Introduction to Diving Scores

```
library(dplyr)
library(purrr)
library(tidyr)
library(ggplot2)
```

For those of you, like me, whose background isn't in diving let's start out with a bit on how diving point totals are calculated. There are a finite number of dives, each of which has an assigned degree of difficulty (DD). When a diver performs a particular dive the performance is judged by a panel of (usually) 3, 5, or 7 judges, who each score the dive between 0 and 10, in increments of 0.5 points. If there are 5 or 7 judges than the highest and lowest, or two highest and lowest scores are thrown out, leaving the three in middle. The three remaining judges' scores, called awards, are then added together and that number is multiplied by the degree of difficultly to get the total points for that particular dive.

For this discussion we're going to sometimes drop the "three judges" component, and talk rather about an average judges' score. This will make things easier later, but right now there's a bit of complexity. Since judges can only award their scores in increments of 0.5 between 0 and 10 the average score can't be just any number between 0 and 10. In fact there are only 61 possible average judges' awards. We need a list of those possibilities.

```
vec <- seq(0, 30, 0.5) # every possible total score, from all three
judges giving 0s to all three judges giving 10s

decimals <- unique((vec %% 3)/3) # possible decimal components for the
average score
integers <- seq(0, 10, 1) # possible integer components for the average
score

l <- unlist(lapply(integers, decimals, FUN = function(x, y) {x + y})) #
add all of the possible decimals to all of the possible integers
Possible_Avg_Awards <- l[l <= 10] # only want values less than or equal
to 10 (the max possible score)</pre>
```

We also need a list of each dive and its degree of difficulty. FINA, the international governing body for diving (and swimming) publishes such a list. I've formatted it for our use, and hosted it on github.

Our first step is to read the dives and DDs into R. For this study we'll be working with "forward" dives, that is dives done using a forward approach and involving a number of half somersaults (flips). Each dive has a number in addition to an equivalent name. The numbers for forward dives are three digits long and always begins with a "1" The second digit is either a "0", for standard forward dives, or a "1", for "flying" dives. We're only going to look at standard forward dives, so our first two digits will be "10". The last digit encodes the number of half somersaults the dive entails. So a third digit of "1" means forward dive, standard, one-half somersault. A half somersault means the diver, who begins standing upright, will flip 180 degrees, and enter the water head first. Similarly in a "102" dive the diver will begin standing upright, do two half somersaults (i.e. one full somersault), for a total flip of 360 degrees, entering the water feet first. There's a progression here, "10X" series dives become more difficult, and have higher DDs as "X" increments from 1 to a maximum of "9", requiring more half somersaults. We'll also restrict

ourselves to dives in the "tuck" position for the sake of consistent comparisons across dives.

Calculating Possible Scores for Each Dive

Now that we have the dives and DDs, we'd like to know what scores are possible for each dive. For each dive we'll multiply the DD by each of the possible average awards to get a list of possible scores for each dive. We'll collect those lists together into a dataframe containing the average judges' award, the DD, the and the corresponding score for each dive.

```
# here's we'll get a list of nine lists. Each list is all the possible
scores for a specific dive
Scores List <- map(Forward DDsDD, function(x, y) {x *
Possible Avg Awards * 3})
# name each list with the dive number it corresponds to
names(Scores List) <- Forward DDs$Number</pre>
Scores List <- Scores List %>%
 bind rows() %>% #stick the lists together
 bind cols(Possible Avg Awards) %>% # add a column containing the list
of possible average judge's awards
 pivot longer (names to = "Number",
               cols = starts_with("1"),
               values to = "Total Score") %>% # go from wide to long
format by creating a new column called
  # number containing each dive number, and a new column called
Total Score containing each possible score
  rename (Award = "...10") %>% # rename our average judge award column
to something sensible
 mutate(Number = as.numeric(Number)) # will need dive number as a
number later
```

Embedded in Scores_List is the maximum possible score for each dive. We'd like to make this information available in a tidy way since we'll be relying on various tidyverse packages like ggplot2 for visualization later. Similarly we want the maximum dive of the previous dive in the series as well, so we can look at moving up/down in the dive series.

```
Scores_List <- Forward_DDs %>%
   mutate(Max_Award = DD * 30, # maximum possible score is the DD times
3 10s
        Prev_Max = lag(Max_Award)) %>% # maximum possible score for
the previous dive in the forward series
```

