The publically available datasets from Statistics Sweden are aggregated tables. Groups with fewer than five records are filtered out not to have any individual data being made public.

In this post, I am going to investigate with what precision it is possible to estimate the causal effect of predictors using aggregated data. I will use the dataset CPS1988 which is contained in the AER library. Cross-section data originating from the March 1988 Current Population Survey by the US Census Bureau.

I will estimate the average treatment effect on wage for ethnicity and experience respectively. I will subclassify the predictors' education and experience. I will balance on the observed confounders and make no attempts to handle unobserved covariates. I will not try to draw any conclusions on causal effects based on SUTVA assumptions.

First, define libraries and functions.

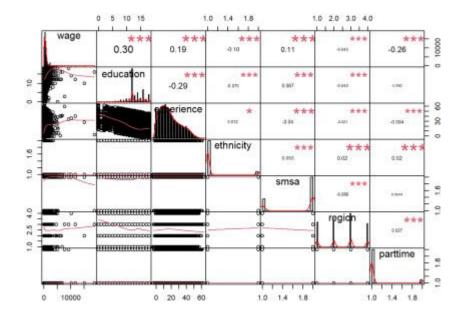
```
library (tidyverse)
## -- Attaching packages ------
tidyverse 1.3.1 --
## v ggplot2 3.3.3 v purrr 0.3.4
## v tibble 3.1.0 v dplyr 1.0.5
## v tidyr 1.1.3
                    v stringr 1.4.0
## v readr 1.4.0 v forcats 0.5.1
## Warning: package 'ggplot2' was built under R version 4.0.3
## Warning: package 'tibble' was built under R version 4.0.5
## Warning: package 'tidyr' was built under R version 4.0.5
## Warning: package 'readr' was built under R version 4.0.3
## Warning: package 'dplyr' was built under R version 4.0.5
## Warning: package 'forcats' was built under R version 4.0.3
## -- Conflicts ------
tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library (AER)
## Warning: package 'AER' was built under R version 4.0.5
## Loading required package: car
## Warning: package 'car' was built under R version 4.0.3
## Loading required package: carData
## Warning: package 'carData' was built under R version 4.0.3
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
     recode
## The following object is masked from 'package:purrr':
##
##
      some
## Loading required package: lmtest
## Warning: package 'lmtest' was built under R version 4.0.4
## Loading required package: zoo
## Warning: package 'zoo' was built under R version 4.0.5
##
```

```
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Warning: package 'sandwich' was built under R version 4.0.3
## Loading required package: survival
## Warning: package 'survival' was built under R version 4.0.5
library (bnlearn)
## Warning: package 'bnlearn' was built under R version 4.0.3
library (PerformanceAnalytics)
## Loading required package: xts
## Warning: package 'xts' was built under R version 4.0.3
## Attaching package: 'xts'
## The following objects are masked from 'package:dplyr':
##
##
      first, last
## Attaching package: 'PerformanceAnalytics'
## The following object is masked from 'package:graphics':
##
##
      legend
library (tableone)
## Warning: package 'tableone' was built under R version 4.0.4
library (Matching)
## Warning: package 'Matching' was built under R version 4.0.5
## Loading required package: MASS
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
      select
## ##
## ## Matching (Version 4.9-9, Build Date: 2021-03-15)
## ## See <a href="http://sekhon.berkeley.edu/matching">http://sekhon.berkeley.edu/matching</a> for additional documentation.
## ## Please cite software as:
## ##
       Jasjeet S. Sekhon. 2011. ``Multivariate and Propensity Score
Matching
## ##
       Software with Automated Balance Optimization: The Matching
package for R.''
## ##
        Journal of Statistical Software, 42(7): 1-52.
## ##
library (WeightIt)
## Warning: package 'WeightIt' was built under R version 4.0.5
library (lavaan)
## Warning: package 'lavaan' was built under R version 4.0.5
## This is lavaan 0.6-8
## lavaan is FREE software! Please report any bugs.
library (tidySEM)
## Registered S3 methods overwritten by 'tidySEM':
## method
                          from
```

```
##
    print.mplus.model MplusAutomation
## print.mplusObject MplusAutomation
##
   summary.mplus.model MplusAutomation
##
## Attaching package: 'tidySEM'
## The following objects are masked from 'package:bnlearn':
##
##
      nodes, nodes<-
library (cobalt)
## Warning: package 'cobalt' was built under R version 4.0.4
## cobalt (Version 4.3.1, Build Date: 2021-03-30 09:50:18 UTC)
library (jtools)
## Warning: package 'jtools' was built under R version 4.0.5
## Attaching package: 'jtools'
## The following object is masked from 'package:tidySEM':
##
##
     get data
# Argument: Vector with binned values; Value: Numeric vector where each
value is the mean of the binwidth
unbin bin <- function(x) {</pre>
 unbin x \leftarrow function(x) (parse number(unlist(strsplit(as.character(x),
",")))[1] + parse number(unlist(strsplit(as.character(x), ",")))[2])/2
 unlist(map(x, unbin x))
}
data(CPS1988)
CPS1988 n <- CPS1988 %>%
 mutate(education = as.numeric(education)) %>%
 mutate(experience = as.numeric(experience)) %>%
 mutate(region = as.numeric(region)) %>%
 mutate(smsa = as.numeric(smsa)) %>%
 mutate(parttime = as.numeric(parttime)) %>%
 mutate(ethnicity = as.numeric(ethnicity))
```

