In this post, we build a network that uses a sequence of observations to predict a value for the very next point in time. What if we’d like to forecast a *sequence* of values, corresponding to, say, a week or a month of measurements?

One thing we could do is feed back into the system the previously forecasted value; this is something we’ll try at the end of this post. Subsequent posts will explore other options, some of them involving significantly more complex architectures. It will be interesting to compare their performances; but the essential goal is to introduce some torch “recipes” that you can apply to your own data.

We start by examining the dataset used. It is a low-dimensional, but pretty polyvalent and complex one.

# Time-series inspection

The vic\_elec dataset, available through package tsibbledata, provides three years of half- hourly electricity demand for Victoria, Australia, augmented by same-resolution temperature information and a daily holiday indicator.

library(tidyverse) library(lubridate)

library(tsibble) # Tidy Temporal Data Frames and Tools library(feasts) # Feature Extraction and Statistics for Time Series library(tsibbledata) # Diverse Datasets for 'tsibble'

vic\_elec %>% glimpse() Rows: 52,608

Columns: 5

$ Time 2012-01-01 00:00:00, 2012-01-01 00:30:00, 2012-01-01 01:00:00,…

$ Demand 4382.825, 4263.366, 4048.966, 3877.563, 4036.230,

3865.597, 369…

$ Temperature 21.40, 21.05, 20.70, 20.55, 20.40, 20.25, 20.10, 19.60,

19.10, …

$ Date 2012-01-01, 2012-01-01, 2012-01-01, 2012-01-01,

2012-01-01, 20…

$ Holiday TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRUE, TRU…

Depending on what subset of variables is used, and whether and how data is temporally aggregated, these data may serve to illustrate a variety of different techniques. In this first introductory post though, as well as in most of its successors, we’ll attempt to forecast Demand without relying on additional information, and we keep the original resolution.

To get an impression of how electricity demand varies over different timescales. Let’s inspect data for two months that nicely illustrate the U-shaped relationship between temperature and demand: January, 2014 and July, 2014.

First, here is July.

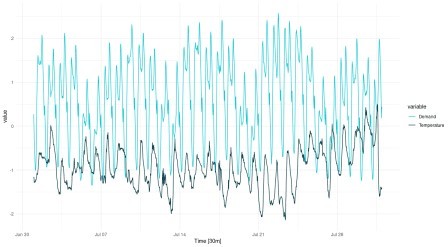
vic\_elec\_2014 <- vic\_elec %>% filter(year(Date) == 2014) %>% select(-c(Date, Holiday)) %>%

mutate(Demand = scale(Demand), Temperature = scale(Temperature)) %>% pivot\_longer(-Time, names\_to = "variable") %>%

update\_tsibble(key = variable)

vic\_elec\_2014 %>% filter(month(Time) == 7) %>% autoplot() +

scale\_colour\_manual(values = c("#08c5d1", "#00353f")) + theme\_minimal()



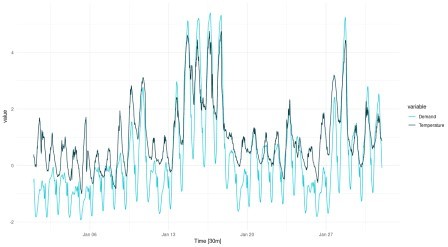
(#fig:unnamed-chunk-3)Temperature and electricity demand (normalized). Victoria, Australia, 07/2014.

It’s winter; temperature fluctuates below average, while electricity demand is above average (heating). There is strong variation over the course of the day; we see troughs in the demand curve corresponding to ridges in the temperature graph, and vice versa. While diurnal variation dominates, there also is variation over the days of the week. Between weeks though, we don’t see much difference.

Compare this with the data for January:

vic\_elec\_2014 %>% filter(month(Time) == 1) %>% autoplot() +

scale\_colour\_manual(values = c("#08c5d1", "#00353f")) + theme\_minimal()



(#fig:unnamed-chunk-5)Temperature and electricity demand (normalized). Victoria, Australia, 01/2014.

We still see the strong circadian variation. We still see some day-of-week variation. But now it is *high* temperatures that cause elevated demand (cooling). Also, there are two periods of unusually high temperatures, accompanied by exceptional demand. We anticipate that in a univariate forecast, not taking into account temperature, this will be hard – or even, impossible – to forecast.

