

# BIMM 143

## Structural Bioinformatics

Lecture 11

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UC San Diego

<http://thegrantlab.org/bimm143>

*“Bioinformatics is the application of computers to the collection, archiving, organization, and analysis of biological data.”*

... A hybrid of biology and computer science

*“Bioinformatics is the application of computers to the collection, archiving, organization, and analysis of biological data.”*

**Bioinformatics is computer aided biology!**

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**Goal: Data to Knowledge**

So what is **structural bioinformatics**?

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**... computer aided structural biology!**

Aims to characterize and interpret biomolecules and their assemblies at the molecular & atomic level

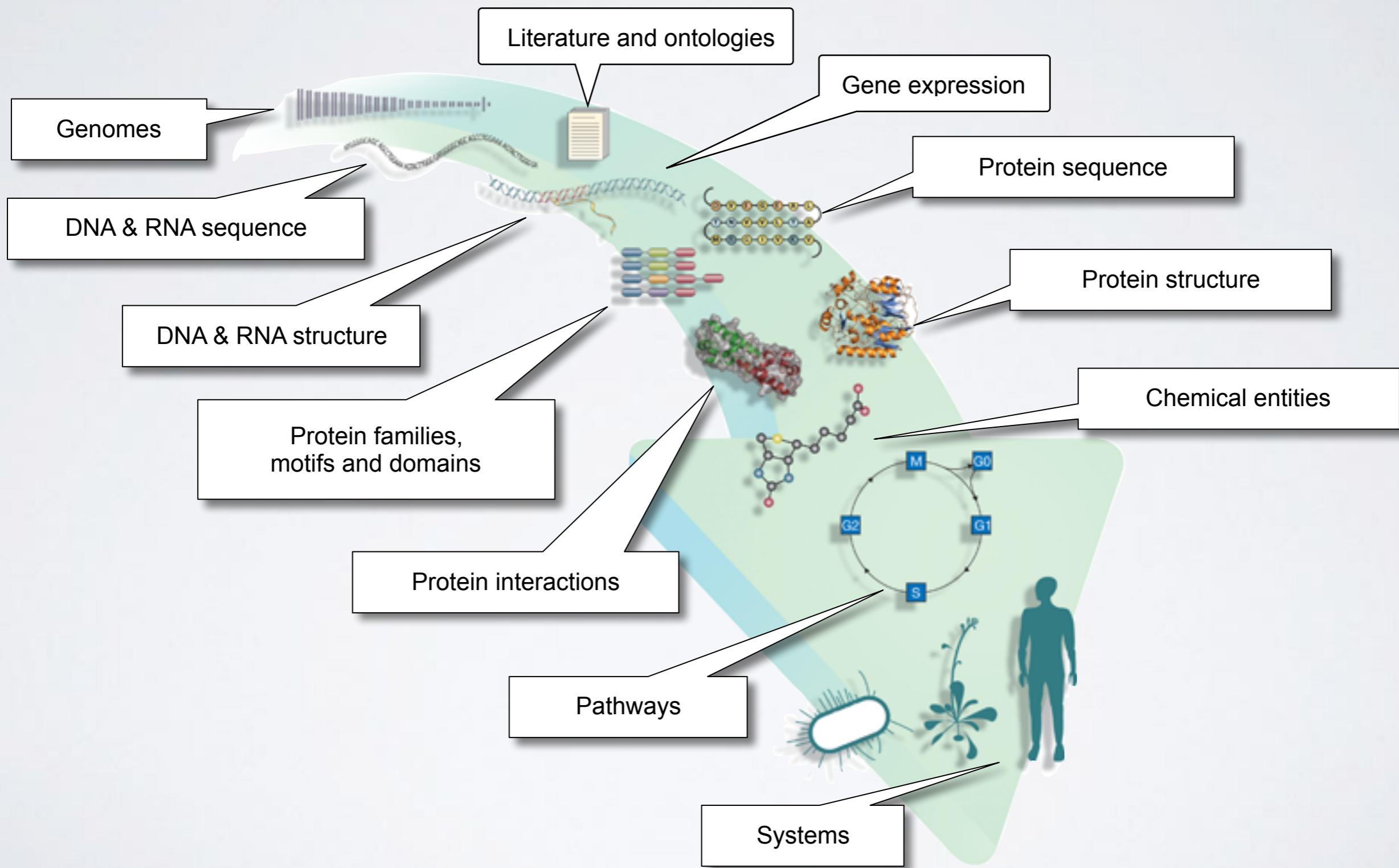
# Why should we care?

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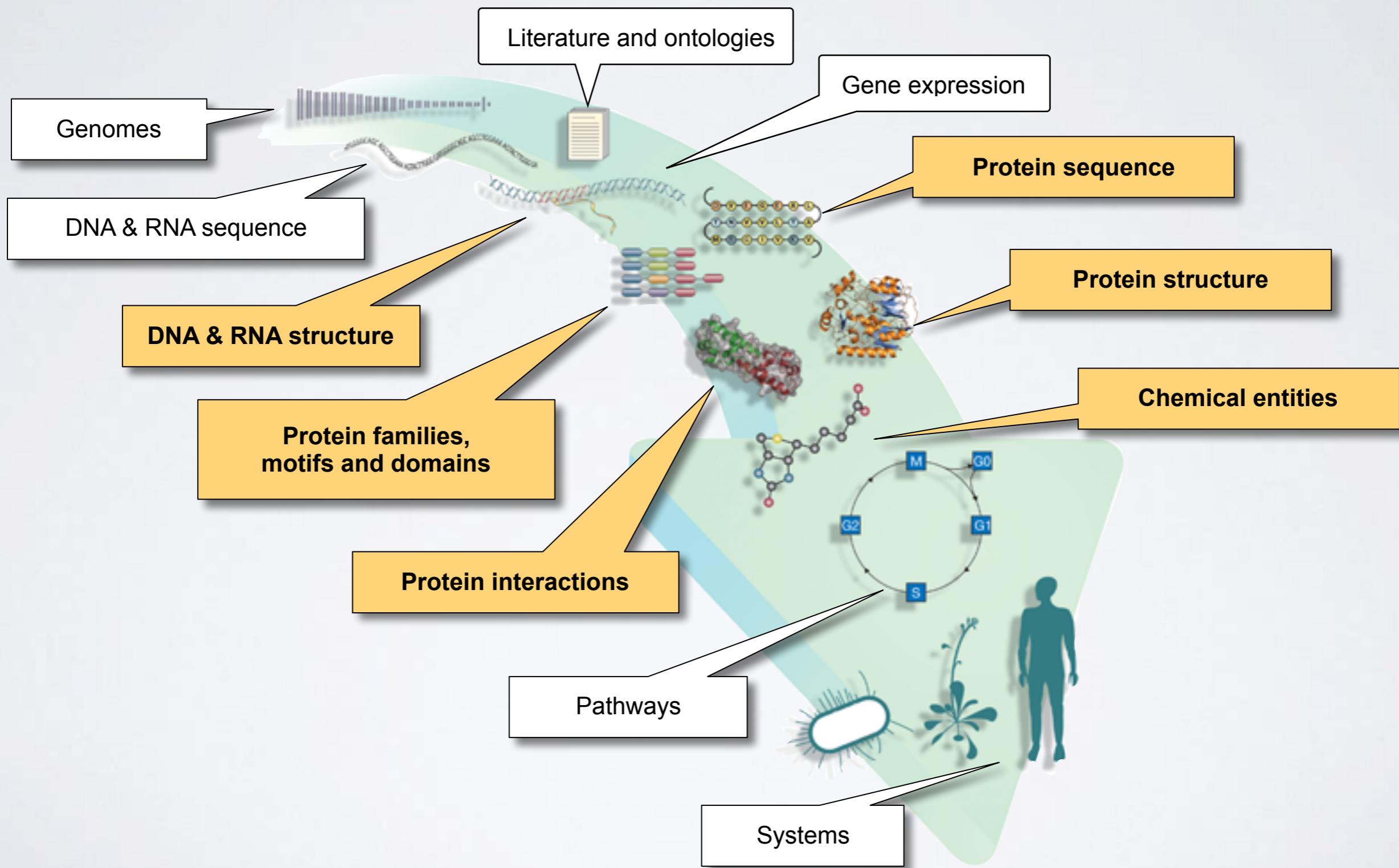
Because biomolecules are “nature’s robots”

... and because it is only by coiling into  
**specific 3D structures** that they are able to  
perform their functions

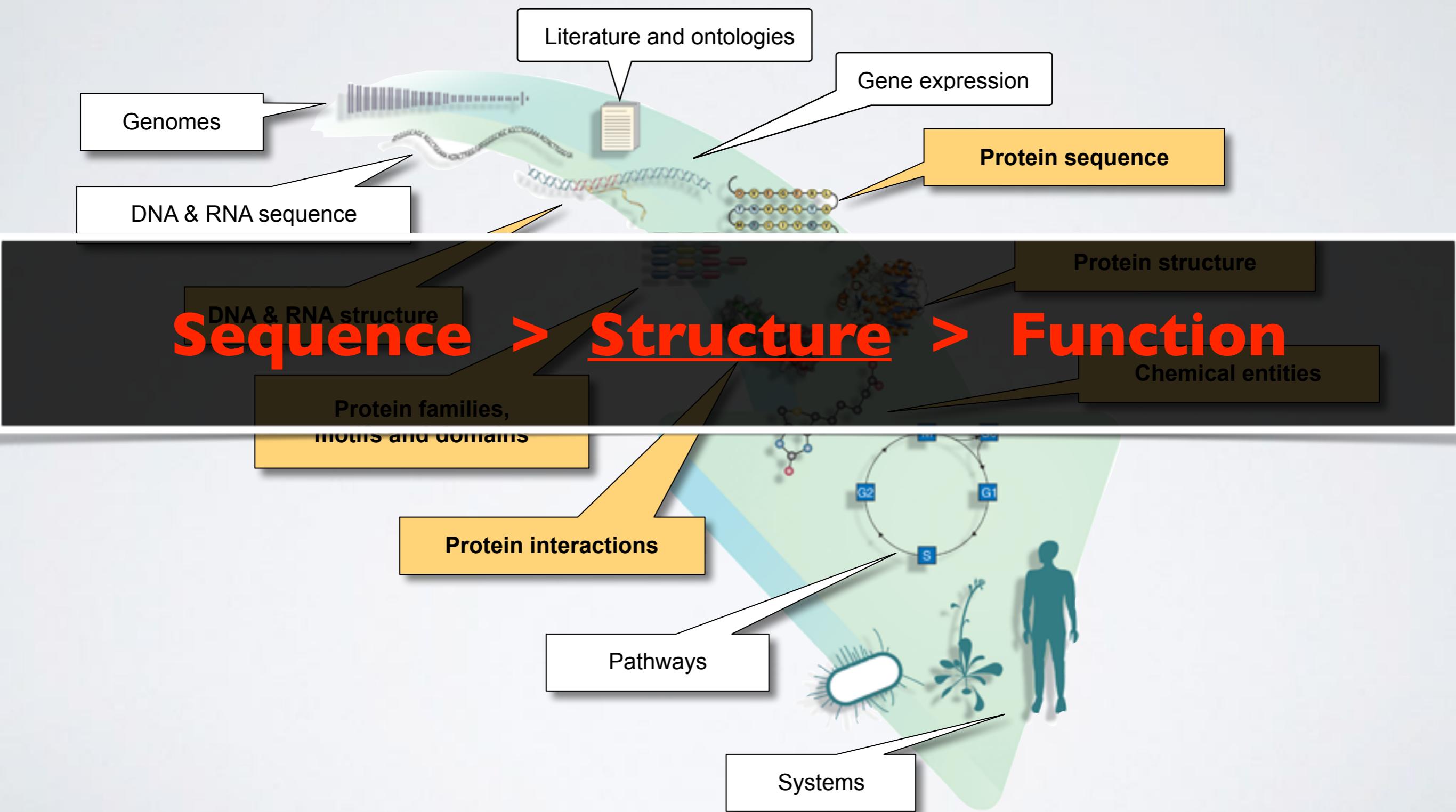
# BIOINFORMATICS DATA



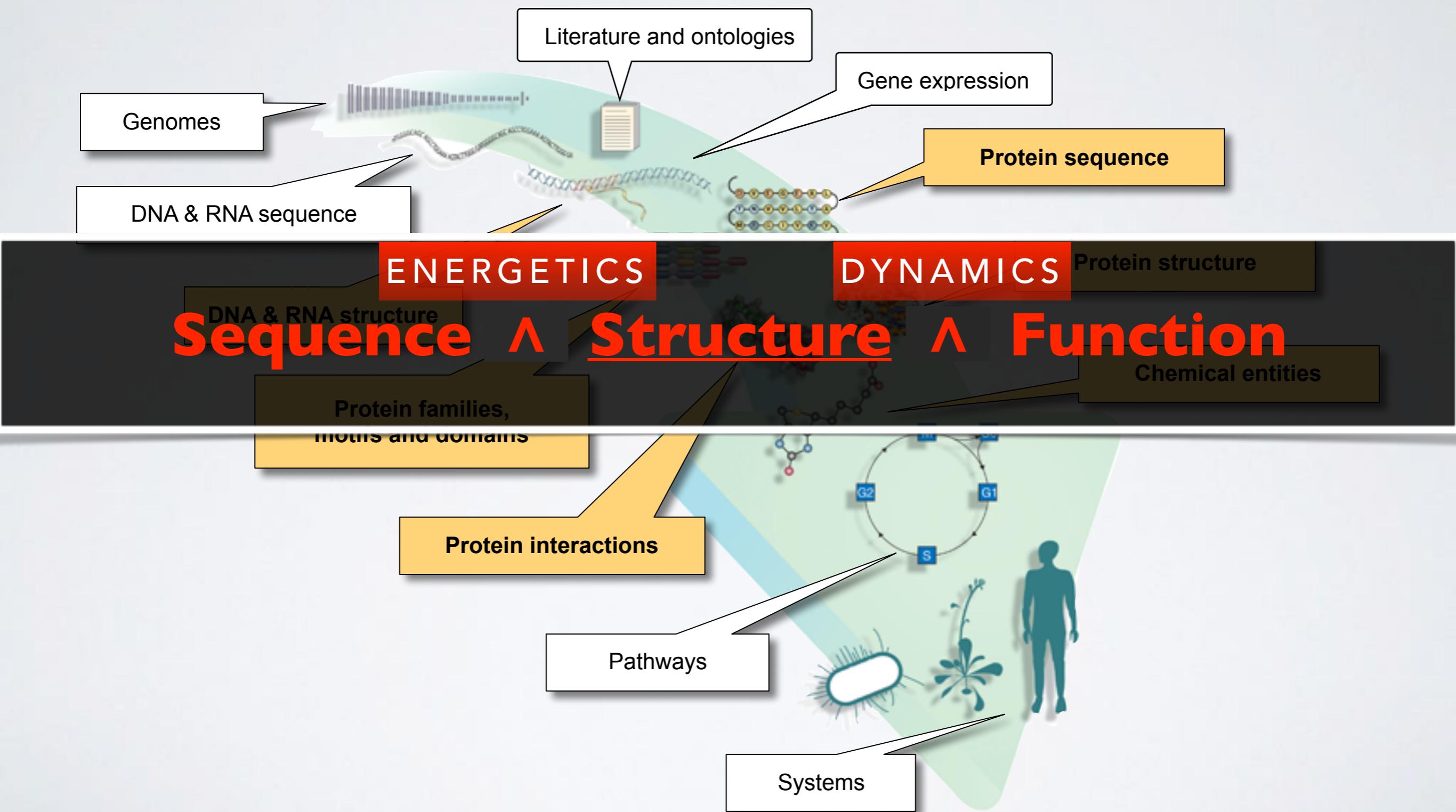
# STRUCTURAL DATA IS CENTRAL

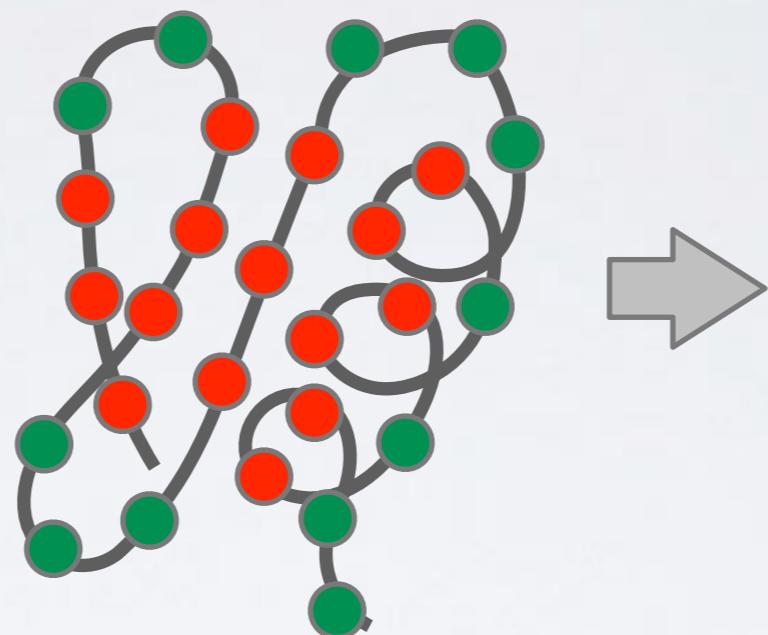
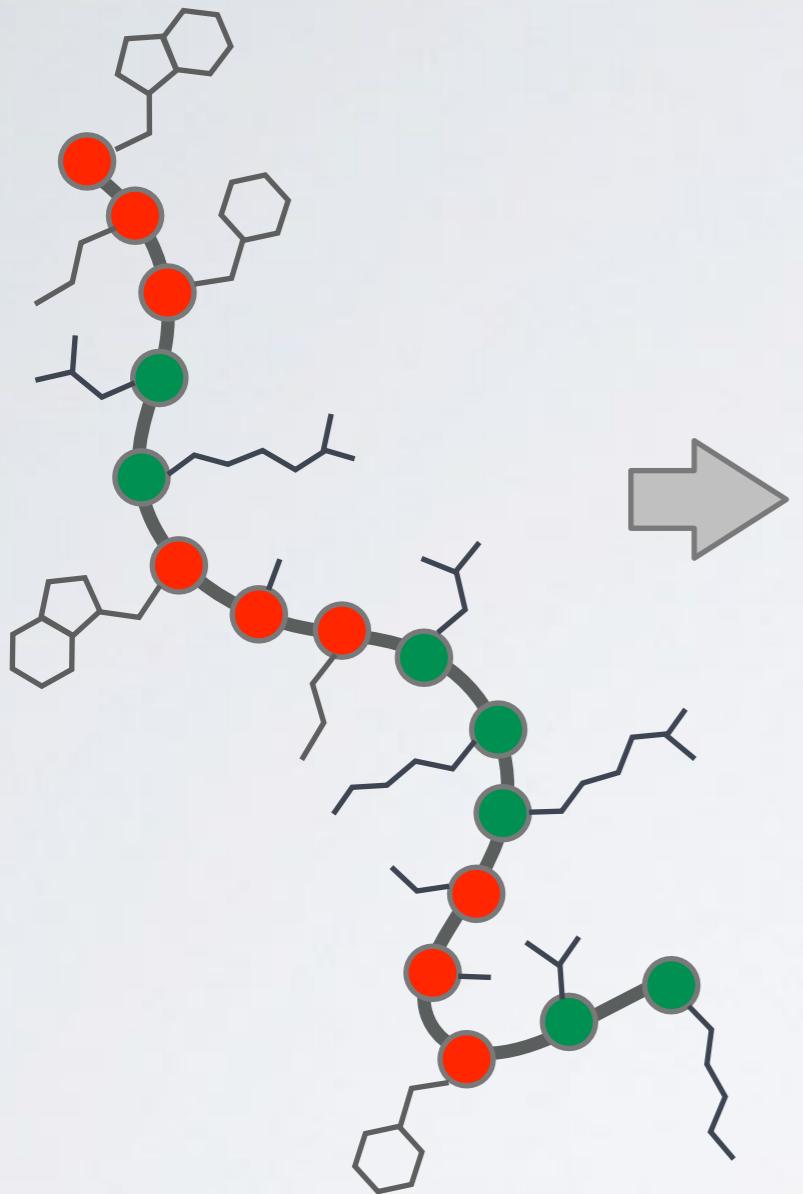


# STRUCTURAL DATA IS CENTRAL



# STRUCTURAL DATA IS CENTRAL





## Sequence

- Unfolded chain of amino acid chain
- Highly mobile
- Inactive

## Structure

- Ordered in a precise 3D arrangement
- Stable but dynamic

## Function

- Active in specific “conformations”
- Specific associations & precise reactions

In daily life, we use machines  
with functional structure and *moving parts*



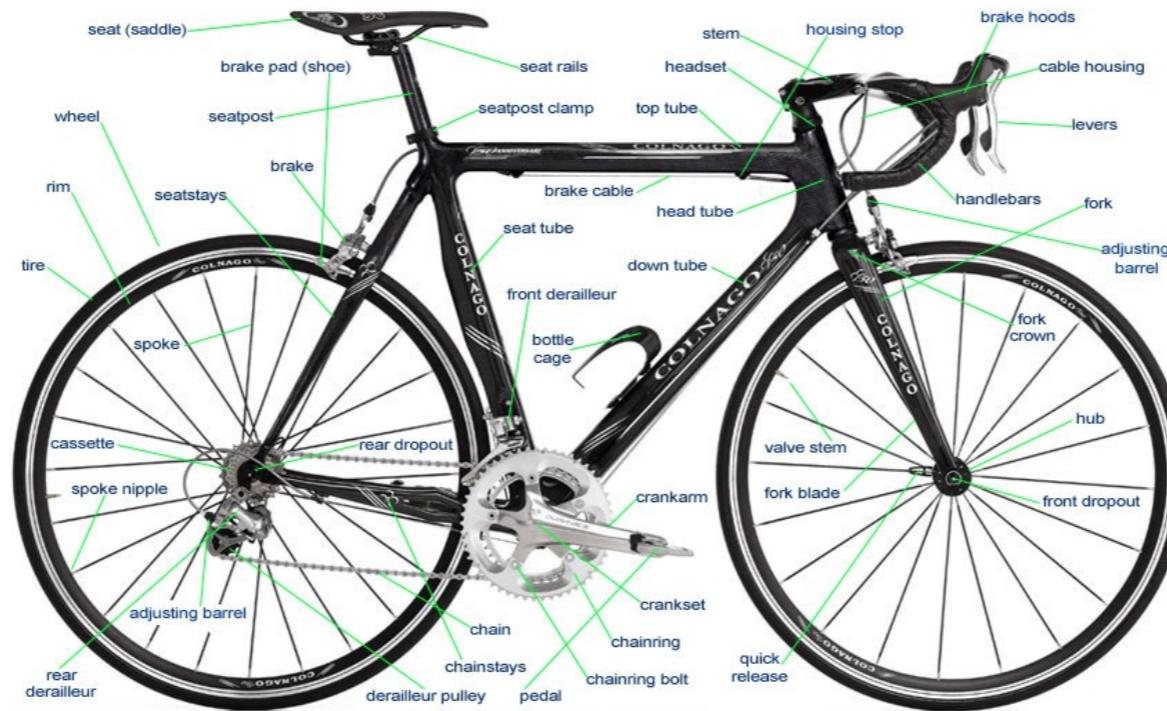
# Genomics is a great start ....

## Track Bike – DL 175

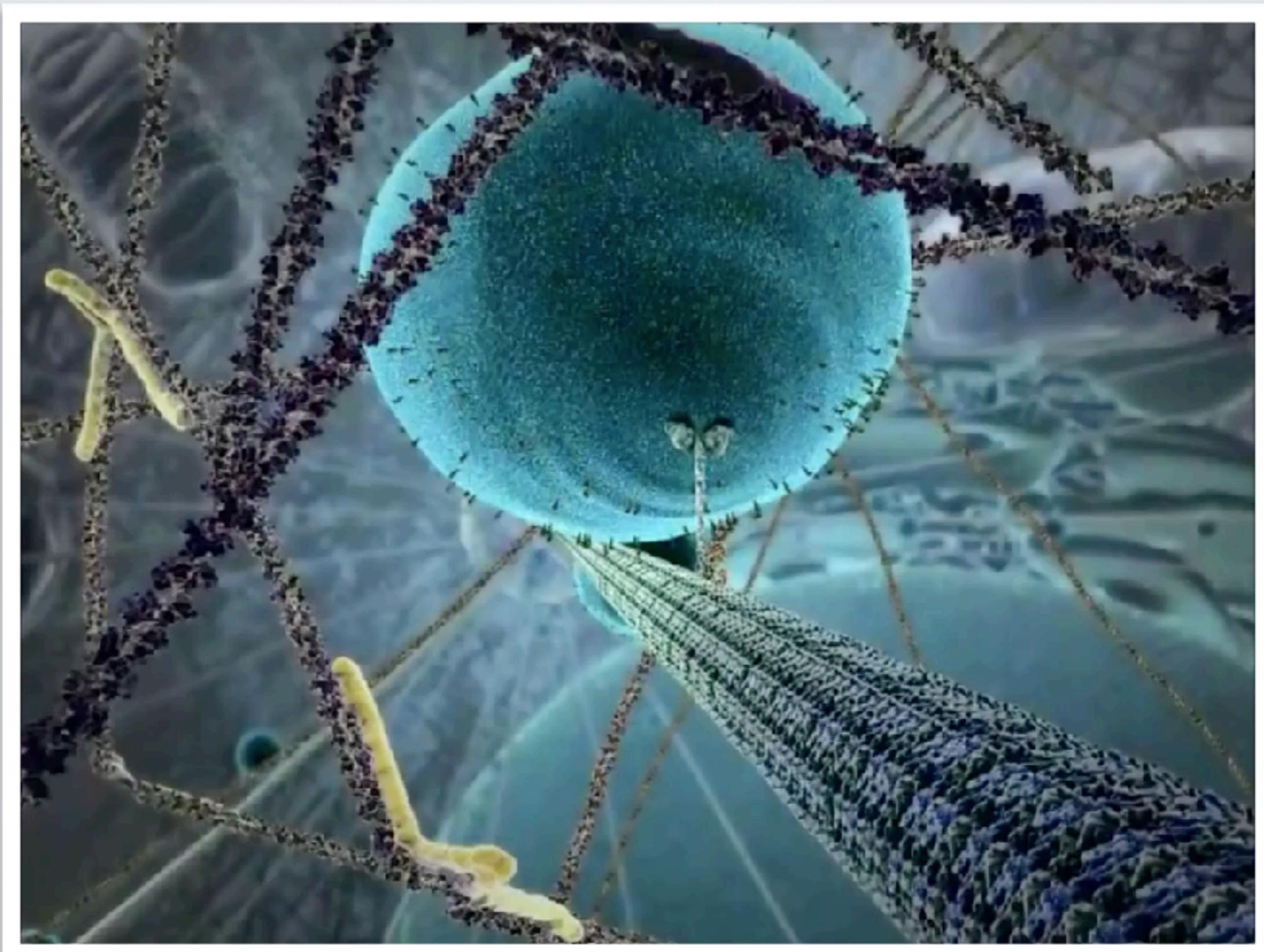
REF. NO.	IBM NO.	DESCRIPTION
1	156011	Track Frame 21", 22", 23", 24", Team Red
2	157040	Fork for 21" Frame
2	157039	Fork for 22" Frame
2	157038	Fork for 23" Frame
2	157037	Fork for 24" Frame
3	191202	Handlebar TTT Competition Track Alloy 15/16"
4		Handlebar Stem, TTT, Specify extension
5	191278	Expander Bolt
6	191272	Clamp Bolt
7	145841	Headset Complete 1 x 24 BSC
8	145842	Ball Bearings
9	190420	175 Raleigh Pistard Seta Tubular Prestavalve 27"
10	190233	Rim, 27" AVA Competition (36H) Alloy Prestavalve
11	145973	Hub, Large Flange Campagnolo Pista Track Alloy (pairs)
12	190014	Spokes, 11 5/8"
13	145837	Sleeve
14	145636	Ball Bearings
15	145170	Bottom Bracket Axle
16	145838	Cone for Sleeve
17	146473	L.H. Adjustable Cup
18	145833	Lockring
19	145239	Straps for Toe Clips
20	145834	Fixing Bolt
21	145835	Fixing Washer
22	145822	Dustcap
23	145823	R.H. and L.H. Crankset with Chainwheel
24	146472	Fixed Cup
25	145235	Toe Clips, Christophe, Chrome (Medium)
26	145684	Pedals, Extra Light, Pairs
27	123021	Chain
28	145980	Seat Post
29		Seat Post Bolt and Nut
30	167002	Saddle, Brooks
31	145933	Track Sprocket, Specify 12, 13, 14, 15, or 16 T.

