

Part 2: Machine learning with biomedical ontologies

Robert Hoehndorf

Challenges with semantic similarity

- not data-driven but hand-crafted

- not task-specific

- usually outputs a single value

- hard to chose a similarity measure

- usually graph-based and losing some information

Next: machine learning methods for and with ontologies

Embedding formal knowledge

Embedding

An embedding is a map (morphism) from one mathematical structure X into another structure Y :

$$f : X \hookrightarrow Y$$

such that X is preserved in Y .

Y may be more suitable than X for some operations/algorithms.

similarity

gradients, optimization

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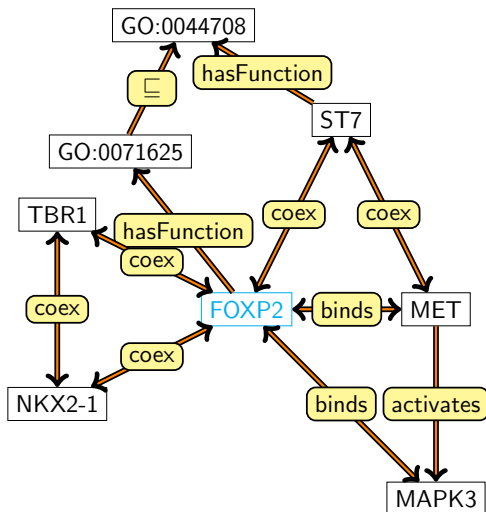
We want to embed *ontologies* in \Re^n . Approaches:

graph-based

syntactic

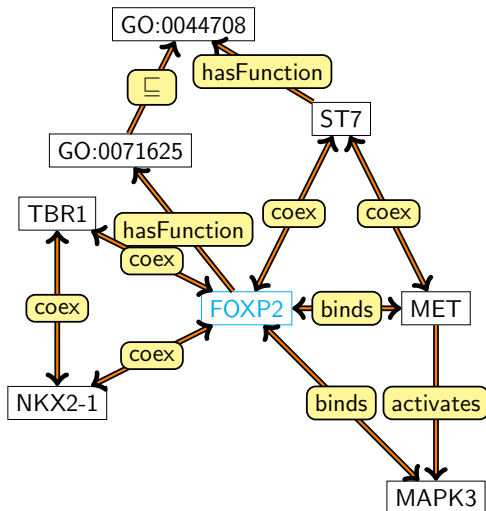
model-theoretic

Random walks



FOXP2 is characterized by *adjacent* and close nodes and edges
different edges may “transmit” information differently

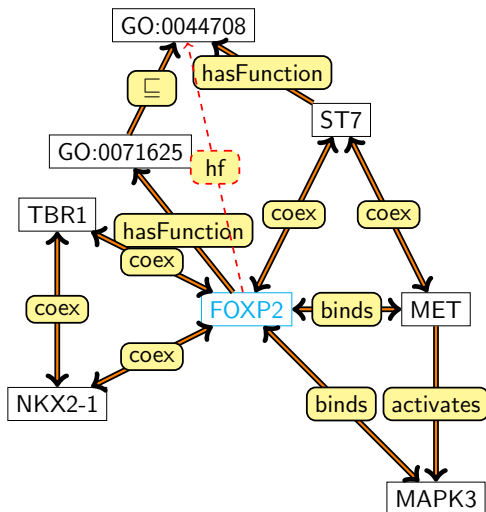
Random walks



precompute the
deductive closure:

for all ϕ : if $\mathcal{KG} \models \phi$,
add ϕ to \mathcal{KG}

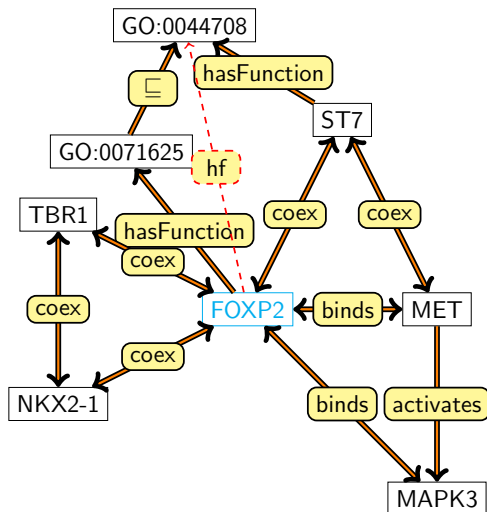
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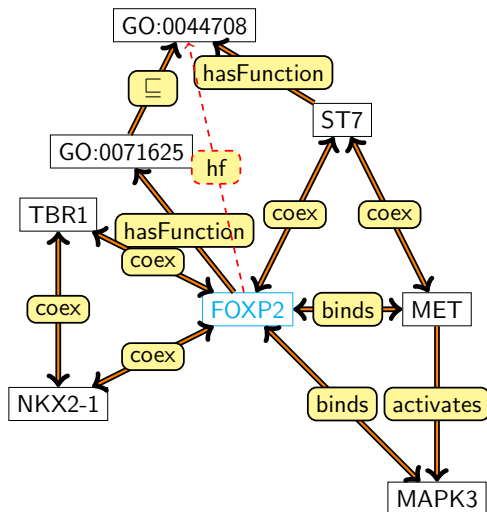
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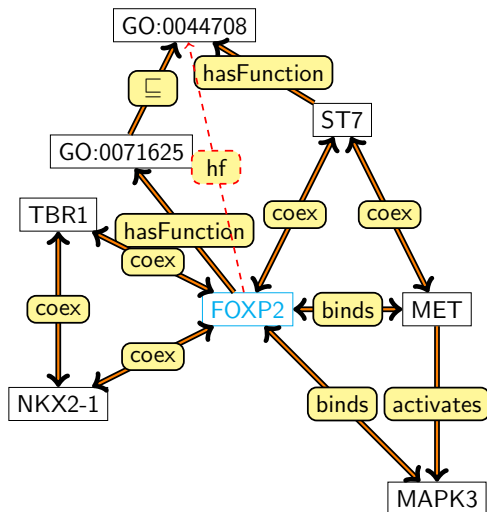
Exploring the graph:

Random walks



Exploring the graph:
:FOXP2 :binds :MET
:coex :ST7
:hasFunction
GO:0044708

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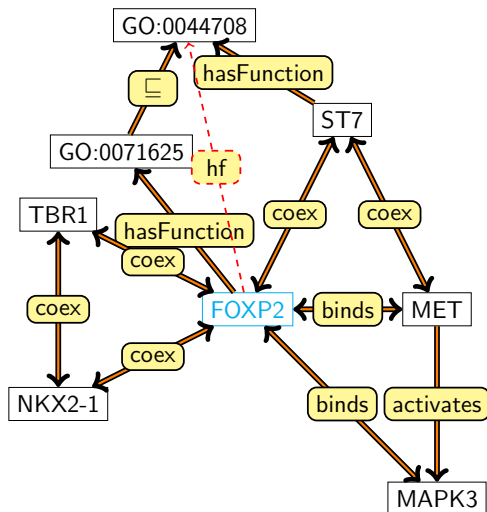
:FOXP2 :hasFunction

GO:0071625

subClassOf

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Random walks



Exploring the graph:

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:FOXP2 :coex :TBR1

:coex :NKX2-1 :coex

:TBR1 :coex ...

Word2Vec

Maximize:

$$\frac{1}{N} \sum_{n=1}^N \sum_{-c \leq j \leq c, j \neq 0} \log p(w_{n+j} | w_n) \quad (1)$$

with

$$p(w_o | w_i) = \frac{\exp(v'_{w_o}{}^T v_{w_i})}{\sum_{w=1}^W \exp(v'_w{}^T v_{w_i})} \quad (2)$$

(at least conceptually; different strategies are used to approximate Eqn. 2)

Word2Vec and Random Walks

- random walks “flatten” a graph

 - walks capture node neighborhood
and generate a “corpus”

- random walks capture graph “structure”

 - hub-nodes, communities, etc.
determine “importance” of nodes

- embeddings capture co-occurrence

 - similar graph neighborhood \Rightarrow similar co-occurrence \Rightarrow
similar vector

- embeddings generate “feature” vectors

 - functions from symbols (words, labels) into \mathbb{R}^n

What to do with embeddings?

useful for edge prediction, similarity, clustering, as feature vectors

supervised: edge prediction (e.g., SVM, ANN)

e.g.: find a function $f : \mathbb{R}^n \times \mathbb{R}^n \mapsto [0, 1]$ s.t.

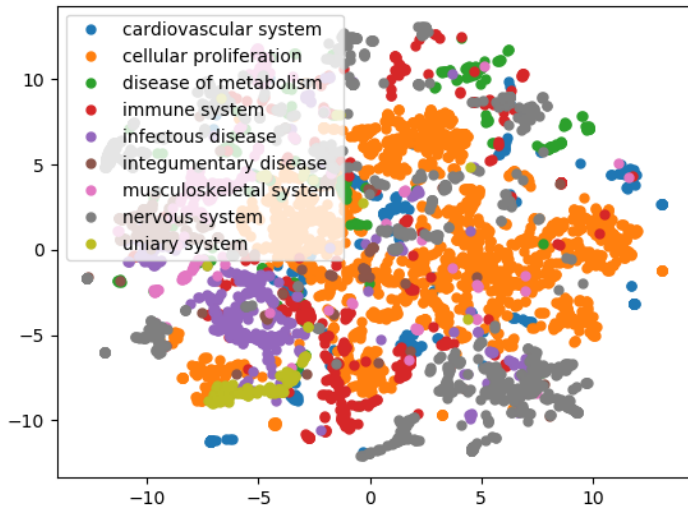
$\sqrt{\frac{\sum_{t=1}^T (\hat{y}_t - y_t)^2}{T}}$ (RMSE) is minimized for a set of true labels y_k

unsupervised: clustering, similarity, visualization

cosine similarity (for L2-normalized features)

Word2Vec embeddings capture similarity between co-occurrence vectors

Visualizing embeddings



Supervised learning

feature vectors represent graph neighborhood of nodes

adjacent nodes and edges

ontology classes (asserted & inferred)

useful in supervised prediction tasks

relation prediction:

input: two features vectors (from embedding function)

output: 0 or 1 (relation or not)

training data: positive and negative cases

$R(x, y)$ and $\neg R(x, y)$

Features: supervised learning

Object property	Source type	Target type	Without reasoning		With reasoning	
			F-measure	AUC	F-measure	AUC
has target	Drug	Gene/Protein	0.94	0.97	0.94	0.98
has disease annotation	Gene/Protein	Disease	0.89	0.95	0.89	0.95
has side-effect*	Drug	Phenotype	0.86	0.93	0.87	0.94
has interaction	Gene/Protein	Gene/Protein	0.82	0.88	0.82	0.88
has function*	Gene/Protein	Function	0.85	0.95	0.83	0.91
has gene phenotype*	Gene/Protein	Phenotype	0.84	0.91	0.82	0.90
has indication	Drug	Disease	0.72	0.79	0.76	0.83
has disease phenotype*	Disease	Phenotype	0.72	0.78	0.70	0.77