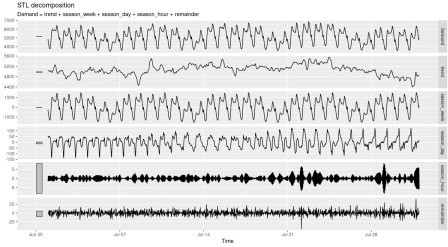
Let’s see a concise portrait of how Demand behaves using feasts::STL(). First, here is the decomposition for July:

vic\_elec\_2014 <- vic\_elec %>% filter(year(Date) == 2014) %>% select(-c(Date, Holiday))

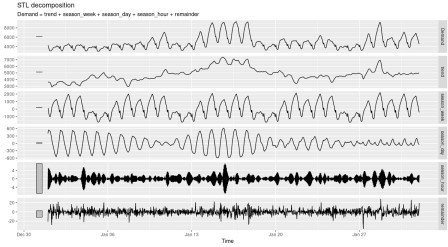
cmp <- vic\_elec\_2014 %>% filter(month(Time) == 7) %>% model(STL(Demand)) %>%

components()

cmp %>% autoplot()



(#fig:unnamed-chunk-7)STL decomposition of electricity demand. Victoria, Australia, 07/2014. And here, for January:



(#fig:unnamed-chunk-8)STL decomposition of electricity demand. Victoria, Australia, 01/2014.

Both nicely illustrate the strong circadian and weekly seasonalities (with diurnal variation substantially stronger in January). If we look closely, we can even see how the trend component is more influential in January than in July. This again hints at much stronger difficulties predicting the January than the July developments.

Now that we have an idea what awaits us, let’s begin by creating a torch dataset.

# Data input

Here is what we intend to do. We want to start our journey into forecasting by using a sequence of observations to predict their immediate successor. In other words, the input (x) for each batch item is a vector, while the target (y) is a single value. The length of the input sequence, x, is parameterized as n\_timesteps, the number of consecutive observations to extrapolate from.

The dataset will reflect this in its .getitem() method. When asked for the observations at index i, it will return tensors like so:

list(

)

x = self$x[start:end], y = self$x[end+1]

where start:end is a vector of indices, of length n\_timesteps, and end+1 is a single index.

Now, if the dataset just iterated over its input in order, advancing the index one at a time, these lines could simply read

list(

)

x = self$x[i:(i + self$n\_timesteps - 1)], y = self$x[self$n\_timesteps + 1]

Since many sequences in the data are similar, we can reduce training time by making use of a fraction of the data in every epoch. This can be accomplished by (optionally) passing a sample\_frac smaller than 1. In initialize(), a random set of start indices is prepared;

.getitem() then just does what it normally does: look for the (x,y) pair at a given index. Here is the complete dataset code:

elec\_dataset <- dataset( name = "elec\_dataset",

initialize = function(x, n\_timesteps, sample\_frac = 1) { self$n\_timesteps <- n\_timesteps

self$x <- torch\_tensor((x - train\_mean) / train\_sd) n <- length(self$x) - self$n\_timesteps

self$starts <- sort(sample.int( n = n,

size = n \* sample\_frac

))

},

.getitem = function(i) { start <- self$starts[i]

end <- start + self$n\_timesteps - 1

list(

x = self$x[start:end], y = self$x[end + 1]

)

},

.length = function() { length(self$starts)

}

)

You may have noticed that we normalize the data by globally defined train\_mean and

train\_sd. We yet have to calculate those.

The way we split the data is straightforward. We use the whole of 2012 for training, and all of 2013 for validation. For testing, we take the “difficult” month of January, 2014. You are invited to compare testing results for July that same year, and compare performances.

vic\_elec\_get\_year <- function(year, month = NULL) { vic\_elec %>%

filter(year(Date) == year, month(Date) == if (is.null(month)) month(Date) else month) %>%

as\_tibble() %>% select(Demand)

}

elec\_train <- vic\_elec\_get\_year(2012) %>% as.matrix() elec\_valid <- vic\_elec\_get\_year(2013) %>% as.matrix()

elec\_test <- vic\_elec\_get\_year(2014, 1) %>% as.matrix() # or 2014, 7,

alternatively

train\_mean <- mean(elec\_train) train\_sd <- sd(elec\_train)

