Naive Bayes with the Breast Cancer data

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In this notebook we compare Naive Bayes and logistic regression on the breast cancer data in package mlbench.

Load the data

The breast cancer data is in the mlbench package. There are 669 observations with 11 columns. Column 1 is an ID that will be ignored later, columns 2-10 are factors specifying information gleaned from bioposies. The final column is the label: benign or malignant. The class distribution is 458 benign to 241 malignant, about 64% benign to 36% malignant.

```
library(mlbench)
data(BreastCancer)
str(BreastCancer)
  'data.frame':
                    699 obs. of 11 variables:
##
   $ Id
                     : chr "1000025" "1002945" "1015425" "1016277" ...
##
   $ Cl.thickness
                     : Ord.factor w/ 10 levels "1"<"2"<"3"<"4"<..: 5 5 3 6 4 8 1 2 2 4 ...
## $ Cell.size
                     : Ord.factor w/ 10 levels "1"<"2"<"3"<"4"<..: 1 4 1 8 1 10 1 1 1 2 ...
## $ Cell.shape
                     : Ord.factor w/ 10 levels "1"<"2"<"3"<"4"<..: 1 4 1 8 1 10 1 2 1 1 ...
## $ Marg.adhesion : Ord.factor w/ 10 levels "1"<"2"<"3"<"4"<..: 1 5 1 1 3 8 1 1 1 1 ...
   $ Epith.c.size
                     : Ord.factor w/ 10 levels "1"<"2"<"3"<"4"<...: 2 7 2 3 2 7 2 2 2 2 ...
                     : Factor w/ 10 levels "1","2","3","4",..: 1 10 2 4 1 10 10 1 1 1 ...
## $ Bare.nuclei
## $ Bl.cromatin
                     : Factor w/ 10 levels "1", "2", "3", "4", ...: 3 3 3 3 3 9 3 3 1 2 ...
## $ Normal.nucleoli: Factor w/ 10 levels "1","2","3","4",..: 1 2 1 7 1 7 1 1 1 1 ...
                     : Factor w/ 9 levels "1","2","3","4",...: 1 1 1 1 1 1 1 5 1 ....
##
   $ Mitoses
## $ Class
                     : Factor w/ 2 levels "benign", "malignant": 1 1 1 1 1 2 1 1 1 1 ...
summary(BreastCancer$Class)
##
      benign malignant
##
         458
                   241
```

Divide data into train, test

First remove the Id column, then divide into 80% train, 20% test.

```
set.seed(1234)
df <- BreastCancer[,-1] # remove ID
i <- sample(1:nrow(df), 0.8*nrow(df), replace=FALSE)
train <- df[i,]
test <- df[-i,]</pre>
```

logistic regression

Build a logistic regression model.

```
glm1 <- glm(Class~., data=train, family=binomial)
## Warning: glm.fit: algorithm did not converge</pre>
```

