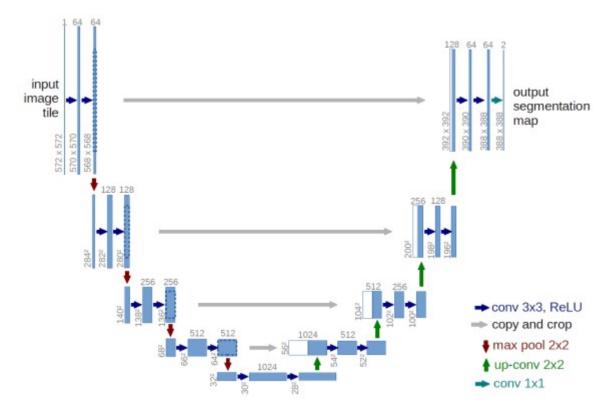
### **U-Net**

Here is the prototypical U-Net, as depicted in the original Rönneberger et al. paper (Ronneberger, Fischer, and Brox 2015).

Of this architecture, numerous variants exist. You could use different layer sizes, activations, ways to achieve downsizing and upsizing, and more. However, there is one defining characteristic: the U-shape, stabilized by the "bridges" crossing over horizontally at all levels.



In a nutshell, the left-hand side of the U resembles the convolutional architectures used in image classification. It successively reduces spatial resolution. At the same time, another dimension – the *channels* dimension – is used to build up a hierarchy of features, ranging from very basic to very specialized.

Unlike in classification, however, the output should have the same spatial resolution as the input. Thus, we need to upsize again – this is taken care of by the right-hand side of the U. But, how are we going to arrive at a good *per-pixel* classification, now that so much spatial information has been lost?

This is what the "bridges" are for: At each level, the input to an upsampling layer is a concatenation of the previous layer's output – which went through the whole compression/decompression routine – and some preserved intermediate representation from the downsizing phase. In this way, a U-Net architecture combines attention to detail with feature extraction.

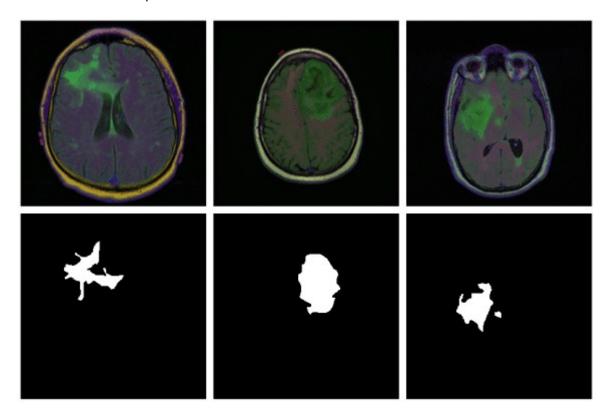
# **Brain image segmentation**

With U-Net, domain applicability is as broad as the architecture is flexible. Here, we want to detect abnormalities in brain scans. The dataset, used in Buda, Saha, and Mazurowski (2019), contains MRI images together with manually created FLAIR abnormality segmentation masks. It is available on Kaggle.

Nicely, the paper is accompanied by a GitHub repository. Below, we closely follow (though not exactly replicate) the authors' preprocessing and data augmentation code.

As is often the case in medical imaging, there is notable class imbalance in the data. For every patient, sections have been taken at multiple positions. (Number of sections per patient varies.) Most sections do not exhibit any lesions; the corresponding masks are colored black everywhere.

Here are three examples where the masks do indicate abnormalities:



Let's see if we can build a U-Net that generates such masks for us.

### **Data**

Before you start typing, here is a Colaboratory notebook to conveniently follow along.

