

# Definition

- Declaration table - to store variable declarations
- Files - to write the code
- Attribute types
  - `code` - File of code generated.
  - `error` - File of semantic errors.
  - `next` - Label of the next instruction on the code file.
  - `top` - Current (predicted) size of run-time stack.
  - `type` - Type of subtree. Used for type-checking.
- Functions
  - `enter(name, n)` - Binds "name" with stack location n. Returns n.
  - `lookup(name)` - Returns the location of "name". Returns 0 if "name" is not found.
  - `gen(file, arg1, ..., argn)` - Writes a new line to "file". The line contains `arg1, ..., argn`. Returns the new, modified file.
  - `open()` - Creates a new file.
  - `close()` - Closes a file.
- Attributes
  - $S(\text{program}) = \{\text{code}\uparrow, \text{error}\uparrow\}$
  - $I(\text{program}) = \{\}$
  - $S(\text{assign}) = \{\text{code}\uparrow, \text{error}\uparrow, \text{next}\uparrow, \text{top}\uparrow, \text{type}\uparrow\}$
  - $I(\text{assign}) = \{\text{code}\downarrow, \text{error}\downarrow, \text{next}\downarrow, \text{top}\downarrow\}$
- Convention
  - All attributes except `type` attributes are both synthesized and inherited.
  - $a\uparrow$  is the synthesized attribute a.
  - $a\downarrow$  is the inherited attribute a.
  - All other nodes except `program` node have the same synthesized and inherited attributes as `assign`.
  - If axiom is missing assume
    - If no kids  $\rightarrow a\uparrow(\epsilon) = a\downarrow(\epsilon)$
    - Else  $\rightarrow a\downarrow(1) = a\downarrow(\epsilon), a\downarrow(i) = a\downarrow(i-1)$  for  $i < i \leq n, a\uparrow(\epsilon) = a\uparrow(n)$

**\*\*Note that not all the AST grammar rules are considered.**

# Axioms

**P**  $\rightarrow$  **<'program' '<identifier:x>' E E E E E '<identifier:y>'>**

$\text{code}_{\downarrow}(2) = \text{open}$

$\text{next}_{\downarrow}(2) = 1$

$\text{top}_{\downarrow}(2) = 0$

$\text{code}_{\uparrow}(\varepsilon) = \text{close}(\text{gen}(\text{code}_{\uparrow}(6), \text{"stop"}))$

**E**  $\rightarrow$  **<'consts' E+>**

Use defaults

**E**  $\rightarrow$  **'consts'**

Use defaults

**E**  $\rightarrow$  **<'const' '<identifier>' E>**

$\text{code}_{\downarrow}(2) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(2) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(2) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\uparrow}(2)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2)$

**E**  $\rightarrow$  **'<integer:n>'**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"lit"}, \text{"n"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$

**E**  $\rightarrow$  **'<char:c>'**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"lit"}, \text{"c"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$

**E**  $\rightarrow$  **<'types' E+>**

Use defaults

**E** → 'types'

Use defaults

**E** → <'type' '<identifier>' E>

$\text{code}_{\downarrow}(2) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(2) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(2) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\uparrow}(2)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2)$

**E** → <'dclns' E+>

Use defaults

**E** → 'dclns'

Use defaults

**E** → <'var' '<identifier>'+ '<identifier>'>

$\text{code}_{\uparrow}(\varepsilon) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon)$

**E** → <'block' E+>

Use defaults

**E** → <'output' E+> (here  $2 \leq i \leq n$ )

$\text{code}_{\downarrow}(1) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(1) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(1) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\downarrow}(i) = \text{gen}(\text{code}_{\uparrow}(i-1), \text{"print"})$

$\text{next}_{\downarrow}(i) = \text{next}_{\uparrow}(i-1) + 1$

$\text{top}_{\downarrow}(i) = \text{top}_{\uparrow}(i-1) - 1$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(n), \text{"print"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(n) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(n) - 1$

**E**  $\rightarrow$  **<'if' E E E?>**

**E**  $\rightarrow$  **<'if' E E>**

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2))$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

**E**  $\rightarrow$  **<'if' E E E>**

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2) + 1)$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

$\text{code}_{\downarrow}(3) = \text{gen}(\text{code}_{\uparrow}(2), \text{"goto"}, \text{next}_{\uparrow}(3))$

$\text{next}_{\downarrow}(3) = \text{next}_{\uparrow}(2) + 1$

**E**  $\rightarrow$  **<'while' E E>**

$\text{code}_{\downarrow}(2) = \text{gen}(\text{code}_{\uparrow}(1), \text{"iffalse"}, \text{next}_{\uparrow}(2) + 1)$

$\text{next}_{\downarrow}(2) = \text{next}_{\uparrow}(1) + 1$

$\text{top}_{\downarrow}(2) = \text{top}_{\uparrow}(1) - 1$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"goto"}, \text{next}_{\downarrow}(\varepsilon))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$