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(glm1)

```
##
## Call:
   glm(formula = Class ~ ., family = binomial, data = train)
##
  Deviance Residuals:
##
          Min
                                  Median
                                                    3Q
                         1Q
                                                                Max
##
   -4.232e-05
                -2.100e-08
                             -2.100e-08
                                            2.100e-08
                                                         5.038e-05
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                    1.515e+05
                                                 0.000
                       -1.514e+01
                                                           1.000
## Cl.thickness.L
                        4.139e+01
                                    1.828e+05
                                                 0.000
                                                           1.000
## Cl.thickness.Q
                        2.477e+01
                                    9.563e+04
                                                 0.000
                                                           1.000
## Cl.thickness.C
                       -2.231e-01
                                                 0.000
                                                           1.000
                                    1.278e+05
## Cl.thickness<sup>4</sup>
                       -4.102e+01
                                    1.331e+05
                                                 0.000
                                                           1.000
## Cl.thickness<sup>5</sup>
                        7.805e+00
                                    1.545e+05
                                                 0.000
                                                           1.000
                                                           1.000
## Cl.thickness^6
                        3.685e+01
                                    1.539e+05
                                                 0.000
## Cl.thickness^7
                        6.812e+00
                                    1.312e+05
                                                 0.000
                                                           1.000
## Cl.thickness<sup>8</sup>
                       -4.545e+01
                                    7.591e+04
                                                -0.001
                                                           1.000
## Cl.thickness<sup>9</sup>
                       -4.518e+01
                                    1.037e+05
                                                 0.000
                                                           1.000
## Cell.size.L
                                    2.194e+05
                                                           1.000
                        1.097e+01
                                                 0.000
## Cell.size.Q
                        4.087e+01
                                    2.150e+05
                                                 0.000
                                                           1.000
## Cell.size.C
                        5.496e+00
                                    1.571e+05
                                                 0.000
                                                           1.000
## Cell.size^4
                       -3.870e+01
                                    2.079e+05
                                                 0.000
                                                           1.000
## Cell.size^5
                       -2.113e+01
                                    1.008e+05
                                                 0.000
                                                           1.000
## Cell.size^6
                                    2.307e+05
                                                           1.000
                       -4.133e+01
                                                 0.000
## Cell.size^7
                       -1.931e+01
                                    1.206e+05
                                                 0.000
                                                           1.000
## Cell.size^8
                        2.570e+01
                                    1.695e+05
                                                           1.000
                                                 0.000
                                                           1.000
## Cell.size^9
                        8.810e+00
                                    2.190e+05
                                                 0.000
## Cell.shape.L
                        6.360e+01
                                    2.526e+05
                                                 0.000
                                                           1.000
## Cell.shape.Q
                                                           1.000
                       -3.578e+01
                                    1.466e+05
                                                 0.000
## Cell.shape.C
                       -4.985e+00
                                    1.793e+05
                                                 0.000
                                                           1.000
## Cell.shape<sup>4</sup>
                        2.534e+01
                                    1.700e+05
                                                 0.000
                                                           1.000
## Cell.shape<sup>5</sup>
                       -3.471e+01
                                    2.097e+05
                                                 0.000
                                                           1.000
## Cell.shape^6
                        2.220e+01
                                    1.784e+05
                                                 0.000
                                                           1.000
## Cell.shape^7
                        2.068e+01
                                    1.418e+05
                                                 0.000
                                                           1.000
## Cell.shape^8
                        6.037e+01
                                    1.264e+05
                                                 0.000
                                                           1.000
## Cell.shape^9
                                    1.324e+05
                                                           1.000
                        2.375e+00
                                                 0.000
## Marg.adhesion.L
                        6.802e+01
                                    1.933e+05
                                                 0.000
                                                           1.000
## Marg.adhesion.Q
                       -1.248e+01
                                    1.909e+05
                                                 0.000
                                                           1.000
## Marg.adhesion.C
                       -2.669e+01
                                    1.993e+05
                                                 0.000
                                                           1.000
## Marg.adhesion<sup>4</sup>
                       -7.226e+00
                                    2.009e+05
                                                 0.000
                                                           1.000
## Marg.adhesion<sup>5</sup>
                                    3.074e+05
                                                           1.000
                        2.564e+01
                                                 0.000
## Marg.adhesion^6
                                    2.558e+05
                                                           1.000
                        2.167e+01
                                                 0.000
## Marg.adhesion 7
                       -2.507e+01
                                    2.279e+05
                                                 0.000
                                                           1.000
## Marg.adhesion^8
                       -1.661e+01
                                    2.617e+05
                                                 0.000
                                                           1.000
## Marg.adhesion 9
                        8.448e+00
                                    2.206e+05
                                                 0.000
                                                           1.000
## Epith.c.size.L
                       -4.147e+01
                                    4.843e+05
                                                 0.000
                                                           1.000
## Epith.c.size.Q
                       -3.595e+00
                                    3.726e+05
                                                 0.000
                                                           1.000