We use pins to obtain the data. Please see this introduction if you haven't used that package before.

```
# deep learning (incl. dependencies)
library(torch)
library(torchvision)

# data wrangling
library(tidyverse)
library(zeallot)

# image processing and visualization
library(magick)
library(cowplot)

# dataset loading
```

```
library(pins)
library(zip)

torch_manual_seed(777)
set.seed(777)

# use your own kaggle.json here
pins::board_register_kaggle(token = "~/kaggle.json")

files <- pins::pin_get("mateuszbuda/lgg-mri-segmentation", board = "kaggle", extract = FALSE)</pre>
```

The dataset is not that big – it includes scans from 110 different patients – so we'll have to do with just a training and a validation set. (Don't do this in real life, as you'll inevitably end up fine-tuning on the latter.)

```
train_dir <- "data/mri_train"
valid_dir <- "data/mri_valid"

if(dir.exists(train_dir)) unlink(train_dir, recursive = TRUE, force = TRUE)

if(dir.exists(valid_dir)) unlink(valid_dir, recursive = TRUE, force = TRUE)

zip::unzip(files, exdir = "data")

file.rename("data/kaggle_3m", train_dir)

# this is a duplicate, again containing kaggle_3m (evidently a packaging error on Kaggle)

# we just remove it unlink("data/lgg-mri-segmentation", recursive = TRUE)

dir.create(valid_dir)</pre>
```

Of those 110 patients, we keep 30 for validation. Some more file manipulations, and we're set up with a nice hierarchical structure, with train\_dir and valid\_dir holding their per-patient sub-directories, respectively.

```
valid_indices <- sample(1:length(patients), 30)

patients <- list.dirs(train_dir, recursive = FALSE)

for (i in valid_indices) {
    dir.create(file.path(valid_dir, basename(patients[i])))
    for (f in list.files(patients[i])) {
        file.rename(file.path(train_dir, basename(patients[i]), f),
    file.path(valid_dir, basename(patients[i]), f))
    }
    unlink(file.path(train_dir, basename(patients[i])), recursive = TRUE)
}</pre>
```

We now need a dataset that knows what to do with these files.

## **Dataset**

Like every torch dataset, this one has <code>initialize()</code> and <code>.getitem()</code> methods. <code>initialize()</code> creates an inventory of scan and mask file names, to be used by <code>.getitem()</code> when it actually reads those files. In contrast to what we've seen in previous posts, though , <code>.getitem()</code> does not simply return input-target pairs in order. Instead, whenever the parameter <code>random\_sampling</code> is true, it will perform weighted sampling, preferring items with sizable lesions. This option will be used for the training set, to counter the class imbalance mentioned above.

The other way training and validation sets will differ is use of data augmentation. Training images/masks may be flipped, re-sized, and rotated; probabilities and amounts are configurable.