Now, to instantiate a dataset, we still need to pick sequence length. From prior inspection, a week seems like a sensible choice.

n\_timesteps <- 7 \* 24 \* 2 # days \* hours \* half-hours

Now we can go ahead and create a dataset for the training data. Let’s say we’ll make use of 50% of the data in each epoch:

train\_ds <- elec\_dataset(elec\_train, n\_timesteps, sample\_frac = 0.5) length(train\_ds)

8615

Quick check: Are the shapes correct?

train\_ds[1]

$x torch\_tensor

-0.4141

-0.5541

[...] ### lines removed by me 0.8204

0.9399

... [the output was truncated (use n=-1 to disable)] [ CPUFloatType{336,1} ]

$y torch\_tensor

-0.6771

[ CPUFloatType{1} ]

Yes: This is what we wanted to see. The input sequence has n\_timesteps values in the first dimension, and a single one in the second, corresponding to the only feature present, Demand. As intended, the prediction tensor holds a single value, corresponding– as we know – to n\_timesteps+1.

That takes care of a single input-output pair. As usual, batching is arranged for by torch’s dataloader class. We instantiate one for the training data, and immediately again verify the outcome:

batch\_size <- 32

train\_dl <- train\_ds %>% dataloader(batch\_size = batch\_size, shuffle = TRUE)

length(train\_dl)

b <- train\_dl %>% dataloader\_make\_iter() %>% dataloader\_next() b

$x torch\_tensor (1,.,.) =

0.4805

0.3125

[...] ### lines removed by me

-1.1756

-0.9981

... [the output was truncated (use n=-1 to disable)] [ CPUFloatType{32,336,1} ]

$y torch\_tensor

0.1890

0.5405

[...] ### lines removed by me 2.4015

0.7891

... [the output was truncated (use n=-1 to disable)] [ CPUFloatType{32,1} ]

We see the added batch dimension in front, resulting in overall shape (batch\_size, n\_timesteps, num\_features). This is the format expected by the model, or more precisely, by its initial RNN layer.

Before we go on, let’s quickly create datasets and dataloaders for validation and test data, as well.

valid\_ds <- elec\_dataset(elec\_valid, n\_timesteps, sample\_frac = 0.5) valid\_dl <- valid\_ds %>% dataloader(batch\_size = batch\_size)

test\_ds <- elec\_dataset(elec\_test, n\_timesteps) test\_dl <- test\_ds %>% dataloader(batch\_size = 1)

# Model

The model consists of an RNN – of type GRU or LSTM, as per the user’s choice – and an output layer. The RNN does most of the work; the single-neuron linear layer that outputs the prediction compresses its vector input to a single value.

Here, first, is the model definition.

model <- nn\_module(

initialize = function(type, input\_size, hidden\_size, num\_layers = 1, dropout = 0) {

self$type <- type self$num\_layers <- num\_layers

self$rnn <- if (self$type == "gru") { nn\_gru(

input\_size = input\_size, hidden\_size = hidden\_size, num\_layers = num\_layers, dropout = dropout,

batch\_first = TRUE

)

} else { nn\_lstm(

input\_size = input\_size, hidden\_size = hidden\_size, num\_layers = num\_layers, dropout = dropout, batch\_first = TRUE

)

}

self$output <- nn\_linear(hidden\_size, 1)

},

forward = function(x) {

# list of [output, hidden]

# we use the output, which is of size (batch\_size, n\_timesteps, hidden\_size)

x <- self$rnn(x)[[1]]

# from the output, we only want the final timestep # shape now is (batch\_size, hidden\_size)

x <- x[ , dim(x)[2], ]

# feed this to a single output neuron # final shape then is (batch\_size, 1) x %>% self$output()

}

)

Most importantly, this is what happens in forward().