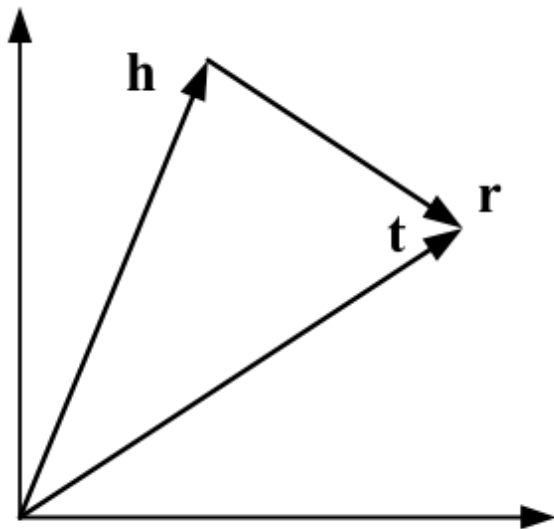
Some limitations

“word”-based (Word2Vec):

semantics is reduced to co-occurrence in the random
“walks”

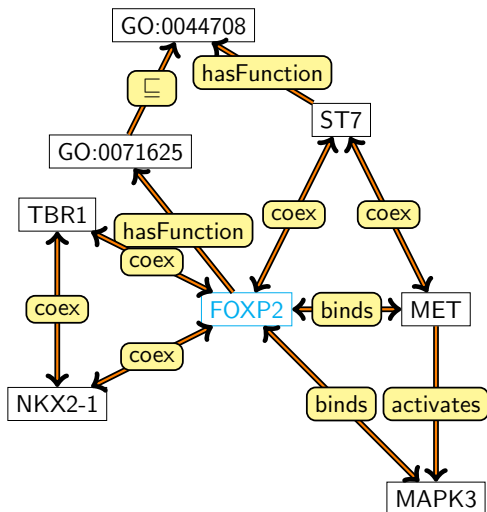
“disjointWith” vs. “part-of” vs. “subclassOf”

Translating embeddings

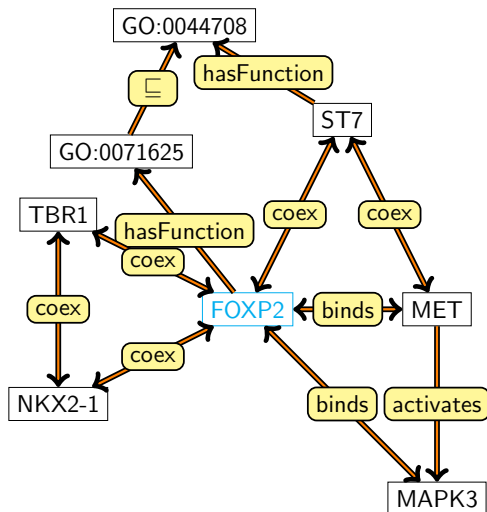


Entity and Relation Space

Translating embeddings

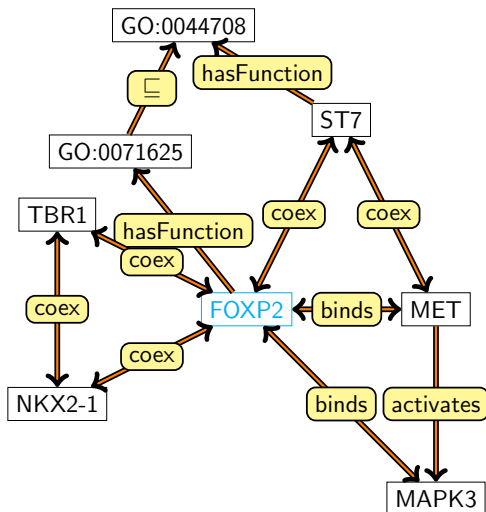


Translating embeddings



FOXP2 + binds =
MET

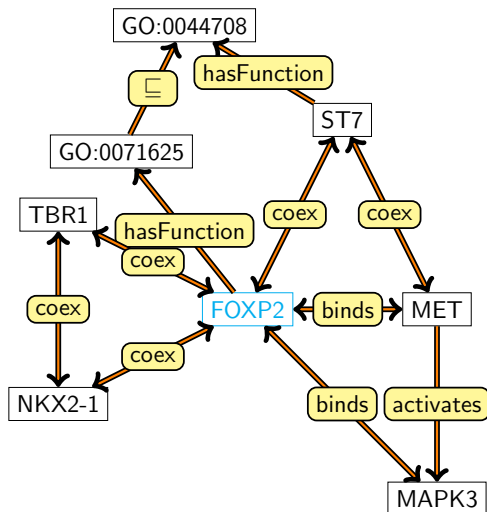
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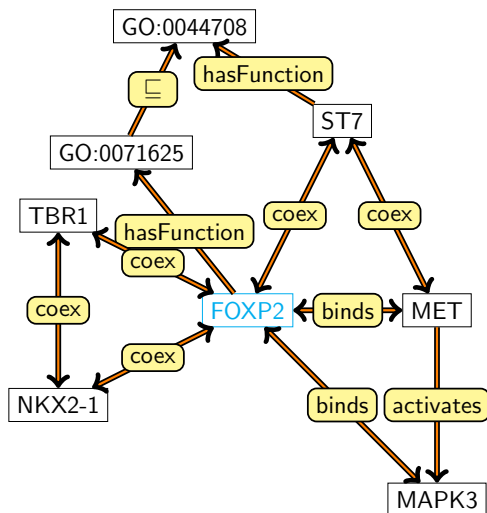


