

Definition

- Declaration table - to store variable declarations
- Files - to write the code
- Attribute types
 - `code` - File of code generated.
 - `error` - File of semantic errors.
 - `next` - Label of the next instruction on the code file.
 - `top` - Current (predicted) size of run-time stack.
 - `type` - Type of subtree. Used for type-checking.
- Functions
 - `enter(name, n)` - Binds "name" with stack location n. Returns n.
 - `lookup(name)` - Returns the location of "name". Returns 0 if "name" is not found.
 - `gen(file, arg1, ..., argn)` - Writes a new line to "file". The line contains `arg1, ..., argn`. Returns the new, modified file.
 - `open()` - Creates a new file.
 - `close()` - Closes a file.
- Attributes
 - $S(\text{program}) = \{\text{code}\uparrow, \text{error}\uparrow\}$
 - $I(\text{program}) = \{\}$
 - $S(\text{assign}) = \{\text{code}\uparrow, \text{error}\uparrow, \text{next}\uparrow, \text{top}\uparrow, \text{type}\uparrow\}$
 - $I(\text{assign}) = \{\text{code}\downarrow, \text{error}\downarrow, \text{next}\downarrow, \text{top}\downarrow\}$
- Convention
 - All attributes except `type` attributes are both synthesized and inherited.
 - $a\uparrow$ is the synthesized attribute a.
 - $a\downarrow$ is the inherited attribute a.
 - All other nodes except `program` node have the same synthesized and inherited attributes as `assign`.
 - If axiom is missing assume
 - If no kids $\rightarrow a\uparrow(\epsilon) = a\downarrow(\epsilon)$
 - Else $\rightarrow a\downarrow(1) = a\downarrow(\epsilon), a\downarrow(i) = a\downarrow(i-1)$ for $i < i \leq n, a\uparrow(\epsilon) = a\uparrow(n)$

****Note that not all the AST grammar rules are considered.**

Axioms

P \rightarrow <'program' '<identifier:x>' E E E E E '<identifier:y>'>

$\text{code}_{\downarrow}(2) = \text{open}$

$\text{next}_{\downarrow}(2) = 1$

$\text{top}_{\downarrow}(2) = 0$

$\text{code}_{\uparrow}(\varepsilon) = \text{close}(\text{gen}(\text{code}_{\uparrow}(6), \text{"stop"}))$

E \rightarrow <'consts' E+>

Use defaults

E \rightarrow 'consts'

Use defaults

E \rightarrow <'const' '<identifier>' E>

$\text{code}_{\downarrow}(2) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(2) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(2) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\uparrow}(2)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2)$

E \rightarrow '<integer:n>'

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"lit"}, \text{"n"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$

E \rightarrow '<char:c>'

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"lit"}, \text{"c"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$

E \rightarrow <'types' E+>

Use defaults

E → 'types'

Use defaults

E → <'type' '<identifier>' E>

$\text{code}_{\downarrow}(2) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(2) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(2) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\uparrow}(2)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2)$

E → <'dclns' E+>

Use defaults

E → 'dclns'

Use defaults

E → <'var' '<identifier>'+ '<identifier>'>

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon)$

E → <'block' E+>

Use defaults

E → <'output' E+> (here $2 \leq i \leq n$ and assume only integer output)

$\text{code}_{\downarrow}(1) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(1) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(1) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\downarrow}(i) = \text{gen}(\text{code}_{\uparrow}(i-1), \text{"print"})$

$\text{next}_{\downarrow}(i) = \text{next}_{\uparrow}(i-1) + 1$

$\text{top}_{\downarrow}(i) = \text{top}_{\uparrow}(i-1) - 1$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(n), \text{"print"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(n) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(n) - 1$

$E \rightarrow \langle \text{'if' } E E E? \rangle$

$E \rightarrow \langle \text{'if' } E E \rangle$

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2))$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

$E \rightarrow \langle \text{'if' } E E E \rangle$

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2) + 1)$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

$\text{code}_{\downarrow}(3) = \text{gen}(\text{code}_{\uparrow}(2), \text{"goto"}, \text{next}_{\uparrow}(3))$

$\text{next}_{\downarrow}(3) = \text{next}_{\uparrow}(2) + 1$

$E \rightarrow \langle \text{'while' } E E \rangle$

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2) + 1)$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"goto"}, \text{next}_{\downarrow}(\varepsilon))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$

$E \rightarrow \langle \text{'repeat' } E^+ E \rangle$ (here $2 \leq i \leq n$)