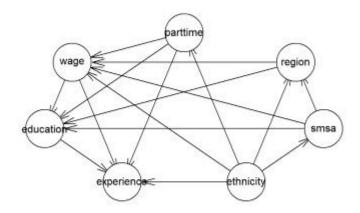
The correlation chart shows that many predictors are correlated with the response variable but also that many predictors are correlated with each other.

```
chart.Correlation(CPS1988 n, histogram = TRUE, pch = 19)
```



A Directed Ascyclical Graph (DAG) is a useful tool to identify backdoor paths, confounders, mediators and colliders. A DAG is usually constructed by expert knowledge in the problem domain. There are also algorithms for Bayesian networks that can estimate a DAG based on the statistical properties of the data, these estimations need to be validated against expert knowledge. I will estimate a DAG using a Bayesian network, the Hill Climbing (HC) algorithm.

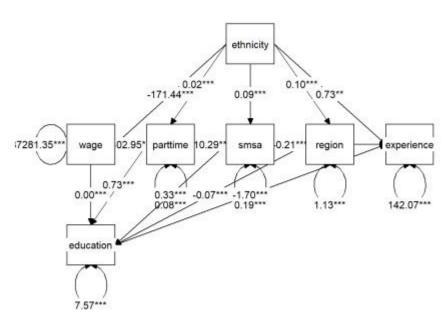
```
hcmodel <- hc(CPS1988 %>%
  mutate(education = as.numeric(education)) %>%
  mutate(experience = as.numeric(experience)))
plot(hcmodel)
```



Structural Equation Modeling (SEM) is a tool to represent a system of regressions. I will use Lavaan to represent the DAG from the Bayesian network above.

```
semmodel = '
  education ~ wage
  wage ~ parttime
```

```
experience ~ wage
  experience ~ parttime
 wage ~ ethnicity
  region ~ ethnicity
 region ~ smsa
 wage ~ smsa
 wage ~ region
 education ~ region
 education ~ parttime
 education ~ smsa
 smsa ~ ethnicity
 experience ~ education
 experience ~ ethnicity
 parttime ~ ethnicity
semfit <- sem(semmodel,</pre>
 data = CPS1988 n)
## Warning in lav_data_full(data = data, group = group, cluster =
cluster, : lavaan
## WARNING: some observed variances are (at least) a factor 1000 times
larger than
## others; use varTable(fit) to investigate
graph sem(model = semfit)
```



