The common coordinate system for the scene
- Also called World Space / Global Space

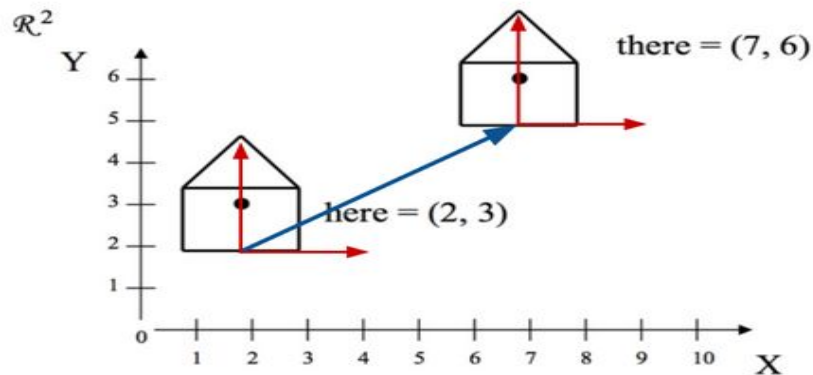


World Coordinates

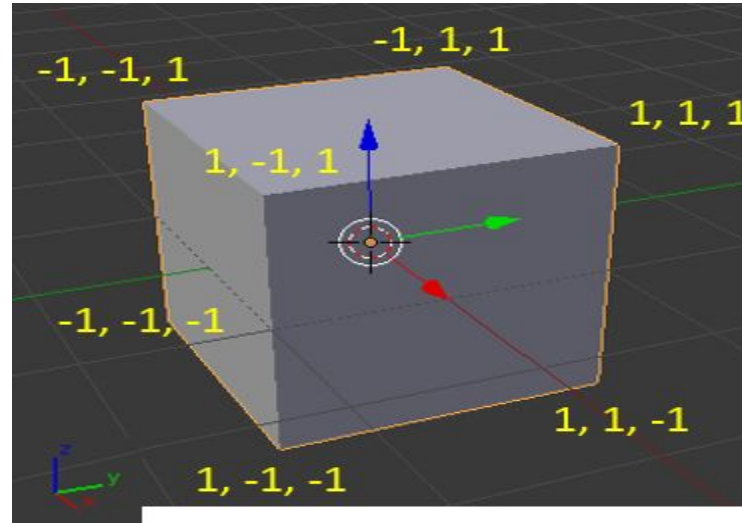
Placing object coordinates in the world

Place the coordinate system for the object in the world

- Don't know or care about the shape of the object



Object Coordinates: Transforming *every point* of an object



Object Coordinates

Object Coordinates

Each object is defined using some **convenient** coordinates

- Often “Axis-aligned”. (when there are natural axes for the object)
- Origin of coordinates is often in the middle of the object
- Origin of coordinates is often at the “base” or corner of the object
- E.g. house in previous example was $(-1,0)$, $(1, 0)$...

Notice: build, manipulate object in object coordinates, also called **Object Space/Local Coordinates**

- Don't know (or care) where the object will end up in the scene.

Screen coordinates

- So far we only have considered:
 - World Coordinates == Screen Coordinates
- We need a camera transform to draw the world from anywhere besides the world origin
 - Places a camera in the world via incremental movements (applying matrices)
 - “Bases” vs “Points” philosophies matter here
 - In “points” thinking, you’re instead “re-orienting the world” to get a particular vantage point

Remember the lecture slide about “points” thinking vs “bases” thinking:

Rule of Thumb

Transforming a point P:

Transformations: T_1, T_2, T_3

Matrix: $\mathbf{M} = \mathbf{M}_3 \mathbf{M}_2 \mathbf{M}_1$

Point transformed by \mathbf{MP}

Each transformation happens with respect to the **same** coordinate system

Transforming a coordinate system:

Transformations: T_1, T_2, T_3

Matrix: $\mathbf{M} = \mathbf{M}_1 \mathbf{M}_2 \mathbf{M}_3$

Transformed point has coordinates \mathbf{MP} in original coordinate system

Each transformation happens with respect to **previous** coordinate system

Look at this again:

$$\begin{bmatrix} ? & 0 & 0 & ? \\ 0 & ? & 0 & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Viewport} * \begin{bmatrix} ? & 0 & ? & ? \\ 0 & ? & ? & ? \\ 0 & 0 & ? & ? \\ 0 & 0 & ? & ? \end{bmatrix} \textit{Projection} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Camera} * \begin{bmatrix} ? & ? & ? & ? \\ ? & ? & ? & ? \\ ? & ? & ? & ? \\ 0 & 0 & 0 & 1 \end{bmatrix} \textit{Model} * \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- The camera matrix is very much like the model transform matrix for placing shapes. But:
 - The shape being placed is the scene's observer
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Camera and Model Transform

- Camera transform goes to the left of model transform since the camera is more of an **initial** basis
 - (because “bases” philosophy **starts** on the left of end of the matrix product, and starts evaluating from there)
- Unlike the model transform, a camera transform takes the thing in question (the camera) and does the matrix inverse of what you want to do to it

Matrix Inverse

- Recall this property of the matrix inverse:
 - $(M_1 * M_2 * M_3)^{-1} = (M_3)^{-1} * (M_2)^{-1} * (M_1)^{-1}$

