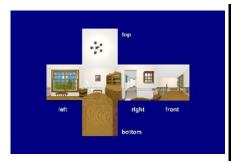


## **Texture Mapping**

### Pasting textures on surfaces

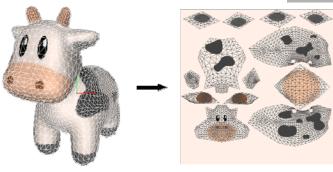




## **Texture Mapping**

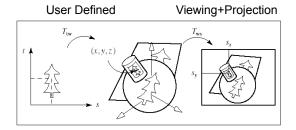
### Pasting textures on surfaces





## **Coordinate Systems Involved**

FIGURE 8.35 Drawing texture on several objects of different shape.

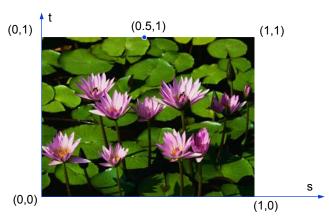


$$(s_x,s_y) = T_{ws}(T_{tw}(s,t))$$

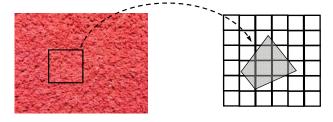
frow: Computer Graphics Using OpenGL, 2e, by F. S. Hill © 2001 by Prentice Hall / Prentice-Hall, Inc., Upper Sackile River, New Jersey 07458

### **Textures are Images**

They are always assigned the shown parametric coordinates (s,t)





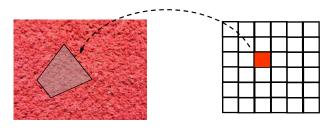


$$(s_x, s_y) = T_{ws}(T_{tw}(s,t))$$

We would have to calculate pixel coverages

### **Screen to Texture**

### Better approach



 $(\mathsf{s},\mathsf{t}) = \mathsf{T}_{\mathsf{wt}}(\mathsf{T}_{\mathsf{sw}}(\mathsf{s}_{\mathsf{x}},\mathsf{s}_{\mathsf{y}}))$ 

Requires inverting the projection matrix

### From Texture to World (Object)

To apply a texture to an object, we must find a correspondance between (s,t) and some object coordinate system

- Mapping via a parametric representation of the object space
- Manually

# Mapping the Texture to an Object Parametric Representation

#### Linear transformation

From texture space (s,t) to object space (u,v)

$$u = u(s,t) = a_u s + b_u t + c_u$$
  
 $v = v(s,t) = a_v s + b_v t + c_v$ 

s in [0,1]

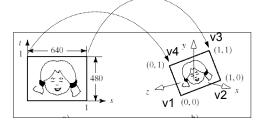
*t* in [0,1]

### **Example 1: Image to a Quadrilateral**

#### **Simply**

$$u = u(s,t) = s$$

$$v = v(s,t) = t$$



glTexCoord2f(0,0); glVertex3dv(v1);

 $glTexCoord2f(1,0)\;;\;\;glVertex3dv(v2)\;;$ 

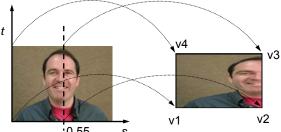
 $glTexCoord2f(1,1)\;;\;\;glVertex3dv(v3)\;;$ 

glTexCoord2f(0,1); glVertex3dv(v4);



### Use only left part

$$u = u(s,t) = 0.55s$$
$$v = v(s,t) = t$$



glTexCoord2f(0,0); glVertex3dv(v1);

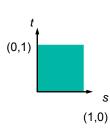
glTexCoord2f(0.55,0); glVertex3dv(v2);

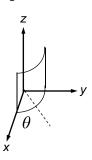
glTexCoord2f(0.55,1); glVertex3dv(v3);

glTexCoord2f(0,1); glVertex3dv(v4);

Packing textures for efficiency

### **Example 3: Square Texture to Cylinder**





Parametric form of cylinder:

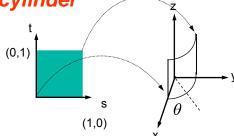
$$x = r \cos \theta$$
,  $y = r \sin \theta$ ,  $z$ 

Surface parameters:  $u = \theta$ , v = z

with  $0 \le u \le \pi/2$ , and  $0 \le v \le 1$ 

### **Example 3: Square Texture to Cylinder**

Square texture to cylinder



We pick the following linear transformation that maps (s,t)=(0,0) to (u,v)=(0,0) and (s,t)=(1,1) to  $(u,v)=(\frac{\pi}{2},1)$ :

$$u = s\frac{\pi}{2}, \quad v = t$$

### **Example 3: Square Texture to Cylinder**

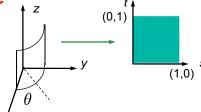
#### From screen to texture



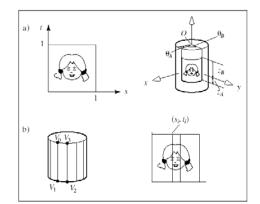
\_\_\_\_

- 1. Inverse transform  $(s_x, s_y)$  to get world position (x, y, z).
- 2. Then having (x,y,z),

$$u = \tan^{-1}(y/x), \quad v = z$$
$$s = 2u/\pi, \quad t = v$$



# Wrapping Textures on Curved Surfaces



$$s = \frac{\theta - \theta_a}{\theta_b - \theta_a}, \quad t = \frac{z - z_a}{z_b - z_a}$$