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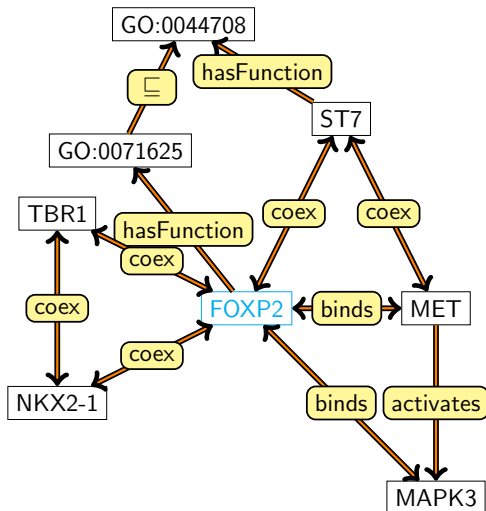
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ST7 + hasFunction
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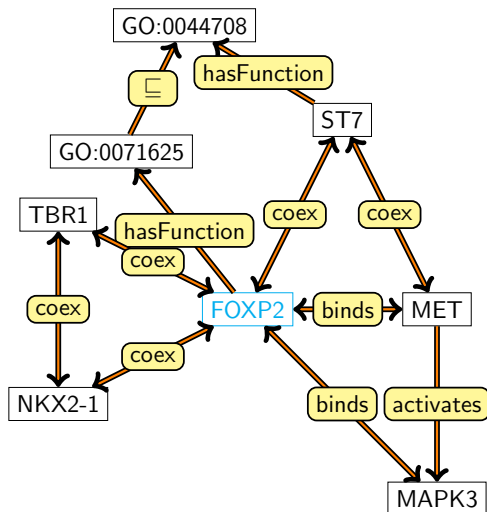
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Translating embeddings



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Translating embeddings

Algorithm 1 Learning TransE

input Training set $S = \{(h, \ell, t)\}$, entities and rel. sets E and L , margin γ , embeddings dim. k .

- 1: **initialize** $\ell \leftarrow \text{uniform}(-\frac{6}{\sqrt{k}}, \frac{6}{\sqrt{k}})$ for each $\ell \in L$
- 2: $\ell \leftarrow \ell / \|\ell\|$ for each $\ell \in L$
- 3: $e \leftarrow \text{uniform}(-\frac{6}{\sqrt{k}}, \frac{6}{\sqrt{k}})$ for each entity $e \in E$
- 4: **loop**
- 5: $e \leftarrow e / \|e\|$ for each entity $e \in E$
- 6: $S_{batch} \leftarrow \text{sample}(S, b)$ // sample a minibatch of size b
- 7: $T_{batch} \leftarrow \emptyset$ // initialize the set of pairs of triplets
- 8: **for** $(h, \ell, t) \in S_{batch}$ **do**
- 9: $(h', \ell, t') \leftarrow \text{sample}(S'_{(h, \ell, t)})$ // sample a corrupted triplet
- 10: $T_{batch} \leftarrow T_{batch} \cup \{((h, \ell, t), (h', \ell, t'))\}$
- 11: **end for**
- 12: Update embeddings w.r.t.
$$\sum_{((h, \ell, t), (h', \ell, t')) \in T_{batch}} \nabla [\gamma + d(\mathbf{h} + \ell, \mathbf{t}) - d(\mathbf{h}' + \ell, \mathbf{t}')]_+$$
- 13: **end loop**

Bordes et al. (2013). Translating Embeddings for Modeling Multi-relational Data.

Some properties of TransE

- graph-based

 - works well on RDF graphs
and ontology graphs

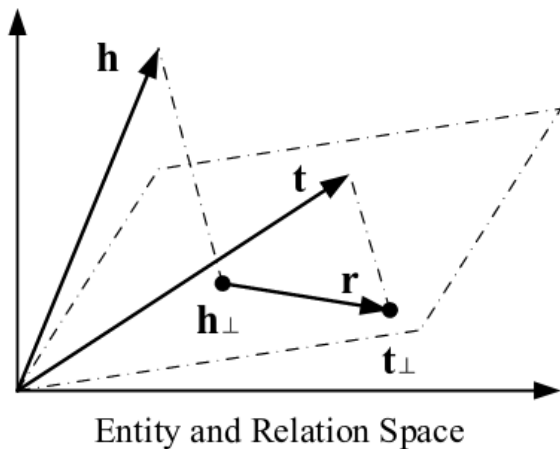
- 1:1 relations only

 - not suitable for hierarchies (1-N relations)

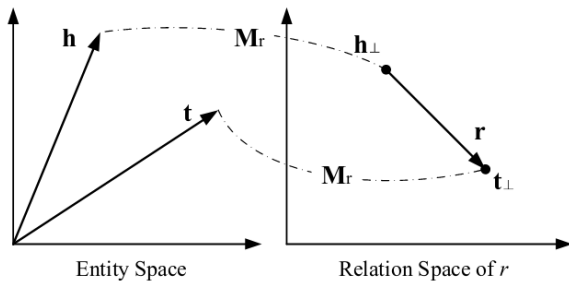
 - not suitable for N-N relations

 - no transitive, symmetric, reflexive relations

Translating embeddings



Translating embeddings



(c) TransR.