$\text{code}_{\downarrow}(1) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(1) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(1) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\downarrow}(i) = \text{code}_{\uparrow}(i-1)$

$\text{next}_{\downarrow}(i) = \text{next}_{\uparrow}(i-1)$

$\text{top}_{\downarrow}(i) = \text{top}_{\uparrow}(i-1)$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(n), \text{"iffalse"}, \text{next}_{\downarrow}(\varepsilon))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(n) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(n) - 1$

$E \rightarrow \langle \text{'read' } \langle \text{identifier:x} \rangle^+ \rangle$ (assume only integer input)

$\text{tempCode} = \text{code}_{\uparrow}(\varepsilon)$

```
tempTop = top↑(ε)
```

```
for each <identifier:x>:  
    if lookup("x") = 0:  
        enter("x", ++tempTop)  
        tempCode = gen(tempCode, "read")  
    else:  
        tempCode = gen(gen(tempCode, "read"), "save", lookup("x"))
```

```
code↑(ε) = tempCode
```

```
next↑(ε) = next↓(ε) + 2 * n
```

```
top↑(ε) = top↓(ε) + # un-assigned identifiers
```

E → '<null>'

Use defaults

E → '<integer>' E>

Use defaults

E → '<string>' E>

Use defaults

E → '<string:s>'

```
code↑(ε) = gen(code↓(ε), "lit", "s")
```

```
next↑(ε) = next↓(ε) + 1
```

```
top↑(ε) = top↓(ε) + 1
```

```
type↑(ε) = "string"
```

E → '<assign>' '<identifier:x>' E>

```
code↑(ε) = if lookup("x") = 0 then enter("x", top↑(2)); code↑(2)  
else gen(code↑(2), "save", lookup("x"))
```

```
next↑(ε) = if lookup("x") = 0 then next↑(2) else next↑(2) + 1
```

```
top↑(ε) = if lookup("x") = 0 then top↑(2) else top↑(2) - 1
```

E → '<swap>' '<identifier:x>' '<identifier:y>'

```
code↑(ε) = gen(gen(gen(gen(code↓(ε), "load", lookup("x")), "load",  
lookup("y")), "save", lookup("x")), "save", lookup("y"))
```

```
next↑(ε) = next↓(ε) + 4
```

E → <'<=' E E> (assume only integer comparison)

code↑(ε) = gen(gen(code↑(2), "greaterthan"), "not")
next↑(ε) = next↑(2) + 2
top↑(ε) = top↑(2) - 1

E → <'<' E E> (assume only integer comparison)

code↑(ε) = gen(code↑(2), "lessthan")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'>=' E E> (assume only integer comparison)

code↑(ε) = gen(gen(code↑(2), "lessthan"), "not")
next↑(ε) = next↑(2) + 2
top↑(ε) = top↑(2) - 1

E → <'>' E E> (assume only integer comparison)

code↑(ε) = gen(code↑(2), "greaterthan")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'=' E E>

code↑(ε) = gen(code↑(2), "equal")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'<>' E E>

code↑(ε) = gen(gen(code↑(2), "equal"), "not")
next↑(ε) = next↑(2) + 2
top↑(ε) = top↑(2) - 1

E → <'+' E E> (assume only integer addition)

code↑(ε) = gen(code↑(2), "add")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'-' E E> (assume only integer subtraction)

code↑(ε) = gen(code↑(2), "subtract")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'or' E E>

code↑(ε) = gen(code↑(2), "or")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'*' E E> (assume only integer multiplication)

code↑(ε) = gen(code↑(2), "multiply")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'/' E E> (assume only integer division)

code↑(ε) = gen(code↑(2), "divide")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'and' E E>

code↑(ε) = gen(code↑(2), "and")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'mod' E E> (assume only integer modulo operation)

code↑(ε) = gen(code↑(2), "mod")
next↑(ε) = next↑(2) + 1
top↑(ε) = top↑(2) - 1

E → <'-' E> (assume only integer comparison)

code↑(ε) = gen(code↑(1), "negate")
next↑(ε) = next↑(1) + 1

E → <'not' E>

code↑(ε) = gen(code↑(1), "not")
next↑(ε) = next↑(1) + 1

E → '<identifier:x>'

code↑(ε) = gen(code↓(ε), "load", lookup("x"))
next↑(ε) = next↓(ε) + 1
top↑(ε) = top↓(ε) + 1