When you invert a product,

- The order gets reversed

AND

- The individual matrices get inverted

The Camera Transform

- Given $C_1 * C_2 * C_3$, a sequence of transforms we'd like to do to the camera, we really get:

$$(C_1 * C_2 * C_3)^{-1} M_1 * M_2 * M_3[p]$$

- Which equals:

$$(C_3)^{-1} * (C_2)^{-1} * (C_1)^{-1} M_1 * M_2 * M_3[p]$$

- So unlike the model transform, all of our first-person camera's new incremental changes come in from the left (pre-multiplying; build the camera transform right to left)

Interpreting a written-out camera-model product

- Notice:

The first warp we apply to the image...

$$(C_3)^{-1} * (C_2)^{-1} * (C_1)^{-1} M_1 * M_2 * \mathbf{M}_3[p]$$

...is also the last (most recent) coordinate system change

Interpreting a written-out camera-model product

- Notice:

And the first warp we apply to an *image of a camera*...



$$(C_3)^{-1} * (C_2)^{-1} * (C_1)^{-1} M_1 * M_2 * M_3[p]$$



Is also the last (most recent) camera repositioning

The Camera Transform

- Conclusion:
 - When thinking of a camera as first-person (as opposed to third-person, where we actually just spin the scene around, which is like doing more to `model_transform`):
 - We incrementally adjust the camera over time, the increments come in as matrices from the *left*.
 - Calls to `mult()` will have to pre-multiply instead of post-multiply to do what we expect.

The Camera Transform

- More things to notice if you want to zoom in or out:
 - Camera transforms and model transforms both often have the form $T * R * T * R * \dots * T * R * \underline{S}$
 - So after inversion and combining them both, it looks like:

$$S^{-1}R^{-1}T^{-1}R^{-1}T^{-1} * TRTRS * [p]$$



Scales the view frustum



Scales the object

Part III: Bee assignment

AKA frequently asked questions

Hierarchy clarifications

- Mainly meant to help you think in terms of hierarchy - the actual coding requirements are minimal
 - Post multiplication satisfies your hierarchical design constraint; methods/function calls satisfy your coding constraint
 - You should think of the bee parts themselves as being in a hierarchy (whatever part you draw first influences the matrix transformations of all parts drawn after)



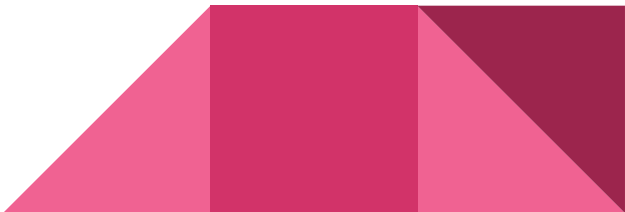
Methods vs Functions

- Methods in JS work the same as they do in C++; the template uses methods
 - Use them for you bee parts as well for simplicity, since just calling `this.method_name(...)` will give you the correct “this”
 - With regular functions, you’d need to make sure “this” context is correct or else any shape draw call will throw an error (you’ll need to use `apply` or `call` to pass “this”)



Methods vs Functions

- From Piazza post 31 -- Things to watch out for when adding your own method:
 - The best existing code to mimic to accomplish adding your own method is actually found in the "Surfaces_Tester" class a bit farther down in the example scenes file. The key things to notice are the syntax for how it declares the class method called 'draw_all_shapes()'. Just re-use that syntax.
 - What is this "list" of methods you see? If you look at the surrounding code, what's really going on is you're passing in something to some function "Declare_Any_Class()". The second argument it wants is a list of all the desired class methods. The list is of JavaScript type "Object", like those declared with curly braces { }.
 - Pay special attention to the fact that there is a comma before the "draw_all_shapes()" declaration (because it's actually a key-value pair in an object declaration, and those are separated by commas).
 - Also pay special attention to how the method is called. Notice the **"this"**. The function "display()" of the Surfaces_Tester has to say **"this.draw_all_shapes()"** to call its own method. JavaScript is not smart enough to infer that you're trying to make the current object do something. You have to type **"this."** yourself. A lot of people will have errors about their function being undefined because they will forget to put the **"this."**.



Variables and model transform

- `model_transform` is just a normal local variable - nothing special about it
 - You can make your own `mat4` variables and use them to store copies of `model_transform`
 - Allows you to quickly jump back to a previous matrix- no need for stacks (this method is actually easier than stacks for this assignment)



Recall using stacks to maintain matrix “history”:

When you do a complicated series of transformations, you want to be able to get back to where your `model_transform` was before. You could handle it by undoing all your transformations, or you could just make a stack:

- `var stack = [];`
 - Now just push your current `model_transform` matrix before a transformation and pop it back afterwards

```
stack.push(model_transform);
```

```
model_transform = stack.pop();
```



Better than stacks: Function calls

- You should know about what the “program stack” or “call stack” is in this course. Google if unsure.
- Every time a function gets called (in any language), a stack is being used behind the scenes.
- This stack can save you from having to use your own.
- Every time a function ends, it’s very similar to backing up one level in the history of your `model_transform` variable, which resumes its value in the caller’s scope



Better than stacks: Function calls

- Conclusion: Instead of a stack operation, use a function instead. Write your own function and pass in `model_transform` by value, then let that function handle its own copy; when you're done with that branch of your shape, back up one level simply by letting the function finish.
- In our template, you would add class methods.
- The emphasis on stacks in graphics courses is just a vestigial holdover from how old (pre-shader) graphics cards used to work.
 - They managed their own stacks of matrix history, and you had to go through it instead of controlling it yourself. Very slow back-and-forth between CPU and GPU. It was inflexible. Modern GPUs run programs that you write.