Translating embeddings

Method	Ent. embedding	Rel. embedding	Scoring function $f_r(h, t)$	Constraints/Regularization
TransE [14]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^d$	$-\ \mathbf{h} + \mathbf{r} - \mathbf{t}\ _{1/2}$	$\ \mathbf{h}\ _2 = 1, \ \mathbf{t}\ _2 = 1$
TransH [15]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r}, \mathbf{w}_r \in \mathbb{R}^d$	$-\ (\mathbf{h} - \mathbf{w}_r^\top \mathbf{h} \mathbf{w}_r) + \mathbf{r} - (\mathbf{t} - \mathbf{w}_r^\top \mathbf{t} \mathbf{w}_r)\ _2^2$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1$ $\ \mathbf{w}_r^\top \mathbf{r}\ / \ \mathbf{r}\ _2 \leq \epsilon, \ \mathbf{w}_r\ _2 = 1$
TransR [16]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^k, \mathbf{M}_r \in \mathbb{R}^{k \times d}$	$-\ \mathbf{M}_r \mathbf{h} + \mathbf{r} - \mathbf{M}_r \mathbf{t}\ _2^2$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$ $\ \mathbf{M}_r \mathbf{h}\ _2 \leq 1, \ \mathbf{M}_r \mathbf{t}\ _2 \leq 1$
TransD [50]	$\mathbf{h}, \mathbf{w}_h \in \mathbb{R}^d$ $\mathbf{t}, \mathbf{w}_t \in \mathbb{R}^d$	$\mathbf{r}, \mathbf{w}_r \in \mathbb{R}^k$	$-\ (\mathbf{w}_r \mathbf{w}_h^\top + \mathbf{I})\mathbf{h} + \mathbf{r} - (\mathbf{w}_r \mathbf{w}_t^\top + \mathbf{I})\mathbf{t}\ _2^2$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$ $\ (\mathbf{w}_r \mathbf{w}_h^\top + \mathbf{I})\mathbf{h}\ _2 \leq 1$ $\ (\mathbf{w}_r \mathbf{w}_t^\top + \mathbf{I})\mathbf{t}\ _2 \leq 1$
TransSparse [51]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^k, \mathbf{M}_r(\theta_r) \in \mathbb{R}^{k \times d}$ $\mathbf{M}_r^1(\theta_r^1), \mathbf{M}_r^2(\theta_r^2) \in \mathbb{R}^{k \times d}$	$-\ \mathbf{M}_r(\theta_r)\mathbf{h} + \mathbf{r} - \mathbf{M}_r(\theta_r)\mathbf{t}\ _{1/2}^2$ $-\ \mathbf{M}_r^1(\theta_r^1)\mathbf{h} + \mathbf{r} - \mathbf{M}_r^2(\theta_r^2)\mathbf{t}\ _{1/2}^2$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$ $\ \mathbf{M}_r(\theta_r)\mathbf{h}\ _2 \leq 1, \ \mathbf{M}_r(\theta_r)\mathbf{t}\ _2 \leq 1$ $\ \mathbf{M}_r^1(\theta_r^1)\mathbf{h}\ _2 \leq 1, \ \mathbf{M}_r^2(\theta_r^2)\mathbf{t}\ _2 \leq 1$
TransM [52]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^d$	$-\theta_r \ \mathbf{h} + \mathbf{r} - \mathbf{t}\ _{1/2}$	$\ \mathbf{h}\ _2 = 1, \ \mathbf{t}\ _2 = 1$
ManifoldE [53]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^d$	$-(\ \mathbf{h} + \mathbf{r} - \mathbf{t}\ _2^2 - \theta_r^2)^2$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$
TransF [54]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^d$	$(\mathbf{h} + \mathbf{r})^\top \mathbf{t} + (\mathbf{t} - \mathbf{r})^\top \mathbf{h}$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$
TransA [55]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{r} \in \mathbb{R}^d, \mathbf{M}_r \in \mathbb{R}^{d \times d}$	$-(\ \mathbf{h} + \mathbf{r} - \mathbf{t}\)^\top \mathbf{M}_r (\ \mathbf{h} + \mathbf{r} - \mathbf{t}\)$	$\ \mathbf{h}\ _2 \leq 1, \ \mathbf{t}\ _2 \leq 1, \ \mathbf{r}\ _2 \leq 1$ $\ \mathbf{M}_r\ _F \leq 1, [\mathbf{M}_r]_{ij} = [\mathbf{M}_r]_{ji} \geq 0$
KG2E [45]	$\mathbf{h} \sim \mathcal{N}(\mu_h, \Sigma_h)$ $\mathbf{t} \sim \mathcal{N}(\mu_t, \Sigma_t)$ $\mu_h, \mu_t \in \mathbb{R}^d$ $\Sigma_h, \Sigma_t \in \mathbb{R}^{d \times d}$	$\mathbf{r} \sim \mathcal{N}(\mu_r, \Sigma_r)$ $\mu_r \in \mathbb{R}^d, \Sigma_r \in \mathbb{R}^{d \times d}$	$-\text{tr}(\Sigma_r^{-1}(\Sigma_h + \Sigma_t)) - \mu^\top \Sigma_r^{-1} \mu - \ln \frac{\det(\Sigma_r)}{\det(\Sigma_h + \Sigma_t)}$ $-\mu^\top \Sigma^{-1} \mu - \ln(\det(\Sigma))$ $\mu = \mu_h + \mu_r - \mu_t$ $\Sigma = \Sigma_h + \Sigma_r + \Sigma_t$	$\ \mu_h\ _2 \leq 1, \ \mu_t\ _2 \leq 1, \ \mu_r\ _2 \leq 1$ $c_{min} \mathbf{I} \leq \Sigma_h \leq c_{max} \mathbf{I}$ $c_{min} \mathbf{I} \leq \Sigma_t \leq c_{max} \mathbf{I}$ $c_{min} \mathbf{I} \leq \Sigma_r \leq c_{max} \mathbf{I}$
TransG [46]	$\mathbf{h} \sim \mathcal{N}(\mu_h, \sigma_h^2 \mathbf{I})$ $\mathbf{t} \sim \mathcal{N}(\mu_t, \sigma_t^2 \mathbf{I})$ $\mu_h, \mu_t \in \mathbb{R}^d$	$\mu_r \sim \mathcal{N}(\mu_r - \mu_h, (\sigma_h^2 + \sigma_r^2) \mathbf{I})$ $\mathbf{r} = \sum_i \pi_r^i \mu_r^i \in \mathbb{R}^d$	$\sum_i \pi_r^i \exp\left(-\frac{\ \mu_h + \mu_r^i - \mu_t\ _2^2}{\sigma_h^2 + \sigma_r^2}\right)$	$\ \mu_h\ _2 \leq 1, \ \mu_t\ _2 \leq 1, \ \mu_r^i\ _2 \leq 1$
UM [56]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	—	$-\ \mathbf{h} - \mathbf{t}\ _2^2$	$\ \mathbf{h}\ _2 = 1, \ \mathbf{t}\ _2 = 1$
SE [57]	$\mathbf{h}, \mathbf{t} \in \mathbb{R}^d$	$\mathbf{M}_r^1, \mathbf{M}_r^2 \in \mathbb{R}^{d \times d}$	$-\ \mathbf{M}_r^1 \mathbf{h} - \mathbf{M}_r^2 \mathbf{t}\ _1$	$\ \mathbf{h}\ _2 = 1, \ \mathbf{t}\ _2 = 1$