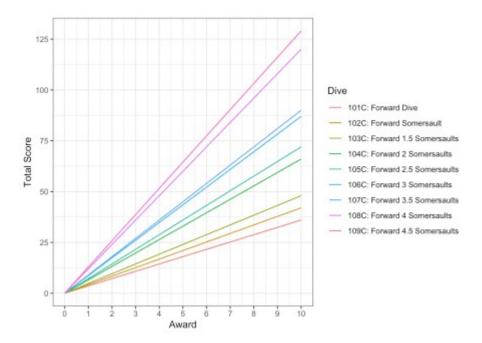
If we compare for example the maximum possible points for a 101C, (36) and then look at the next dive in the series, a 102C which has a DD of 1.4 we can determine what judges' award would be needed on a 102C to score more than the maximum possible score on a 101C. That number is the max score for a 101C, divided by the DD for a 102C, divided by 3 (for the three judges), so 36, divided by 1.4 divided by 3, which is 8.57. However, 8.57 isn't actually possible as an average judges' score. It's not on our Possible_Avg_Awards list. So we need a way to go from our computed number to the nearest, higher possible score.

```
Award_Match <- function(x, D_D = DD, Pos = Possible_Avg_Awards) {
   Pos[base::findInterval(x / (D_D) / 3, Pos) + 1] # matches the next
highest element of Possible_Avg_Awards, by adding one to the match
}</pre>
```

So the actual possible combination of judges awards that makes a 102C worth more points than are possible to score when diving a 101C is 8.67.

Possible Points for Each Dive

There's a linear relationship between judges' award and possible score for each dive, dictated by that dive's DD, which is the slope of each line in the plot below.



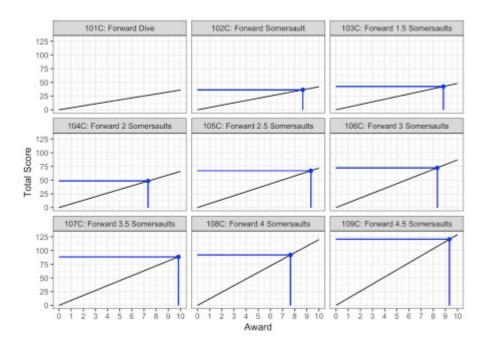
Since judges' awards are limited to a maximum of 10 (total 30), each dive then has a maximum possible score. For a diver to improve their total score it eventually becomes necessary to perform a harder dive, with a correspondingly higher DD, and higher maximum score. Where exactly are these crossover points though?

Crossover Points

As we saw for the 101C/102C case above there's a point, corresponding to a possible combination of judges' awards, for each pair of dives where the dive with the higher DD becomes mathematically more valuable in terms of points scored than the lower DD dive. We'll plot that point of strict mathematical superiority for each neighbor-pair of dives in the forward dive series. That means 101C and 102C are a pair, 102C and 103C, 103C and 104C etc.

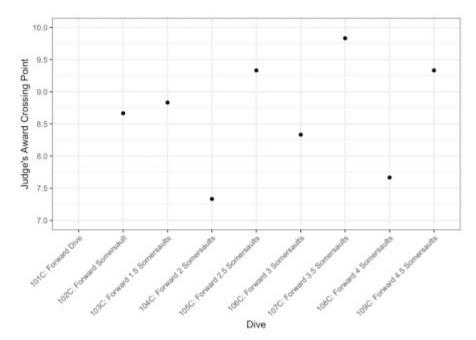
```
Scores List %>%
 ggplot() +
 geom line(aes(x = Award,
                y = Total_Score,
                group = Number)) +
 geom segment (aes (
    x = 0,
   xend = Award Match(Prev Max, DD, Possible Avg Awards),
    y = Award_Match(Prev_Max, DD, Possible_Avg_Awards) * 3 * DD,
    yend = Award Match (Prev Max, DD, Possible Avg Awards) * 3 * DD
  ),
  color = "blue") +
 geom segment(aes(
    x = Award Match (Prev Max, DD, Possible Avg Awards),
    xend = Award Match(Prev Max, DD, Possible Avg Awards),
    y = 0,
    yend = Award Match (Prev Max, DD, Possible Avg Awards) * 3 * DD
  ),
  color = "blue") +
 geom point (aes (
    x = Award Match(Prev Max, DD, Possible Avg Awards),
```

```
y = Award_Match(Prev_Max, DD, Possible_Avg_Awards) * 3 * DD
),
color = "blue",
alpha = 0.5) +
scale_x_continuous(breaks = seq(0, 10 , 1)) +
scale_y_continuous(breaks = seq(0, 150 , 25)) +
facet_wrap(. ~ Dive_Label) +
labs(y = "Total Score") +
theme bw()
```