1. The RNN returns a list. The list holds two tensors, an *output*, and a synopsis of *hidden states*. We discard the state tensor, and keep the output only. The distinction between state and output, or rather, the way it is reflected in what a torch RNN returns, deserves to be inspected more closely. We’ll do that in a second.

x <- self$rnn(x)[[1]]

1. Of the output tensor, we’re interested in only the final time-step, though.

x <- x[ , dim(x)[2], ]

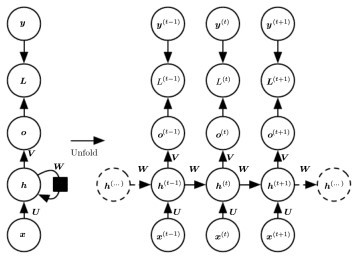
1. Only this one, thus, is passed to the output layer.

x %>% self$output()

1. Finally, the said output layer’s output is returned.

Now, a bit more on *states* vs. *outputs*. Consider Fig. 1, from Goodfellow, Bengio, and Courville

(2016).



Let’s pretend there are three time steps only, corresponding to \(t-1\), \(t\), and \(t+1\). The input sequence, accordingly, is composed of \(x\_{t-1}\), \(x\_{t}\), and \(x\_{t+1}\).

At each \(t\), a hidden state is generated, and so is an output. Normally, if our goal is to predict

\(y\_{t+2}\), that is, the very next observation, we want to take into account the complete input sequence. Put differently, we want to have run through the complete machinery of state updates. The logical thing to do would thus be to choose \(o\_{t+1}\), for either direct return from forward() or for further processing.

Indeed, return \(o\_{t+1}\) is what a Keras LSTM or GRU would do by default.1 Not so its torch counterparts. In torch, the output tensor comprises all of \(o\). This is why, in step two above, we select the single time step we’re interested in – namely, the last one.

In later posts, we will make use of more than the last time step. Sometimes, we’ll use the sequence of hidden states (the \(h\)s) instead of the outputs (the \(o\)s). So you may feel like asking, what if we used \(h\_{t+1}\) here instead of \(o\_{t+1}\)? The answer is: With a GRU, this would not make a difference, as those two are identical. With LSTM though, it would, as LSTM keeps a second, namely, the “cell”, state2.

On to initialize(). For ease of experimentation, we instantiate either a GRU or an LSTM based on user input. Two things are worth noting:

We pass batch\_first = TRUE when creating the RNNs. This is required with torch RNNs when we want to consistently have batch items stacked in the first dimension. And we *do* want that; it is arguably less confusing than a change of dimension semantics for one sub-type of module.

num\_layers can be used to build a stacked RNN, corresponding to what you’d get in Keras when chaining two GRUs/LSTMs (the first one created with return\_sequences

= TRUE). This parameter, too, we’ve included for quick experimentation.

Let’s instantiate a model for training. It will be a single-layer GRU with thirty-two units.

# training RNNs on the GPU currently prints a warning that may clutter # the console

# alternatively, use # device <- "cpu"

device <- torch\_device(if (cuda\_is\_available()) "cuda" else "cpu")

net <- model("gru", 1, 32) net <- net$to(device = device)

# Training

After all those RNN specifics, the training process is completely standard.

optimizer <- optim\_adam(net$parameters, lr = 0.001) num\_epochs <- 30

train\_batch <- function(b) {

optimizer$zero\_grad()

output <- net(b$x$to(device = device)) target <- b$y$to(device = device)

loss <- nnf\_mse\_loss(output, target) loss$backward()

optimizer$step()

loss$item()

}

valid\_batch <- function(b) {

output <- net(b$x$to(device = device)) target <- b$y$to(device = device)

loss <- nnf\_mse\_loss(output, target) loss$item()

}

for (epoch in 1:num\_epochs) { net$train()

train\_loss <- c()

coro::loop(for (b in train\_dl) { loss <-train\_batch(b)

train\_loss <- c(train\_loss, loss)

})

cat(sprintf("\nEpoch %d, training: loss: %3.5f \n", epoch,

mean(train\_loss))

net$eval() valid\_loss <- c()

coro::loop(for (b in valid\_dl) { loss <- valid\_batch(b)

valid\_loss <- c(valid\_loss, loss)

})

cat(sprintf("\nEpoch %d, validation: loss: %3.5f \n", epoch, mean(valid\_loss))