- But a parts list is not enough to understand how a bicycle works

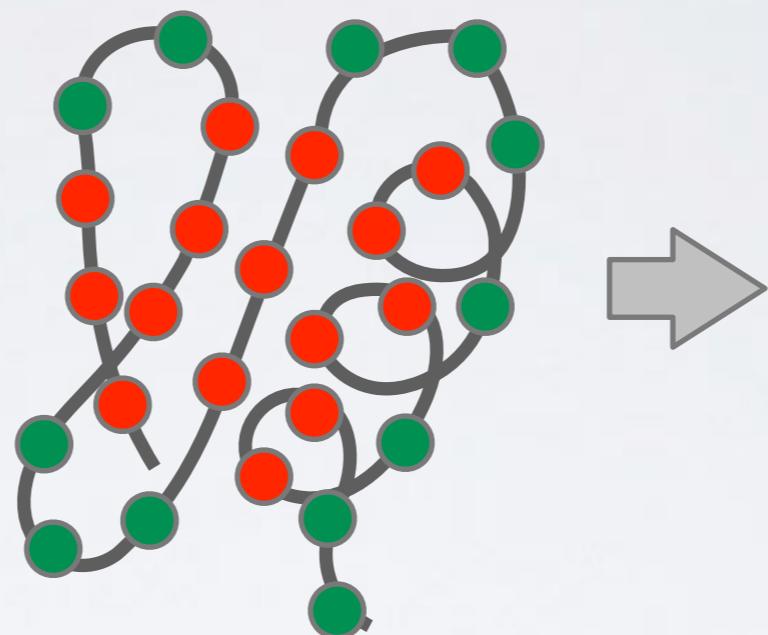
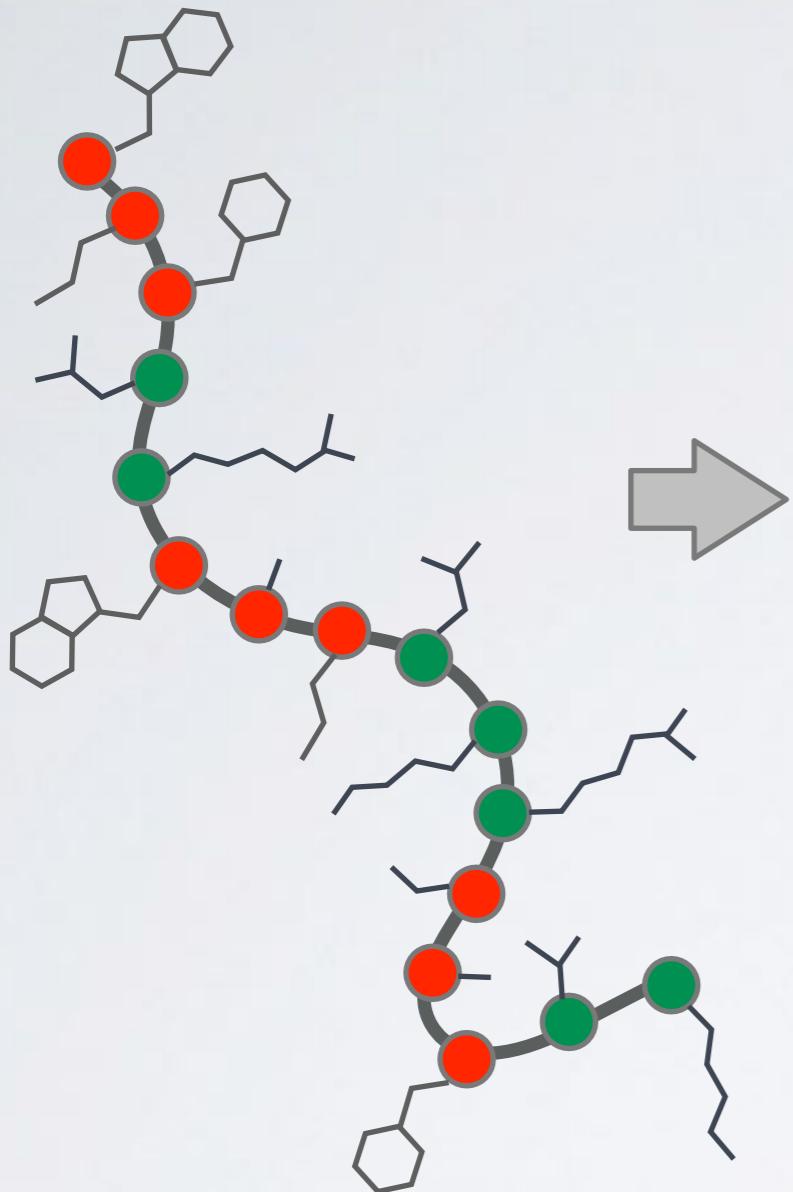
# ... but not the end



- We want the full spatiotemporal picture, and an ability to control it
- Broad applications, including drug design, medical diagnostics, chemical manufacturing, and energy



Extracted from The Inner Life of a Cell by Cellular Visions and Harvard  
[YouTube link: <https://www.youtube.com/watch?v=y-uuk4Pr2i8> ]



## Sequence

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- Highly mobile
- Inactive

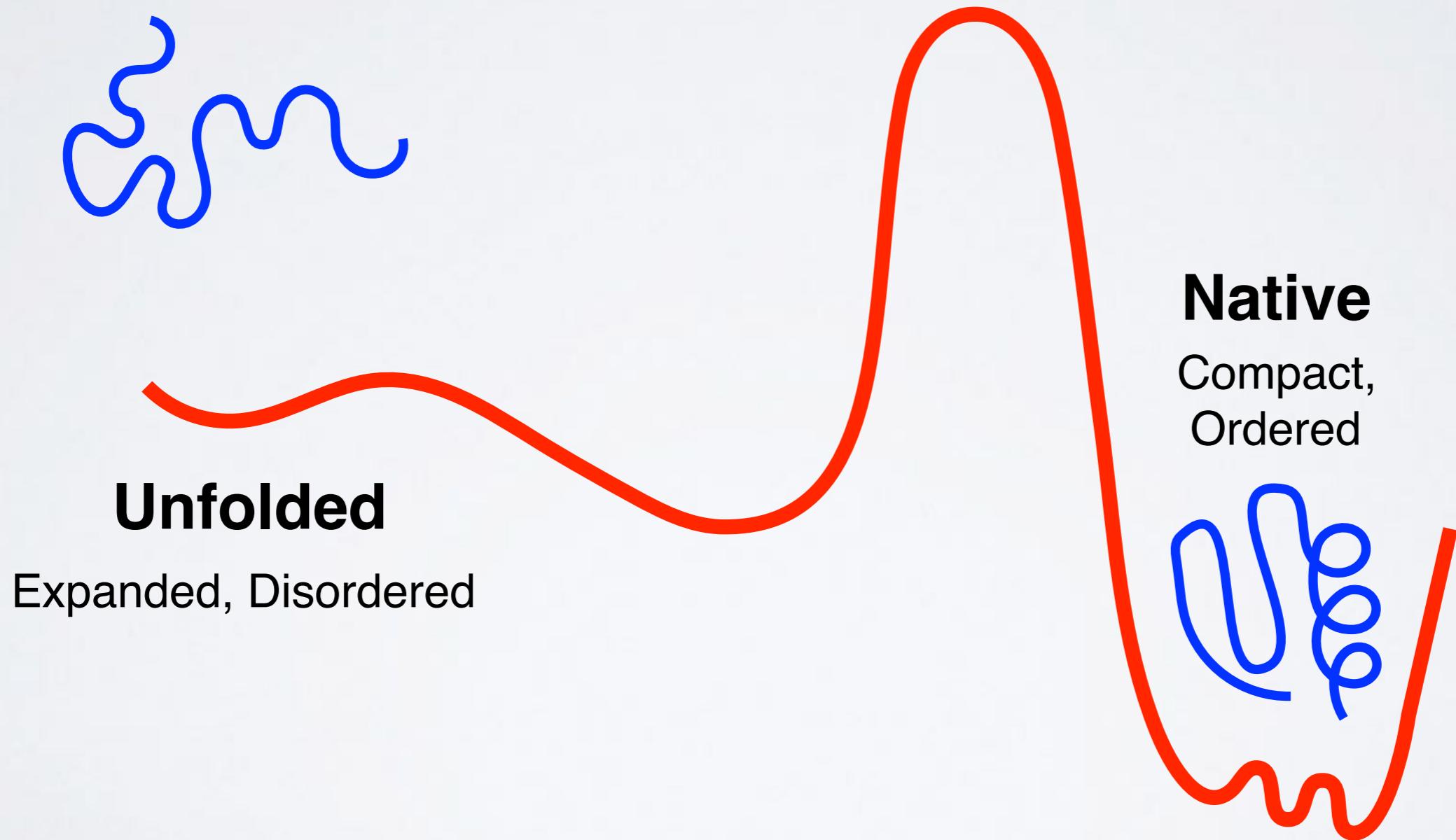
## Structure

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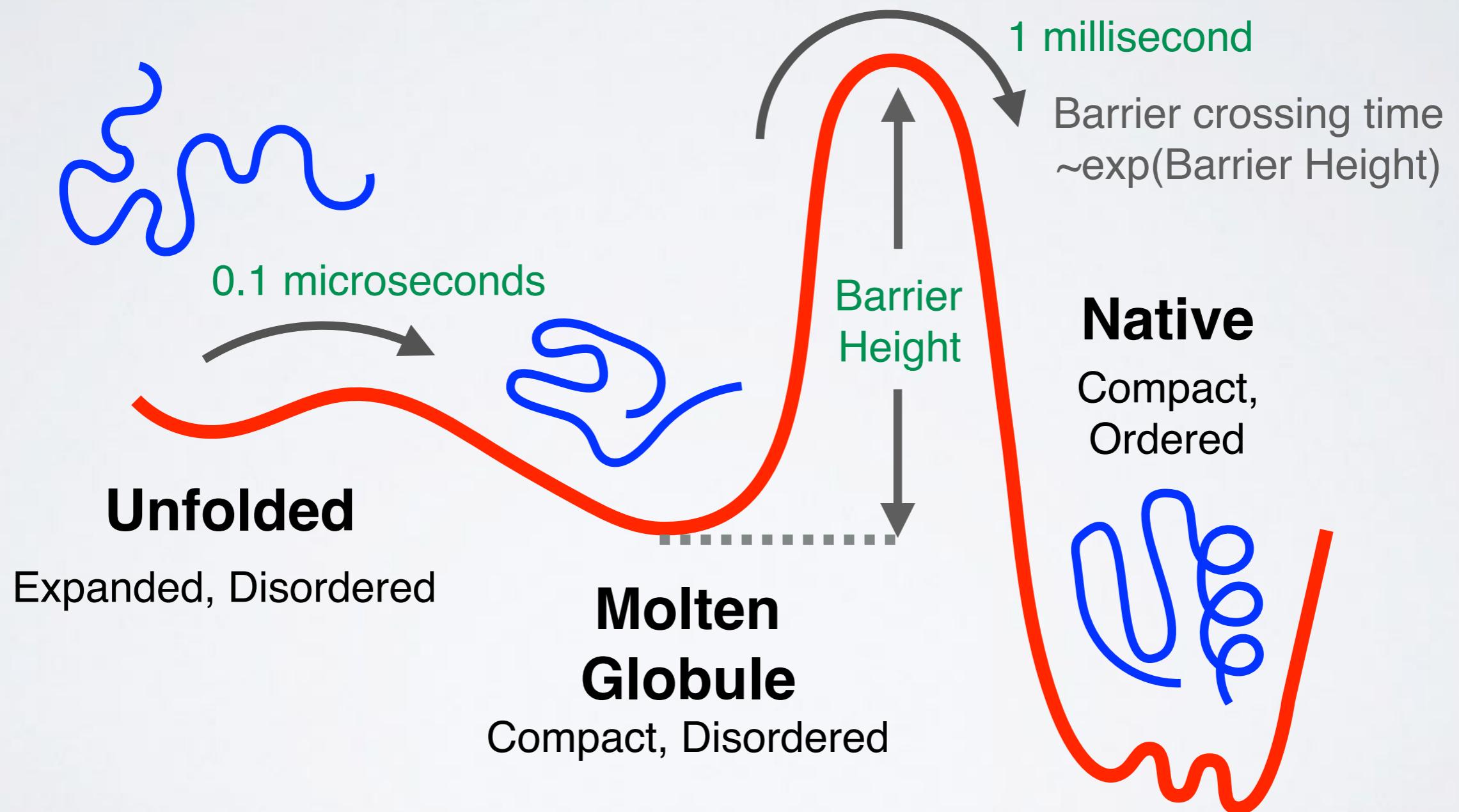
## Function

- Active in specific “conformations”
- Specific associations & precise reactions

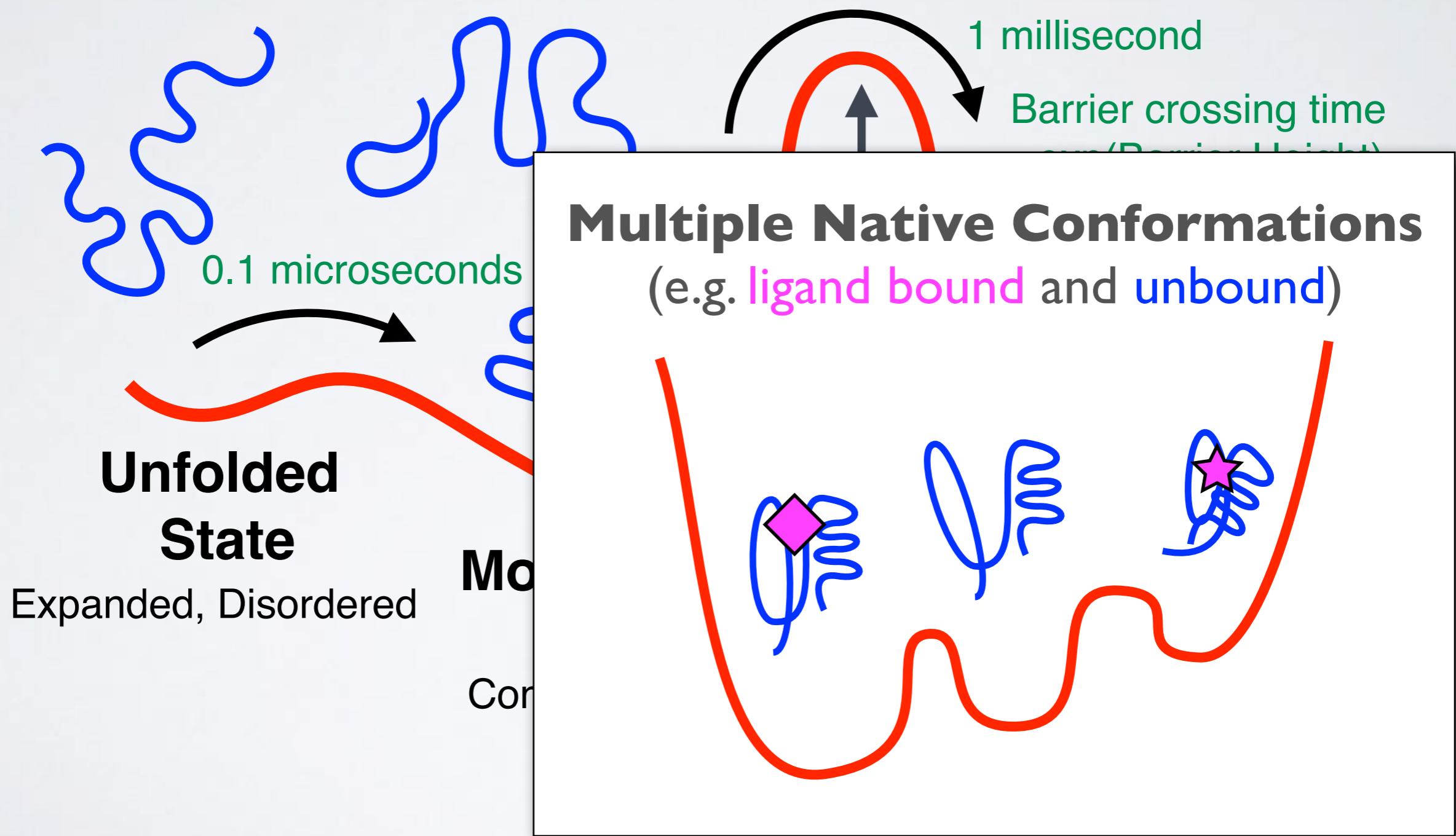
# KEY CONCEPT: ENERGY LANDSCAPE



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# **OUTLINE:**

- ▶ **Overview of structural bioinformatics**
  - Major motivations, goals and challenges
- ▶ **Fundamentals of protein structure**
  - Composition, form, forces and dynamics
- ▶ **Representing and interpreting protein structure**
  - Modeling energy as a function of structure
- ▶ **Example application areas**
  - Predicting functional dynamics & drug discovery

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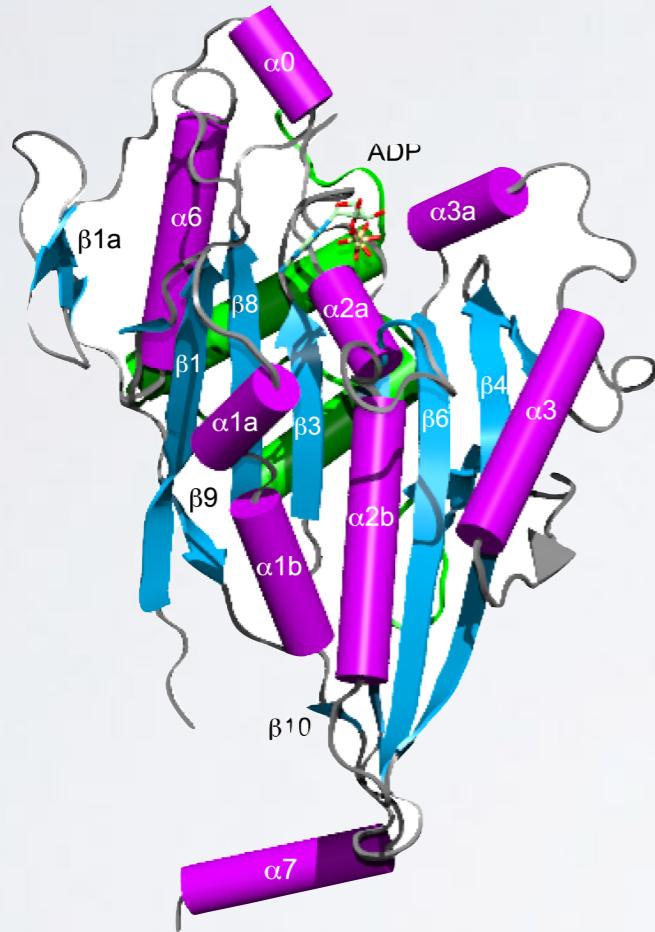
- ▶ **Representing and interpreting protein structure**

- Modeling energy as a function of structure

- ▶ **Example application areas**

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# TRADITIONAL FOCUS **PROTEIN**, **DNA** AND **SMALL MOLECULE** DATA SETS WITH **MOLECULAR STRUCTURE**



Protein  
(PDB)

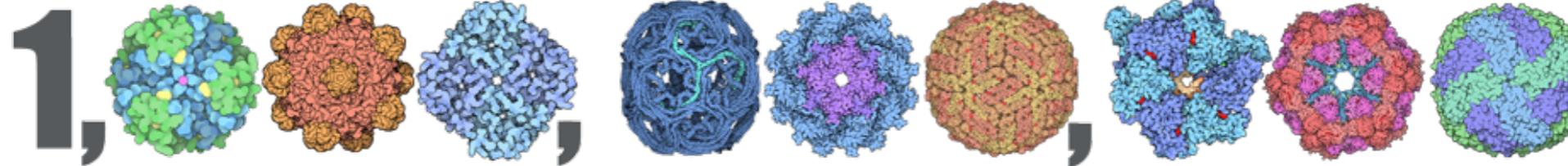


DNA  
(NDB)

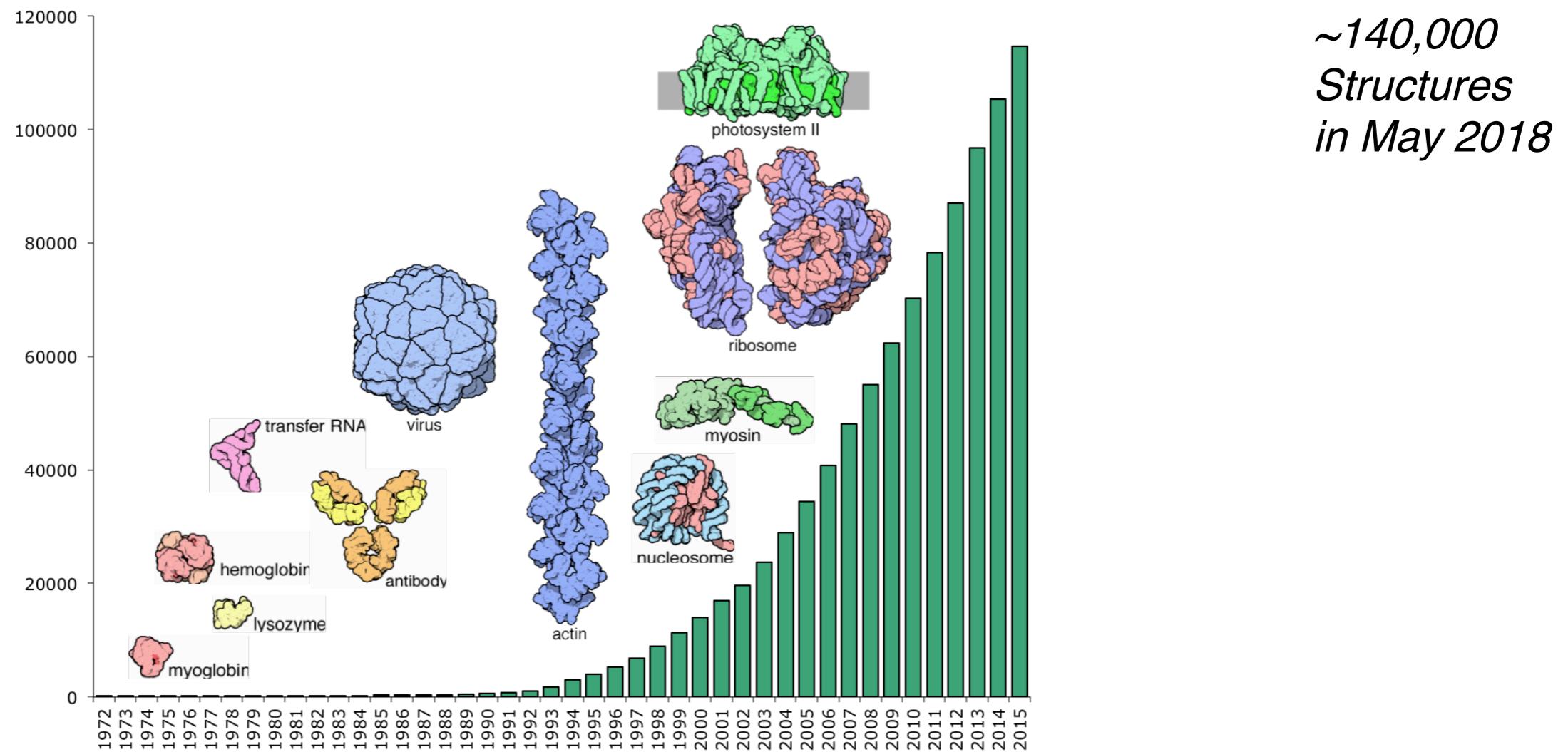


Small Molecules  
(CCDB)

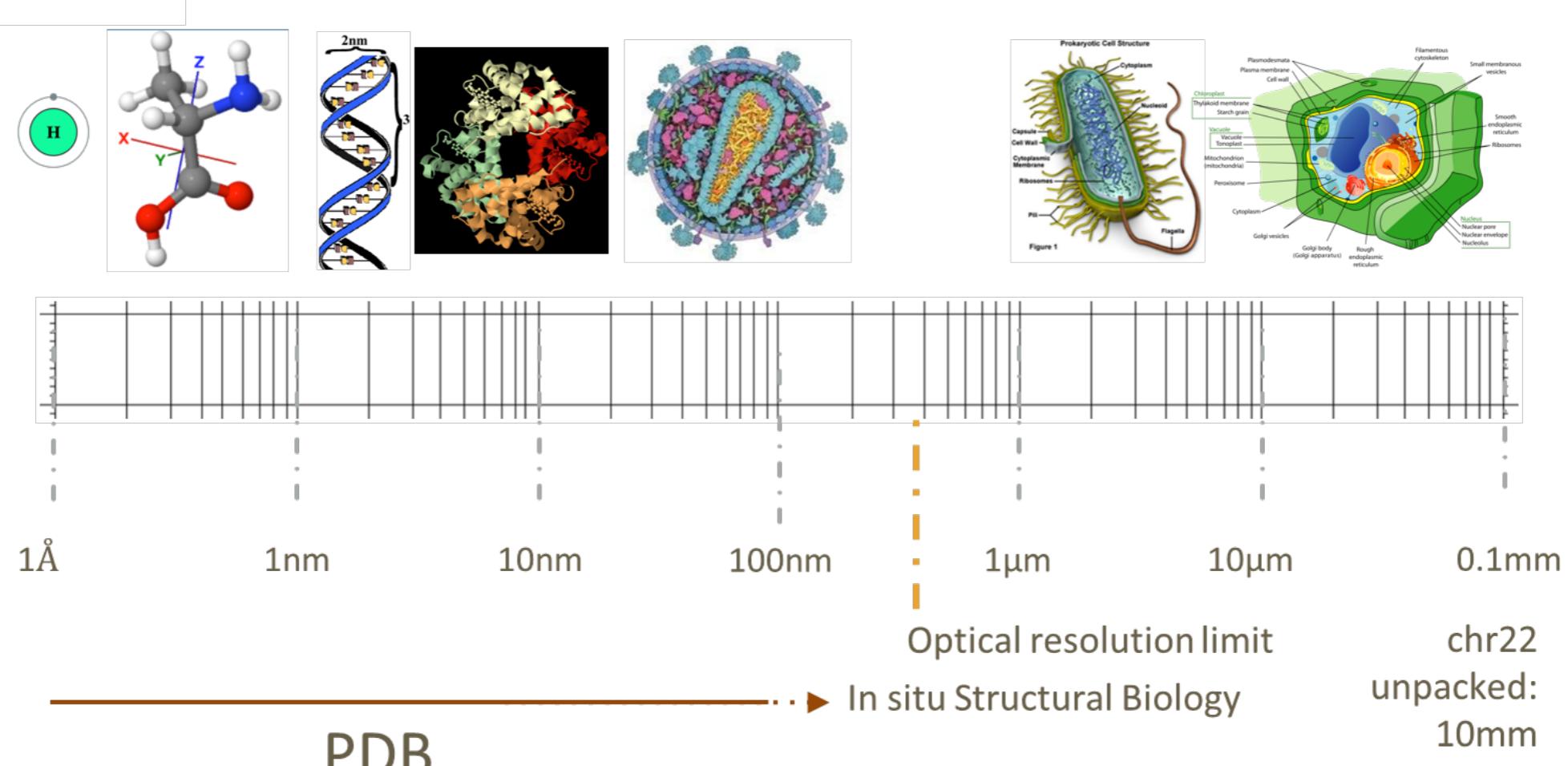
# PDB – A Billion Atom Archive



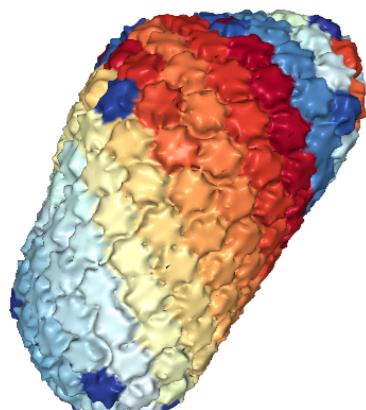
*> 1 billion atoms in the asymmetric units*



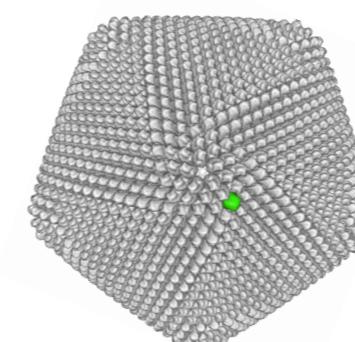
# Growing Structure Size and Complexity



Largest asymmetric structure in PDB



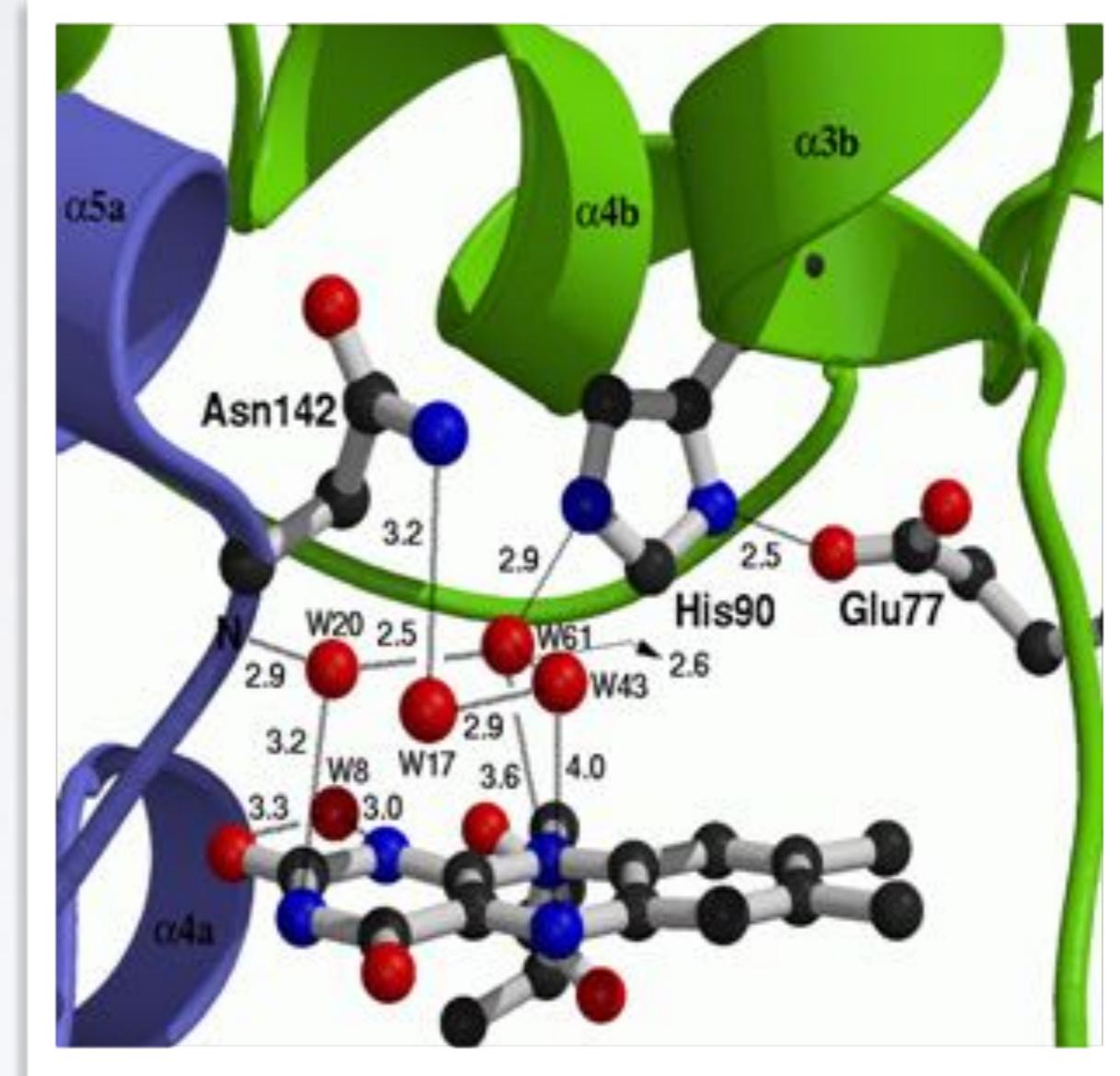
HIV-1 capsid: PDB ID 3J3Q  
 $\sim 2.4\text{M}$  unique atoms



Faustovirus major capsid: PDB ID 5J7V  
 $\sim 40\text{M}$  overall atoms

## Motivation 1: Detailed understanding of molecular interactions

Provides an invaluable structural context for conservation and mechanistic analysis leading to functional insight.