Since ethnicity is a binary variable I will use the Match algorithm to find individuals that are as similar as possible from the two groups African American and Caucasian. I will do a greedy matching based on Mahalanobis distance.

```
##
                                                                                                                   afam
                                                                                                                                                           SMD
                                                                              cauc
##
                                                                              25923
                                                                                                                     2232
         education (mean (SD)) 13.13 (2.90) 12.33 (2.77) 0.284
##
##
            experience (mean (SD)) 18.15 (13.04) 18.74 (13.51) 0.044
                                                            19095 (73.7) 1837 (82.3) 0.210
##
         smsa = yes (%)
##
           region (%)
                                                                                                                                                              0.644
##
                   northeast
                                                                              6073 (23.4)
                                                                                                                       368 (16.5)
##
                     midwest
                                                                                6486 (25.0)
                                                                                                                        377 (16.9)
                                                                                7468 (28.8) 1292 (57.9)
##
                     south
##
                     west
                                                                                5896 (22.7)
                                                                                                                       195 (8.7)
##
             parttime = yes (%)
                                                                                2280 (8.8)
                                                                                                                         244 (10.9) 0.072
greedymatch \leftarrow Match (Tr = as.integer (CPS1988$ethnicity) - 1, M = 1, X =
data.frame(data.matrix(CPS1988[xvars])), replace = FALSE)
matched <- CPS1988[unlist(greedymatch[c("index.treated",</pre>
"index.control")]), ]
print(CreateTableOne(vars = xvars, strata = "ethnicity", data =
matched, test = FALSE), smd = TRUE)
                                                                           Stratified by ethnicity
##
##
                                                                              cauc
                                                                                                                    afam
                                                                                                                                                           SMD
##
                                                                                2232
                                                                                                                    2232
         education (mean (SD)) 12.33 (2.76) 12.33 (2.77) 0.001
##
        experience (mean (SD)) 18.71 (13.44) 18.74 (13.51) 0.003
##
        smsa = yes (%)
                                                                             1837 (82.3) 1837 (82.3) <0.001
##
          region (%)
                                                                                                                                                              0.003
##
                  northeast
                                                                                368 (16.5)
                                                                                                                      368 (16.5)
##
                     midwest
                                                                                  375 (16.8)
                                                                                                                        377 (16.9)
                                                                                1293 (57.9) 1292 (57.9)
##
                     south
##
                                                                                  196 (8.8)
                                                                                                                       195 (8.7)
                      west
             parttime = yes (%)
                                                                                   244 (10.9)
##
                                                                                                                      244 (10.9) < 0.001
matched <- matched %>% mutate(ethnicity n = as.integer(ethnicity) - 1)
\texttt{t.test} \, (\texttt{matched\$wage} \, [\texttt{matched\$ethnicity\_n} \, == \, 1] \, - \, \texttt{matched\$wage} \, [\texttt{matched\$} \, ] \, + \, \texttt{matched\$wage} \, [\texttt{matched\$} \, ] \, + \, \texttt{matched\$} \, ] \, + \, \texttt{matched\$} \, ] \, + \, \texttt{matched\$} \, + \, \texttt{matched\$} \, ] \, + \, \texttt{matched\$} \, + \, \texttt{match
ethnicity n == 0])
##
##
         One Sample t-test
## data: matched$wage[matched$ethnicity n == 1] -
matched$wage[matched$ethnicity n == 0]
## t = -12.989, df = 2231, p-value < 2.2e-16
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -131.18979 -96.77381
## sample estimates:
## mean of x
## -113.9818
```

Another way to estimate the causal effect of ethnicity on wage is by calculating the propensity score. By regressing on the treatment, i.e. the variable that we want to calculate the effect for,