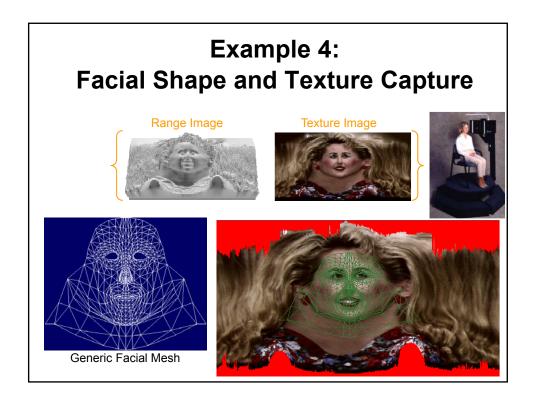
Cylinder with N faces

Left edge at azimuth  $\theta_i = 2\pi i / N$ 

Upper left vertex texture coordinates  $s_i = \frac{\theta_i - \theta_a}{\theta_b - \theta_a}$ ,  $t_i = 1$ 

# **Guerrilla CG Tutorial 09:** The Basics of UV Mapping

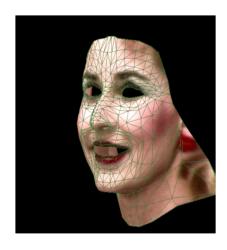




### **Textured 3D Geometric Model**

# Texture map coordinates

 Positions of fitted mesh nodes in RGB texture image



# **Example 5: Multiple Texture Maps Many Vertices and Texture Coordinates**

Geometry



**Texture maps** 







+ lighting =



# How Does this Work With the Graphics Pipeline?

Rendering polygons

Only vertices go down the graphics pipeline

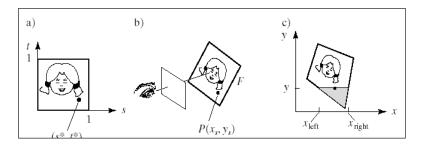
Interior points?

Calculate texture coordinates by interpolation along scanlines

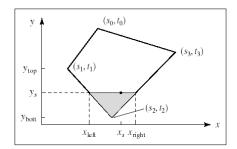
## **Rendering the Texture**

### Scanline in screen space

• Generating s,t coordinates for each pixel



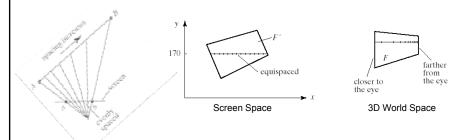
# Interpolation of Texture Coordinates



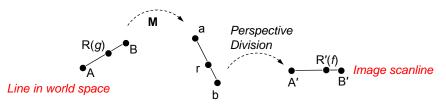
### **Problem**

### Perspective foreshortening

- Scan conversion takes equal steps along scanline in screen space
- Equal steps in screen space are **not** equal steps in world space



### **Reminder: In-Between Points**



$$R'_{1}(f) = \frac{lerp(a_{1},b_{1},g)}{lerp(a_{4},b_{4},g)}$$

$$R'_{1}(f) = lerp\left(\frac{a_{1}}{a_{4}},\frac{b_{1}}{b_{4}},f\right)$$

$$\Rightarrow g = \frac{f}{lerp(\frac{b_{4}}{a_{4}},1,f)}$$

substituting this in R(g) = (1 - g)A + gB yields

$$R_{1} = \frac{lerp(\frac{A_{1}}{a_{4}}, \frac{B_{1}}{b_{4}}, f)}{lerp(\frac{1}{a_{4}}, \frac{1}{b_{4}}, f)}$$
 and similarly for  $R_{2}$  and  $R_{3}$ 

### **Rendering Images Incrementally**

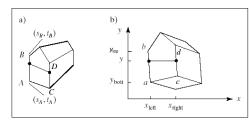
A maps to a (homogeneous)

B maps to b

C maps to c

D maps to d

For scanline y and two edges:



$$s_{left}(y) = \frac{lerp(\frac{s_A}{a_4}, \frac{s_B}{b_4}, f_l)}{lerp(\frac{1}{a_4}, \frac{1}{b_4}, f_l)}, \quad s_{right}(y) = \frac{lerp(\frac{s_C}{c_4}, \frac{s_D}{d_4}, f_r)}{lerp(\frac{1}{c_4}, \frac{1}{d_4}, f_r)}$$

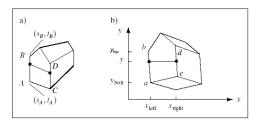
Once we have  $s_{\it left}$  and  $s_{\it right}$  another hyperbolic interpolation fills in the scanline

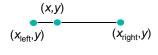
### **Interpolation Along the Scanline**

$$s_{left}(y) = \frac{lerp(\frac{s_A}{a_4}, \frac{s_B}{b_4}, f_l)}{lerp(\frac{1}{a_4}, \frac{1}{b_4}, f_l)},$$

$$s_{right}(y) = \frac{lerp(\frac{s_C}{c_4}, \frac{s_D}{d_4}, f_r)}{lerp(\frac{1}{c_4}, \frac{1}{d_4}, f_r)}$$

$$s(x, y) = \frac{lerp(\frac{s_{left}}{h_{left}}, \frac{s_{right}}{h_{right}}, f)}{lerp(\frac{1}{h_{left}}, \frac{1}{h_{right}}, f)}$$





What are f and the h's?