An instance of brainseg dataset encapsulates all this functionality:

```
brainseg dataset <- dataset(</pre>
  name = "brainseg dataset",
  initialize = function(img dir,
                         augmentation params = NULL,
                          random sampling = FALSE) {
    self$images <- tibble(</pre>
      img = grep(
        list.files(
          img dir,
          full.names = TRUE,
          pattern = "tif",
          recursive = TRUE
        ),
        pattern = 'mask',
        invert = TRUE,
        value = TRUE
      ),
      mask = grep(
        list.files(
          img_dir,
          full.names = TRUE,
          pattern = "tif",
          recursive = TRUE
        ),
        pattern = 'mask',
        value = TRUE
      )
    self$slice weights <- self$calc slice weights(self$images$mask)</pre>
    self$augmentation params <- augmentation params</pre>
    self$random sampling <- random sampling</pre>
  },
  .getitem = function(i) {
    index <-
      if (self$random sampling == TRUE)
```

```
sample(1:self$.length(), 1, prob = self$slice_weights)
    else
      i
    img <- self$images$img[index] %>%
      image read() %>%
      transform to tensor()
    mask <- self$images$mask[index] %>%
      image read() %>%
      transform to tensor() %>%
      transform rgb to grayscale() %>%
      torch unsqueeze(1)
    img <- self$min max scale(img)</pre>
    if (!is.null(self$augmentation params)) {
      scale param <- self$augmentation params[1]</pre>
      c(img, mask) %<-% self$resize(img, mask, scale param)</pre>
      rot param <- self$augmentation params[2]</pre>
      c(img, mask) %<-% self$rotate(img, mask, rot param)
      flip param <- self$augmentation params[3]</pre>
      c(img, mask) %<-% self$flip(img, mask, flip param)
    }
   list(img = img, mask = mask)
  },
  .length = function() {
   nrow(self$images)
  },
 calc slice weights = function(masks) {
    weights <- map_dbl(masks, function(m) {</pre>
        as.integer(magick::image data(image read(m), channels =
"gray"))
      sum(img / 255)
    })
    sum weights <- sum(weights)</pre>
    num weights <- length(weights)</pre>
    weights <- weights %>% map dbl(function(w) {
      w \leftarrow (w + sum weights * 0.1 / num weights) / (sum weights * 1.1)
    })
   weights
  },
 min_max_scale = function(x) {
   min = x \sin() \sin()
```

```
max = x max() item()
  x$clamp (min = min, max = max)
  x$add (-min)$div (max - min + 1e-5)
},
resize = function(img, mask, scale param) {
  img size <- dim(img)[2]</pre>
  rnd scale <- runif(1, 1 - scale param, 1 + scale param)</pre>
  img <- transform resize(img, size = rnd scale * img size)</pre>
  mask <- transform resize(mask, size = rnd scale * img size)</pre>
  diff <- dim(img)[2] - img size</pre>
  if (diff > 0) {
    top <- ceiling(diff / 2)</pre>
    left <- ceiling(diff / 2)</pre>
    img <- transform_crop(img, top, left, img_size, img_size)</pre>
    mask <- transform crop(mask, top, left, img size, img size)</pre>
  } else {
    img <- transform_pad(img,</pre>
                           padding = -c(
                             ceiling(diff / 2),
                              floor(diff / 2),
                              ceiling(diff / 2),
                              floor(diff / 2)
                            ) )
    mask <- transform pad(mask, padding = -c(</pre>
      ceiling(diff / 2),
      floor(diff /
               2),
      ceiling(diff /
                 2),
      floor(diff /
               2)
    ))
  list(img, mask)
},
rotate = function(img, mask, rot param) {
  rnd rot <- runif(1, 1 - rot param, 1 + rot param)</pre>
  img <- transform rotate(img, angle = rnd rot)</pre>
  mask <- transform rotate(mask, angle = rnd rot)</pre>
  list(img, mask)
},
flip = function(img, mask, flip param) {
  rnd flip <- runif(1)</pre>
  if (rnd flip > flip param) {
    img <- transform_hflip(img)</pre>
    mask <- transform hflip(mask)</pre>
  }
```

```
list(img, mask)
}
```

After instantiation, we see we have 2977 training pairs and 952 validation pairs, respectively:

```
train_ds <- brainseg_dataset(
   train_dir,
   augmentation_params = c(0.05, 15, 0.5),
   random_sampling = TRUE
)

length(train_ds)
# 2977

valid_ds <- brainseg_dataset(
   valid_dir,
   augmentation_params = NULL,
   random_sampling = FALSE
)

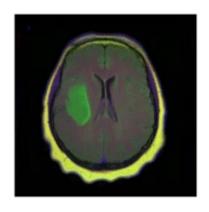
length(valid_ds)
# 952</pre>
```

As a correctness check, let's plot an image and associated mask:

```
par(mfrow = c(1, 2), mar = c(0, 1, 0, 1))

img_and_mask <- valid_ds[27]
img <- img_and_mask[[1]]
mask <- img_and_mask[[2]]

img$permute(c(2, 3, 1)) %>% as.array() %>% as.raster() %>% plot()
mask$squeeze() %>% as.array() %>% as.raster() %>% plot()
```