we can reduce the selection bias by balancing on the covariates. Below you can see the balancing before and after using the propensity score.

```
W.out <- weightit(ethnicity ~ education + experience + smsa + region +
parttime,
  data = CPS1988, method = "ebal")
model lm ethnicity <- lm(wage ~ ethnicity, data = CPS1988, weights =
W.out$weights)
bal.tab(ethnicity ~ education + experience + smsa + region + parttime,
  data = CPS1988, estimand = "ATT", m.threshold = .05)
## Balance Measures
##
                        Type Diff.Un M.Threshold.Un
## education Contin. -0.2909 Not Balanced, >0.05
                    Contin. 0.0435 Balanced, < 0.05
## experience
## smsa_yes Binary 0.0864 Not Balanced, >0.05
## region northeast Binary -0.0694 Not Balanced, >0.05
## region_midwest Binary -0.0813 Not Balanced, >0.05
## region_south Binary 0.2908 Not Balanced, >0.05
## region_west Binary -0.1401 Not Balanced, >0.05
## parttime_yes Binary 0.0214 Balanced, <0.05</pre>
##
## Balance tally for mean differences
                       count
## Balanced, <0.05
## Not Balanced, >0.05
## Variable with the greatest mean difference
## Variable Diff.Un M.Threshold.Un
## education -0.2909 Not Balanced, >0.05
##
## Sample sizes
## cauc afam
## All 25923 2232
bal.tab(W.out, m.threshold = .05, disp.v.ratio = TRUE)
## Call
## weightit(formula = ethnicity ~ education + experience + smsa +
      region + parttime, data = CPS1988, method = "ebal")
##
## Balance Measures
                       Type Diff.Adj M.Threshold V.Ratio.Adj
##
## education Contin. 0.0001 Balanced, <0.05
                                                               0.7731
                    Contin. 0.0000 Balanced, < 0.05
## experience
                                                               0.9613
## smsa_yes Binary 0.0000 Balanced, <0.05
## region northeast Binary 0.0000 Balanced, <0.05</pre>
## region_midwest Binary -0.0000 Balanced, <0.05
## region_south Binary -0.0000 Balanced, <0.05
## region_west Binary -0.0000 Balanced, <0.05
## parttime_yes Binary 0.0001 Balanced, <0.05</pre>
##
```

```
## Balance tally for mean differences
##
## Balanced, <0.05
## Not Balanced, >0.05
## Variable with the greatest mean difference
## Variable Diff.Adj M.Threshold
## education 0.0001 Balanced, <0.05
##
## Effective sample sizes
     cauc afam
## Unadjusted 25923. 2232.
## Adjusted 25833.39 1233.1
Estimate the causal effect of experience on wage by calculating the propensity score.
W.out <- weightit(experience ~ ethnicity + education + smsa + region +
parttime,
 data = CPS1988, method = "ebal")
model lm experience <- lm(wage ~ experience, data = CPS1988, weights =
W.out$weights)
bal.tab(experience ~ ethnicity + education + smsa + region + parttime,
  data = CPS1988, estimand = "ATT", m.threshold = .05)
## Balance Measures
                     Type Corr.Un
## ethnicity afam Binary 0.0121
## education Contin. -0.2867
             Binary -0.0397
## smsa yes
## region northeast Binary 0.0251
## region midwest Binary -0.0166
## region_south Binary 0.0114
## region_west Binary -0.0212
## parttime yes
                   Binary -0.0942
## Sample sizes
## Total
## All 28155
bal.tab(W.out, m.threshold = .05, disp.v.ratio = TRUE)
## Call
## weightit(formula = experience ~ ethnicity + education + smsa +
   region + parttime, data = CPS1988, method = "ebal")
##
## Balance Measures
                    Type Corr.Adj Diff.Adj M.Threshold
## ethnicity afam Binary -0 -0 Balanced, <0.05
## smsa_yes Binary -0
## region_northeast Binary 
## rociss
                                         0 Balanced, <0.05
                                      -0 Balanced, <0.05
                                         0 Balanced, <0.05
## region midwest Binary 0
                                         0 Balanced, <0.05
```

```
-0
## region south
                 Binary
                                    -0 Balanced, <0.05
## region west
                            -0
                                   -0 Balanced, <0.05
                 Binary
                            0
## parttime yes
                                    0 Balanced, <0.05
                 Binary
## Balance tally for target mean differences
##
                   count
## Balanced, <0.05
## Not Balanced, >0.05
##
## Variable with the greatest target mean difference
  Variable Diff.Adj M.Threshold
##
## Effective sample sizes
##
            Total
## Unadjusted 28155.
## Adjusted 25793.54
```

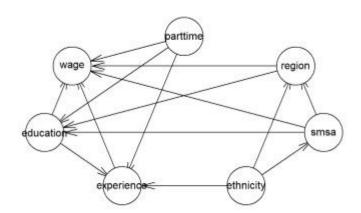
Let's now investigate how aggregating the numerical predictors in the data affects the precision when estimating the causal effect on wage. I will also filter out groups with less than 5 persons in them so that any individual can not be identified in the material. The binning and filtering reduces the original dataset by 98.9 %. By expanding the reduced dataset the original dataset can be estimated.

```
CPS1988 refi <- CPS1988 %>%
 mutate(education = as.numeric(education)) %>%
 mutate(experience = as.numeric(experience)) %>%
 mutate(education = cut interval(education, 5)) %>%
 mutate(experience = cut interval(experience, 5)) %>%
 group by (education, experience, ethnicity, smsa, region, parttime)
응>응
 mutate (wage = mean(wage)) %>%
 group by (wage, education, experience, ethnicity, smsa, region,
parttime) %>%
 tally() %>%
 mutate(experience = unbin bin(experience)) %>%
 mutate(education = unbin bin(education)) %>%
 filter(n > 4)
dim(CPS1988 refi)
## [1] 302 8
CPS1988 refiexp <- CPS1988 refi[rep(seq(nrow(CPS1988 refi)),</pre>
CPS1988 refi$n),]
dim(CPS1988 refiexp)
## [1] 27797
```

How has the reduction affected the DAG? It is not possible to use weights in the hc algorithm. Therefore I will use the expanded table based on the data in the aggregated table.