}

Epoch 1, training: loss: 0.21908

Epoch 1, validation: loss: 0.05125

Epoch 2, training: loss: 0.03245

Epoch 2, validation: loss: 0.03391

Epoch 3, training: loss: 0.02346

Epoch 3, validation: loss: 0.02321

Epoch 4, training: loss: 0.01823

Epoch 4, validation: loss: 0.01838

Epoch 5, training: loss: 0.01522

Epoch 5, validation: loss: 0.01560

Epoch 6, training: loss: 0.01315

Epoch 6, validation: loss: 0.01374

Epoch 7, training: loss: 0.01205

Epoch 7, validation: loss: 0.01200

Epoch 8, training: loss: 0.01155

Epoch 8, validation: loss: 0.01157

Epoch 9, training: loss: 0.01118

Epoch 9, validation: loss: 0.01096

Epoch 10, training: loss: 0.01070

Epoch 10, validation: loss: 0.01132

|  |  |  |
| --- | --- | --- |
| Epoch | 11, | training: loss: 0.01003 |
| Epoch | 11, | validation: loss: 0.01150 |
| Epoch | 12, | training: loss: 0.00943 |
| Epoch | 12, | validation: loss: 0.01106 |
| Epoch | 13, | training: loss: 0.00922 |
| Epoch | 13, | validation: loss: 0.01069 |
| Epoch | 14, | training: loss: 0.00862 |
| Epoch | 14, | validation: loss: 0.01125 |
| Epoch | 15, | training: loss: 0.00842 |
| Epoch | 15, | validation: loss: 0.01095 |
| Epoch | 16, | training: loss: 0.00820 |
| Epoch | 16, | validation: loss: 0.00975 |
| Epoch | 17, | training: loss: 0.00802 |
| Epoch | 17, | validation: loss: 0.01120 |
| Epoch | 18, | training: loss: 0.00781 |
| Epoch | 18, | validation: loss: 0.00990 |
| Epoch | 19, | training: loss: 0.00757 |
| Epoch | 19, | validation: loss: 0.01017 |
| Epoch | 20, | training: loss: 0.00735 |
| Epoch | 20, | validation: loss: 0.00932 |
| Epoch | 21, | training: loss: 0.00723 |
| Epoch | 21, | validation: loss: 0.00901 |
| Epoch | 22, | training: loss: 0.00708 |
| Epoch | 22, | validation: loss: 0.00890 |
| Epoch | 23, | training: loss: 0.00676 |
| Epoch | 23, | validation: loss: 0.00914 |

|  |  |  |
| --- | --- | --- |
| Epoch | 24, | training: loss: 0.00666 |
| Epoch | 24, | validation: loss: 0.00922 |
| Epoch | 25, | training: loss: 0.00644 |
| Epoch | 25, | validation: loss: 0.00869 |
| Epoch | 26, | training: loss: 0.00620 |
| Epoch | 26, | validation: loss: 0.00902 |
| Epoch | 27, | training: loss: 0.00588 |
| Epoch | 27, | validation: loss: 0.00896 |
| Epoch | 28, | training: loss: 0.00563 |
| Epoch | 28, | validation: loss: 0.00886 |
| Epoch | 29, | training: loss: 0.00547 |
| Epoch | 29, | validation: loss: 0.00895 |
| Epoch | 30, | training: loss: 0.00523 |
| Epoch | 30, | validation: loss: 0.00935 |

Loss decreases quickly, and we don’t seem to be overfitting on the validation set.

Numbers are pretty abstract, though. So, we’ll use the test set to see how the forecast actually

*looks*.

# Evaluation

Here is the forecast for January, 2014, thirty minutes at a time.

net$eval()

preds <- rep(NA, n\_timesteps) coro::loop(for (b in test\_dl) {

output <- net(b$x$to(device = device)) preds <- c(preds, output %>% as.numeric())

})

ic\_elec\_jan\_2014 <- vic\_elec %>% filter(year(Date) == 2014, month(Date) == 1) %>% select(Demand)

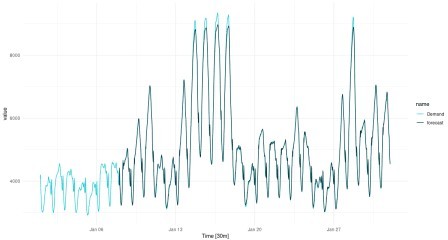
preds\_ts <- vic\_elec\_jan\_2014 %>%

add\_column(forecast = preds \* train\_sd + train\_mean) %>%

pivot\_longer(-Time) %>% update\_tsibble(key = name)

preds\_ts %>% autoplot() +

scale\_colour\_manual(values = c("#08c5d1", "#00353f")) + theme\_minimal()



(#fig:unnamed-chunk-26)One-step-ahead predictions for January, 2014.