Wang et al. Knowledge Graph Embedding: A Survey of Approaches and Applications.

Beyond graphs

so far, all the methods were based on graphs

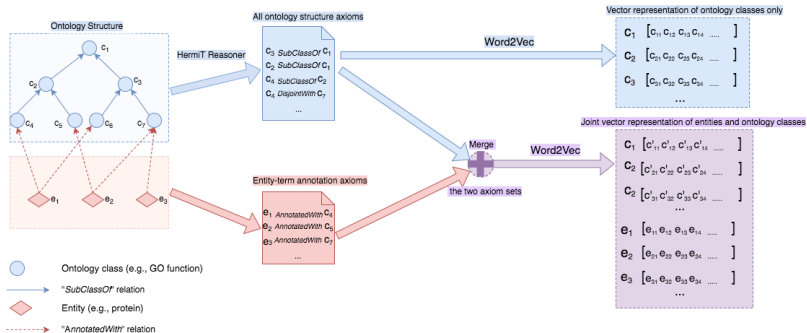
- ontologies are not graphs!

- converting ontologies to graphs loses information

- no axioms, no definitions

maybe we won't need the graph?

Onto2Vec



Combination with text

ontologies contain more than axioms:

labels, synonyms, definitions, authors, etc.

Description Logic axioms \neq natural language

transfer learning: learn on one domain/task, apply to another

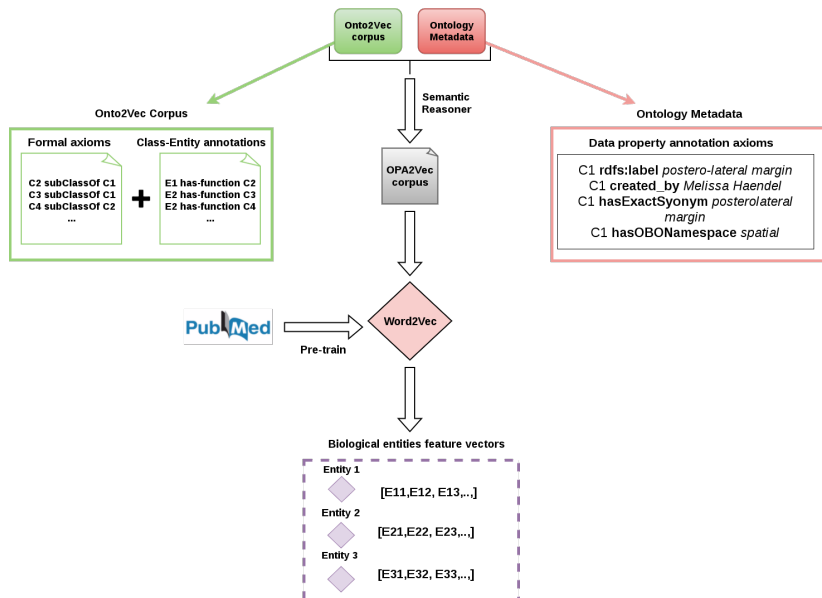
e.g.: learn on literature, apply to ontologies

words have “meaning” in literature, Description Logic

symbols have “meaning” in ontology axioms

Ontologies Plus Annotations 2 Vec (OPA2Vec) combines both

Ontologies Plus Annotations 2 Vec



Axioms contribute to prediction tasks: GO and GO-PLUS

	Human	Yeast	Arabidopsis
<i>GO_Onto2Vec</i>	0.7660	0.7701	0.7559
<i>GO_Onto2Vec_NN</i>	0.8779	0.8711	0.8364
<i>GO_plus_Onto2Vec</i>	0.7880	0.7943	0.7889
<i>GO_plus_Onto2Vec_NN</i>	0.9021	0.8937	0.8834