### **Interpolation Along the Scanline**

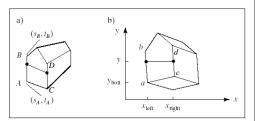
$$s_{left}(y) = \frac{lerp(\frac{s_{A}}{a_{4}}, \frac{s_{B}}{b_{4}}, f_{l})}{lerp(\frac{1}{a_{4}}, \frac{1}{b_{4}}, f_{l})}, \quad s_{right}(y) = \frac{lerp(\frac{s_{C}}{c_{4}}, \frac{s_{D}}{d_{4}}, f_{r})}{lerp(\frac{1}{c_{4}}, \frac{1}{d_{4}}, f_{r})}$$

$$s(x, y) = \frac{lerp(\frac{s_{left}}{h_{left}}, \frac{s_{right}}{h_{right}}, f)}{lerp(\frac{1}{h_{left}}, \frac{1}{h_{right}}, f)}$$

$$h_{left} = lerp(a_4, b_4, f_l)$$

$$h_{right} = lerp(c_4, d_4, f_r)$$

$$f = (x - x_{left})/(x_{right} - x_{left})$$



# Interpolating Information (Incrementally)

# Texture coordinates, Color, Normal, etc.

Right edge (1.2):

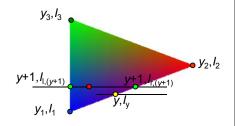
$$\frac{I_{r,(y+1)} - I_{r,y}}{(y+1) - y} = \frac{I_1 - I_2}{y_1 - y_2} \Rightarrow I_{r,(y+1)} = I_{r,y} + \frac{I_1 - I_2}{y_1 - y_2}$$

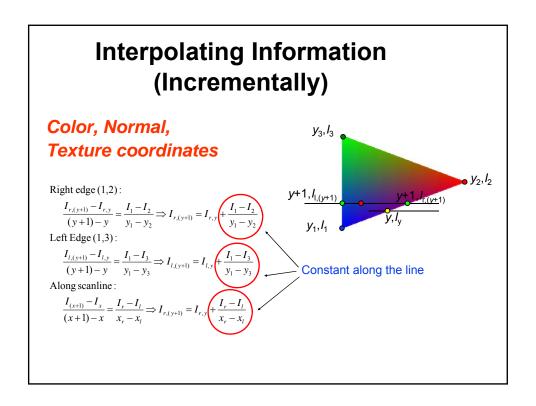
Left Edge (1,3):

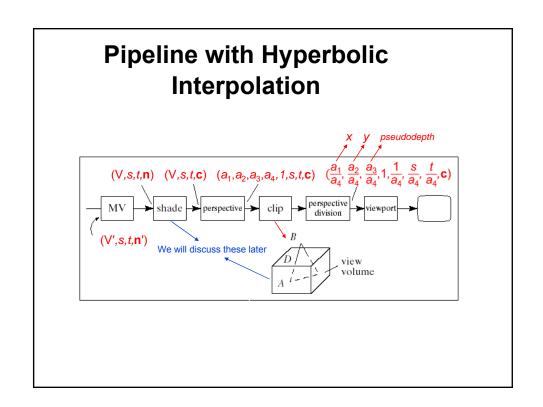
$$\frac{I_{I,(y+1)}-I_{I,y}}{(y+1)-y} = \frac{I_1-I_3}{y_1-y_3} \Rightarrow I_{I,(y+1)} = I_{I,y} + \frac{I_1-I_3}{y_1-y_3}$$

Along scanline:

$$\frac{I_{(x+1)} - I_x}{(x+1) - x} = \frac{I_r - I_t}{x_r - x_t} \Rightarrow I_{r,(y+1)} = I_{r,y} + \frac{I_r - I_t}{x_r - x_t}$$







## **Light Maps**

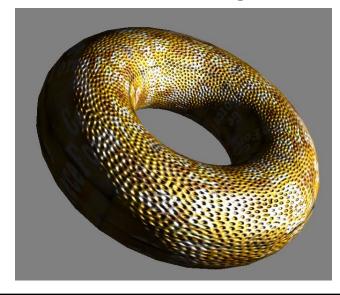
## For static objects







## **Bump Mapping**



# **Guerrilla CG Tutorial 10: Displacement and Bump Mapping**



### **Procedural Texture**

Volumetric textures

C = B(x,y,z)