## Motivation 1: Detailed understanding of molecular interactions

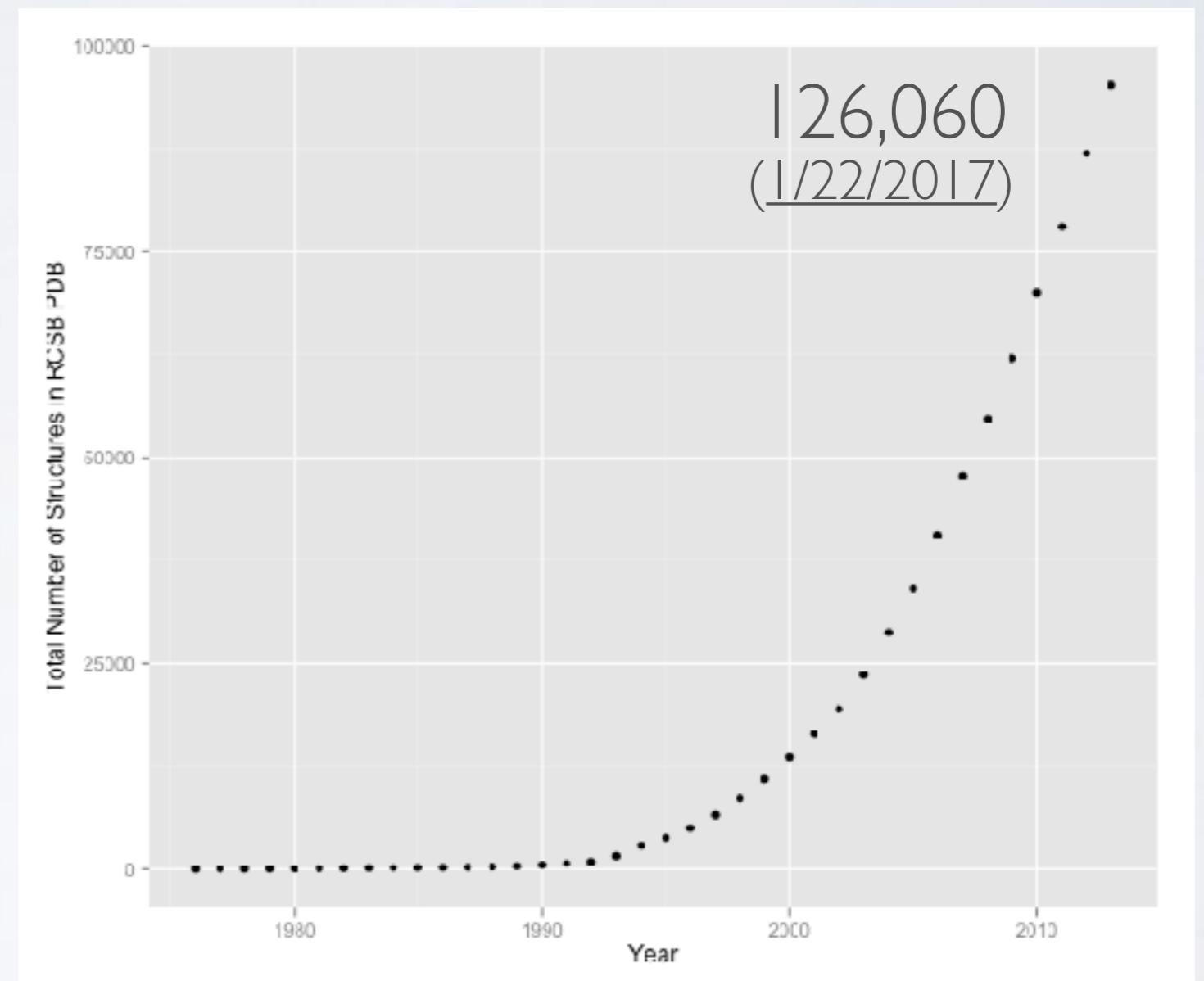
Computational modeling can provide detailed insight into functional interactions, their regulation and potential consequences of perturbation.



Grant et al. PLoS. Comp. Biol. (2010)

## Motivation 2: Lots of structural data is becoming available

Structural Genomics has  
contributed to driving  
down the cost and time  
required for structural  
determination



Data from: <http://www.rcsb.org/pdb/statistics/>

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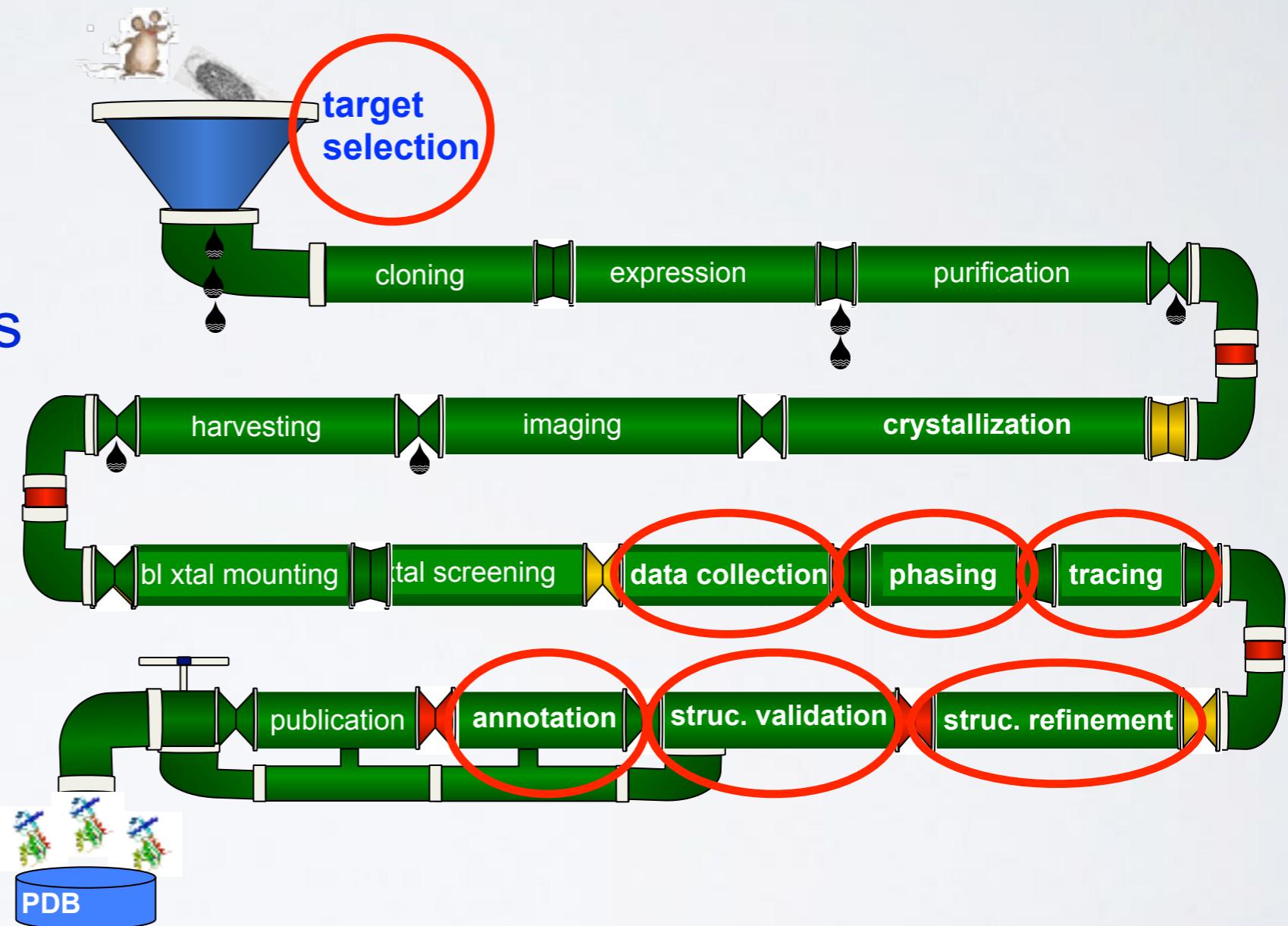
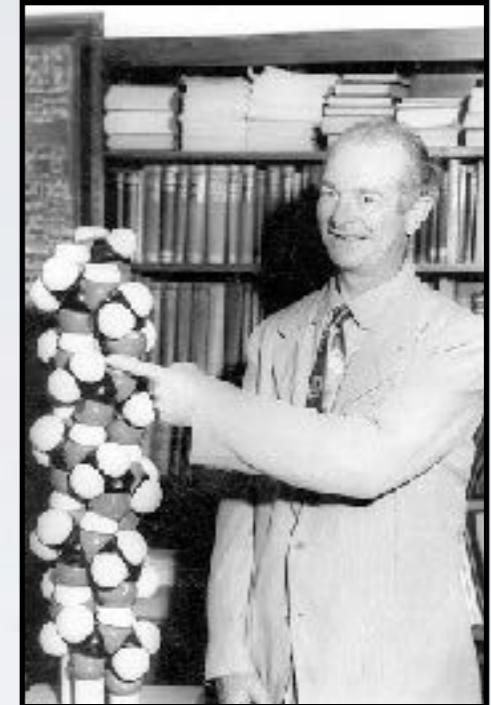


Image Credit: "Structure determination assembly line" Adam Godzik

**Motivation 3:**  
Theoretical and  
computational predictions  
have been, and continue  
to be, enormously  
valuable and influential!



# SUMMARY OF KEY **MOTIVATIONS**

## **Sequence > Structure > Function**

- Structure determines function, so understanding structure helps our understanding of function

## **Structure is more conserved than sequence**

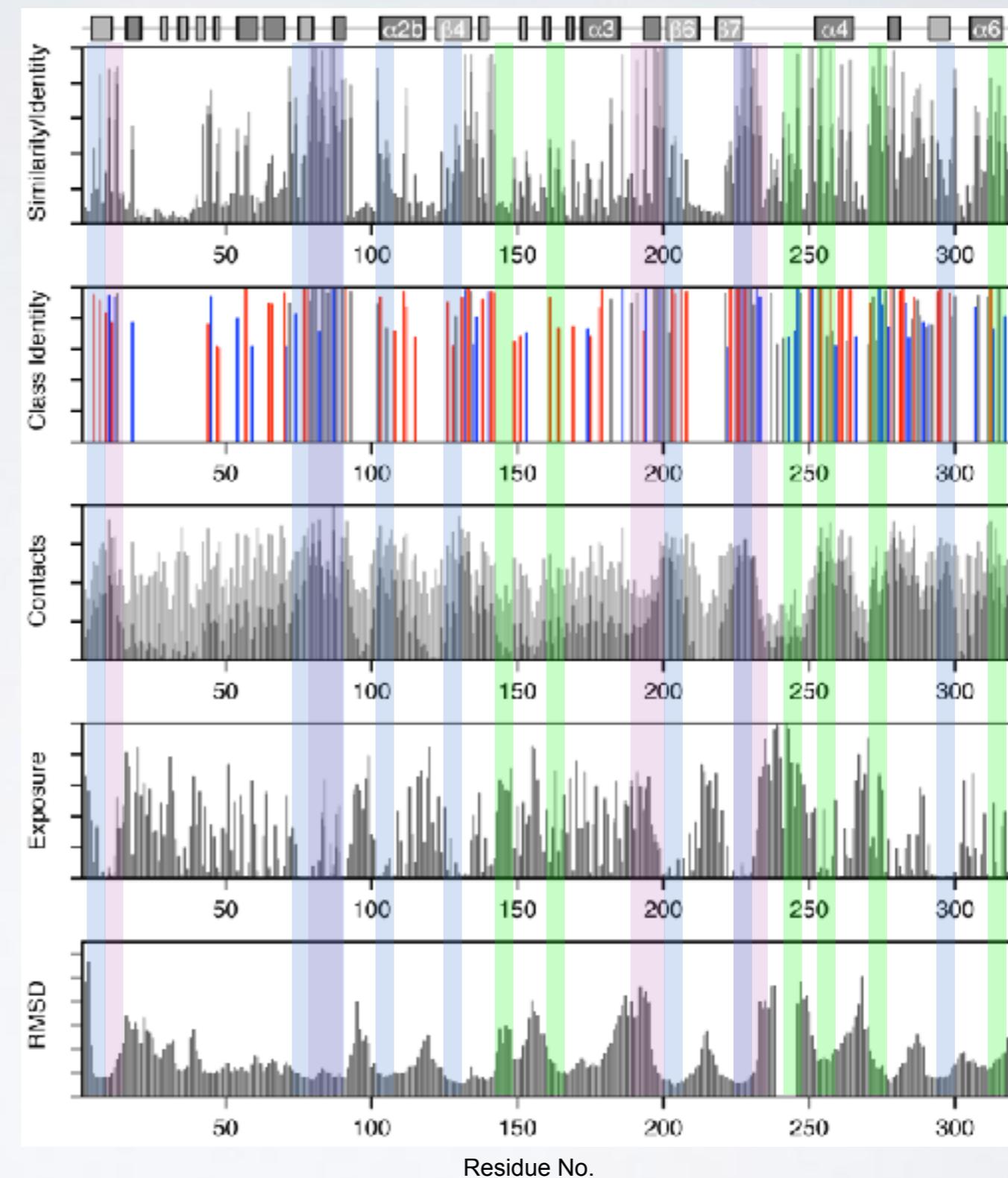
- Structure allows identification of more distant evolutionary relationships

## **Structure is encoded in sequence**

- Understanding the determinants of structure allows design and manipulation of proteins for industrial and medical advantage

## Goals:

- Analysis
- Visualization
- Comparison
- Prediction
- Design



## Goals:

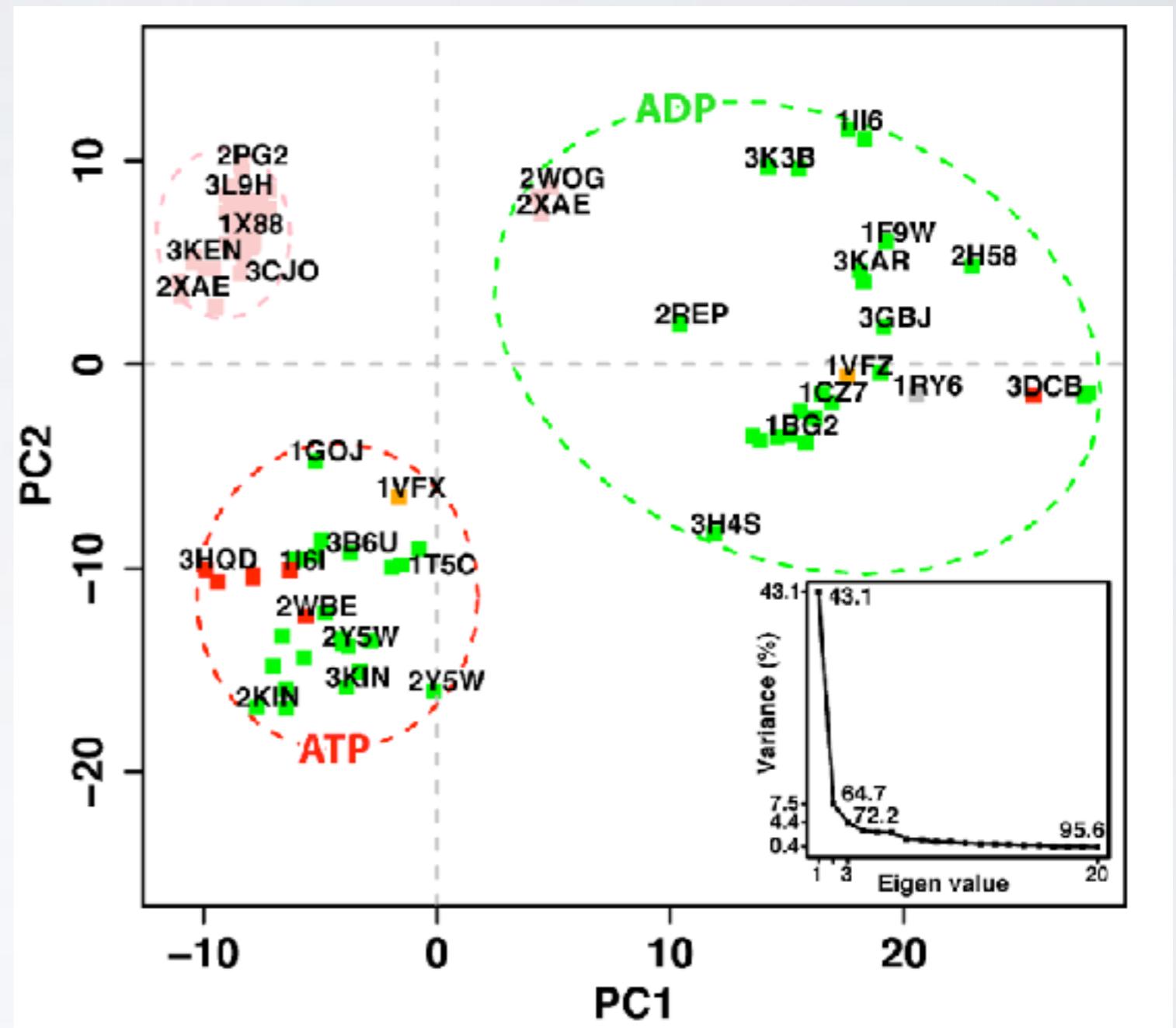
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Scarabelli and Grant. PLoS. Comp. Biol. (2013)

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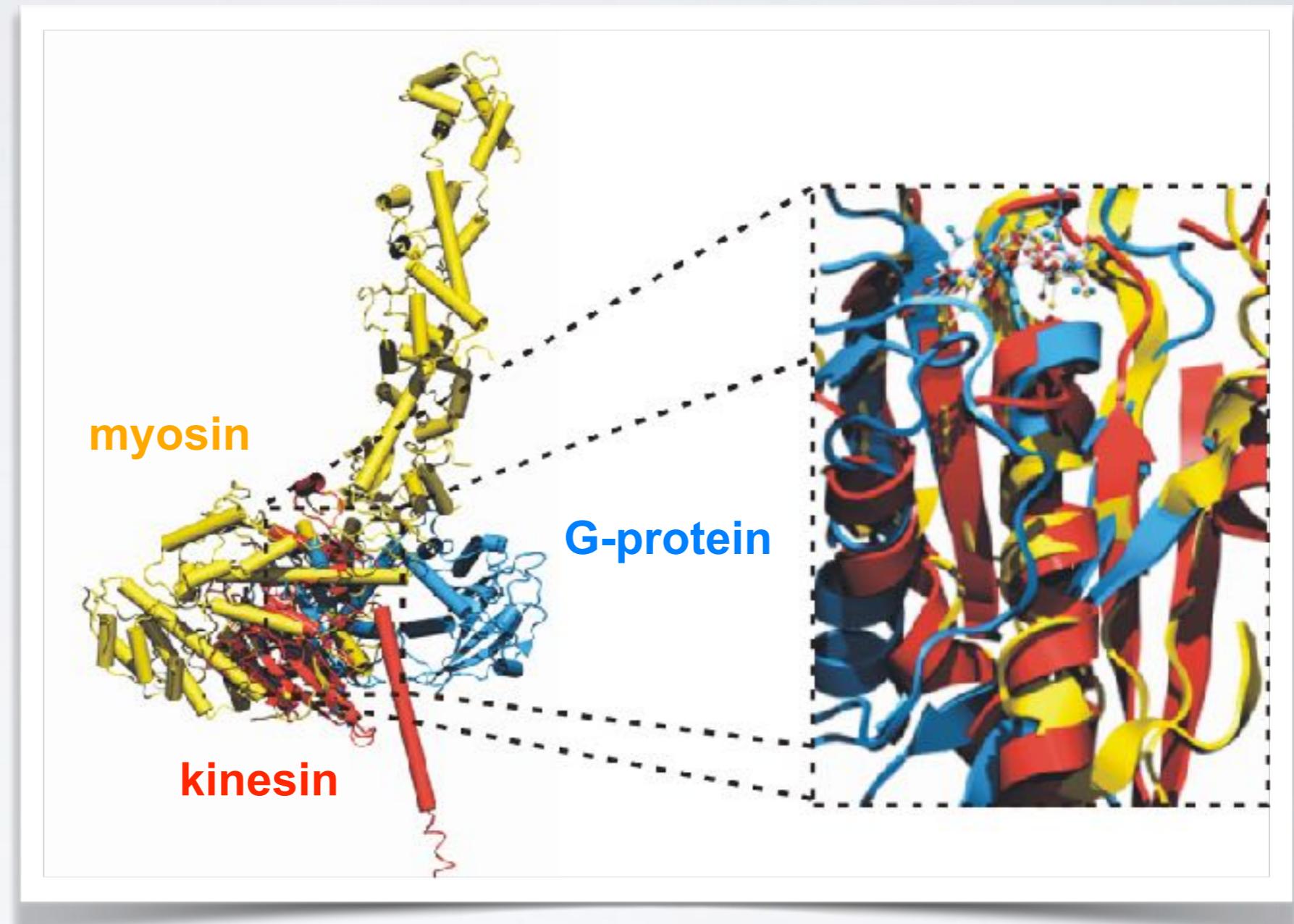
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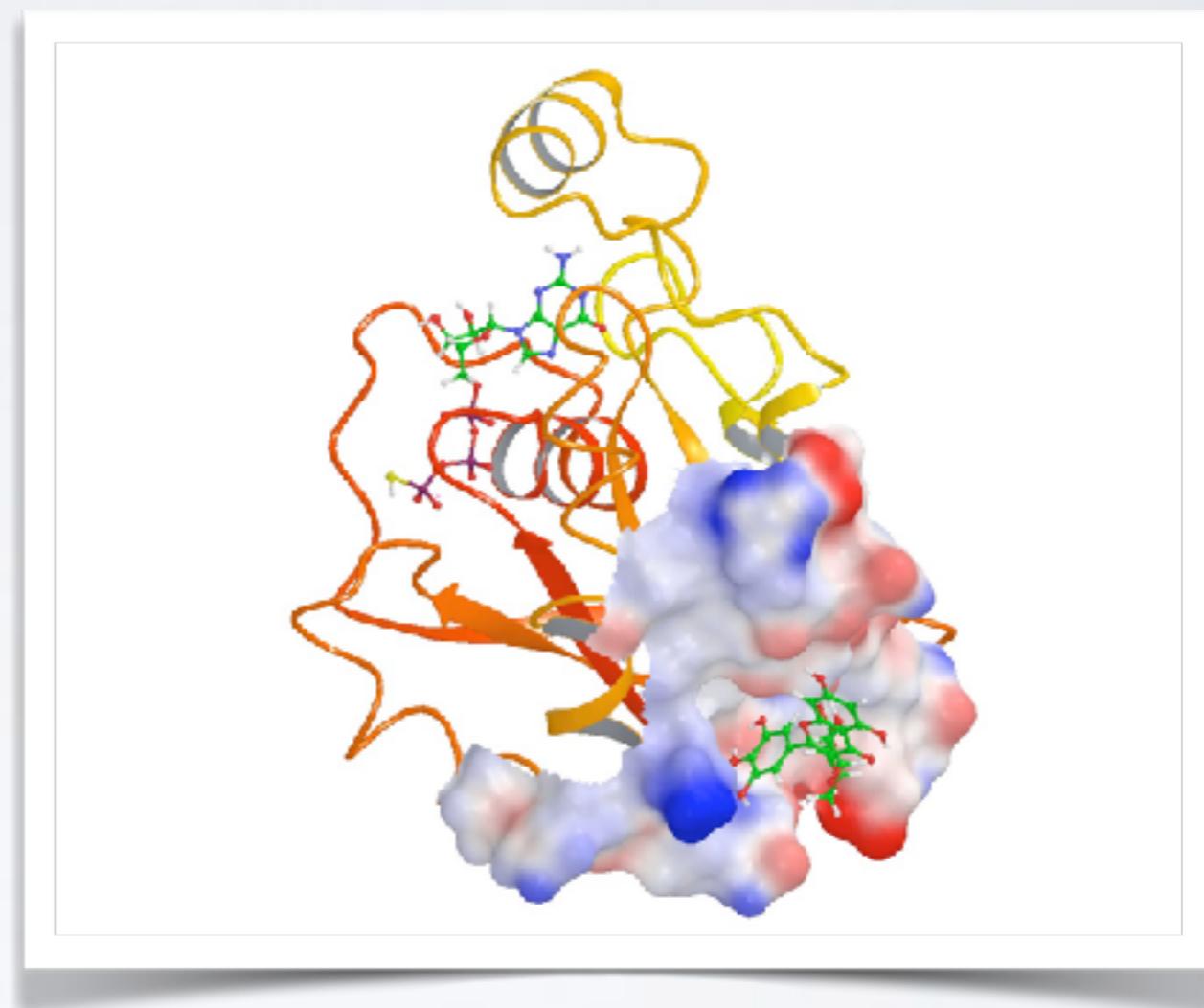
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Grant et al. unpublished

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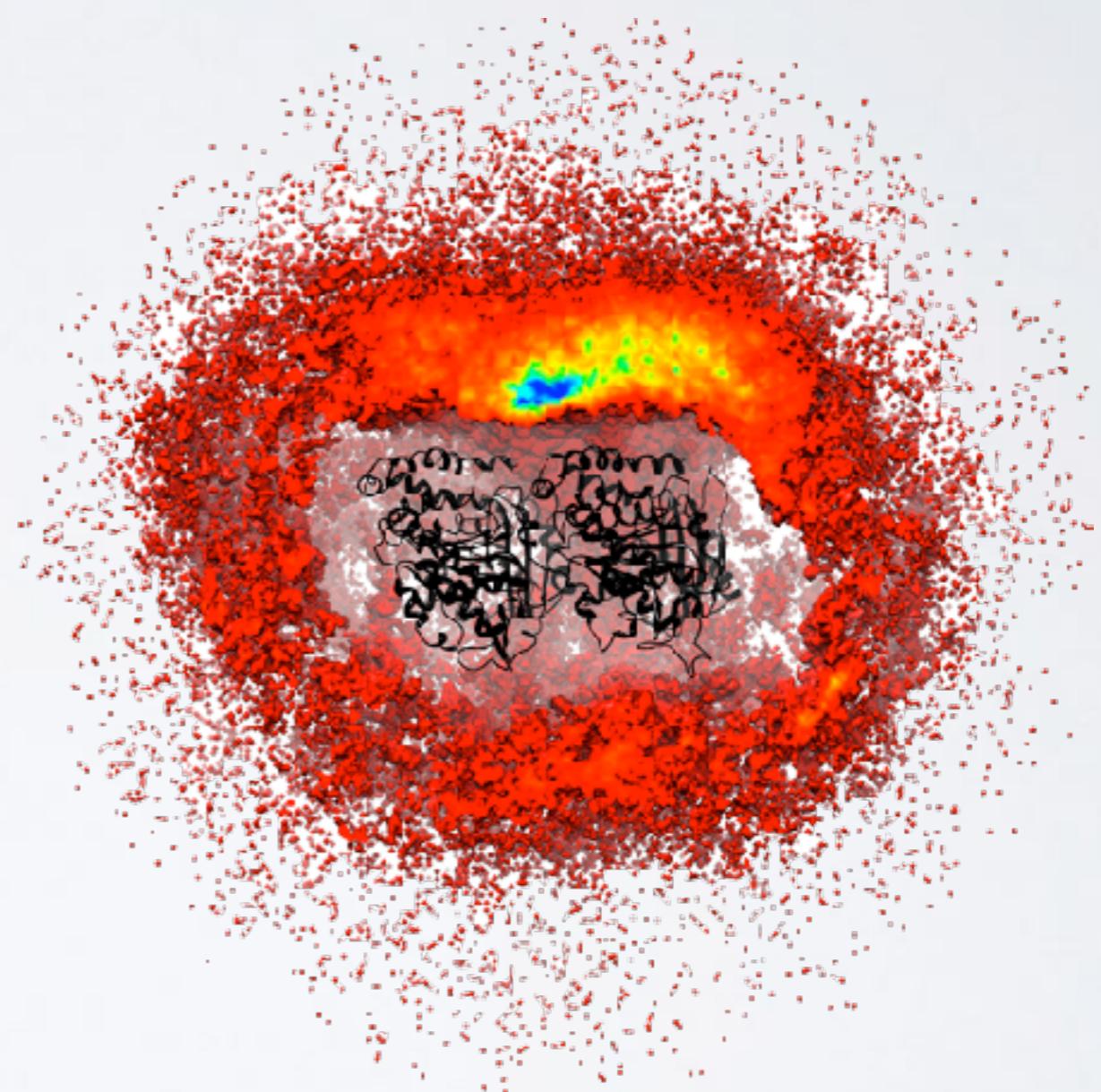
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Grant et al. PLoS One (2011, 2012)

## Goals:

- Analysis
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Grant et al. PLoS Biology (2011)

# MAJOR RESEARCH AREAS AND CHALLENGES

Include but are not limited to:

- Protein classification
- Structure prediction from sequence
- Binding site detection
- Binding prediction and drug design
- Modeling molecular motions
- Predicting physical properties (stability, binding affinities)
- Design of structure and function
- etc...