How to overcome the semantic gap?

none of the models discussed above are truly “semantic”
all syntactic
graph-based or based on axioms

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universal algebra over formal languages (with signature Σ)

Description Logic EL++

Name	Syntax	Semantics
top	\top	$\Delta^{\mathcal{I}}$
bottom	\perp	\emptyset
nominal	$\{a\}$	$\{a^{\mathcal{I}}\}$
conjunction	$C \sqcap D$	$C^{\mathcal{I}} \cap D^{\mathcal{I}}$
existential restriction	$\exists r.C$	$\{x \in \Delta^{\mathcal{I}} \mid \exists y \in \Delta^{\mathcal{I}} : (x, y) \in r^{\mathcal{I}} \wedge y \in C^{\mathcal{I}}\}$
generalized concept inclusion	$C \sqsubseteq D$	$C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$
role inclusion	$r_1 \circ \dots \circ r_n \sqsubseteq r$	$r_1^{\mathcal{I}} \circ \dots \circ r_n^{\mathcal{I}} \subseteq r^{\mathcal{I}}$

Models

Interpretations and Σ -structures

Model \mathfrak{A} of a formula ϕ : ϕ is true in \mathfrak{A} ($\mathfrak{A} \models \phi$)

Theory T : set of formulas

\mathfrak{A} is a model of T if \mathfrak{A} is a model of all formulas in T

Ontologies are (special kinds of) theories

EL Embeddings

given a theory/ontology T with signature $\Sigma(T)$

aim: find $f_e : \Sigma(T) \mapsto \mathbb{R}^n$ s.t. $f_e(\Sigma(T))$ is a model of T
($f_e(\Sigma(T)) \models T$)

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any consistent EL++ theory has models in \mathbb{R}^n
(Loewenheim-Skolem, upwards)

Key idea

for all $r \in \Sigma(T)$ and $C \in \Sigma(T)$, define $f_e(r)$ and $f_e(C)$

$f_e(C)$ maps to points in an open n -ball such that $f_e(C) = C^{\mathcal{I}}$:
 $C^{\mathcal{I}} = \{x \in \mathbb{R}^n \mid \|f_e(C) - x\| < r_e(C)\}$

these are the *extension* of a class in \mathfrak{R}^n

$f_e(r)$ maps a binary relation r to a vector such that
 $r^{\mathcal{I}} = \{(x, y) \mid x + f_e(r) = y\}$

that's the TransE property for *individuals*

use the axioms in T as constraints

Algorithm

normalize the theory:

every \mathcal{EL}^{++} theory can be expressed using four normal forms (Baader et al., 2005)

eliminate the ABox: replace each individual symbol with a singleton class: a becomes $\{a\}$

rewrite relation assertions $r(a, b)$ and class assertions $C(a)$ as $\{a\} \sqsubseteq \exists r. \{b\}$ and $\{a\} \sqsubseteq C$

something to remember for the next class-vs-instance discussion?

normalization rules to generate:

$$C \sqsubseteq D$$

$$C \sqcap D \sqsubseteq E$$

$$C \sqsubseteq \exists R. D$$

$$\exists R. C \sqsubseteq D$$

Algorithm: loss functions

$$\begin{aligned} \text{loss}_{C \sqsubseteq D}(c, d) = \\ \max(0, \|f_\eta(c) - f_\eta(d)\| + r_\eta(c) - r_\eta(d) - \gamma) \\ + |\|f_\eta(c)\| - 1| + |\|f_\eta(d)\| - 1| \end{aligned} \quad (3)$$

Algorithm: loss functions

Let $h = \frac{r_\eta(c)^2 - r_\eta(d)^2 + \|f_\eta(c) - f_\eta(d)\|^2}{2\|f_\eta(c) - f_\eta(d)\|}$, then the center and radius of the smallest n -ball containing the intersection of $\eta(C)$ and $\eta(D)$ are $f_\eta(c) + \frac{h}{\|f_\eta(c) - f_\eta(d)\|}(f_\eta(d) - f_\eta(c))$ and $\sqrt{r_\eta(c)^2 - h^2}$.