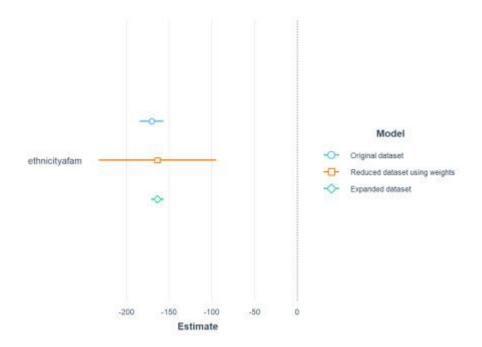
```
hcmodel_refiexp <- hc(dplyr::select(CPS1988_refiexp %>%
   mutate(education = as.numeric(education)) %>%
```

```
mutate(experience = as.numeric(experience)), -n))
plot(hcmodel refiexp)
```



For comparison, I will plot the coefficients for ethnicity for the linear model based on the original data, aggregated data and the expanded data. I will use robust (Heteroskedasticity-Consistent) error estimates.

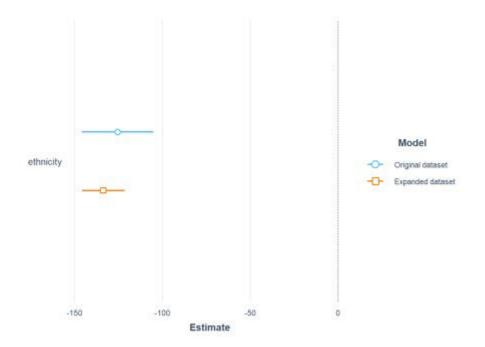
```
model <- lm(wage ~ ethnicity, data = CPS1988)</pre>
model refi <- lm(wage ~ ethnicity, data = CPS1988 refi, weights = n)</pre>
model refiexp <- lm(wage ~ ethnicity, data = CPS1988 refiexp)</pre>
plot_summs(model, model_refi, model_refiexp, robust = "HC1",
 model.names = c(
    "Original dataset",
    "Reduced dataset using weights",
    "Expanded dataset"))
## Loading required namespace: broom.mixed
## Warning in checkMatrixPackageVersion(): Package version
inconsistency detected.
## TMB was built with Matrix version 1.3.2
## Current Matrix version is 1.2.18
## Please re-install 'TMB' from source using install.packages('TMB',
type = 'source') or ask CRAN for a binary version of 'TMB' matching
CRAN's 'Matrix' package
```



Now let's estimate the causal effect of ethnicity on wage using propensity scores. I will use the expanded dataset since I did not get any reasonable results using the argument s.weights in weightit.

```
W.out <- weightit(ethnicity ~ education + experience + smsa + region +
parttime,
  data = CPS1988 refiexp, method = "ebal")
model refiexp <- lm(wage ~ ethnicity, data = CPS1988 refiexp, weights =
W.out$weights)
coeftest(model_refiexp, vcov = vcovHC, type = "HC1")
## t test of coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
##
                              1.4634 421.541 < 2.2e-16 ***
## (Intercept)
                  616.8706
## ethnicityafam -133.7648
                               6.1773 -21.654 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
bal.tab(ethnicity ~ education + experience + smsa + region + parttime,
 data = CPS1988 refiexp, estimand = "ATT", m.threshold = .05)
## Balance Measures
##
                       Type Diff.Un
                                         M.Threshold.Un
## education
                    Contin. -0.2050 Not Balanced, >0.05
## experience
                    Contin. -0.0567 Not Balanced, >0.05
                    Binary 0.0995 Not Balanced, >0.05
## smsa yes
## region northeast Binary -0.0784 Not Balanced, >0.05
## region midwest
                    Binary -0.0800 Not Balanced, >0.05
## region south
                    Binary 0.3059 Not Balanced, >0.05
                    Binary -0.1475 Not Balanced, >0.05
## region west
## parttime yes
                    Binary -0.0052
                                      Balanced, <0.05
## Balance tally for mean differences
```

```
##
                      count
## Balanced, <0.05
## Not Balanced, >0.05
## Variable with the greatest mean difference
       Variable Diff.Un M.Threshold.Un
## region south 0.3059 Not Balanced, >0.05
##
## Sample sizes
   cauc afam
## All 25732 2065
bal.tab(W.out, m.threshold = .05, disp.v.ratio = TRUE)
## Call
## weightit(formula = ethnicity ~ education + experience + smsa +
##
      region + parttime, data = CPS1988 refiexp, method = "ebal")
##
## Balance Measures
                                      M.Threshold V.Ratio.Adj
                      Type Diff.Adj
## education
                  Contin. 0.0001 Balanced, < 0.05 0.6710
## experience
                  Contin. 0.0000 Balanced, < 0.05
                                                       0.8969
                   Binary 0.0000 Balanced, <0.05
## smsa yes
## region northeast Binary 0.0000 Balanced, <0.05
## region midwest Binary 0.0001 Balanced, <0.05</pre>
## region south
                 Binary -0.0000 Balanced, <0.05
## region west
                   Binary -0.0001 Balanced, <0.05
## parttime yes
                   Binary -0.0000 Balanced, <0.05
##
## Balance tally for mean differences
##
                     count
## Balanced, <0.05
## Not Balanced, >0.05
## Variable with the greatest mean difference
         Variable Diff.Adj M.Threshold
## region midwest 0.0001 Balanced, <0.05</pre>
##
## Effective sample sizes
                cauc afam
## Unadjusted 25732. 2065.
## Adjusted 25650.5 1094.35
plot summs(model lm ethnicity, model refiexp, scale = TRUE, robust =
"HC1",
 model.names = c(
   "Original dataset",
   "Expanded dataset"))
```