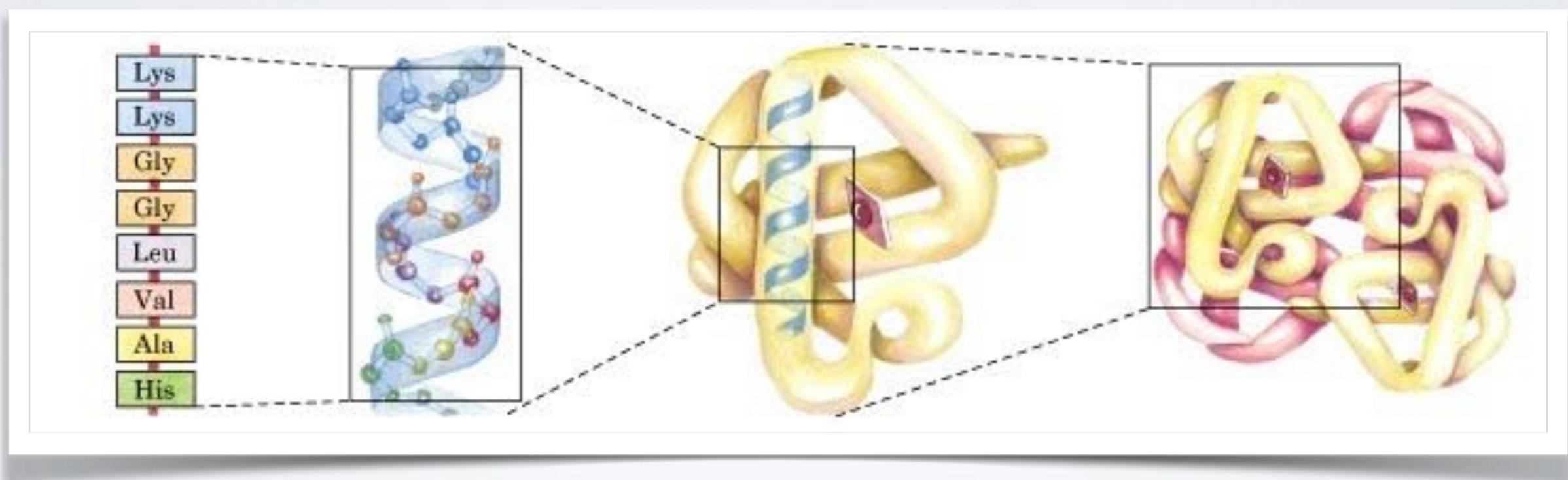
With applications to Biology, Medicine, Agriculture and Industry

# NEXT UP:

- ▶ **Overview of structural bioinformatics**
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# HIERARCHICAL STRUCTURE OF PROTEINS

Primary > Secondary > Tertiary > Quaternary



amino acid  
residues

Alpha  
helix

Polypeptide  
chain

Assembled  
subunits

# RECAP: AMINO ACID NOMENCLATURE

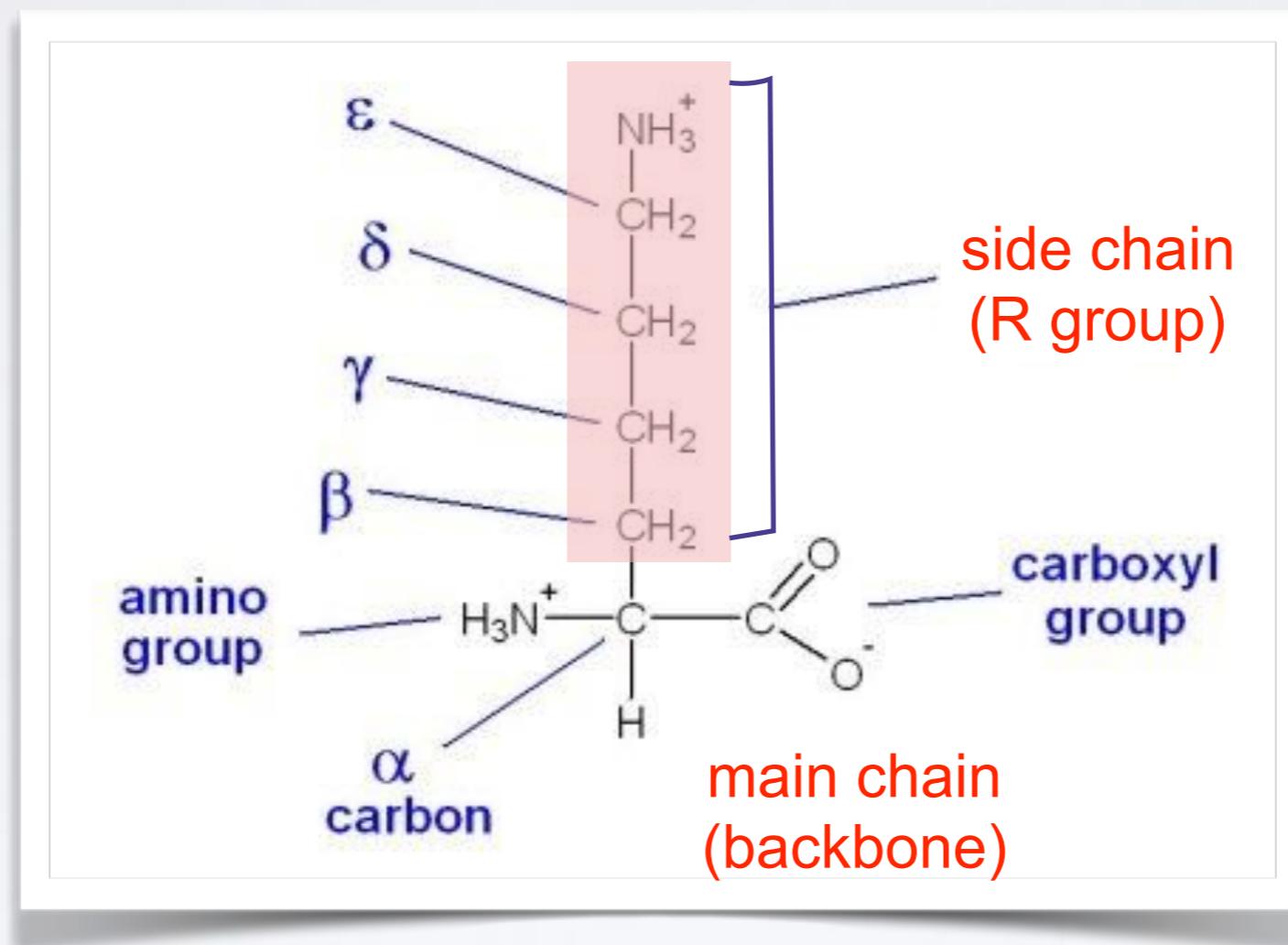
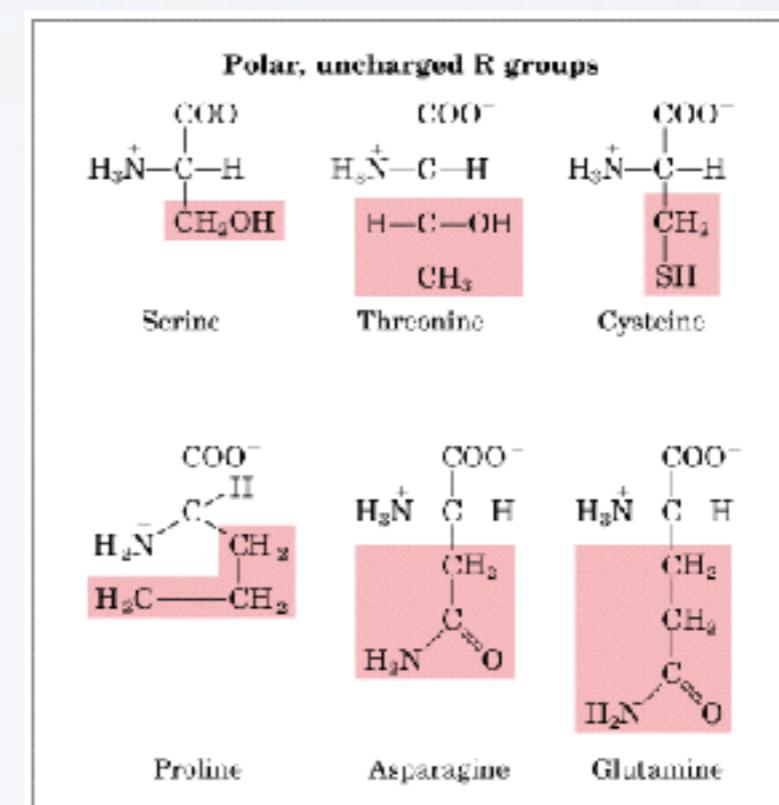
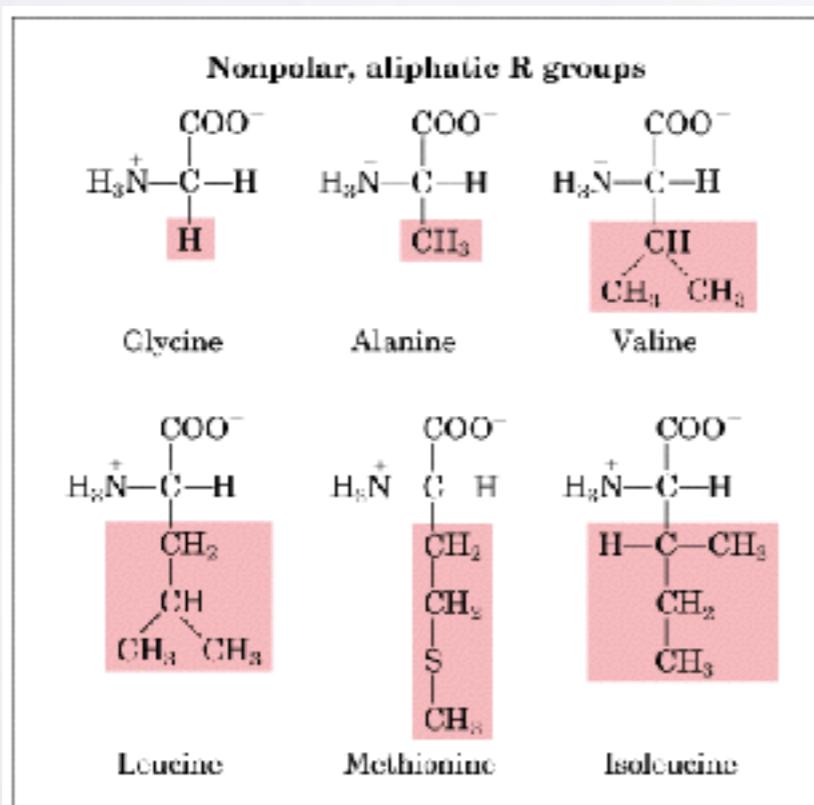
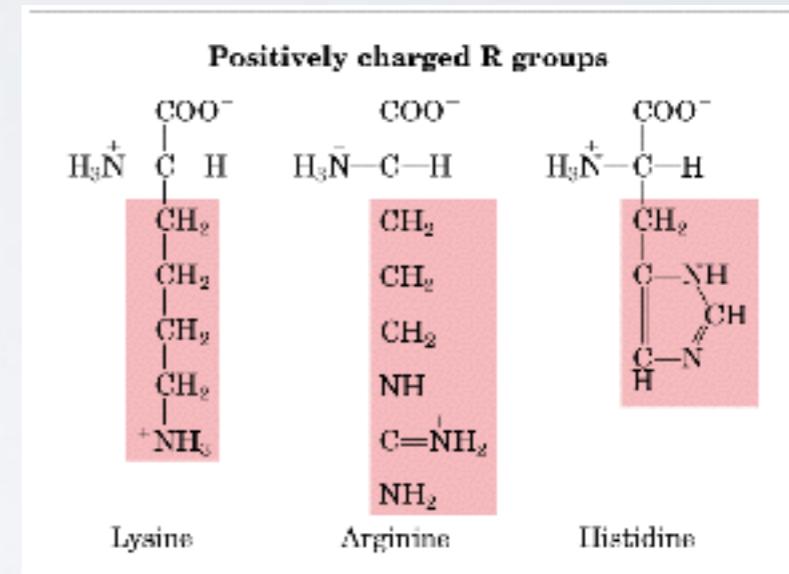
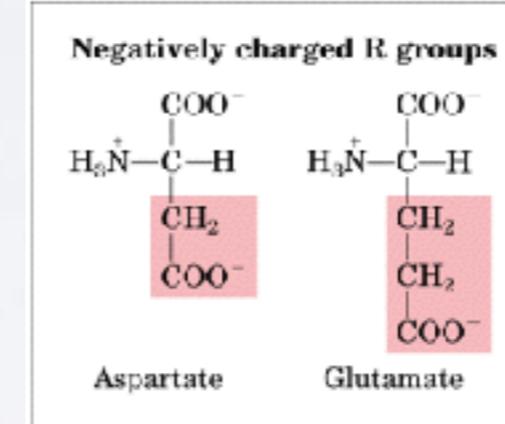
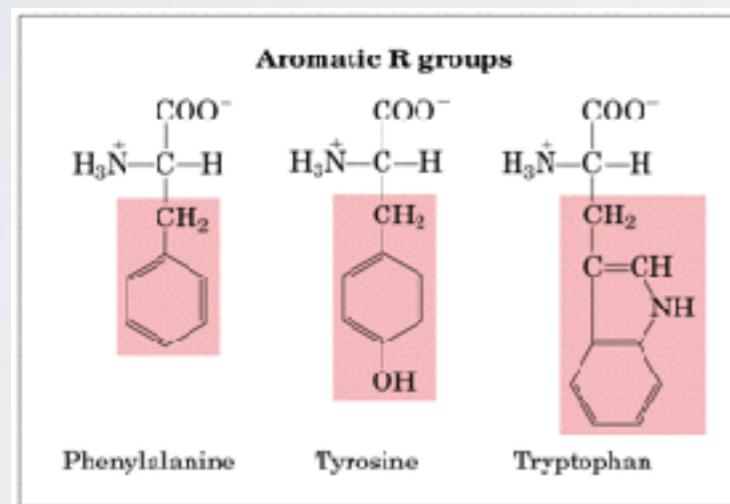
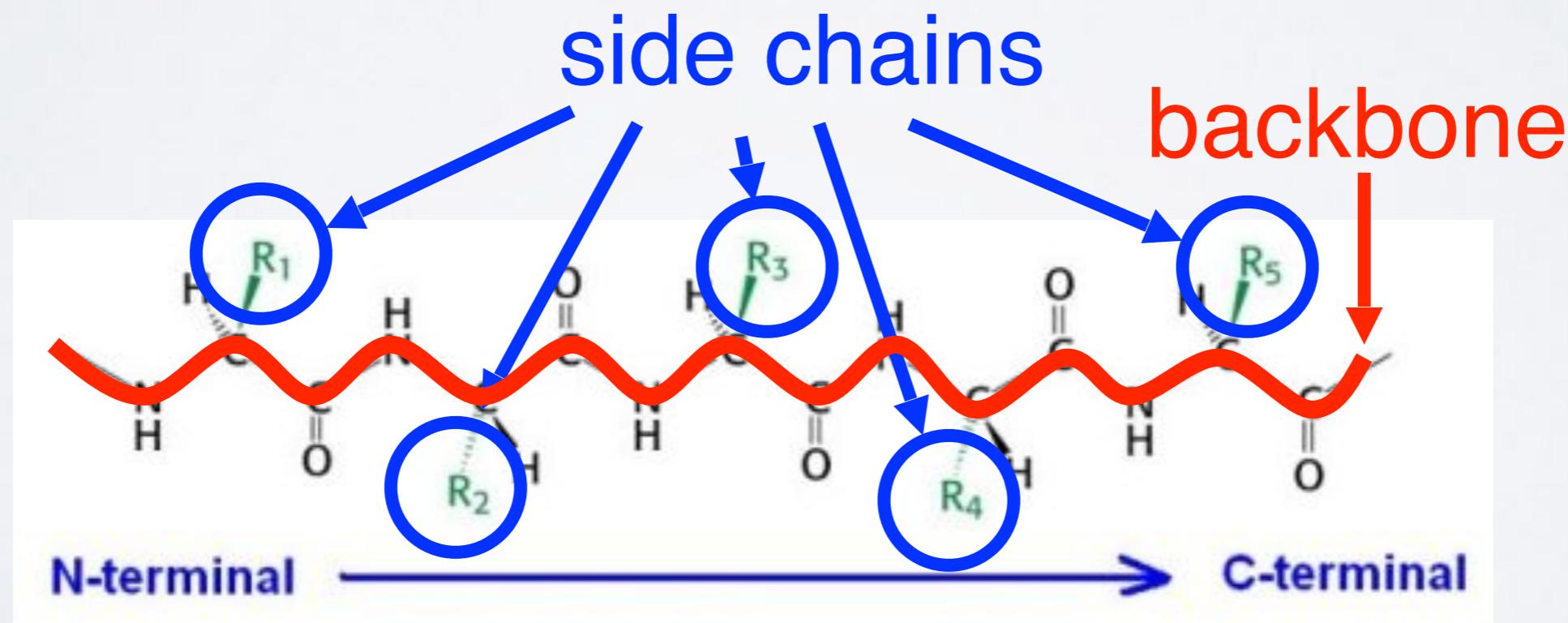
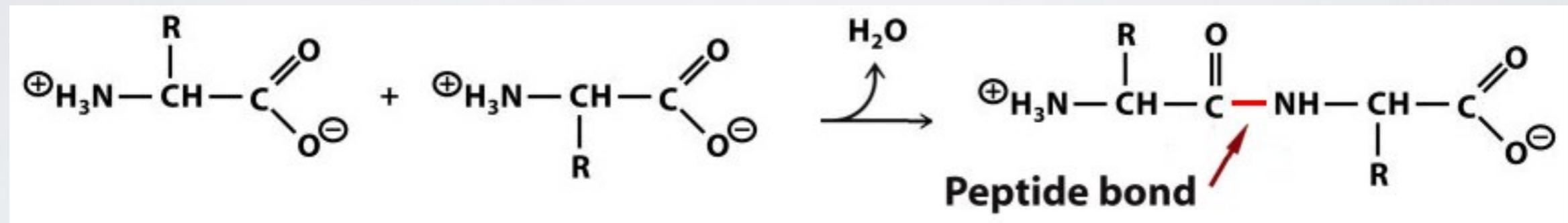


Image from: <http://www.ncbi.nlm.nih.gov/books/NBK21581/>

# AMINO ACIDS CAN BE GROUPED BY THE PHYSIOCHEMICAL PROPERTIES



# AMINO ACIDS POLYMERIZE THROUGH PEPTIDE BOND FORMATION



# PEPTIDES CAN ADOPT DIFFERENT CONFORMATIONS BY VARYING THEIR PHI & PSI BACKBONE TORSIONS

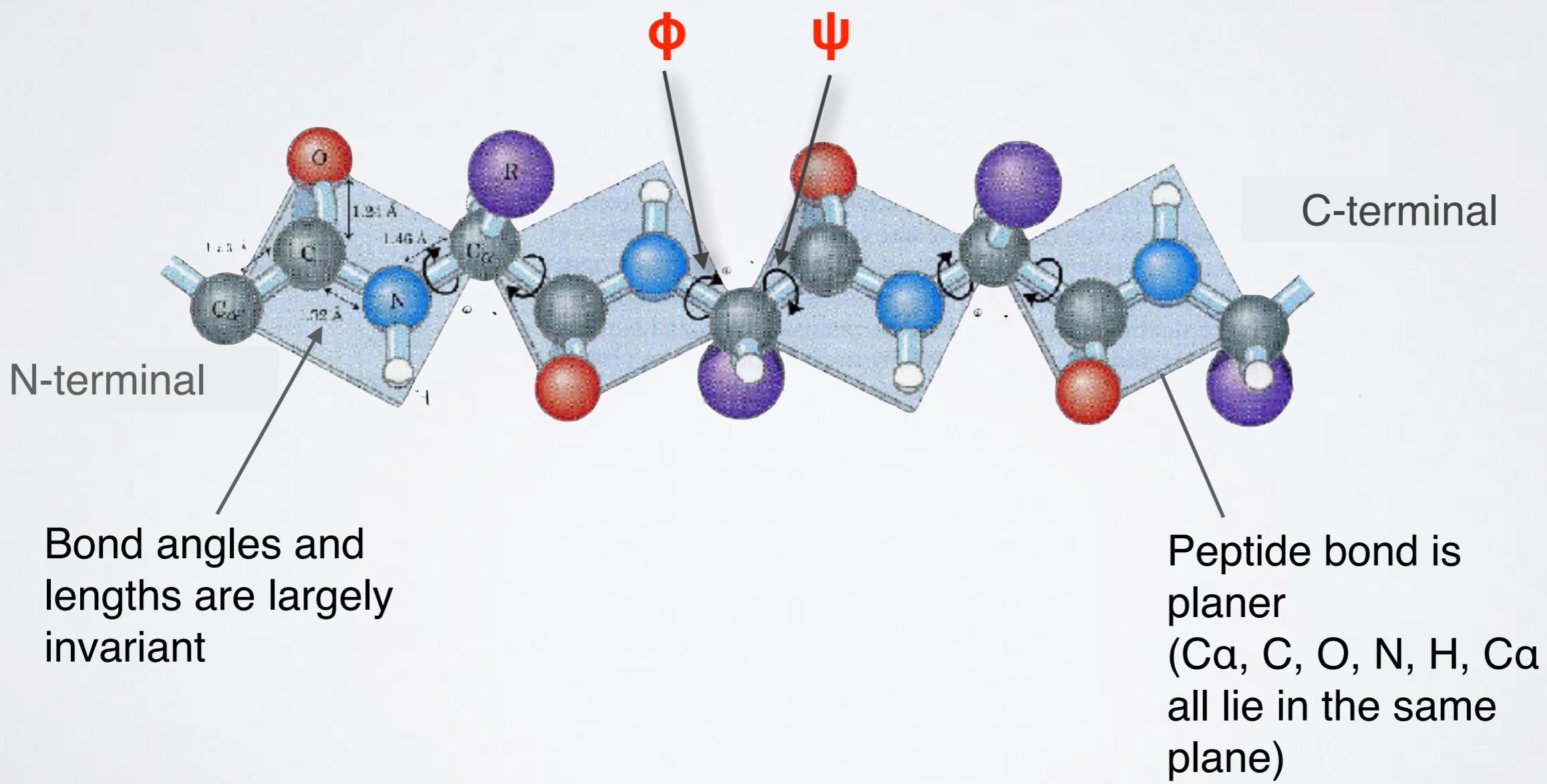
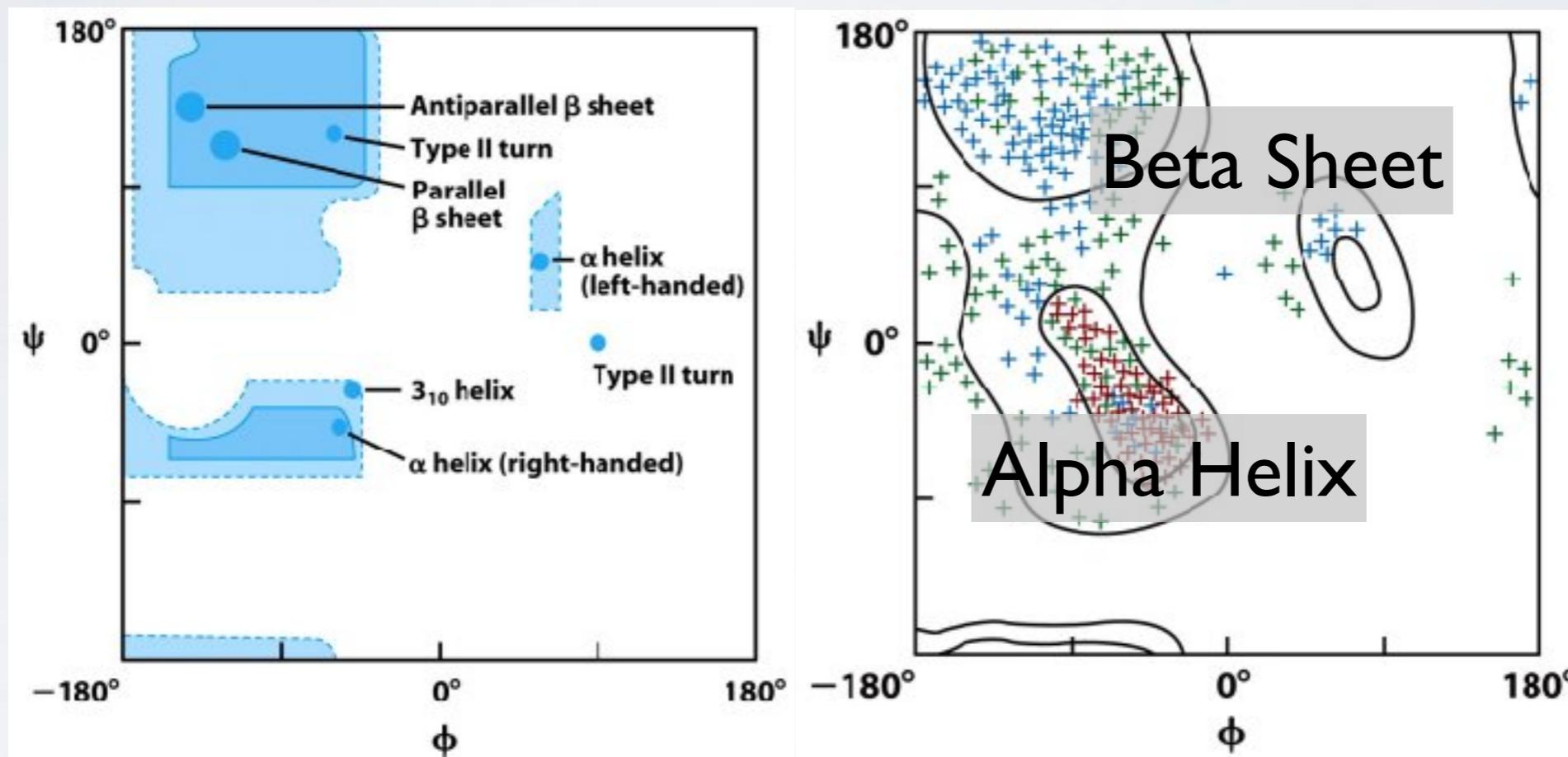