## Epith.c.size.C
                        2.454e+01
                                    1.706e+05
                                                 0.000
                                                           1.000
## Epith.c.size<sup>4</sup>
                        6.592e+01
                                    3.006e+05
                                                 0.000
                                                           1.000
```

```
## Epith.c.size<sup>5</sup>
                       3.269e+01
                                               0.000
                                                         1.000
                                  4.152e+05
## Epith.c.size^6
                       2.110e+01
                                  3.335e+05
                                               0.000
                                                         1.000
## Epith.c.size^7
                       5.731e+01
                                  1.724e+05
                                               0.000
                                                         1.000
## Epith.c.size^8
                       2.699e+01
                                  1.353e+05
                                               0.000
                                                         1.000
## Epith.c.size^9
                      -4.999e+00
                                  1.186e+05
                                               0.000
                                                         1.000
## Bare.nuclei2
                       1.307e+01
                                  1.012e+05
                                               0.000
                                                         1.000
## Bare.nuclei3
                       3.042e+01
                                  4.511e+04
                                               0.001
                                                         0.999
## Bare.nuclei4
                       3.640e+01
                                  1.192e+05
                                               0.000
                                                         1.000
## Bare.nuclei5
                       4.132e+01
                                  2.611e+04
                                               0.002
                                                         0.999
## Bare.nuclei6
                       5.184e+01
                                  3.611e+05
                                               0.000
                                                         1.000
## Bare.nuclei7
                       7.735e+01
                                  4.943e+05
                                               0.000
                                                         1.000
## Bare.nuclei8
                       4.455e+01
                                  1.415e+05
                                               0.000
                                                         1.000
                       1.290e+02
                                  5.197e+05
                                                         1.000
## Bare.nuclei9
                                               0.000
                       5.082e+01
## Bare.nuclei10
                                  7.020e+04
                                               0.001
                                                         0.999
## Bl.cromatin2
                       1.417e+01
                                  1.124e+05
                                               0.000
                                                         1.000
## Bl.cromatin3
                       1.066e+01
                                  5.170e+04
                                               0.000
                                                         1.000
## Bl.cromatin4
                       8.994e+00
                                  1.274e+05
                                                         1.000
                                               0.000
## Bl.cromatin5
                      -4.868e-01
                                  7.020e+04
                                                         1.000
                                               0.000
                       3.660e+01
## Bl.cromatin6
                                  2.673e+05
                                               0.000
                                                         1.000
## Bl.cromatin7
                       4.728e+00
                                  1.544e+05
                                               0.000
                                                         1.000
## Bl.cromatin8
                       1.746e+01
                                  2.210e+05
                                               0.000
                                                         1.000
                                  2.203e+05
## Bl.cromatin9
                      -1.918e+01
                                               0.000
                                                         1.000
## Bl.cromatin10
                      -2.536e+01
                                  3.244e+05
                                               0.000
                                                         1.000
## Normal.nucleoli2
                      -3.369e+01
                                  2.094e+05
                                               0.000
                                                         1.000
## Normal.nucleoli3
                      -3.208e-01
                                  1.599e+05
                                               0.000
                                                         1.000
## Normal.nucleoli4
                       1.397e+01
                                  1.814e+05
                                               0.000
                                                         1.000
## Normal.nucleoli5
                      -1.425e+01
                                  1.816e+05
                                               0.000
                                                         1.000
## Normal.nucleoli6
                       2.031e+01
                                  1.963e+05
                                               0.000
                                                         1.000
## Normal.nucleoli7
                      -3.473e+01
                                  1.573e+05
                                               0.000
                                                         1.000
## Normal.nucleoli8
                      -2.679e+01
                                  4.728e+05
                                                         1.000
                                               0.000
## Normal.nucleoli9
                       7.097e+01
                                  2.071e+05
                                               0.000
                                                         1.000
## Normal.nucleoli10
                       1.862e+01
                                  2.154e+05
                                               0.000
                                                         1.000
## Mitoses2
                       3.765e+01
                                  1.112e+05
                                               0.000
                                                         1.000
## Mitoses3
                       5.382e+01
                                  1.491e+05
                                                         1.000
                                               0.000
## Mitoses4
                      -1.267e+01
                                  3.089e+05
                                                         1.000
                                               0.000
## Mitoses5
                      -4.642e+01
                                  3.149e+05
                                               0.000
                                                         1.000
## Mitoses6
                      -1.207e+02
                                  4.714e+05
                                               0.000
                                                         1.000
## Mitoses7
                       1.618e+01
                                  1.458e+05
                                               0.000
                                                         1.000
## Mitoses8
                                                         1.000
                      -1.144e+01
                                  3.349e+05
                                               0.000
                       1.355e+02 3.444e+05
## Mitoses10
                                               0.000
                                                         1.000
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 6.9750e+02
                                   on 548 degrees of freedom
## Residual deviance: 2.2578e-08
                                   on 468
                                            degrees of freedom
     (10 observations deleted due to missingness)
## AIC: 162
##
## Number of Fisher Scoring iterations: 25
```