Algorithm: loss functions

$$\begin{aligned} \text{loss}_{C \sqsubseteq \exists R.D}(c, d, r) = \\ \max(0, \|f_\eta(c) + f_\eta(r) - f_\eta(d)\| + r_\eta(c) - r_\eta(d) - \gamma) \quad (4) \\ + |\|f_\eta(c)\| - 1| + |\|f_\eta(d)\| - 1| \end{aligned}$$

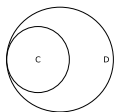
Algorithm: loss functions

$$\begin{aligned} \text{loss}_{\exists R.C \sqsubseteq D}(c, d, r) = \\ \max(0, \|f_\eta(c) - f_\eta(r) - f_\eta(d)\| - r_\eta(c) - r_\eta(d) - \gamma) \quad (5) \\ + |\|f_\eta(c)\| - 1| + |\|f_\eta(d)\| - 1| \end{aligned}$$

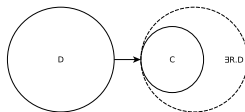
Algorithm: loss functions

$$\begin{aligned} \text{loss}_{C \cap D \sqsubseteq \perp}(c, d, e) = \\ \max(0, r_\eta(c) + r_\eta(d) - \|f_\eta(c) - f_\eta(d)\| + \gamma) \\ + |\|f_\eta(c)\| - 1| + |\|f_\eta(d)\| - 1| \end{aligned} \quad (6)$$

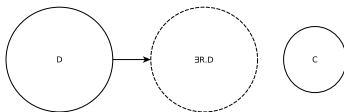
Algorithm: loss functions



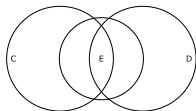
$C \subset D$



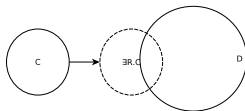
$C \subseteq \exists R.D$



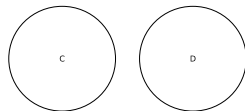
$C \not\subseteq \exists R.D$



$C \cap D \subseteq E$



$\exists R.C \subseteq D$



$C \cap D \subseteq \perp$

EL Embeddings

$$Male \sqsubseteq Person \quad (7)$$
$$Female \sqsubseteq Person \quad (8)$$
$$Father \sqsubseteq Male \quad (9)$$
$$Mother \sqsubseteq Female \quad (10)$$
$$Father \sqsubseteq Parent \quad (11)$$
$$Mother \sqsubseteq Parent \quad (12)$$
$$Female \sqcap Male \sqsubseteq \perp \quad (13)$$
$$Female \sqcap Parent \sqsubseteq Mother \quad (14)$$
$$Male \sqcap Parent \sqsubseteq Father \quad (15)$$
$$\exists hasChild.Person \sqsubseteq Parent \quad (16)$$
$$Parent \sqsubseteq Person \quad (17)$$
$$Parent \sqsubseteq \exists hasChild.\top \quad (18)$$

EL Embeddings

model with $\Delta = R^n$

support quantifiers, negation, conjunction,...

Zero-shot prediction with EL Embeddings

zero-shot prediction:

no instance of class C is observed

e.g., no protein has *ever* been observed with function C

e.g., no individual has *ever* been observed with disease C

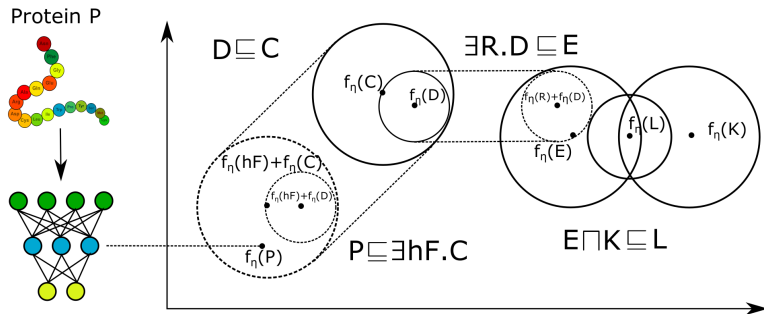
zero-shot prediction: predict instances of C

assumption: C is used in axioms, e.g., $C \sqsubseteq \exists R.D$ or $C \equiv A \sqcap B$

no training data

can we exploit axioms and entailment within the embedding space?

Zero-shot prediction with EL Embeddings



Kulmanov & Hoehndorf, DeepGOZero: Improving protein function prediction from sequence and zero-shot learning based on ontology axioms. ISMB, 2022.

Zero-shot prediction: more general

Embedding

An embedding is a map (morphism) from one mathematical structure X into another structure Y :

$$f : X \hookrightarrow Y$$

such that X is preserved in Y .

Zero-shot prediction: more general

Embedding

An embedding is a map (morphism) from one mathematical structure X into another structure Y :

$$f : X \hookrightarrow Y$$

such that X is preserved in Y .

- existence of f^{-1}

 - inverse embedding

 - allows “extraction” of X from Y

- formulation of the prediction problem in X

 - e.g., classification: $X \sqsubseteq \exists R.Y$

 - loss expressed in terms of f^{-1}

- joint embedding of X and Z in Y

 - Z is a third structure providing external information

mOWL

high-performance software library for machine learning with
Semantic Web (OWL) ontologies

ontology embeddings, zero-shot, constrained optimization
contains

- graph generation (DL2Vec, OWL2Vec*, Taxonomy)

- graph embedding (random walk + word2vec, node2vec,
various knowledge graph embedding methods from
PyKEEN)

- model-based embeddings (ELEm, EMEI, ELBE)

- category-theoretical embeddings

- FuzzFuzzFuzz ALC embeddings

Algorithms written in Python + Scala (OWLAPI), tuned for
performance

<https://github.com/bio-ontology-research-group/mowl>

Hands-on part

There is a notebook available that shows how to use mOWL with all the methods introduced here. Run the code in the Notebook. When complete, change the task from prediction of PPIs to the prediction of gene–disease associations as in the Semantic Similarity notebook.

Temporary page!

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