## Supervised learning – Classification (Demo)

Method of k-Nearest Neighbors (k-NN)

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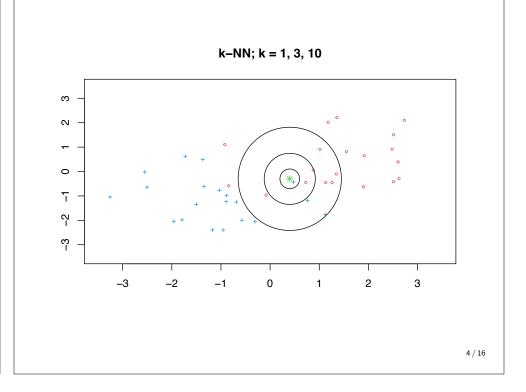
Spring 2025 (wk6)

# K-NN Algorithm

- For each test point to be classified, find the K nearest samples in the training data
- Classify the point according to the majority vote of their class labels

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## Illustration: How k-NN classifies a new observation



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## Training data and testing data

#### Example:

Use the familiar iris data as an example.

Classes g = 3, variables p = 4, total observations n = 150.

Set 70% as training data, 30% as testing data.

```
library(class) # for k-nn function
data(iris)
myDat = iris # Plot titles need to match
trainRate = 0.7 # training vs testing data
set.seed(2023)
trainNo=sample(dim(myDat)[1],trainRate*dim(myDat)[1])
```

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## Fit k-NN model for k=1

```
## knn1
## setosa versicolor virginica
## setosa 14 0 0
## versicolor 0 13 0
## virginica 0 1 17
```

```
myDat[1:2,]
    Sepal.Length Sepal.Width Petal.Length Petal.Width Spec
              5.1
                          3.5
## 1
                                      1.4
                                                  0.2 set
## 2
              4.9
                          3.0
                                      1.4
                                                  0.2 set
trainNo[1:10]
## [1] 117 105 26 44 98 29 49 125 133 72
table(myDat[trainNo,]$Species) # training class label
##
##
       setosa versicolor virginica
##
          36
                     37
                                 32
table(myDat[-trainNo,]$Species) # testing class label
##
##
       setosa versicolor virginica
##
          14
                     13
                                 18
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```

#### Fit k-NN model for k=10

```
##
               knn10
##
                setosa versicolor virginica
##
                    14
                                 0
     setosa
##
     versicolor
                     0
                                12
                                           1
     virginica
                     0
                                1
                                          17
```

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#### Fit k-NN model for k=7

```
knn7 = knn(train=myDat[trainNo,1:4],
           test=myDat[-trainNo,1:4],
    cl=myDat$Species[trainNo],k=7,prob=TRUE)
table(myDat$Species[-trainNo],knn7)
##
               knn7
##
                setosa versicolor virginica
     setosa
                     14
                                 0
##
                     0
                                12
##
     versicolor
                                           1
     virginica
                      0
                                          17
##
                                 1
```

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## Which k? Use training and validation data

The data set is small enough to tryout various k's on k-NN model. For each k, randomly pick training/validation data, 100 times.

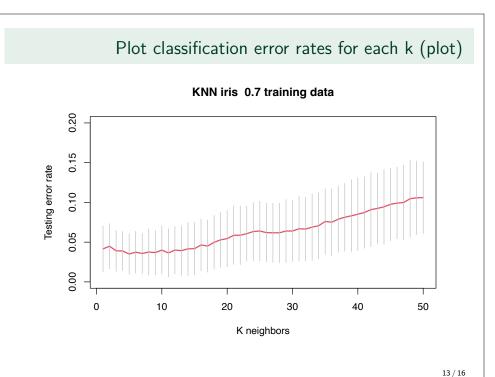
```
## $levels
## [1] "setosa" "versicolor" "virginica"
##
## $class
## [1] "factor"
##
## $prob
## [1] 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.
## [11] 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 0.
## [21] 0.8571 0.5714 1.0000 0.8889 1.0000 1.0000 1.0000 1.
## [31] 1.0000 1.0000 1.0000 1.0000 0.8571 0.7143 1.0000 1.
## [41] 1.0000 1.0000 1.0000 1.0000 1.0000
```

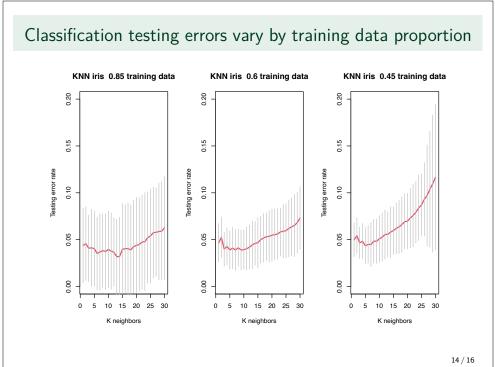
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## Plot classification error rates for each k (code)

```
plot(1:K,ylim=c(0,.2),type="n",
        ylab="Testing error rate",xlab="K neighbors",
        main=paste("KNN iris ", trainRate, "training data"))
points(1:K,colMeans(errMat),type="l",col=2,lwd=2)
segments(1:K, colMeans(errMat)-sqrt(diag(cov(errMat))),
        1:K, colMeans(errMat)+sqrt(diag(cov(errMat))),
        col='gray')
```

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## Comparisons

**Discussions** (based on the error rates plots)

From the error rate plots,

- What is a good choice of k, the number of nearest neighbors?
- How should we choose the size of training data vs testing data?
- Observations: variance trade-off.
- Scaling or normalizing variables are often necessary.