Image from: <http://www.ncbi.nlm.nih.gov/books/NBK21581/>

# PHI vs PSI PLOTS ARE KNOWN AS RAMACHANDRAN DIAGRAMS

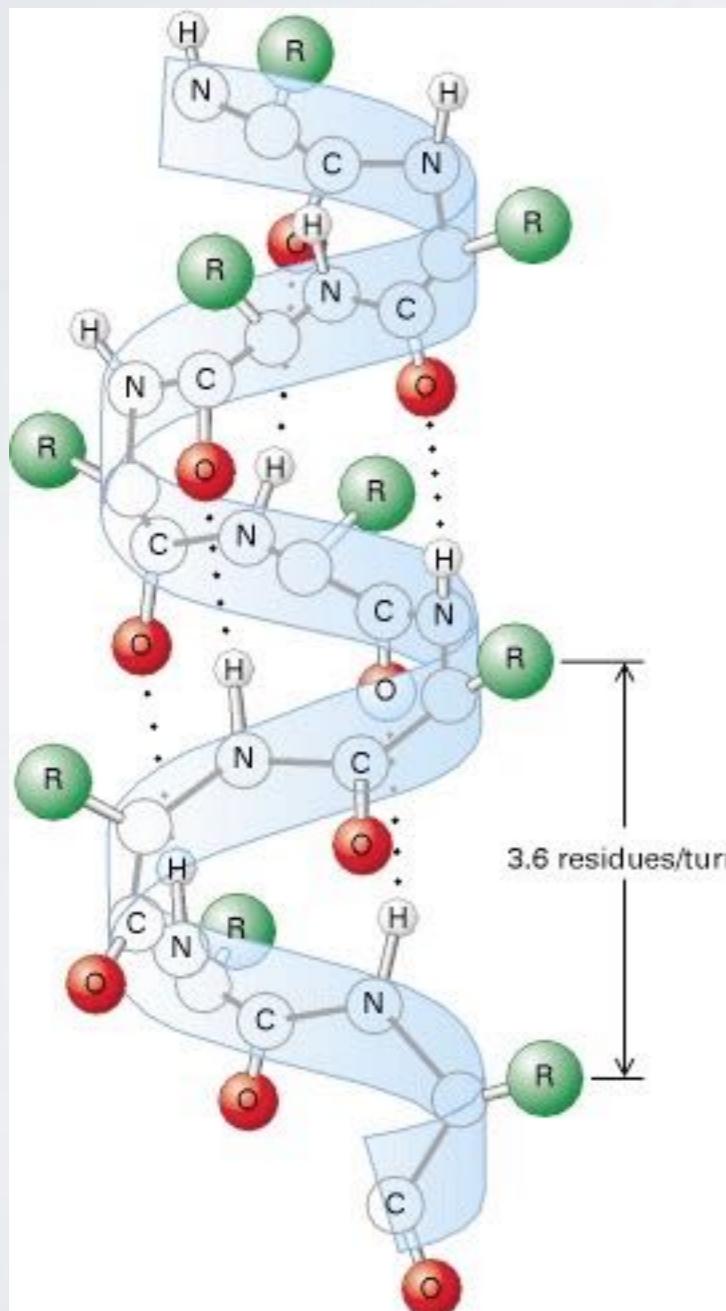


- Steric hindrance dictates torsion angle preference
- Ramachandran plot show preferred regions of  $\phi$  and  $\psi$  dihedral angles which correspond to major forms of **secondary structure**

Image from: <http://www.ncbi.nlm.nih.gov/books/NBK21581/>

# MAJOR SECONDARY STRUCTURE TYPES

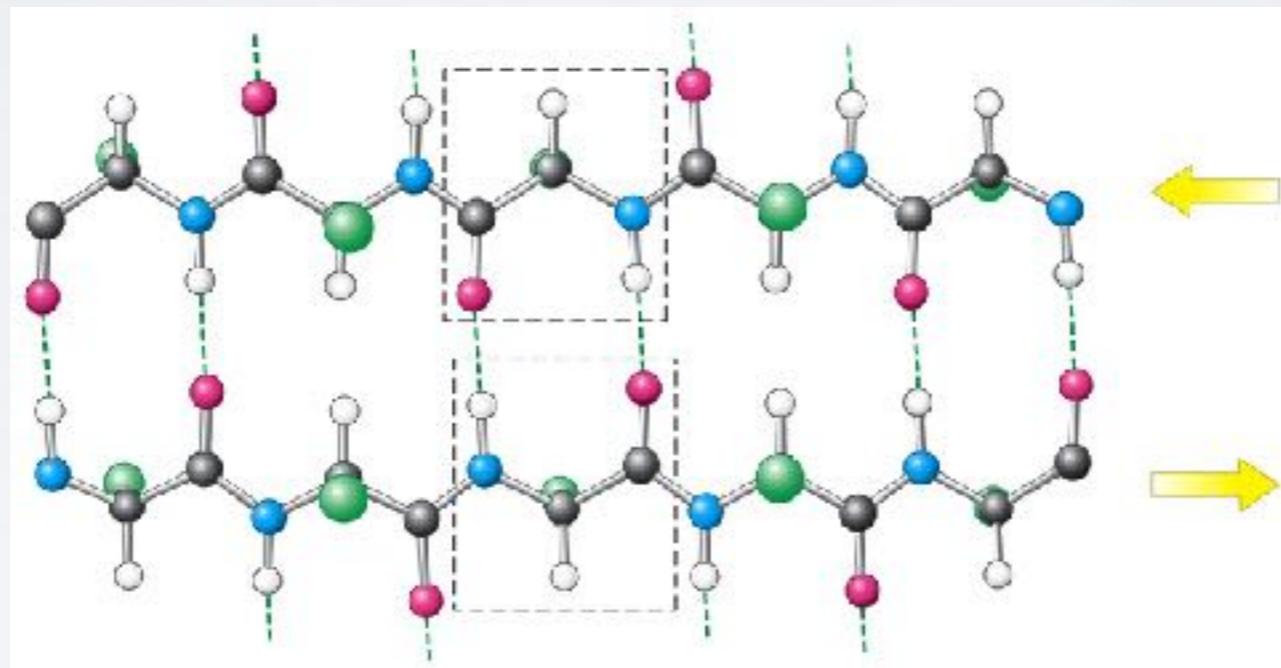
## ALPHA HELIX & BETA SHEET



### **$\alpha$ -helix**

- Most common form has 3.6 residues per turn (number of residues in one full rotation)
- Hydrogen bonds (dashed lines) between residue  $i$  and  $i+4$  stabilize the structure
- The side chains (in green) protrude outward
- $3_{10}$ -helix and  $\pi$ -helix forms are less common

# MAJOR SECONDARY STRUCTURE TYPES ALPHA HELIX & **BETA SHEET**

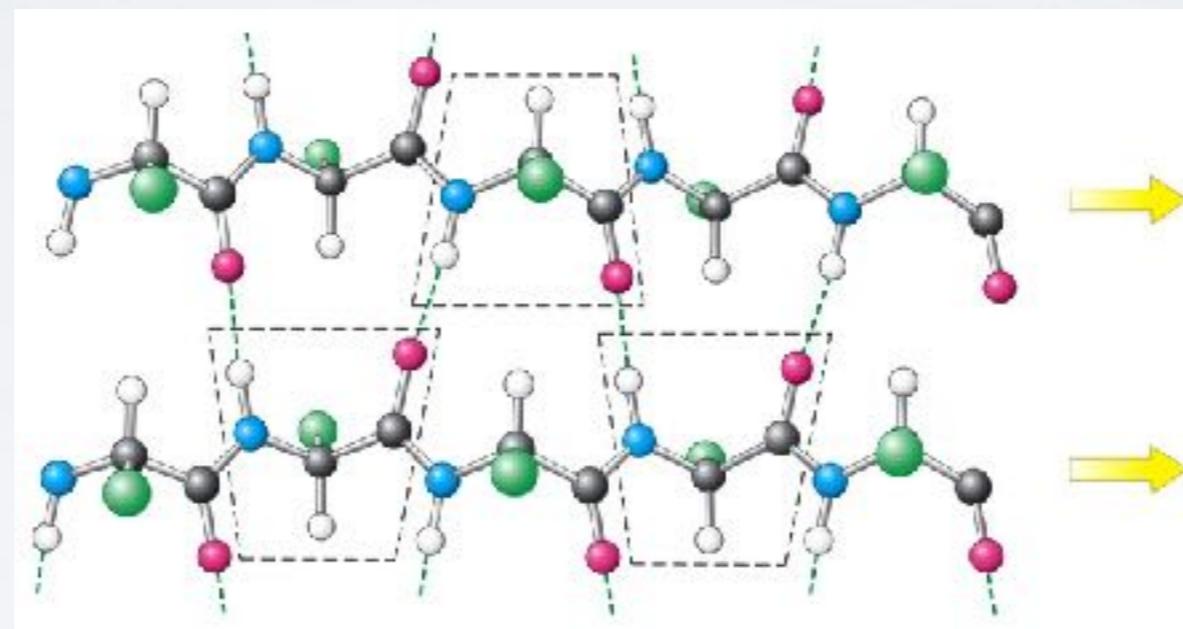


In antiparallel  $\beta$ -sheets

- Adjacent  $\beta$ -strands run in opposite directions
- Hydrogen bonds (dashed lines) between NH and CO stabilize the structure
- The side chains (in green) are above and below the sheet

Image from: <http://www.ncbi.nlm.nih.gov/books/NBK21581/>

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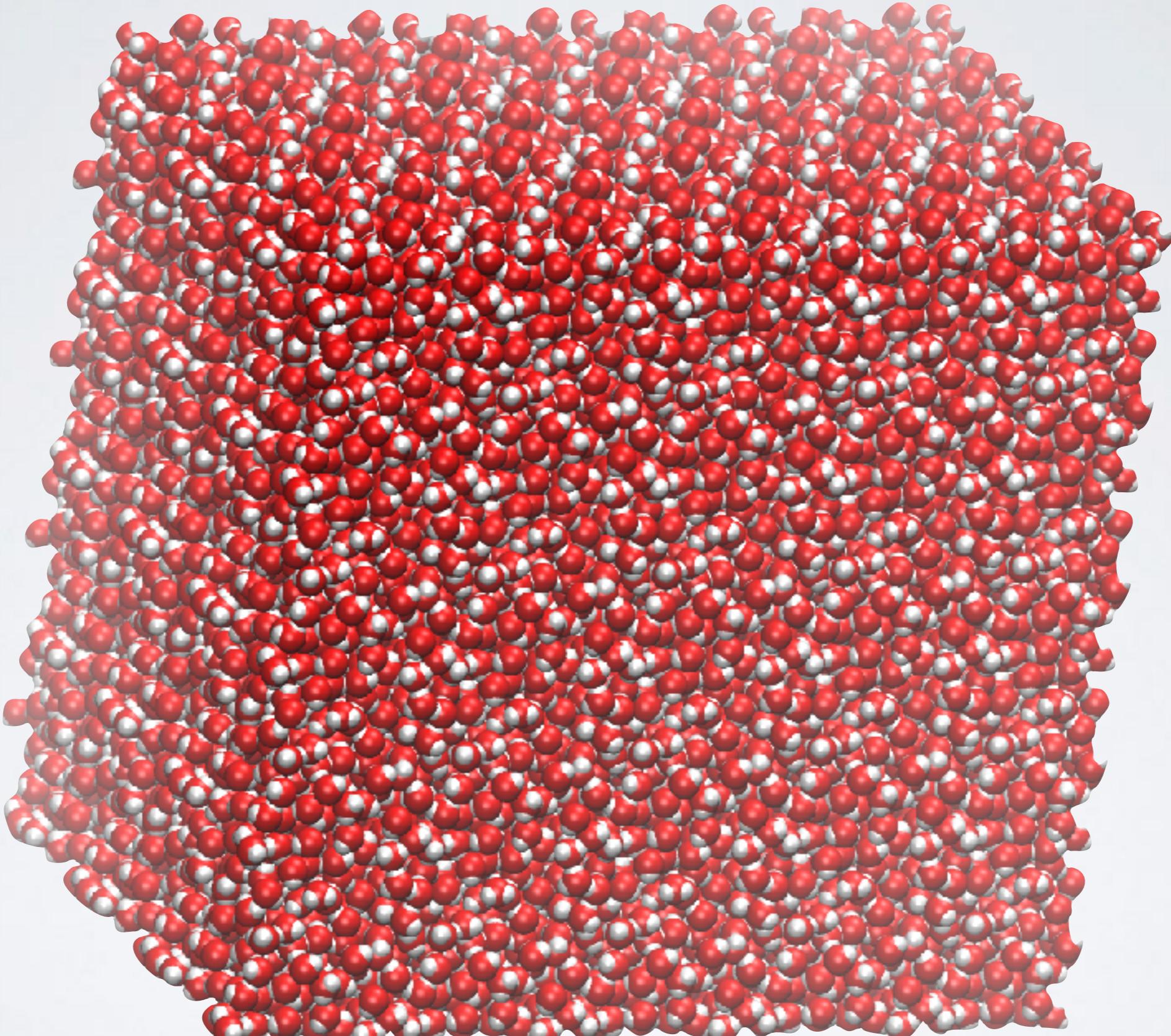


## In parallel $\beta$ -sheets

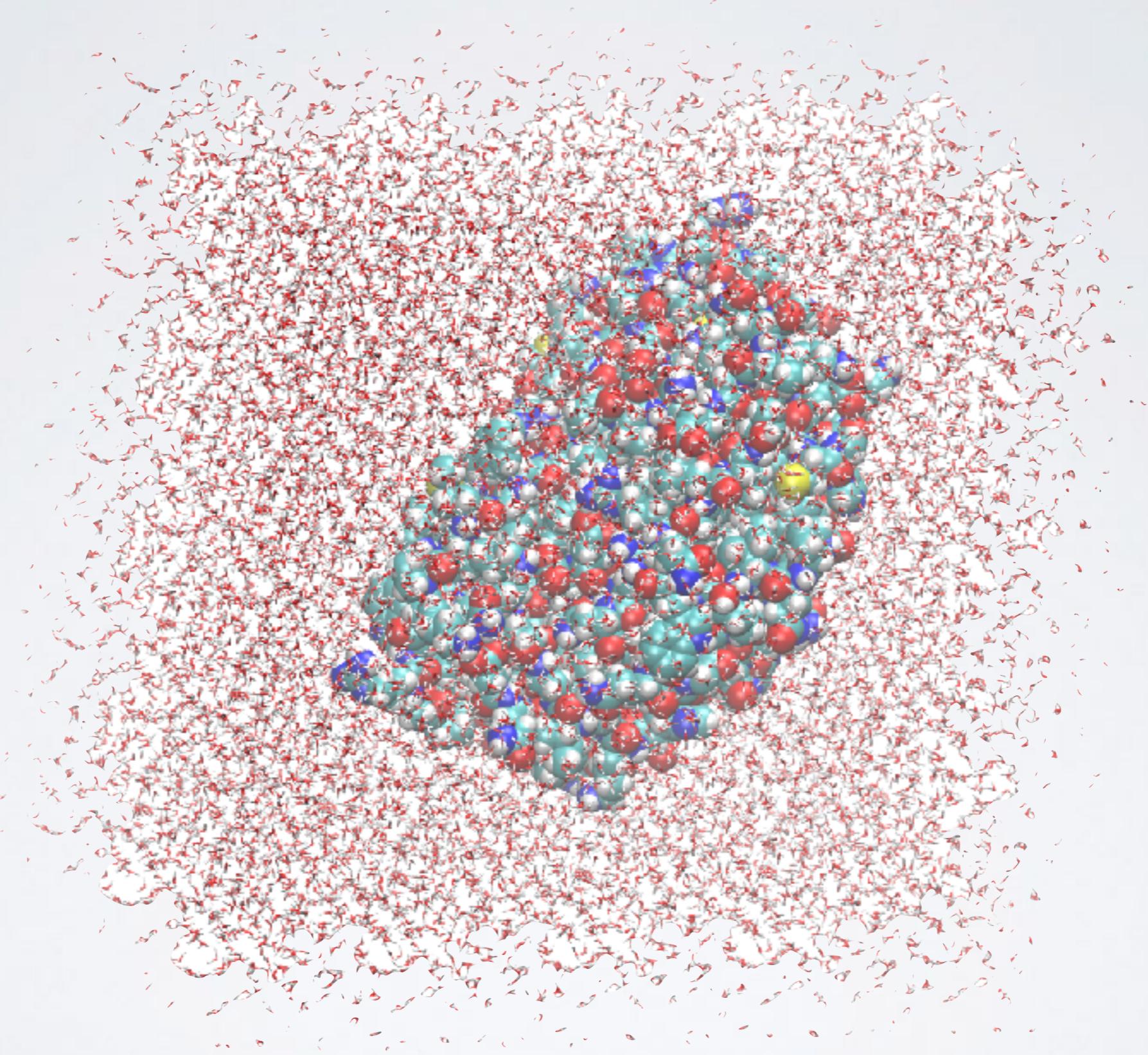
- Adjacent  $\beta$ -strands run in same direction
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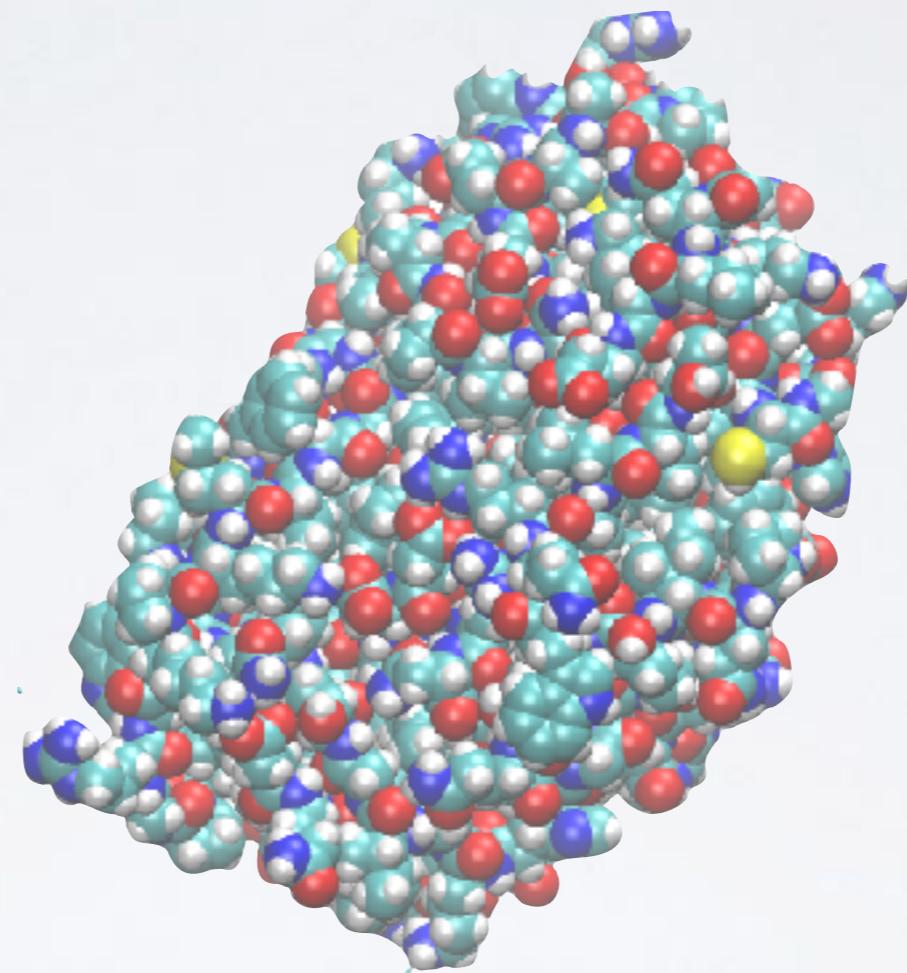
# What Does a Protein Look like?



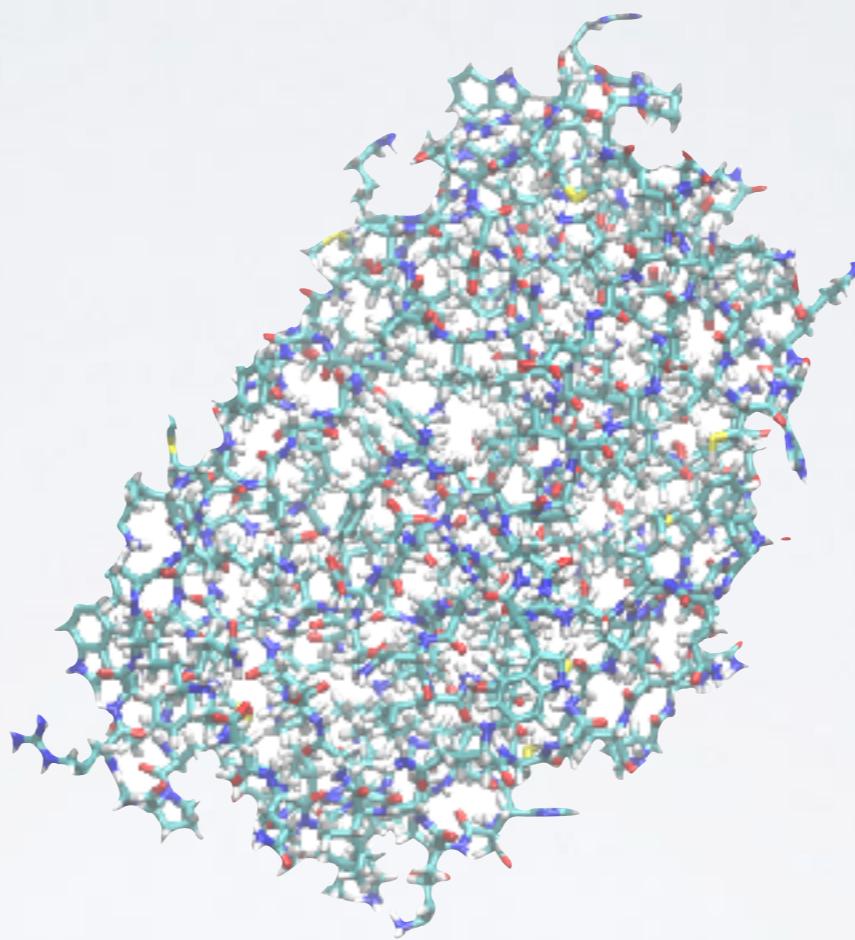
- Proteins are stable (and hidden) in water



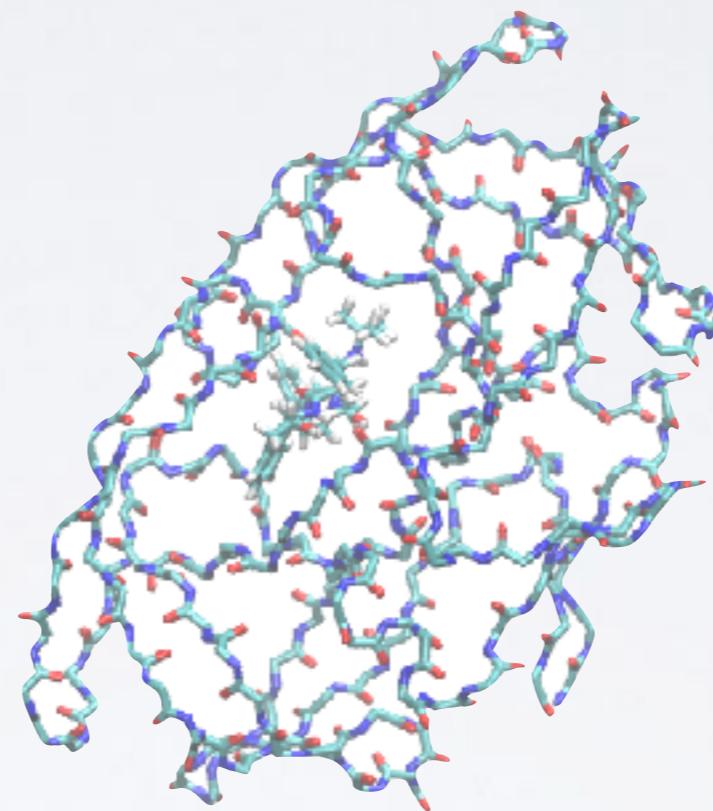
- Proteins closely interact with water



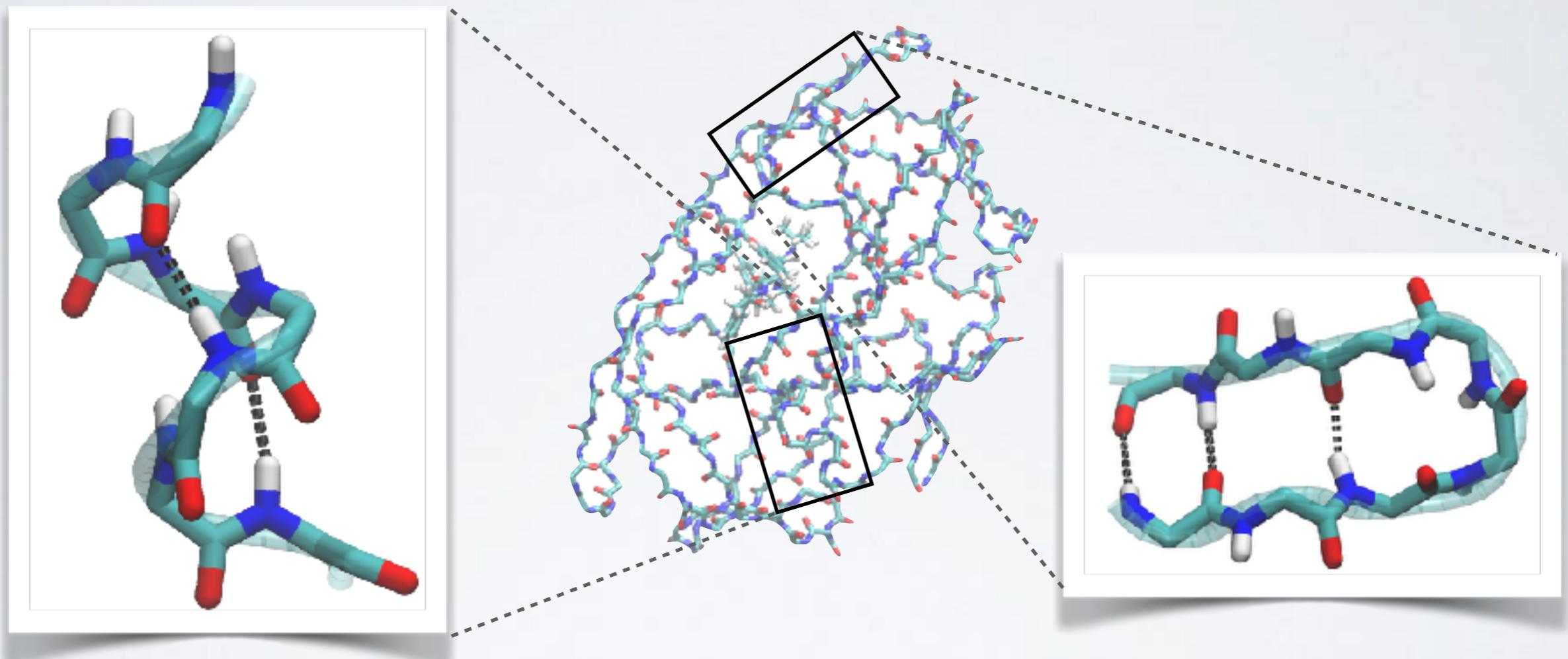
- Proteins are close packed solid but flexible objects (globular)



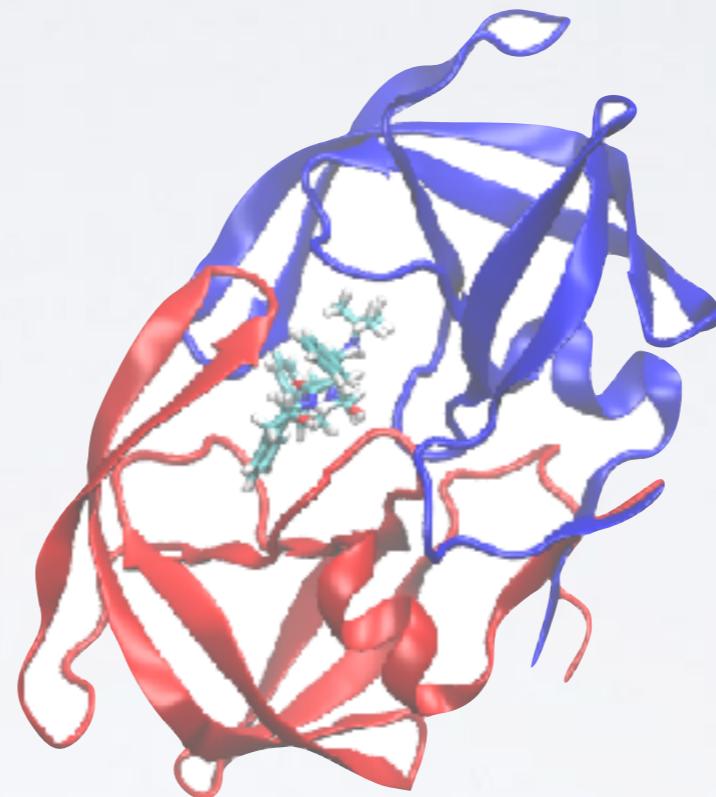
- Due to their large size and complexity it is often hard to see what's important in the structure