With torch, it is straightforward to inspect what happens when you change augmentation-related parameters. We just pick a pair from the validation set, which has not had any augmentation applied as yet, and call valid\_ds\$ directly. Just for fun, let's use more "extreme" parameters here than we do in actual training. (Actual training uses the settings from Mateusz' GitHub repository, which we assume have been carefully chosen for optimal performance. 1)

```
img_and_mask <- valid_ds[77]</pre>
img <- img_and_mask[[1]]</pre>
mask <- img_and_mask[[2]]</pre>
imgs <- map (1:24, function(i) {</pre>
  # scale factor; train ds really uses 0.05
  c(img, mask) %<-% valid_ds$resize(img, mask, 0.2)</pre>
  c(img, mask) %<-% valid ds$flip(img, mask, 0.5)
  # rotation angle; train ds really uses 15
  c(img, mask) %<-% valid ds$rotate(img, mask, 90)
  img %>%
    transform rgb to grayscale() %>%
    as.array() %>%
    as tibble() %>%
    rowid_to_column(var = "Y") %>%
    gather(key = "X", value = "value", -Y) %>%
    mutate(X = as.numeric(gsub("V", "", X))) %>%
    ggplot(aes(X, Y, fill = value)) +
    geom raster() +
    theme void() +
    theme(legend.position = "none") +
    theme (aspect.ratio = 1)
})
plot_grid(plotlist = imgs, nrow = 4)
```

Now we still need the data loaders, and then, nothing keeps us from proceeding to the next big task: building the model.

```
batch_size <- 4
train_dl <- dataloader(train_ds, batch_size)
valid_dl <- dataloader(valid_ds, batch_size)</pre>
```

# Model

Our model nicely illustrates the kind of modular code that comes "naturally" with torch. We approach things top-down, starting with the U-Net container itself.

unet takes care of the global composition – how far "down" do we go, shrinking the image while incrementing the number of filters, and then how do we go "up" again?

Importantly, it is also in the system's memory. In forward(), it keeps track of layer outputs seen going "down", to be added back in going "up".

```
unet <- nn module(</pre>
  "unet",
  initialize = function(channels in = 3,
                         n classes = 1,
                         depth = 5,
                         n filters = 6) {
    self$down_path <- nn_module_list()</pre>
    prev channels <- channels in</pre>
    for (i in 1:depth) {
      self$down path$append(down block(prev channels, 2 ^ (n filters +
i - 1)))
     prev channels <- 2 ^ (n filters + i -1)</pre>
    }
    self$up path <- nn module list()</pre>
    for (i in ((depth - 1):1)) {
      self$up path$append(up block(prev channels, 2 ^ (n filters + i -
1)))
     prev channels <- 2 ^ (n filters + i - 1)</pre>
    }
    self$last = nn conv2d(prev channels, n classes, kernel size = 1)
  },
  forward = function(x) {
   blocks <- list()</pre>
    for (i in 1:length(self$down path)) {
      x <- self$down path[[i]](x)</pre>
      if (i != length(self$down path)) {
       blocks <- c(blocks, x)
        x <- nnf max pool2d(x, 2)
      }
    for (i in 1:length(self$up path)) {
      x <- self$up path[[i]](x, blocks[[length(blocks) - i +</pre>
1]]$to(device = device))
    }
    torch sigmoid(self$last(x))
```

```
}
```

unet delegates to two containers just below it in the hierarchy: down\_block and up\_block. While down\_block is "just" there for aesthetic reasons (it immediately delegates to its own workhorse, conv\_block), in up\_block we see the U-Net "bridges" in action.

```
down block <- nn module(</pre>
  "down block",
  initialize = function(in size, out size) {
    self$conv block <- conv block(in size, out size)</pre>
  },
  forward = function(x) {
    self$conv block(x)
)
up block <- nn module(
  "up_block",
  initialize = function(in_size, out_size) {
    self$up = nn conv transpose2d(in size,
                                    out size,
                                    kernel size = 2,
                                    stride = 2)
    self$conv block = conv block(in size, out size)
  },
  forward = function(x, bridge) {
    up <- self up(x)
    torch_cat(list(up, bridge), 2) %>%
      self$conv block()
  }
)
```