Overall, the forecast is excellent, but it is interesting to see how the forecast “regularizes” the most extreme peaks. This kind of “regression to the mean” will be seen much more strongly in later setups, when we try to forecast further into the future.

Can we use our current architecture for multi-step prediction? We can.

One thing we can do is feed back the current prediction, that is, append it to the input sequence as soon as it is available. Effectively thus, for each batch item, we obtain a sequence of predictions in a loop.

We’ll try to forecast 336 time steps, that is, a complete week.

n\_forecast <- 2 \* 24 \* 7

test\_preds <- vector(mode = "list", length = length(test\_dl)) i <- 1

coro::loop(for (b in test\_dl) {

input <- b$x

output <- net(input$to(device = device)) preds <- as.numeric(output)

for(j in 2:n\_forecast) {

input <- torch\_cat(list(input[ , 2:length(input), ], output$view(c(1, 1, 1))), dim = 2)

output <- net(input$to(device = device)) preds <- c(preds, as.numeric(output))

}

test\_preds[[i]] <- preds i <<- i + 1

})

For visualization, let’s pick three non-overlapping sequences.

test\_pred1 <- test\_preds[[1]]

test\_pred1 <- c(rep(NA, n\_timesteps), test\_pred1, rep(NA, nrow(vic\_elec\_jan\_2014) - n\_timesteps - n\_forecast))

test\_pred2 <- test\_preds[[408]]

test\_pred2 <- c(rep(NA, n\_timesteps + 407), test\_pred2, rep(NA, nrow(vic\_elec\_jan\_2014) - 407 - n\_timesteps - n\_forecast))

test\_pred3 <- test\_preds[[817]]

test\_pred3 <- c(rep(NA, nrow(vic\_elec\_jan\_2014) - n\_forecast), test\_pred3)

preds\_ts <- vic\_elec %>%

filter(year(Date) == 2014, month(Date) == 1) %>% select(Demand) %>%

add\_column(

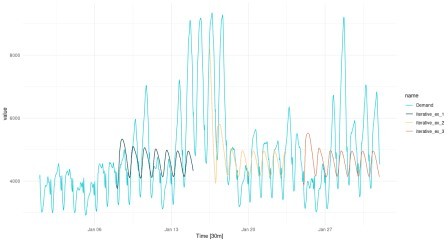
iterative\_ex\_1 = test\_pred1 \* train\_sd + train\_mean, iterative\_ex\_2 = test\_pred2 \* train\_sd + train\_mean, iterative\_ex\_3 = test\_pred3 \* train\_sd + train\_mean) %>%

pivot\_longer(-Time) %>% update\_tsibble(key = name)

preds\_ts %>% autoplot() +

scale\_colour\_manual(values = c("#08c5d1", "#00353f", "#ffbf66", "#d46f4d")) +

theme\_minimal()



(#fig:unnamed-chunk-29)Multi-step predictions for January, 2014, obtained in a loop. Even with this very basic forecasting technique, the diurnal rhythm is preserved, albeit in a

strongly smoothed form. There even is an apparent day-of-week periodicity in the forecast. We do see, however, very strong regression to the mean, even in loop instances where the network was “primed” with a higher input sequence.

# Conclusion

Hopefully this post provided a useful introduction to time series forecasting with torch. Evidently, we picked a challenging time series – challenging, that is, for at least two reasons:

To correctly factor in the trend, external information is needed: external information in form of a temperature forecast, which, “in reality”, would be easily obtainable.

In addition to the highly important trend component, the data are characterized by multiple levels of seasonality.

Of these, the latter is less of a problem for the techniques we’re working with here. If we found that some level of seasonality went undetected, we could try to adapt the current configuration in a number of uncomplicated ways:

Use an LSTM instead of a GRU. In theory, LSTM should better be able to capture additional lower-frequency components due to its secondary storage, the cell state.

Stack multiple layers of GRU/LSTM. In theory, this should allow for learning a hierarchy of temporal features, analogously to what we see in a convolutional neural network.