- Backbone or main-chain representation can help trace chain topology

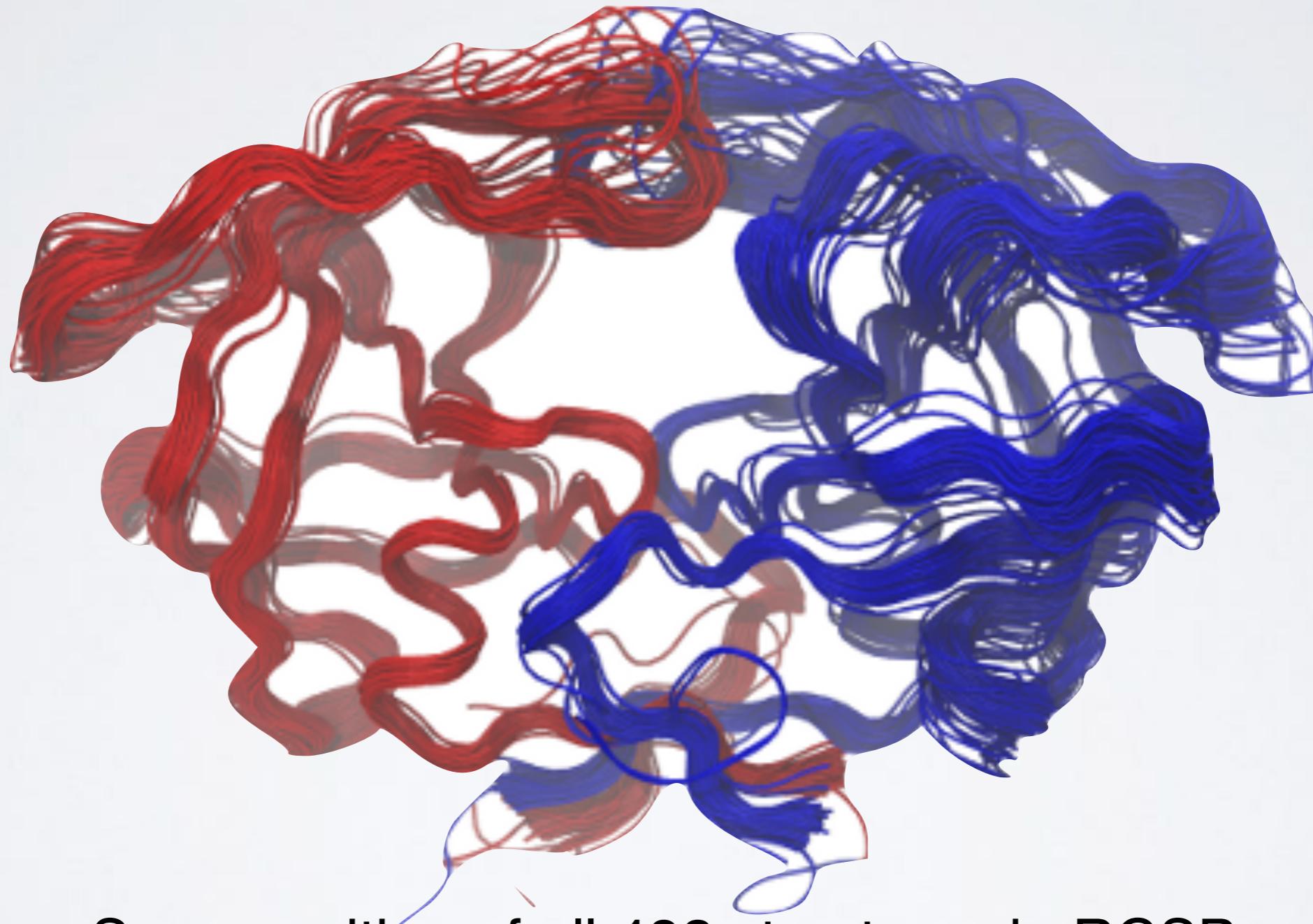


- Backbone or main-chain representation can help trace chain topology & reveal secondary structure



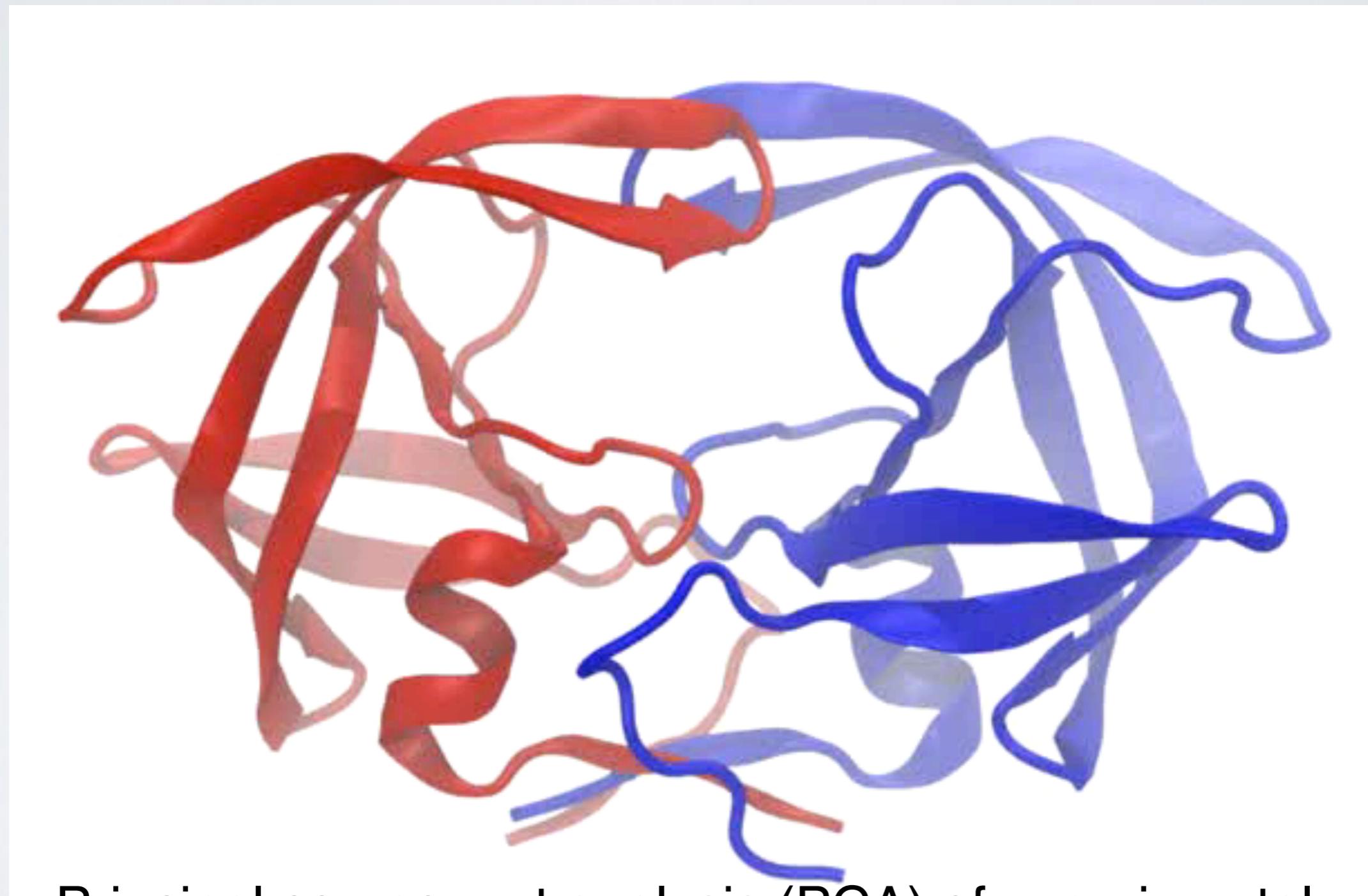
- Simplified secondary structure representations are commonly used to communicate structural details
- Now we can clearly see 2<sup>o</sup>, 3<sup>o</sup> and 4<sup>o</sup> structure
- Coiled chain of connected secondary structures

DISPLACEMENTS REFLECT INTRINSIC FLEXIBILITY



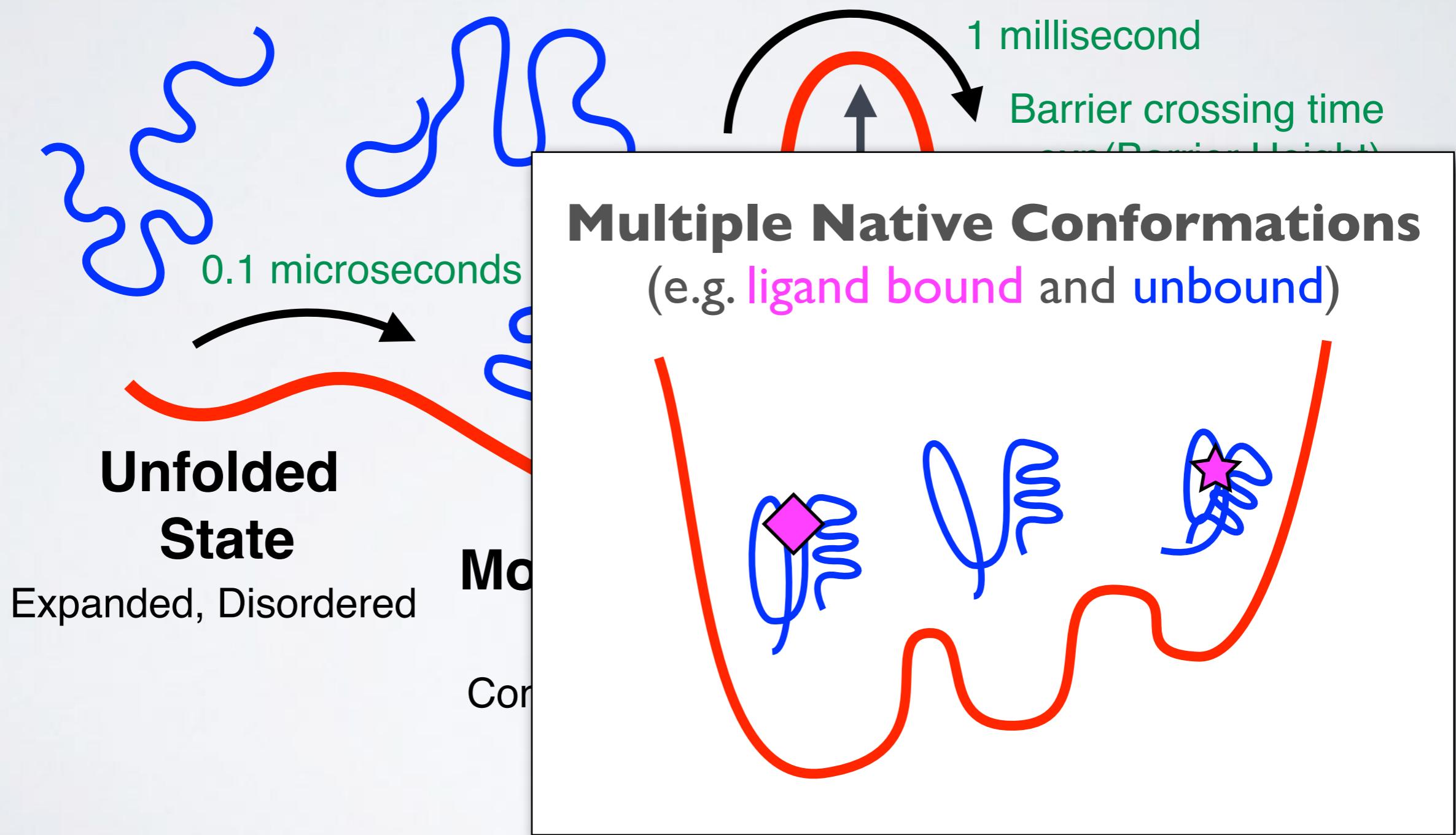
Superposition of all 482 structures in RCSB  
PDB (23/09/2015)

# DISPLACEMENTS REFLECT INTRINSIC FLEXIBILITY



Principal component analysis (PCA) of experimental structures

# KEY CONCEPT: ENERGY LANDSCAPE



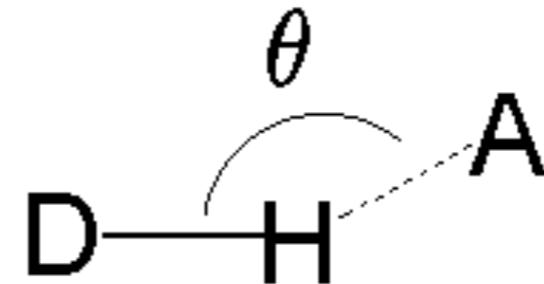
# Key forces affecting structure:

- H-bonding
- Van der Waals
- Electrostatics
- Hydrophobicity

Hydrogen-bond donor      Hydrogen-bond acceptor



← d →

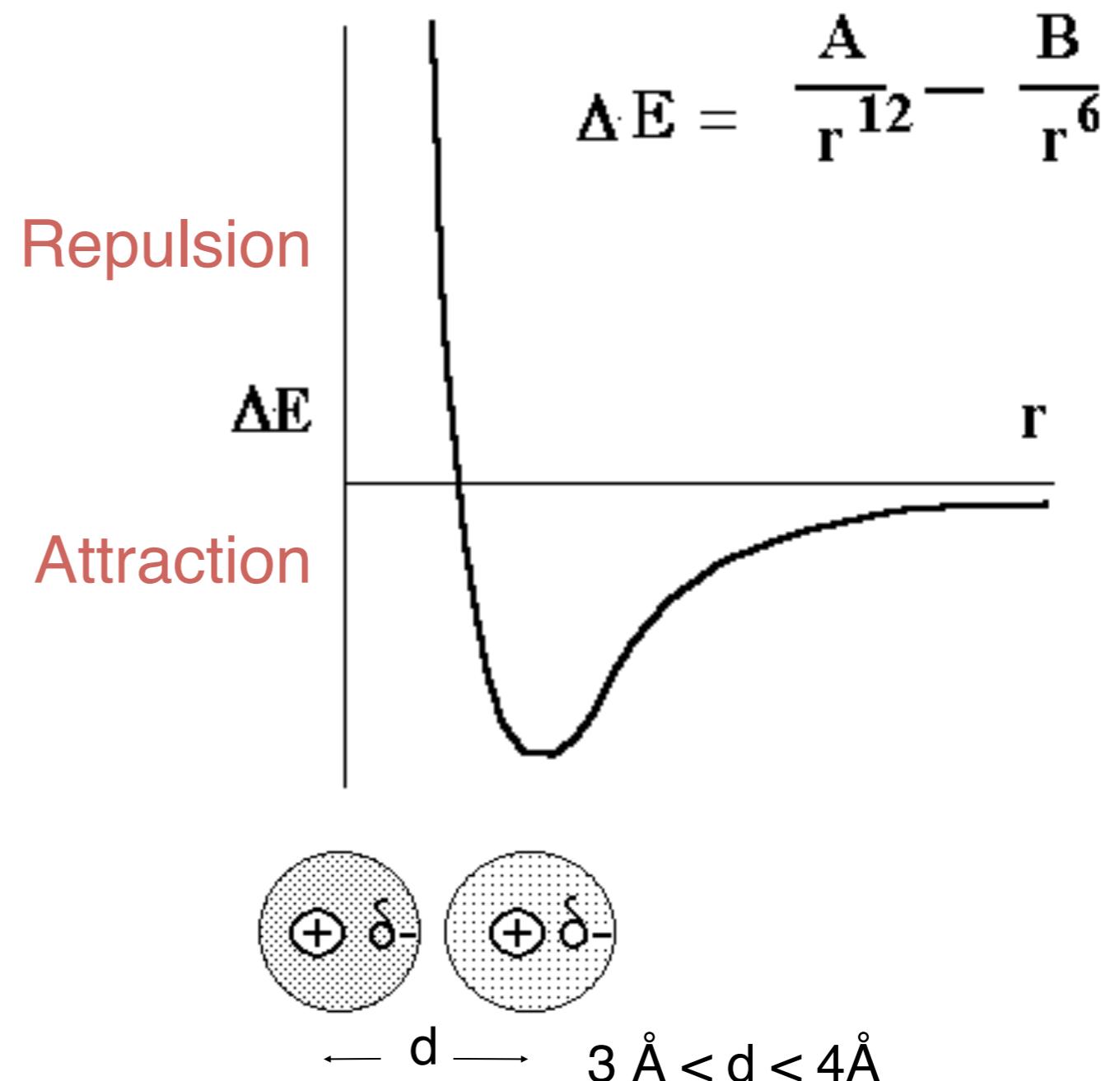


$2.6 \text{ \AA} < d < 3.1 \text{ \AA}$

$150^\circ < \theta < 180^\circ$

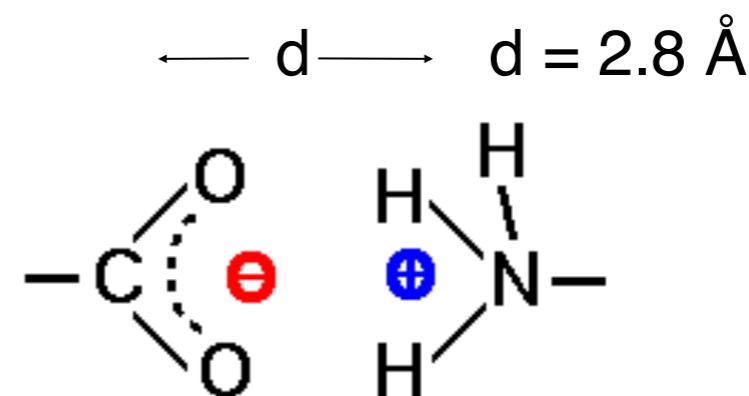
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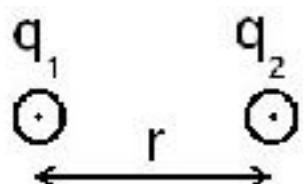
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- Electrostatics
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carboxyl group and amino group

(some time called IONIC BONDs or SALT BRIDGEs)



## Coulomb's law

$$E = \frac{K q_1 q_2}{D r}$$

E = Energy

k = constant

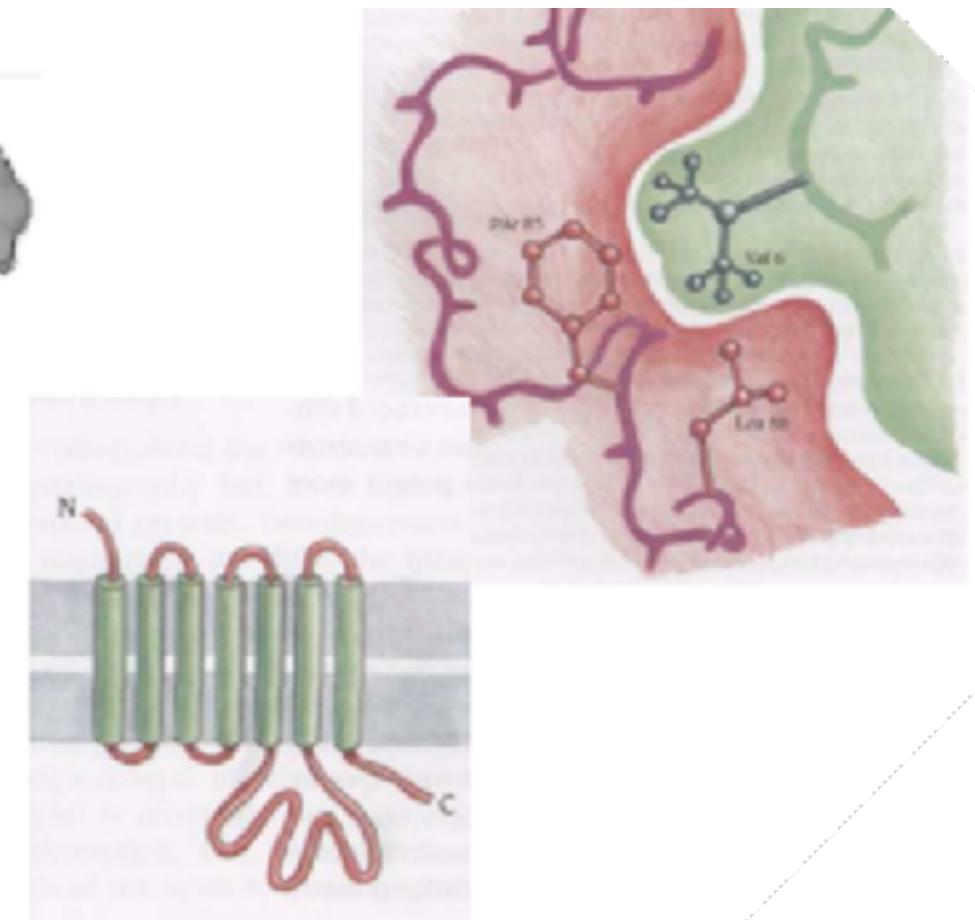
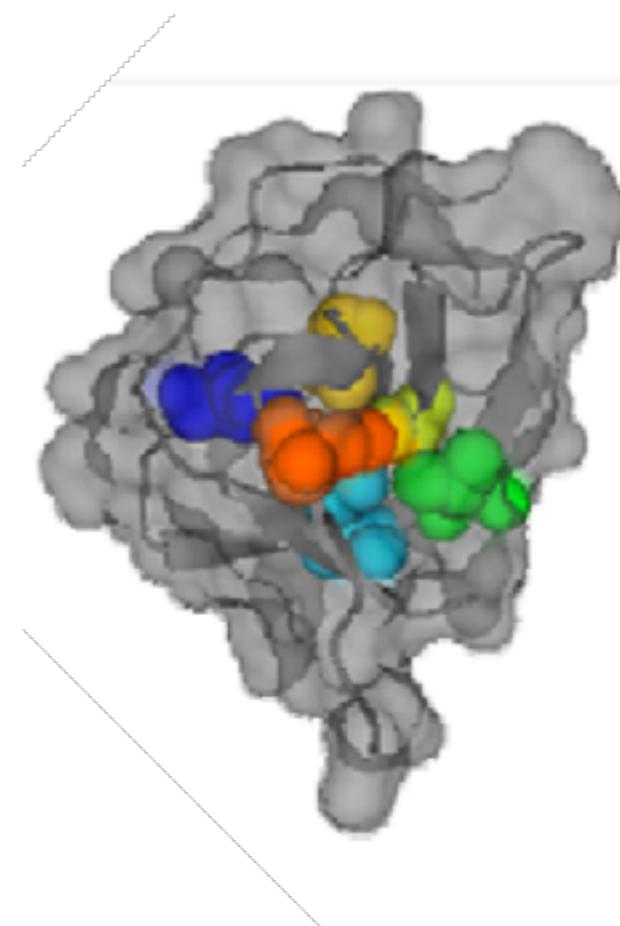
D = Dielectric constant (vacuum = 1; H<sub>2</sub>O = 80)

q<sub>1</sub> & q<sub>2</sub> = electronic charges (Coulombs)

r = distance (Å)

# Key forces affecting structure:

- H-bonding
- Van der Waals
- Electrostatics
- Hydrophobicity



The force that causes hydrophobic molecules or nonpolar portions of molecules to aggregate together rather than to dissolve in water is called Hydrophobicity (*Greek, “water fearing”*). This is not a separate bonding force; rather, it is the result of the energy required to insert a nonpolar molecule into water.

Do it Yourself!

# Hand-on time!

[https://bioboot.github.io/bimm143\\_S18/lectures/#11](https://bioboot.github.io/bimm143_S18/lectures/#11)

Focus on **section 1 to 3** only please!

# SIDE-NOTE: PDB FILE FORMAT

				Chain name			
				Sequence Number			
				-----Coordinates-----			
		Amino Acid	Element	X	Y	Z	(etc.)
ATOM	1	N	ASP L	1	4.060	7.307	5.186
ATOM	2	CA	ASP L	1	4.042	7.776	6.553
ATOM	3	C	ASP L	1	2.668	8.426	6.644
ATOM	4	O	ASP L	1	1.987	8.438	5.606
ATOM	5	CB	ASP L	1	5.090	8.827	6.797
ATOM	6	CG	ASP L	1	6.338	8.761	5.929
ATOM	7	OD1	ASP L	1	6.576	9.758	5.241
ATOM	8	OD2	ASP L	1	7.065	7.759	5.948

\\  
Element position within amino acid

- **PDB files** contains atomic coordinates and associated information.

# SIDE-NOTE: PDB FILE FORMAT

Amino Acid  
Element  
Chain  
Seq

ATOM	1	N	ASP	L	1
ATOM	2	CA	ASP	L	1
ATOM	3	C	ASP	L	1
ATOM	4	O	ASP	L	1
ATOM	5	CB	ASP	L	1
ATOM	6	CG	ASP	L	1
ATOM	7	OD1	ASP	L	1
ATOM	8	OD2	ASP	L	1

\\  
Element position within amino acid

Diagram illustrating the structure of an alpha-amino acid. The structure shows the alpha-carbon (C-alpha) bonded to an amino group ( $\text{H}_3\text{N}^+$ ), a side chain (R-group), and a carboxyl group ( $\text{C}(=\text{O})\text{O}^-$ ). The side chain is highlighted in pink and labeled with Greek letters  $\epsilon$ ,  $\delta$ ,  $\gamma$ ,  $\beta$ , and  $\alpha$  from the amino group end to the carboxyl group end.

- **PDB files** contains atomic coordinates and associated information.

# NEXT UP:

- ▶ **Overview of structural bioinformatics**
  - Major motivations, goals and challenges
- ▶ **Fundamentals of protein structure**
  - Composition and dynamics
- ▶ **Representing protein structure**
  - Modeling energy as a function of structure
- ▶ **Example application areas**
  - Predicting functional dynamics & drug discovery

Change from here on!!!

Just do docking???

**KEY CONCEPT:** POTENTIAL FUNCTIONS  
DESCRIBE A SYSTEMS **ENERGY** AS A FUNCTION  
OF ITS **STRUCTURE**

Two main approaches:

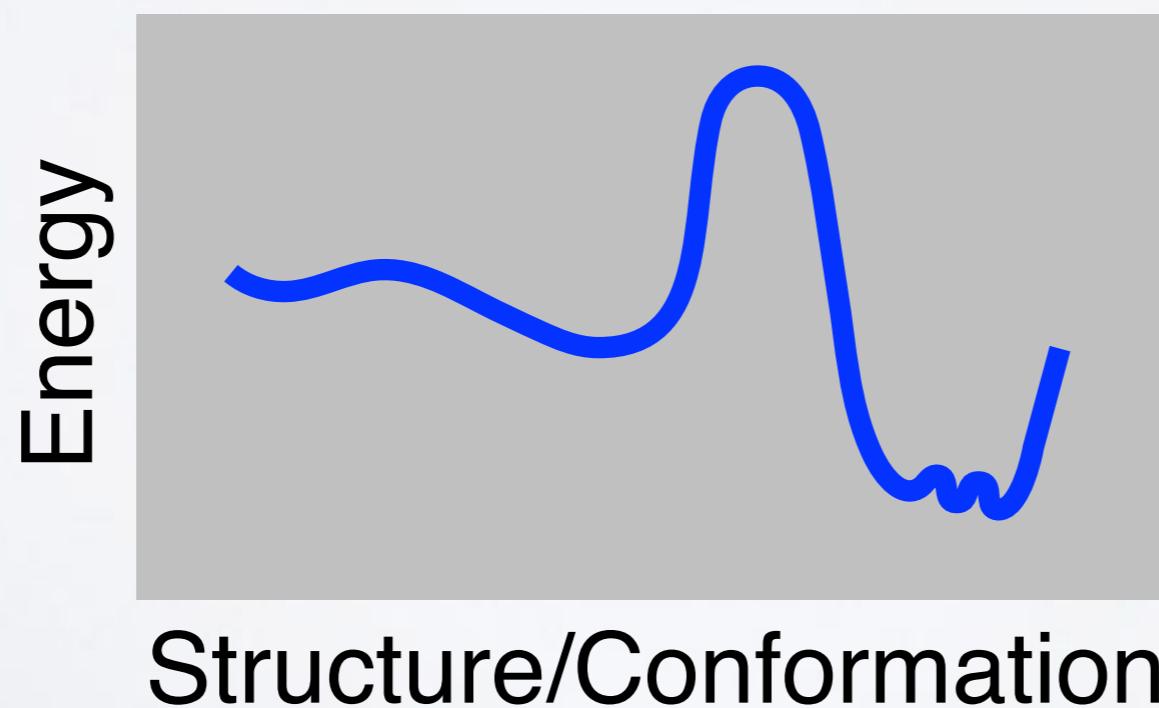
- (1). Physics-Based
- (2). Knowledge-Based

# **KEY CONCEPT: POTENTIAL FUNCTIONS**

DESCRIBE A SYSTEMS **ENERGY** AS A FUNCTION  
OF ITS **STRUCTURE**

Two main approaches:

- (1). Physics-Based
- (2). Knowledge-Based

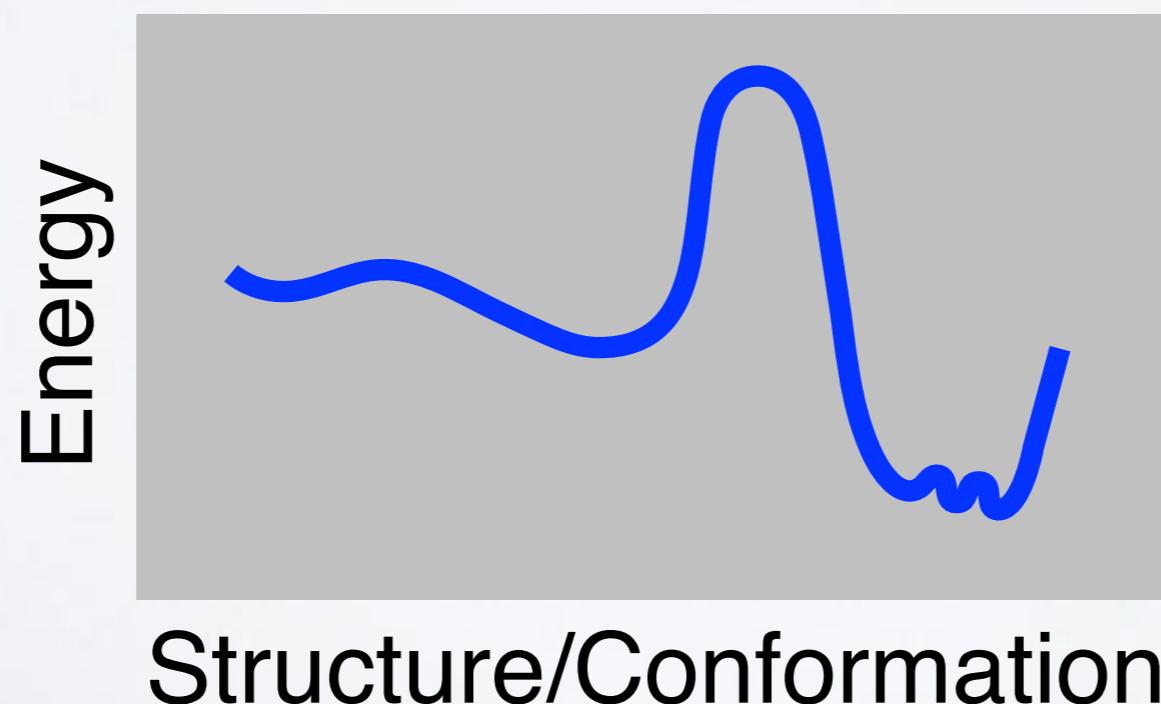


# **KEY CONCEPT:** POTENTIAL FUNCTIONS DESCRIBE A SYSTEMS **ENERGY** AS A FUNCTION OF ITS **STRUCTURE**

Two main approaches:

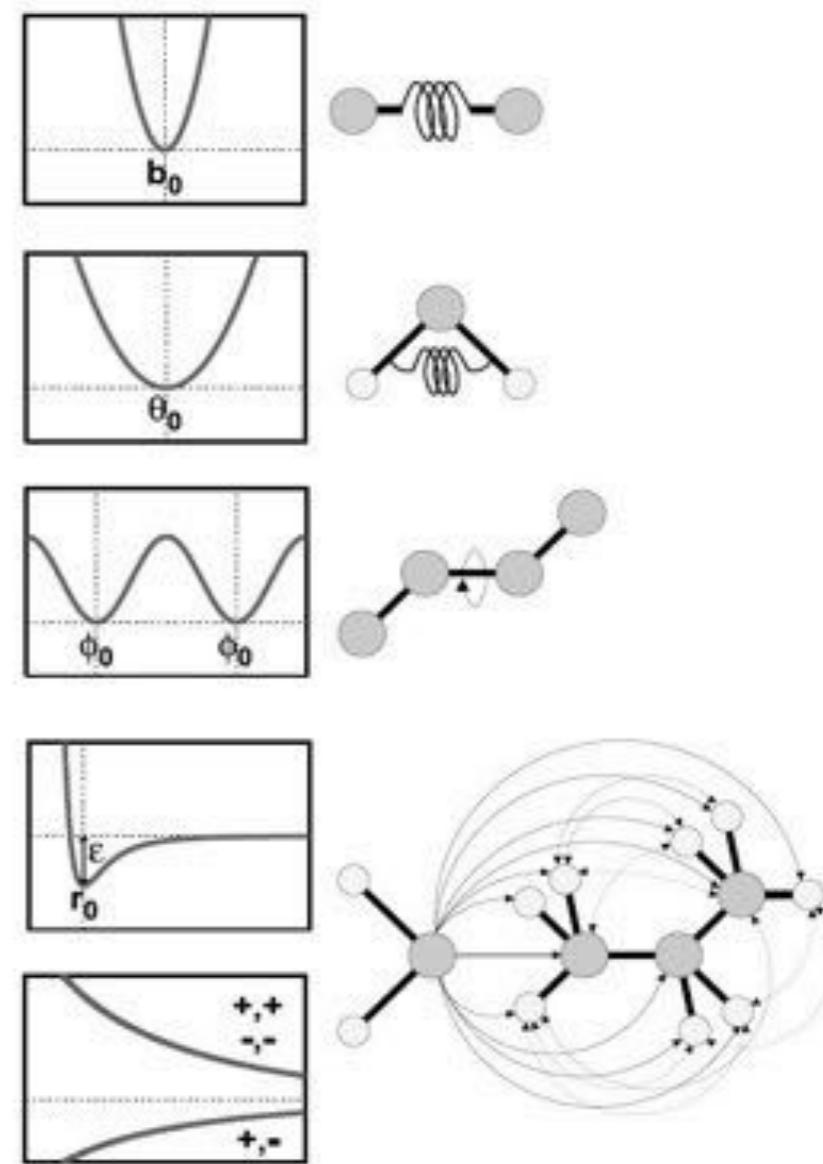
(1). **Physics-Based**

(2). **Knowledge-Based**



# **PHYSICS-BASED POTENTIALS ENERGY TERMS FROM PHYSICAL THEORY**

$$U(\vec{R}) = \underbrace{\sum_{bonds} k_i^{bond} (r_i - r_0)^2}_{U_{bond}} + \underbrace{\sum_{angles} k_i^{angle} (\theta_i - \theta_0)^2}_{U_{angle}} + \\ \underbrace{\sum_{dihedrals} k_i^{dihed} [1 + \cos(n_i \phi_i + \delta_i)]}_{U_{dihedral}} + \\ \underbrace{\sum_i \sum_{j \neq i} 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \sum_i \sum_{j \neq i} \frac{q_i q_j}{\epsilon r_{ij}}}_{U_{nonbond}}$$



$U_{bond}$  = oscillations about the equilibrium bond length

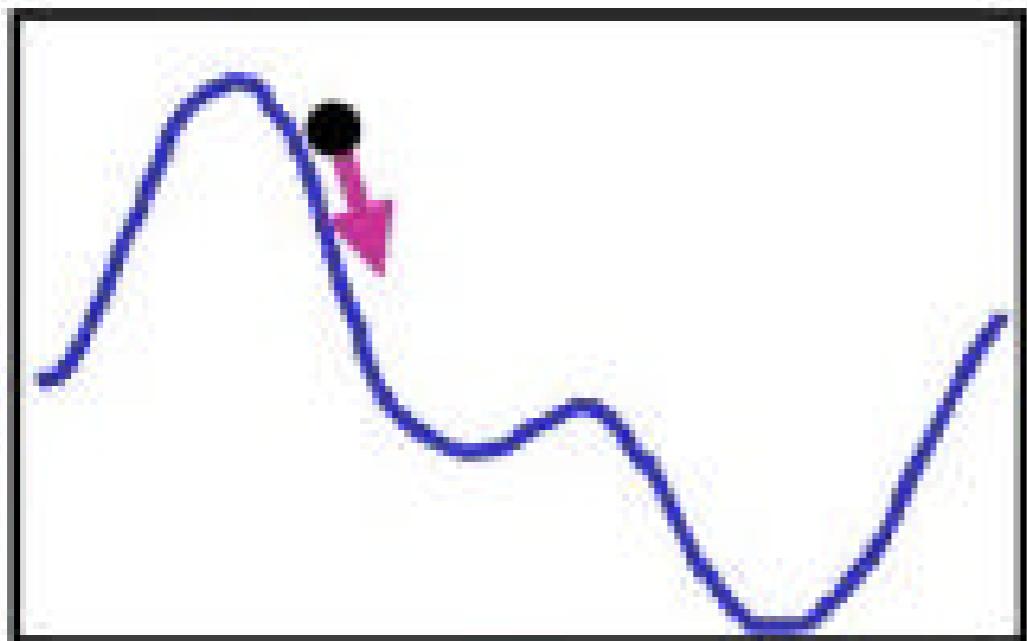
$U_{angle}$  = oscillations of 3 atoms about an equilibrium bond angle

$U_{dihedral}$  = torsional rotation of 4 atoms about a central bond

$U_{nonbond}$  = non-bonded energy terms (electrostatics and Lenard-Jones)

# TOTAL POTENTIAL ENERGY

Energy,  $U$



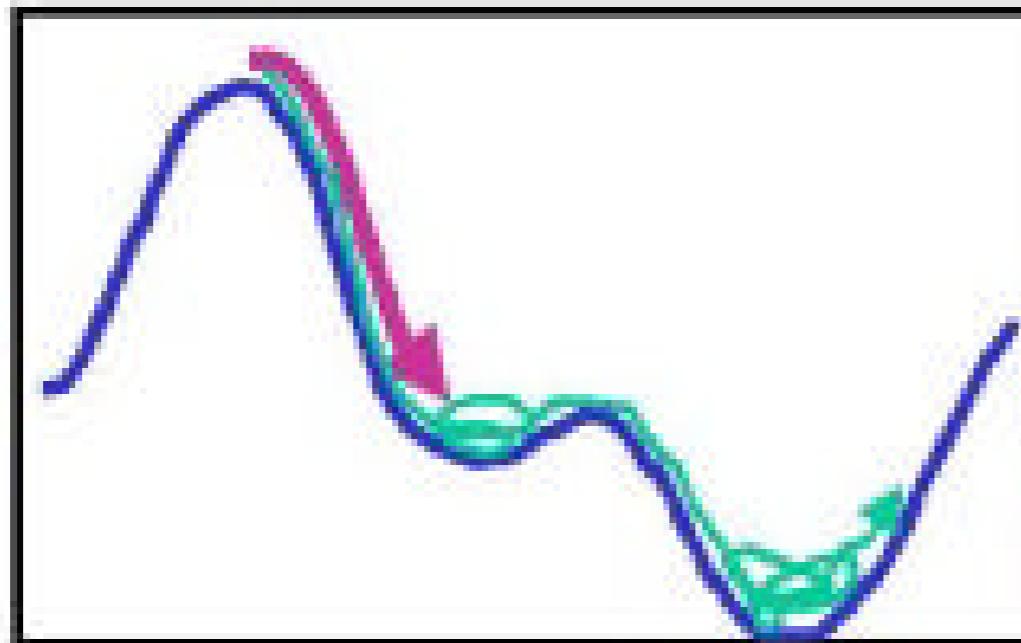
$$F(x) = -dU/dx$$

- The total potential energy or enthalpy fully defines the system,  $U$ .
- The forces are the gradients of the energy.
- The energy is a sum of independent terms for:  
Bond, Bond angles,  
Torsion angles and non-  
bonded atom pairs.

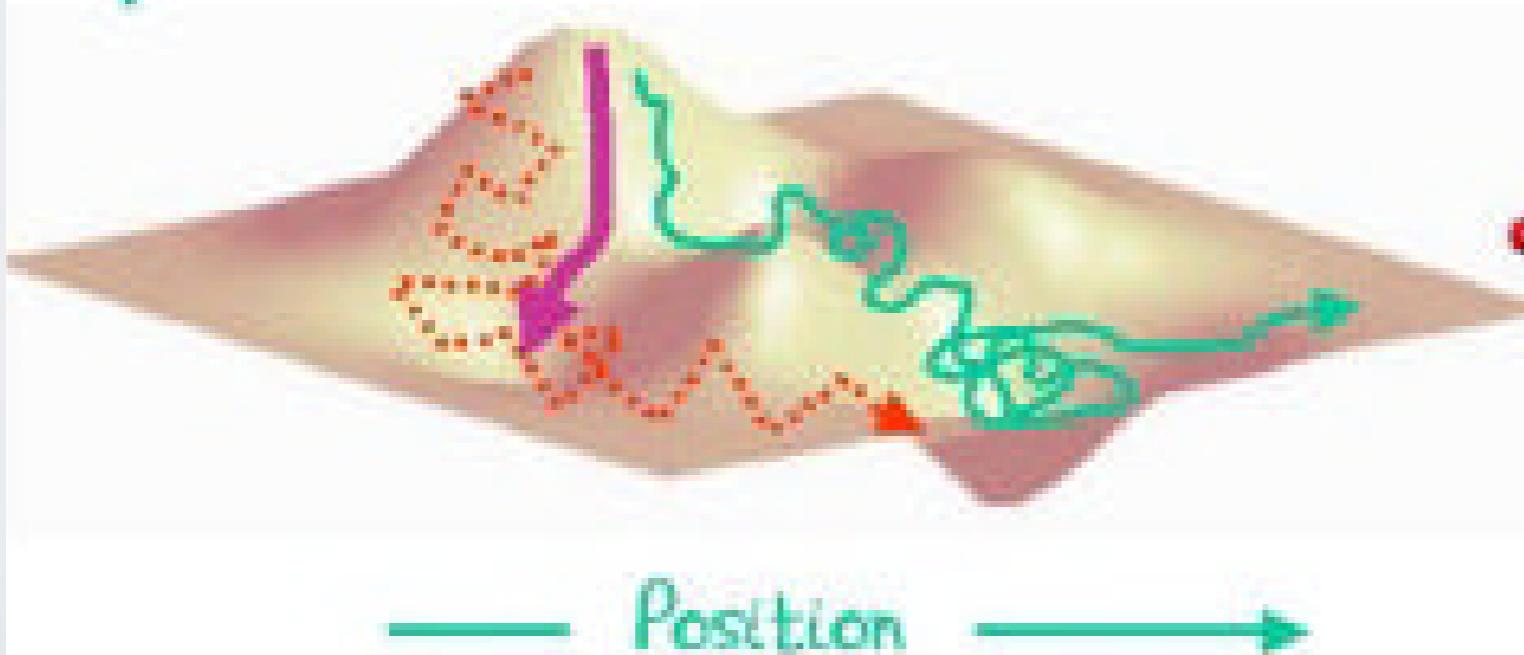
Slide Credit: Michael Levitt

# MOVING OVER THE ENERGY SURFACE

Energy,  $E$



- Energy Minimization drops into local minimum.



- Monte Carlo Moves are random. Accept with probability  $\exp(-\Delta U/kT)$ .

Slide Credit: Michael Levitt

# PHYSICS-ORIENTED APPROACHES

## Weaknesses

Fully physical detail becomes computationally intractable

Approximations are unavoidable

(Quantum effects approximated classically, water may be treated crudely)

Parameterization still required

## Strengths

Interpretable, provides guides to design

Broadly applicable, in principle at least

Clear pathways to improving accuracy

## Status

Useful, widely adopted but far from perfect

Multiple groups working on fewer, better approxs

Force fields, quantum  
entropy, water effects

Moore's law: hardware improving

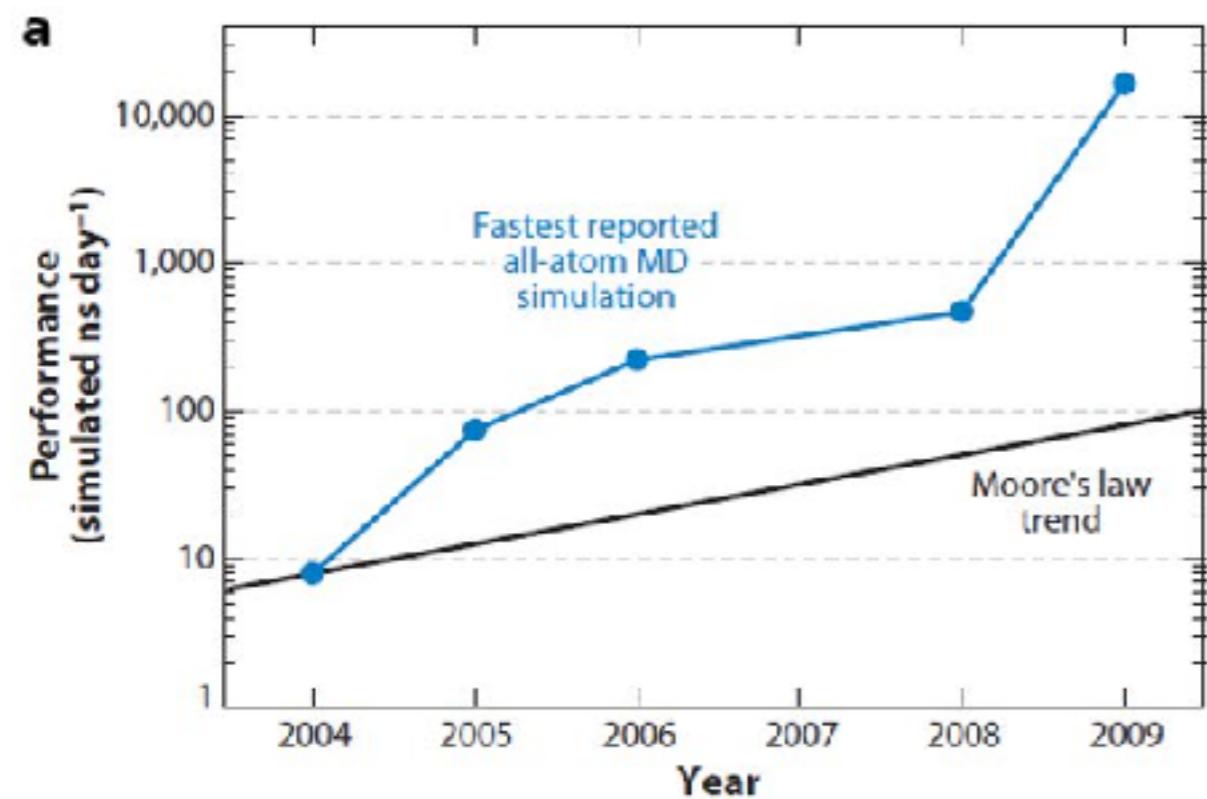
## HOW COMPUTERS HAVE CHANGED

DATE	COST	SPEED	MEMORY	SIZE
1967	\$10M	0.1 MHz	1 MB	WALL
2013	\$14,000	1 GHz	10 GB	LAPTOP
CHANGE	10,000	10,000	10,000	10,000

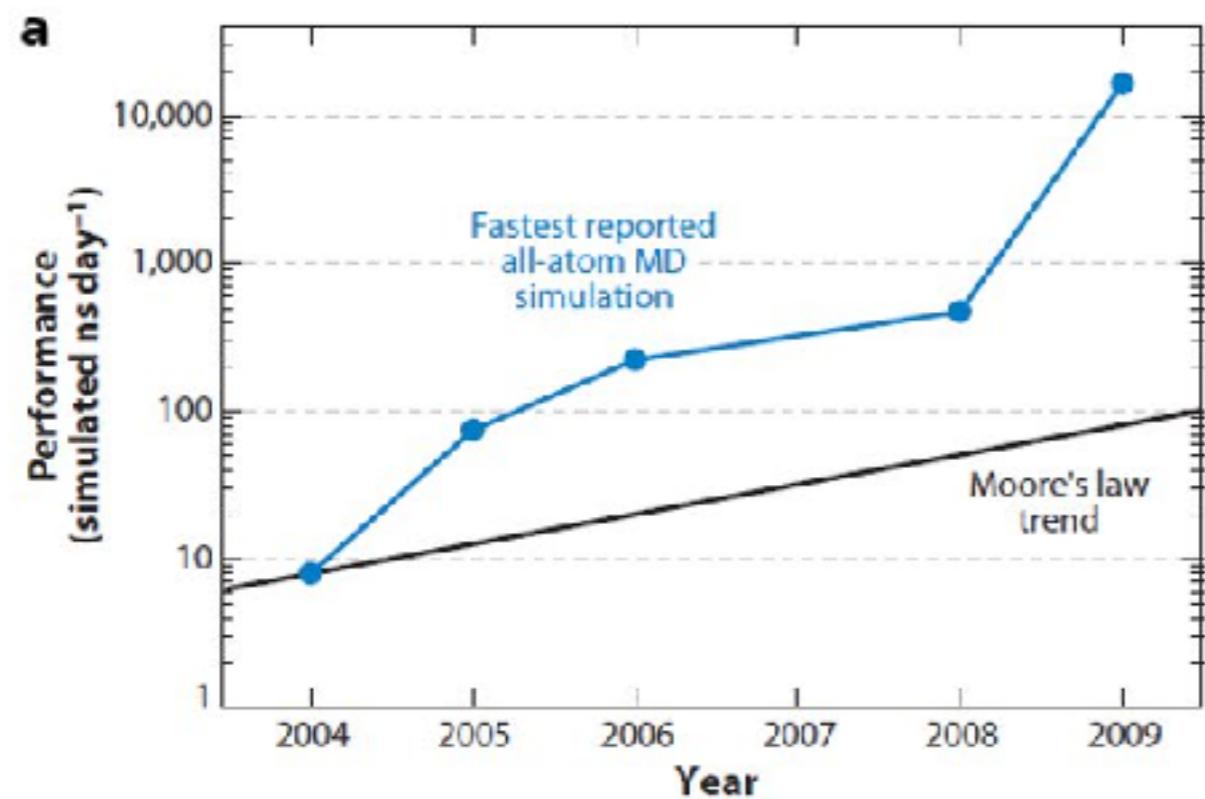
If cars were like computers then a new Vehc  
would cost \$3, would have a top speed of  
1,000,000 Km/hr, would carry 50,000  
adults and would park in a shadow.



# SIDE-NOTE: GPUS AND ANTON SUPERCOMPUTER



# SIDE-NOTE: GPUS AND ANTON SUPERCOMPUTER

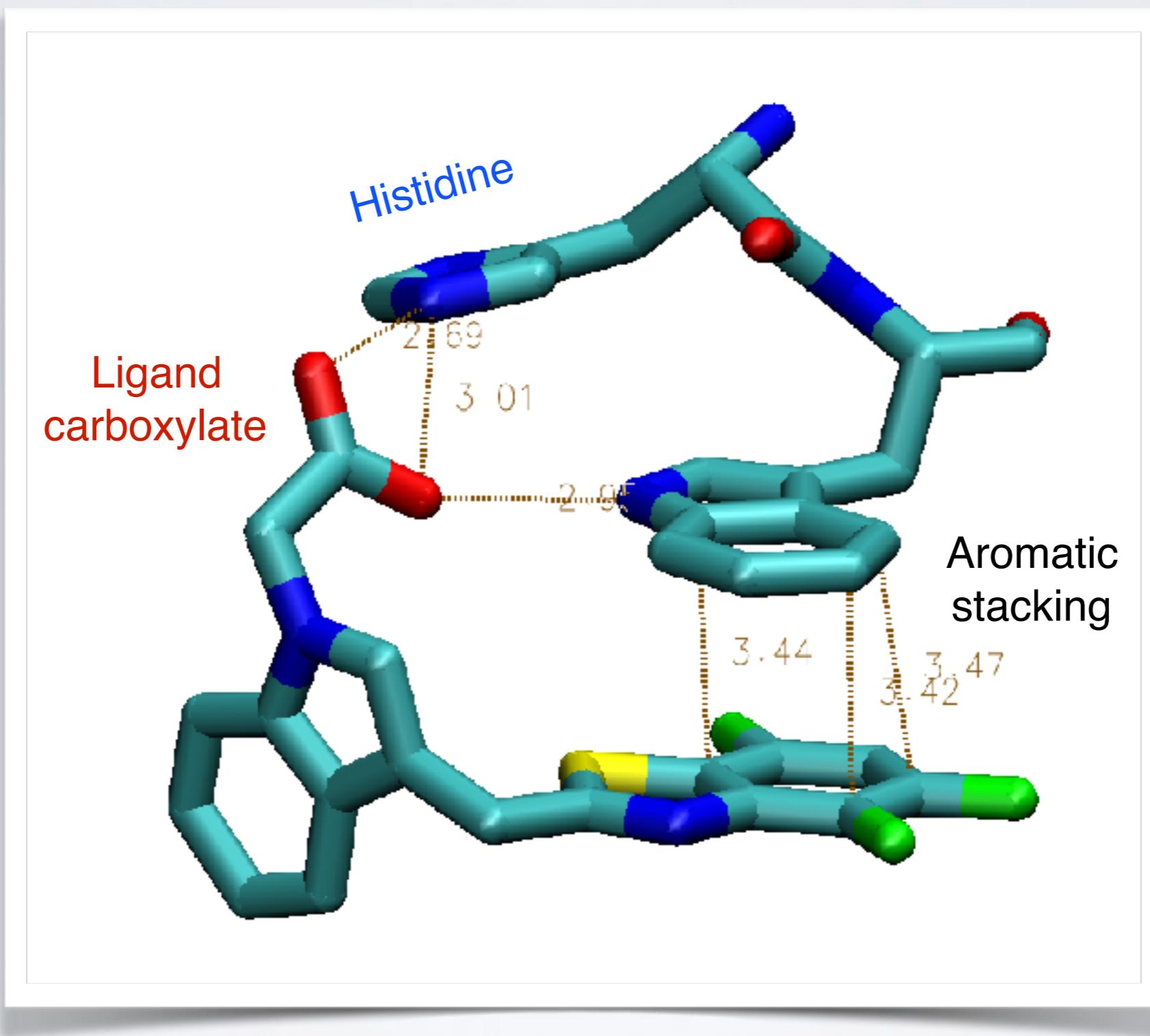


# **KEY CONCEPT:** POTENTIAL FUNCTIONS DESCRIBE A SYSTEMS **ENERGY** AS A FUNCTION OF ITS **STRUCTURE**

Two main approaches:

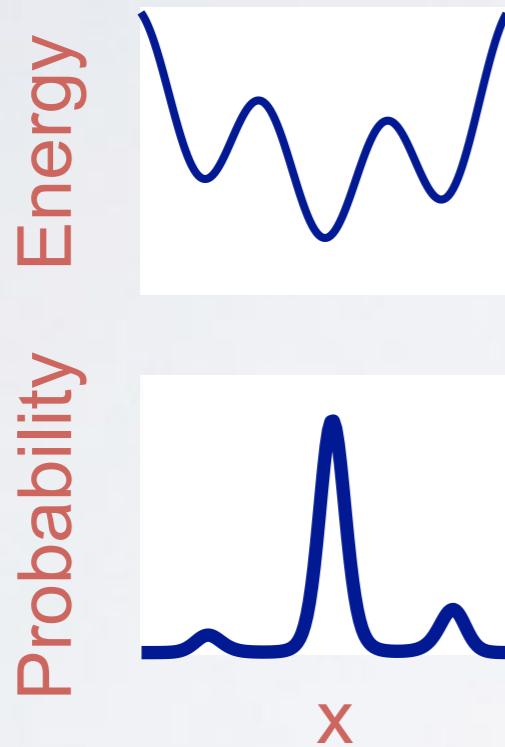
- (1). Physics-Based
- (2). Knowledge-Based

# KNOWLEDGE-BASED DOCKING POTENTIALS



# ENERGY DETERMINES **PROBABILITY** (STABILITY)

Basic idea: Use probability as a proxy for energy



Boltzmann:

$$p(r) \propto e^{-E(r)/RT}$$

Inverse Boltzmann:

$$E(r) = -RT \ln[p(r)]$$

**Example: ligand carboxylate O to protein histidine N**

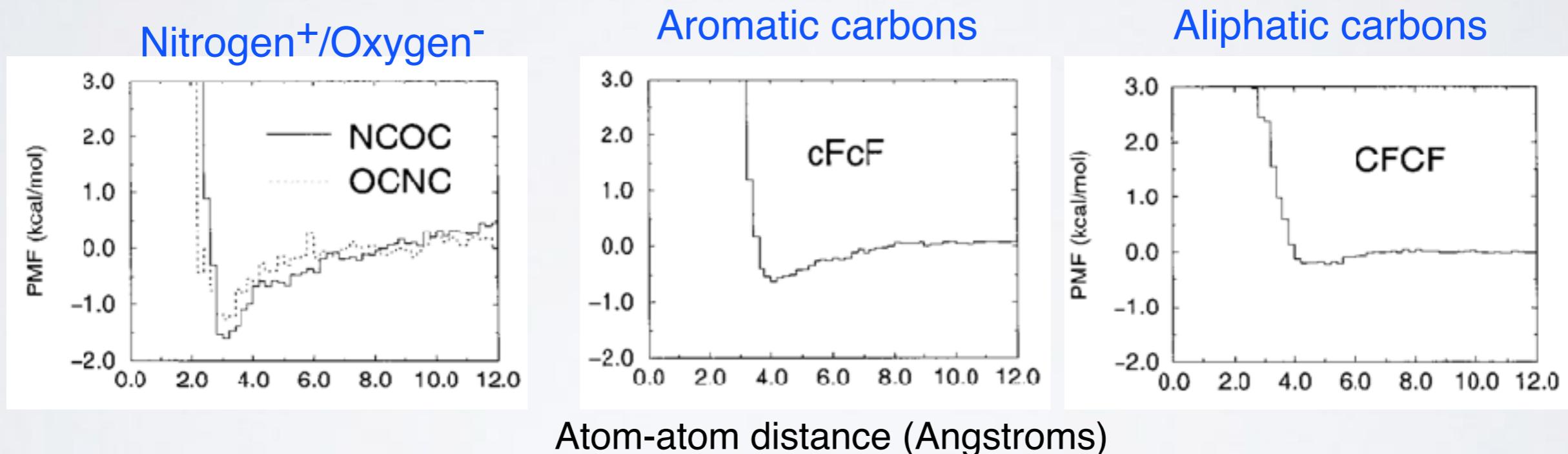
Find all protein-ligand structures in the PDB with a ligand carboxylate O

1. For each structure, histogram the distances from O to every histidine N
2. Sum the histograms over all structures to obtain  $p(r_{O-N})$
3. Compute  $E(r_{O-N})$  from  $p(r_{O-N})$

# KNOWLEDGE-BASED DOCKING POTENTIALS

“PMF”, Muegge & Martin, J. Med. Chem. (1999) 42:791

A few types of atom pairs, out of several hundred total



$$E_{prot-lig} = E_{vdw} + \sum_{pairs(ij)} E_{type(ij)}(r_{ij})$$

# KNOWLEDGE-BASED POTENTIALS

## Weaknesses

Accuracy limited by availability of data

## Strengths

Relatively easy to implement

Computationally fast

## Status

Useful, far from perfect

May be at point of diminishing returns

(not always clear how to make improvements)

Do it Yourself!