Finally, a <code>conv\_block</code> is a sequential structure containing convolutional, ReLU, and dropout layers.

```
conv_block <- nn_module(
  "conv_block",

initialize = function(in_size, out_size) {

  self$conv_block <- nn_sequential(
     nn_conv2d(in_size, out_size, kernel_size = 3, padding = 1),
     nn_relu(),
     nn_dropout(0.6),
     nn_conv2d(out_size, out_size, kernel_size = 3, padding = 1),
     nn_relu()</pre>
```

```
)
},

forward = function(x){
   self$conv_block(x)
}
```

Now instantiate the model, and possibly, move it to the GPU:

```
device <- torch_device(if(cuda_is_available()) "cuda" else "cpu")
model <- unet(depth = 5)$to(device = device)</pre>
```

# **Optimization**

We train our model with a combination of cross entropy and dice loss.

The latter, though not shipped with torch, may be implemented manually:

```
calc_dice_loss <- function(y_pred, y_true) {
  smooth <- 1
  y_pred <- y_pred$view(-1)
  y_true <- y_true$view(-1)
  intersection <- (y_pred * y_true)$sum()

1 - ((2 * intersection + smooth) / (y_pred$sum() + y_true$sum() + smooth))
}
dice_weight <- 0.3</pre>
```

Optimization uses stochastic gradient descent (SGD), together with the one-cycle learning rate scheduler introduced in the context of image classification with torch.

```
optimizer <- optim_sgd(model$parameters, lr = 0.1, momentum = 0.9)
num_epochs <- 20
scheduler <- lr_one_cycle(
   optimizer,
   max_lr = 0.1,
   steps_per_epoch = length(train_dl),
   epochs = num_epochs
)</pre>
```

# **Training**

The training loop then follows the usual scheme. One thing to note: Every epoch, we save the model (using  $torch\_save()$ ), so we can later pick the best one, should performance have degraded thereafter.

```
train batch <- function(b) {</pre>
```

```
optimizer$zero grad()
  output <- model(b[[1]]$to(device = device))</pre>
  target <- b[[2]]$to(device = device)</pre>
  bce loss <- nnf binary cross entropy(output, target)</pre>
  dice_loss <- calc_dice_loss(output, target)</pre>
  loss <- dice weight * dice loss + (1 - dice weight) * bce loss
  loss$backward()
  optimizer$step()
  scheduler$step()
  list(bce_loss$item(), dice_loss$item(), loss$item())
}
valid batch <- function(b) {</pre>
  output <- model(b[[1]]$to(device = device))</pre>
  target <- b[[2]]$to(device = device)</pre>
 bce loss <- nnf binary cross entropy(output, target)</pre>
  dice loss <- calc dice loss(output, target)</pre>
  loss <- dice_weight * dice_loss + (1 - dice_weight) * bce loss</pre>
  list(bce loss$item(), dice loss$item(), loss$item())
}
for (epoch in 1:num epochs) {
  model$train()
  train bce <- c()
  train dice <- c()
  train loss <- c()</pre>
  for (b in enumerate(train dl)) {
    c(bce loss, dice loss, loss) %<-% train batch(b)
   train_bce <- c(train_bce, bce_loss)</pre>
    train dice <- c(train dice, dice loss)</pre>
    train loss <- c(train loss, loss)</pre>
  }
  torch save(model, paste0("model ", epoch, ".pt"))
  cat(sprintf("\nEpoch %d, training: loss:%3f, bce: %3f, dice: %3f\n",
               epoch, mean(train loss), mean(train bce),
mean(train dice)))
 model$eval()
  valid bce <- c()</pre>
  valid dice <- c()</pre>
```

```
valid loss <- c()</pre>
  i <- 0
  for (b in enumerate(valid dl)) {
    i <<- i + 1
   c(bce loss, dice loss, loss) %<-% valid batch(b)
   valid_bce <- c(valid_bce, bce_loss)</pre>
    valid dice <- c(valid dice, dice loss)</pre>
   valid loss <- c(valid loss, loss)</pre>
  }
  cat(sprintf("\nEpoch %d, validation: loss:%3f, bce: %3f, dice:
%3f\n",
              epoch, mean(valid loss), mean(valid bce),
mean(valid dice)))
Epoch 1, training: loss:0.304232, bce: 0.148578, dice: 0.667423
Epoch 1, validation: loss:0.333961, bce: 0.127171, dice: 0.816471
Epoch 2, training: loss:0.194665, bce: 0.101973, dice: 0.410945
Epoch 2, validation: loss:0.341121, bce: 0.117465, dice: 0.862983
[...]
Epoch 19, training: loss:0.073863, bce: 0.038559, dice: 0.156236
Epoch 19, validation: loss:0.302878, bce: 0.109721, dice: 0.753577
Epoch 20, training: loss:0.070621, bce: 0.036578, dice: 0.150055
Epoch 20, validation: loss:0.295852, bce: 0.101750, dice: 0.748757
```