Let's compare the coefficients for experience for the linear model based on the original data, aggregated data and the expanded data.

```
model <- lm(wage ~ experience, data = CPS1988_refi, weights = n)

model_refi <- lm(wage ~ experience, data = CPS1988_refi, weights = n)

model_refiexp <- lm(wage ~ experience, data = CPS1988_refiexp)

plot_summs(model, model_refi, model_refiexp, robust = "HC1",
    model.names = c(
    "Original dataset",
    "Reduced dataset using weights",
    "Expanded dataset"))

Model

Original dataset

Produced dataset using weights

Expanded dataset

The dataset using weights

Expanded dataset

The dataset using weights

Expanded dataset
```

Let's estimate the causal effect of ethnicity on wage using propensity scores. I will use the expanded dataset since I did not get any reasonable results using the argument s.wights in weightit.

Estimate

```
W.out <- weightit(experience ~ ethnicity + education + smsa + region +
parttime,
  data = CPS1988 refiexp, method = "ebal")
model refiexp <- lm(wage ~ experience, data = CPS1988 refiexp, weights
= W.out$weights)
coeftest(model refiexp, vcov = vcovHC, type = "HC1")
##
## t test of coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 452.45062 2.25958 200.237 < 2.2e-16 ***
## experience 8.60394 0.14098 61.029 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
bal.tab(experience ~ ethnicity + education + smsa + region + parttime,
  data = CPS1988_refiexp, estimand = "ATT", m.threshold = .05)
## Balance Measures
                     Type Corr.Un
## ethnicity_afam Binary -0.0143
## education Contin. -0.2736
## smsa yes
             Binary -0.0339
## region northeast Binary 0.0256
## region midwest Binary -0.0156
## region south
                   Binary 0.0092
## region west
                   Binary -0.0202
## parttime_yes
                   Binary -0.1072
##
## Sample sizes
## Total
## All 27797
bal.tab(W.out, m.threshold = .05, disp.v.ratio = TRUE)
## Call
## weightit(formula = experience ~ ethnicity + education + smsa +
     region + parttime, data = CPS1988 refiexp, method = "ebal")
## Balance Measures
##
                   Type Corr.Adj Diff.Adj M.Threshold
## ethnicity afam Binary -0 -0 Balanced, <0.05
## education Contin.
                                -0
                                        -0 Balanced, <0.05
## smsa_yes Binary
## region_northeast Binary
                                       -0 Balanced, <0.05
                               -0
                                0
                                         0 Balanced, <0.05
## region_midwest Binary
                                0
                                         0 Balanced, <0.05
                   Dinary -0
Binary -0
Binary -0
                                       0 Balanced, <0.05
-0 Balanced, <0.05
-0 Balanced, <0.05
## region_south Binary
## region west
## parttime yes
                                        -0 Balanced, <0.05
##
## Balance tally for target mean differences
##
                      count
```

```
## Balanced, <0.05
## Not Balanced, >0.05
##
## Variable with the greatest target mean difference
## Variable Diff.Adj M.Threshold
## education -0 Balanced, <0.05
##
## Effective sample sizes
##
                 Total
## Unadjusted 27797.
## Adjusted 25618.89
plot summs(model lm experience, model refiexp, robust = "HC1",
  model.names = c(
    "Original dataset",
    "Expanded dataset"))
                                               Model
 experience
                                           -O- Original dataset
                                            -D- Expanded dataset
        0.0
                2.5
                                7.5
                                        10.0
                      Estimate
```