**E**  $\rightarrow$  **<'repeat' E+ E>** (here  $2 \leq i \leq n$ )

$\text{code}_{\downarrow}(1) = \text{code}_{\downarrow}(\varepsilon)$

$\text{next}_{\downarrow}(1) = \text{next}_{\downarrow}(\varepsilon)$

$\text{top}_{\downarrow}(1) = \text{top}_{\downarrow}(\varepsilon)$

$\text{code}_{\downarrow}(i) = \text{code}_{\uparrow}(i-1)$

$\text{next}_{\downarrow}(i) = \text{next}_{\uparrow}(i-1)$

$\text{top}_{\downarrow}(i) = \text{top}_{\uparrow}(i-1)$

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(n), \text{"iffalse"}, \text{next}_{\downarrow}(\varepsilon))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(n) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(n) - 1$

**E**  $\rightarrow$  **<'read' '<identifier:x>'+>**

$\text{code}_{\uparrow}(\varepsilon) = \text{for each } x: \text{gen}(\text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"read"}), \text{"save"}, \text{lookup}(\text{"x"}))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 2 * n$   
 $\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon)$

**E** → '<null>'

Use defaults

**E** → <'integer' E>

Use defaults

**E** → <'string' E>

Use defaults

**E** → '<string:s>'

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"lit"}, \text{"s"})$   
 $\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$   
 $\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$   
 $\text{type}_{\uparrow}(\varepsilon) = \text{"string"}$

**E** → <'assign' '<identifier:x>' E>

$\text{code}_{\uparrow}(\varepsilon) = \text{if lookup("x")} = 0 \text{ then enter("x", top}_{\uparrow}(2)); \text{code}_{\uparrow}(2)$   
 $\text{else gen}(\text{code}_{\uparrow}(2), \text{"save"}, \text{lookup("x")})$   
 $\text{next}_{\uparrow}(\varepsilon) = \text{if lookup("x")} = 0 \text{ then next}_{\uparrow}(2) \text{ else next}_{\uparrow}(2) + 1$   
 $\text{top}_{\uparrow}(\varepsilon) = \text{if lookup("x")} = 0 \text{ then top}_{\uparrow}(2) \text{ else top}_{\uparrow}(2) - 1$

**E** → <'swap' '<identifier:x>' '<identifier:y>'>

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{gen}(\text{gen}(\text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"load"}, \text{lookup("x")}), \text{"load"},$   
 $\text{lookup("y")}), \text{"save"}, \text{lookup("x")}), \text{"save"}, \text{lookup("y")})$   
 $\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 4$

**E** → <'<=' E E> (assume only integer comparison)

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{gen}(\text{code}_{\uparrow}(2), \text{"greaterthan"}), \text{"not"})$   
 $\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 2$   
 $\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**E** → <'<' E E> (assume only integer comparison)

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"lessthan"})$   
 $\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$   
 $\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**$E \rightarrow <'>= ' E E >$  (assume only integer comparison)**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{gen}(\text{code}_\uparrow(2), \text{"lessthan"}), \text{"not"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 2$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'>' E E >$  (assume only integer comparison)**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"greaterthan"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'=' E E >$**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"equal"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'<>' E E >$**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{gen}(\text{code}_\uparrow(2), \text{"equal"}), \text{"not"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 2$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'+' E E >$  (assume only integer addition)**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"add"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'-' E E >$  (assume only integer subtraction)**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"subtract"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'or' E E >$**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"or"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$   
 $\text{top}_\uparrow(\varepsilon) = \text{top}_\uparrow(2) - 1$

**$E \rightarrow <'*' E E >$  (assume only integer multiplication)**

$\text{code}_\uparrow(\varepsilon) = \text{gen}(\text{code}_\uparrow(2), \text{"multiply"})$   
 $\text{next}_\uparrow(\varepsilon) = \text{next}_\uparrow(2) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**$E \rightarrow \langle ' / ' E E \rangle$  (assume only integer division)**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"divide"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**$E \rightarrow \langle ' \text{and} ' E E \rangle$**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"and"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**$E \rightarrow \langle ' \text{mod} ' E E \rangle$  (assume only integer modulo operation)**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(2), \text{"mod"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(2) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\uparrow}(2) - 1$

**$E \rightarrow \langle ' - ' E \rangle$  (assume only integer comparison)**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(1), \text{"negate"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(1) + 1$

**$E \rightarrow \langle ' \text{not} ' E \rangle$**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\uparrow}(1), \text{"not"})$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\uparrow}(1) + 1$

**$E \rightarrow ' \langle \text{identifier} : x \rangle '$**

$\text{code}_{\uparrow}(\varepsilon) = \text{gen}(\text{code}_{\downarrow}(\varepsilon), \text{"load"}, \text{lookup}(\text{"x"}))$

$\text{next}_{\uparrow}(\varepsilon) = \text{next}_{\downarrow}(\varepsilon) + 1$

$\text{top}_{\uparrow}(\varepsilon) = \text{top}_{\downarrow}(\varepsilon) + 1$