Test

Evaluate on the test data. The logistic regression model gets 92% accuracy.

```
probs1 <- predict(glm1, newdata=test, type="response")</pre>
pred1 <- ifelse(probs1>0.5, 2, 1)
table(pred1, test$Class)
##
## pred1 benign malignant
##
       1
             73
##
                        50
acc1 <- mean(pred1==as.integer(test$Class), na.rm=TRUE)</pre>
acc1
## [1] 0.9179104
Examine the results using the caret package.
library(caret)
## Warning: package 'caret' was built under R version 3.4.3
## Loading required package: lattice
## Loading required package: ggplot2
confusionMatrix(pred1, as.integer(test$Class), positive="1")
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction 1 2
            1 73 7
##
            2 4 50
##
##
##
                  Accuracy : 0.9179
##
                    95% CI: (0.8579, 0.9583)
##
       No Information Rate: 0.5746
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.8309
##
    Mcnemar's Test P-Value: 0.5465
##
##
               Sensitivity: 0.9481
##
               Specificity: 0.8772
            Pos Pred Value: 0.9125
##
            Neg Pred Value: 0.9259
##
##
                Prevalence: 0.5746
            Detection Rate: 0.5448
##
##
      Detection Prevalence: 0.5970
##
         Balanced Accuracy: 0.9126
##
##
          'Positive' Class : 1
##
```

Build a Naive Bayes classifier

Use the same test and train data for comparison.

```
library(e1071)
nb1 <- naiveBayes(train[,-10], train[,10])</pre>
summary(nb1)
           Length Class Mode
## apriori 2
                  table numeric
## tables 9
                  -none- list
## levels 2
                  -none- character
## call
           3
                  -none- call
Evaluate on the test data
The Naive Bayes model gets 96% accuracy.
pred2 <- predict(nb1, newdata=test[,-10], type="class")</pre>
table(pred2, test$Class)
##
## pred2
               benign malignant
##
                    78
     benign
                    4
                              57
##
     malignant
acc2 <- mean(pred2==test$Class)</pre>
acc2
## [1] 0.9642857
Evaluate the results with the caret package.
confusionMatrix(pred2, test$Class, positive="benign")
## Confusion Matrix and Statistics
##
##
              Reference
## Prediction benign malignant
##
     benign
                    78
                              57
##
     malignant
##
##
                  Accuracy: 0.9643
                    95% CI : (0.9186, 0.9883)
##
       No Information Rate: 0.5857
##
       P-Value [Acc > NIR] : <2e-16
##
##
##
                      Kappa: 0.927
##
    Mcnemar's Test P-Value: 0.3711
##
##
               Sensitivity: 0.9512
##
               Specificity: 0.9828
##
            Pos Pred Value: 0.9873
##
            Neg Pred Value: 0.9344
##
                Prevalence: 0.5857
##
            Detection Rate: 0.5571
      Detection Prevalence: 0.5643
##
         Balanced Accuracy: 0.9670
##
##
##
          'Positive' Class : benign
```