Each point on the plot above is the score a diver must achieve on a given dive to score mathematically more points on that dive than would be possible on the previous dive. The 101C doesn't have a point drawn because there is not a previous dive to compare to - it's the first dive. Let's pull out just these points.

```
Scores List %>%
 group by (Name) %>%
 mutate(
    Slope = lm(Award ~ (Total Score))$coefficients[2],
   Award Cross = Award Match (Prev Max, DD, Possible Avg Awards)
  summarise(Award Cross = unique(Award Cross)) %>%
 ggplot() +
 geom point(aes(x = Name, y = Award Cross)) +
 scale x discrete(labels = unique(Scores List$Dive Label)) +
 scale y continuous (breaks = seq(7, 10.5, 0.5)) +
  coord cartesian(ylim = c(7, 10)) +
  theme bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(y = "Judge's Award Crossing Point",
       x = "Dive")
```



We can see that FINA believes going from an odd number of half somersaults (10X, X is odd) to an even number is harder than going even to odd, because the strict points for switching to even dive numbers are much lower than the strict points for switching to odd dive numbers.

Changing Dives

Here's the thing though - most divers don't expect (or deserve) 10s on the dives they do. That might sound unfair coming from an official, but consider the case of a hypothetical diver, Riley Ripit. Let's say Riley can do a 101C for 10s, scoring a total of 36 points. She goes to a meet, dives as planned, gets her 10s and her 36 points. Great! The next week she goes to another meet and dives even better. Her height off the board is higher, her rotation in the air is faster, her entry is perfect, she's on fire! She still gets 10s though, because that's the maximum possible award. She has no upside risk in her dive. Of course if she goes to a third meet and has a bad day, she can get lower than 10s, much lower even. That's to say she has a lot of downside risk. This is a bad situation to be in. What she wants is to do a harder dive, with an approximately equivalent expected score (36 points), but with some upside risk, so if she dives better than expected she can score more points. Also if she dives poorly she won't fall as low, meaning less downside risk. A similar argument is possible with 9.5s. If Riley expects 9.5s, and dives well she can only get a little award bump, up to 10s. Ideally she'd plan her dives to have upside risk and minimal downside risk, although exactly how much she wants of either is between her and her coach. This is the answer to today's overall question about the lack of 10s though - we don't see many 10s in diving competitions because it doesn't make sense from the diver's side to aim for 10s. Still, it's a dream of mine to one day award some deserving diver a 10.

It would be useful to know, given a dive done for a particular average judges' award, what award a new dive would need to be done for to make a switch worth considering. Let's make a function to do that.

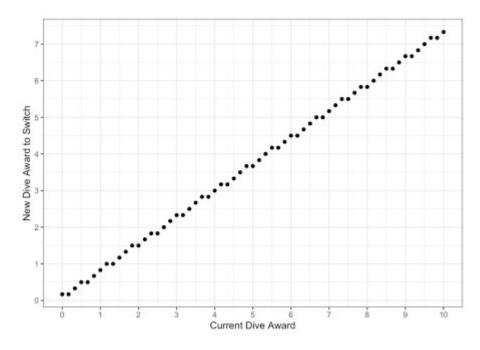
```
dive_calc <- function(current_dive, new_dive, current_award, FDDs =
Forward_DDs, Pos = Possible_Avg_Awards){
    # given an incumbent dive and an incumbent average score, what
    average score would be required on a given new dive to get at least the
    same total number of points
        current_DD <- FDDs[FDDs$Number == current_dive, ]$DD # get DD on
    current dive</pre>
```

```
new_DD <- FDDs[FDDs$Number == new_dive, ]$DD # get DD of new dive
new_award <- (current_award * current_DD)/new_DD # calculate score
where two dives are equivalent
  new_award_switch <- round(Pos[base::findInterval(new_award, Pos) +
1], 2) # convert score to possible award
  return(new_award_switch)
}</pre>
```

We can use our function to determine the equivalence point between a 103C done for 5.5s and a 104C.

```
round(dive_calc(current_dive = 103, new_dive = 104, current_award =
5.5, FDDs = Forward_DDs, Pos = Possible_Avg_Awards), 2)
## [1] 4.17
```

Let's also look a every possible switching point for a given pair of dives by mapping dive_calc across every possible judges' award.



The plot isn't exactly linear, because not every score is available, due to the limited set of possible judges' awards.

Conclusions

We answered our initial question about the dearth of 10s in diving competitions by examining upside risk from the diver's perspective. Going into a competition expecting 10s doesn't leave any upside risk, so unless a diver can do the most difficult dives available perfectly (like in the Olympics) doing more difficult, higher DD dives for lower expected judges' awards makes more sense than aiming for 10s on easier dives.