#### **Evaluation**

In this run, it is the final model that performs best on the validation set. Still, we'd like to show how to load a saved model, using  $torch_load()$ .

Once loaded, put the model into eval mode:

```
saved_model <- torch_load("model_20.pt")
model <- saved_model
model$eval()</pre>
```

Now, since we don't have a separate test set, we already know the average out-of-sample metrics; but in the end, what we care about are the generated masks. Let's view some, displaying ground truth and MRI scans for comparison.

```
# without random sampling, we'd mainly see lesion-free patches
eval_ds <- brainseg_dataset(valid_dir, augmentation_params = NULL,
random_sampling = TRUE)
eval_dl <- dataloader(eval_ds, batch_size = 8)</pre>
```

```
batch <- eval dl %>% dataloader make iter() %>% dataloader next()
par(mfcol = c(3, 8), mar = c(0, 1, 0, 1))
for (i in 1:8) {
  img <- batch[[1]][i, .., drop = FALSE]</pre>
 inferred mask <- model(img$to(device = device))</pre>
 true mask <- batch[[2]][i, .., drop = FALSE]$to(device = device)</pre>
 bce <- nnf binary cross entropy(inferred mask, true mask)$to(device =</pre>
"cpu") %>%
   as.numeric()
  dc <- calc dice loss(inferred mask, true mask)$to(device = "cpu") %>%
as.numeric()
  cat(sprintf("\nSample %d, bce: %3f, dice: %3f\n", i, bce, dc))
  inferred mask <- inferred mask$to(device = "cpu") %>% as.array() %>%
.[1, 1, , ]
  inferred mask <- ifelse(inferred mask > 0.5, 1, 0)
 img[1, 1, ,] %>% as.array() %>% as.raster() %>% plot()
 true mask$to(device = "cpu")[1, 1, ,] %>% as.array() %>% as.raster()
%>% plot()
 inferred mask %>% as.raster() %>% plot()
}
```

We also print the individual cross entropy and dice losses; relating those to the generated masks might yield useful information for model tuning.

```
Sample 1, bce: 0.088406, dice: 0.387786}

Sample 2, bce: 0.026839, dice: 0.205724

Sample 3, bce: 0.042575, dice: 0.187884

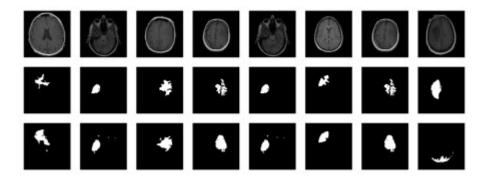
Sample 4, bce: 0.094989, dice: 0.273895

Sample 5, bce: 0.026839, dice: 0.205724

Sample 6, bce: 0.020917, dice: 0.139484

Sample 7, bce: 0.094989, dice: 0.273895

Sample 8, bce: 2.310956, dice: 0.999824
```



While far from perfect, most of these masks aren't that bad – a nice result given the small dataset!