# Hand-on time!

[https://bioboot.github.io/bimm143\\_S18/lectures/#11](https://bioboot.github.io/bimm143_S18/lectures/#11)

Focus on **section 4 & 5**

# NEXT UP:

- ▶ **Overview of structural bioinformatics**

- Major motivations, goals and challenges

- ▶ **Fundamentals of protein structure**

- Composition, form, forces and dynamics

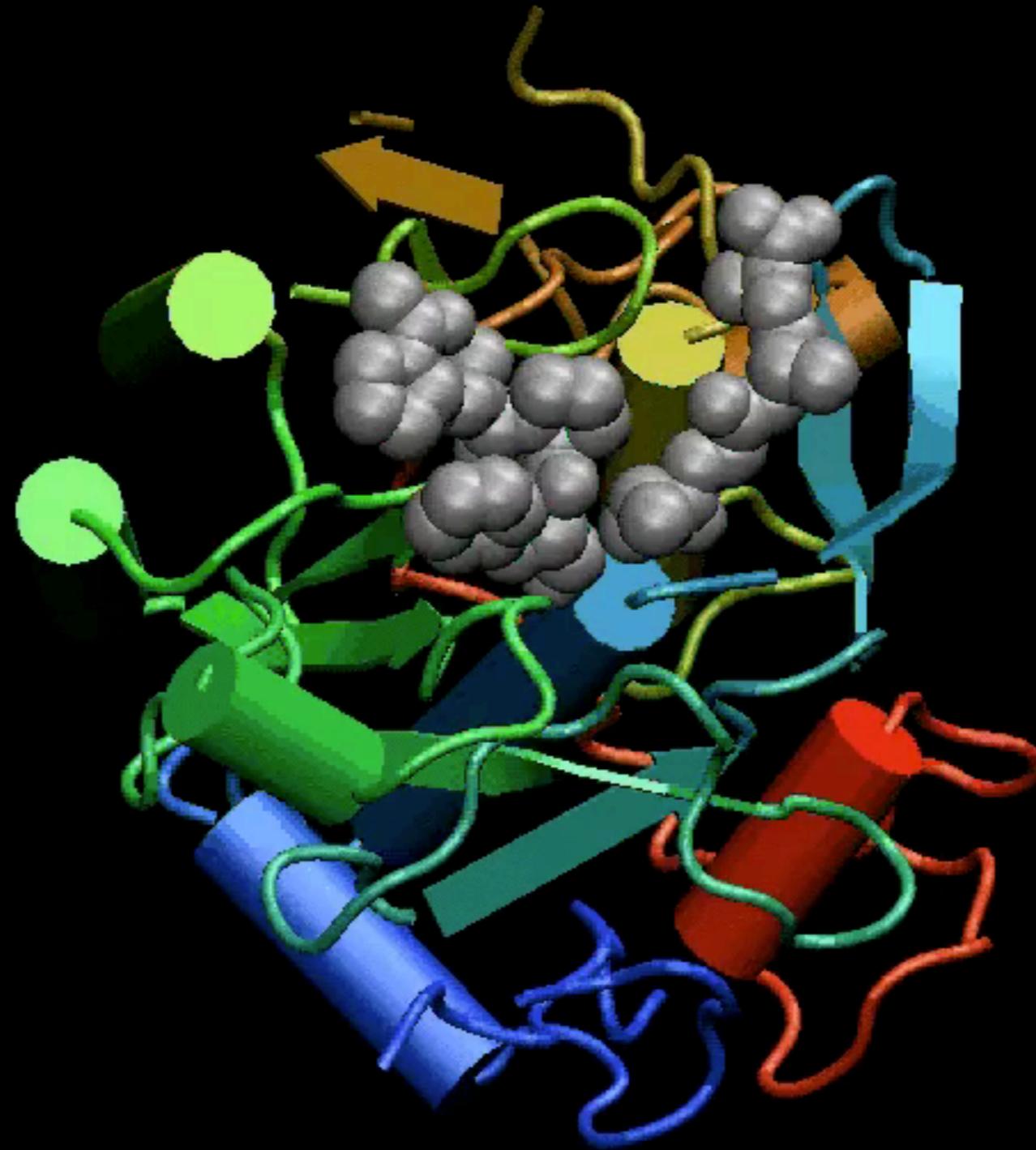
- ▶ **Representing and interpreting protein structure**

- Modeling energy as a function of structure

- ▶ **Example application areas**

- Predicting functional dynamics & drug discovery

NMA models the protein as a network of elastic strings



Proteinase K

Do it Yourself!

# Hand-on time!

[https://bioboot.github.io/bimm143\\_S18/lectures/#11](https://bioboot.github.io/bimm143_S18/lectures/#11)

Focus on **section 6** to **7**

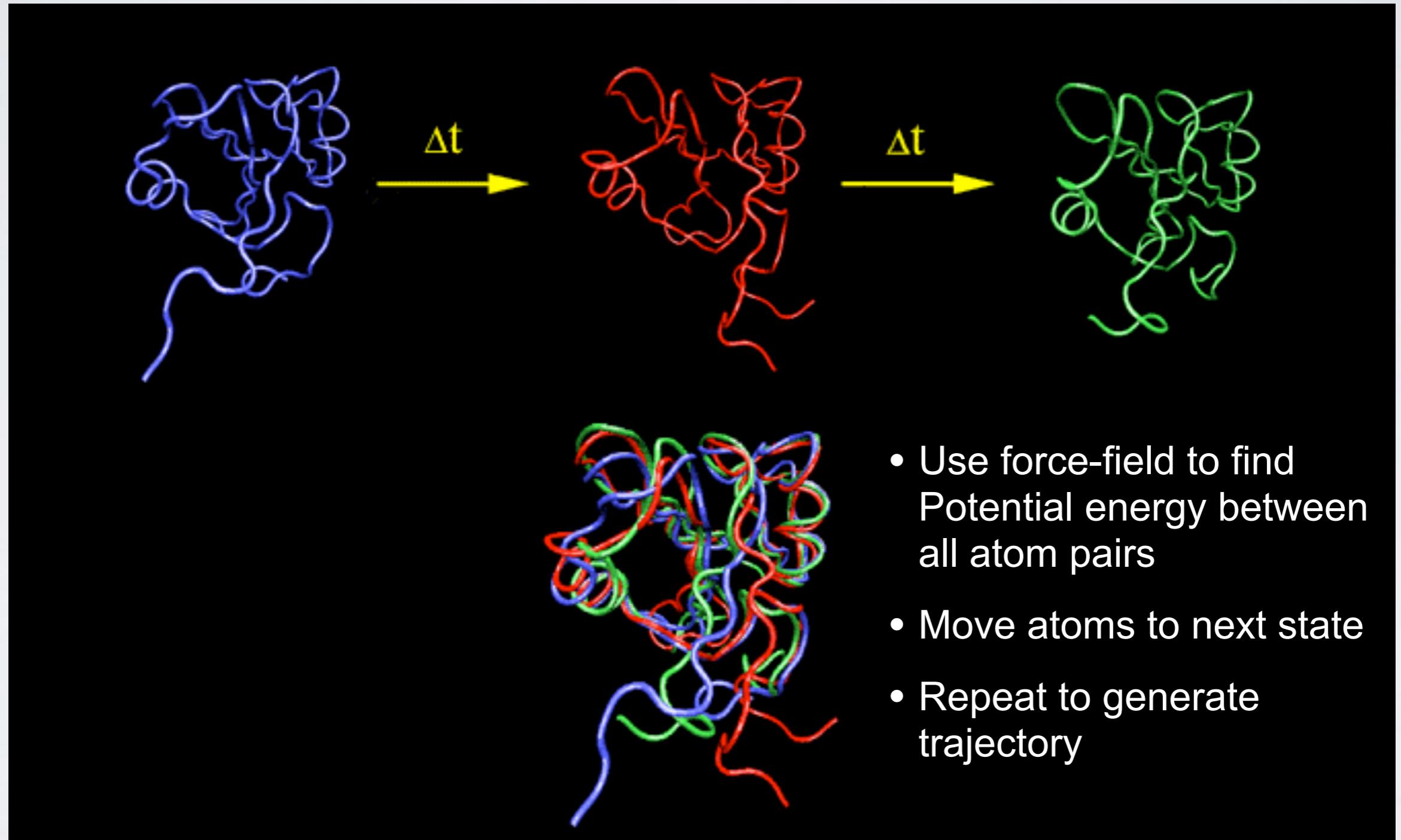
Optional:  
Stop here for Today!

[ Muddy Point Assessment ]

# PREDICTING FUNCTIONAL DYNAMICS

- Proteins are intrinsically flexible molecules with internal motions that are often intimately coupled to their biochemical function
  - E.g. ligand and substrate binding, conformational activation, allosteric regulation, etc.
- Thus knowledge of dynamics can provide a deeper understanding of the mapping of structure to function
  - Molecular dynamics (MD) and normal mode analysis (NMA) are two major methods for predicting and characterizing molecular motions and their properties

# MOLECULAR DYNAMICS SIMULATION



McCammon, Gelin & Karplus, *Nature* (1977)

[ See: <https://www.youtube.com/watch?v=ui1ZysMFcKk> ]

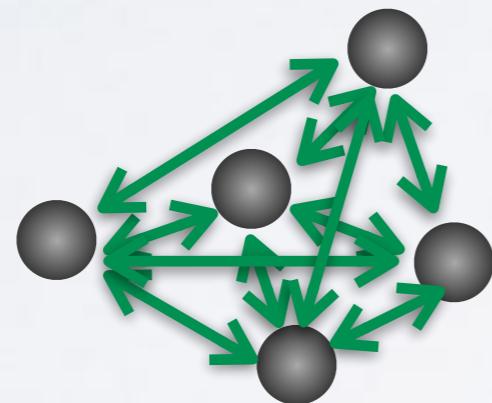
- ▶ Divide **time** into discrete ( $\sim 1\text{fs}$ ) **time steps ( $\Delta t$ )**  
(for integrating equations of motion, see below)



- ▶ Divide **time** into discrete ( $\sim 1\text{fs}$ ) **time steps ( $\Delta t$ )**  
(for integrating equations of motion, see below)



- ▶ At each time step calculate pair-wise atomic **forces ( $F(t)$ )**  
(by evaluating **force-field** gradient)



*Nucleic motion described classically*

$$m_i \frac{d^2}{dt^2} \vec{R}_i = -\vec{\nabla}_i E(\vec{R})$$

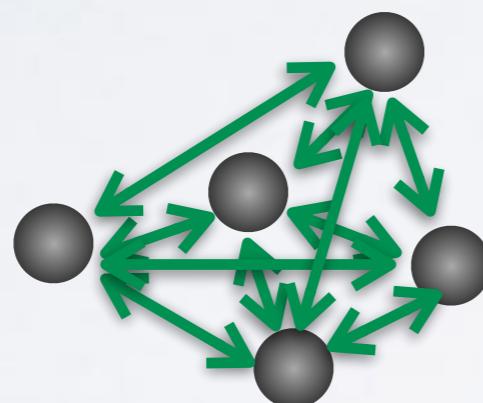
*Empirical force field*

$$E(\vec{R}) = \sum_{\text{bonded}} E_i(\vec{R}) + \sum_{\text{non-bonded}} E_i(\vec{R})$$

- ▶ Divide **time** into discrete ( $\sim 1\text{fs}$ ) **time steps ( $\Delta t$ )**  
(for integrating equations of motion, see below)



- ▶ At each time step calculate pair-wise atomic **forces ( $F(t)$ )**  
(by evaluating **force-field** gradient)



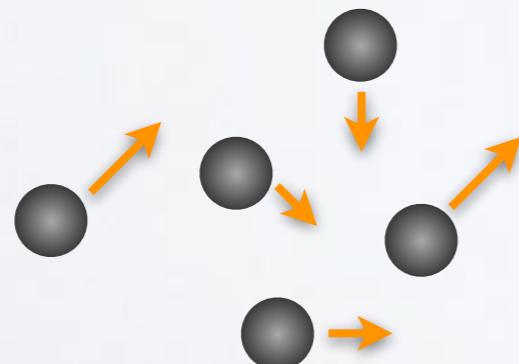
*Nucleic motion described classically*

$$m_i \frac{d^2}{dt^2} \vec{R}_i = -\vec{\nabla}_i E(\vec{R})$$

*Empirical force field*

$$E(\vec{R}) = \sum_{\text{bonded}} E_i(\vec{R}) + \sum_{\text{non-bonded}} E_i(\vec{R})$$

- ▶ Use the forces to calculate **velocities** and move atoms to new **positions**  
(by integrating numerically via the “leapfrog” scheme)



$$\boxed{v(t + \frac{\Delta t}{2})} = v(t - \frac{\Delta t}{2}) + \frac{\mathbf{F}(t)}{m} \Delta t$$

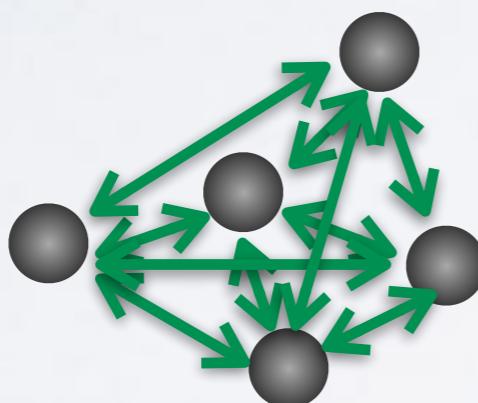
$$\mathbf{r}(t + \Delta t) = \mathbf{r}(t) + \boxed{v(t + \frac{\Delta t}{2})} \Delta t$$

# BASIC ANATOMY OF A MD SIMULATION

- ▶ Divide **time** into discrete ( $\sim 1\text{fs}$ ) **time steps** ( $\Delta t$ )  
(for integrating equations of motion, see below)



- ▶ At each time step calculate pair-wise atomic **forces** ( $F(t)$ )  
(by evaluating **force-field** gradient)



*Nucleic motion described classically*

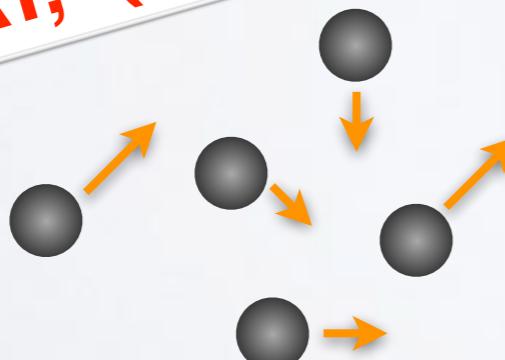
$$m_i \frac{d^2}{dt^2} \vec{R}_i = -\vec{\nabla}_i E(\vec{R})$$

*Empirical force function*

$$E(\vec{R}) = \sum_{i=1}^N \sum_{j \neq i, \text{non-bonded}} E_i(\vec{R})$$

- ▶ Use the forces to calculate **velocities** and move atoms to new **positions**  
(numerically via the “leapfrog” scheme)

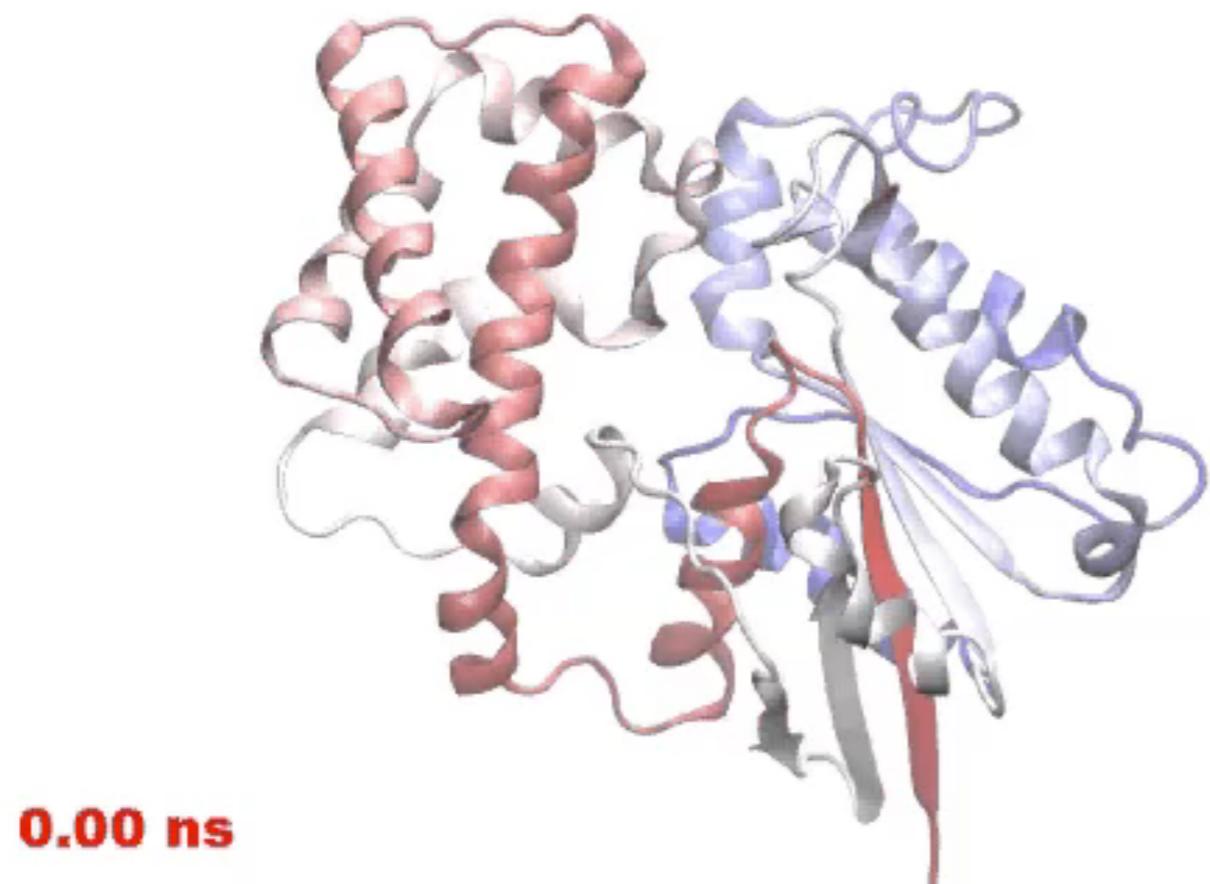
**REPEAT, (iterate many, many times... 1ms =  $10^{12}$  time steps)**



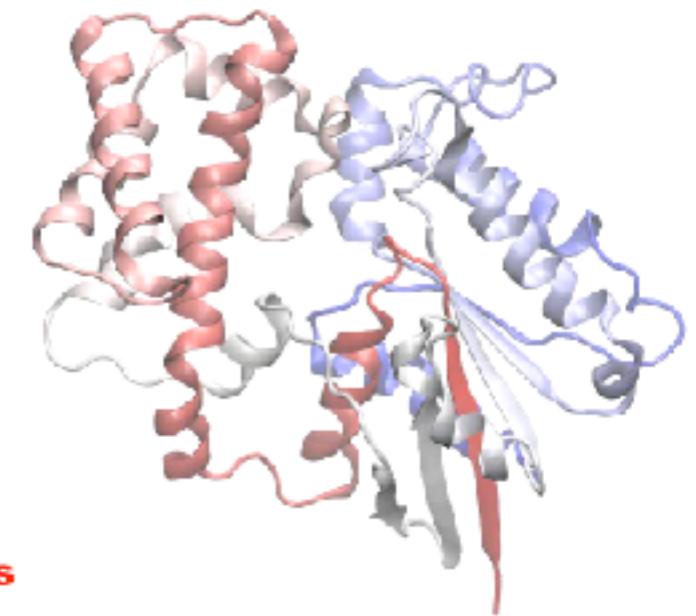
$$\begin{aligned} \mathbf{v}(t + \frac{\Delta t}{2}) &= \mathbf{v}(t - \frac{\Delta t}{2}) + \frac{\mathbf{F}(t)}{m} \Delta t \\ \mathbf{r}(t + \Delta t) &= \mathbf{r}(t) + \mathbf{v}(t + \frac{\Delta t}{2}) \Delta t \end{aligned}$$

# MD Prediction of Functional Motions

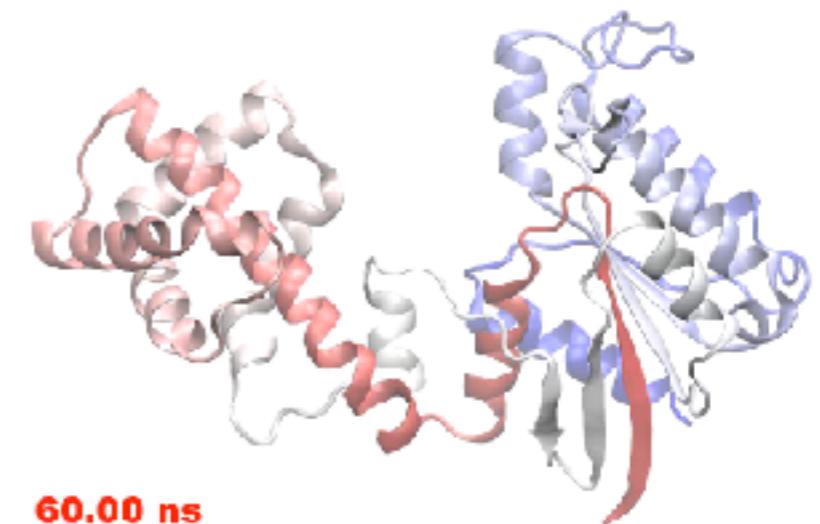
Accelerated MD simulation of  
nucleotide-free transducin alpha subunit



“close”

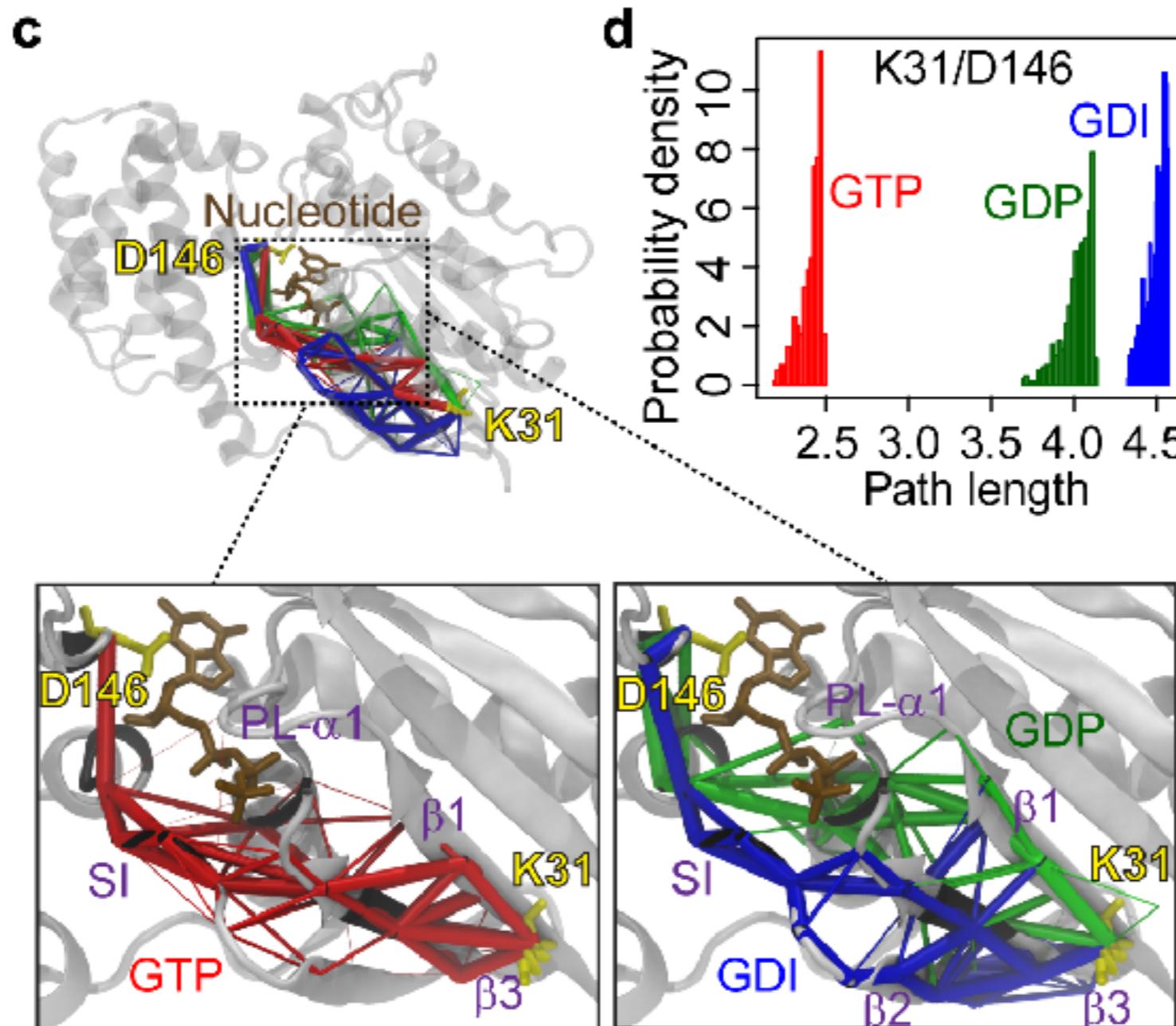


“open”

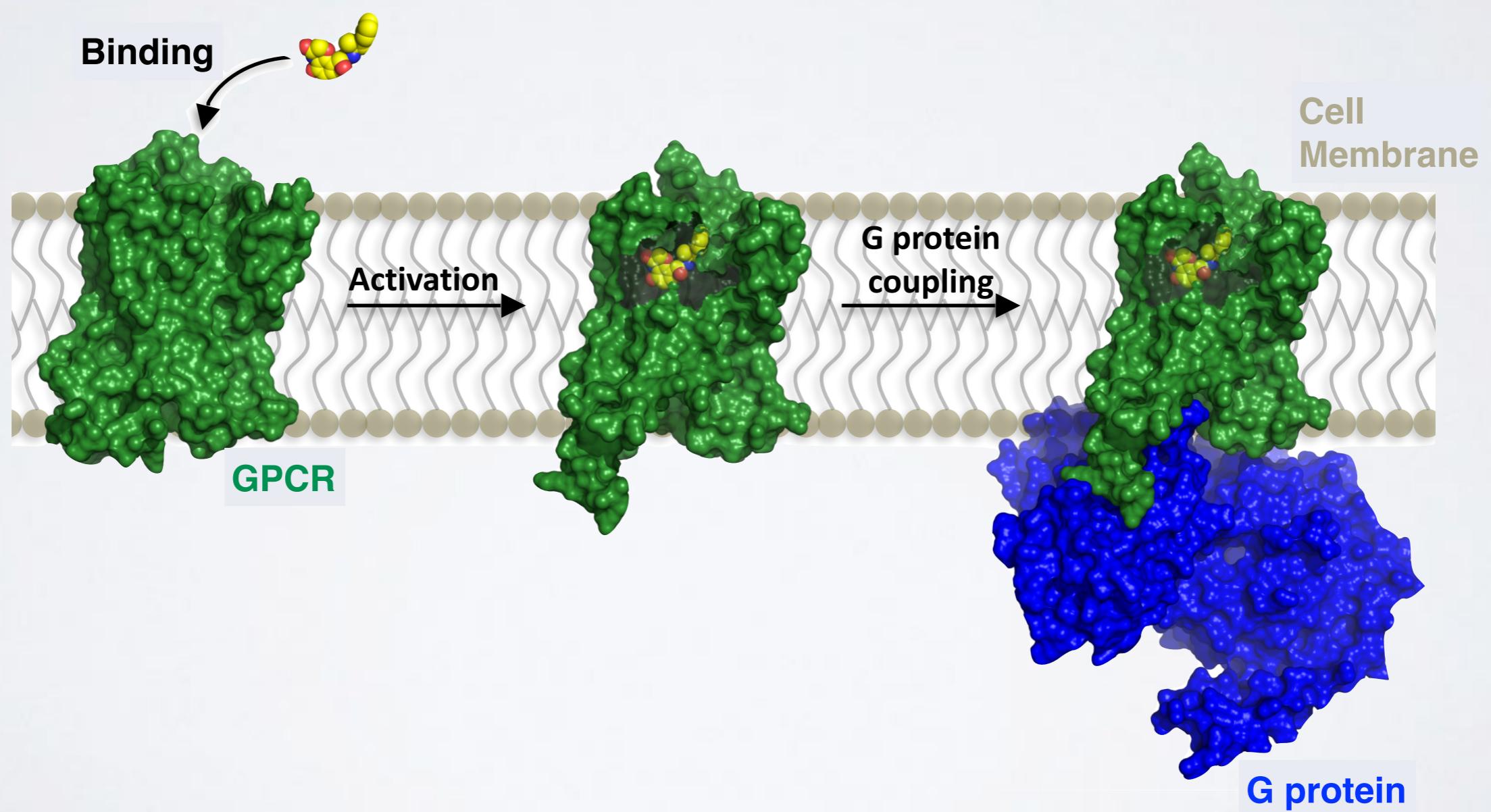


Yao and Grant, Biophys J. (2013)

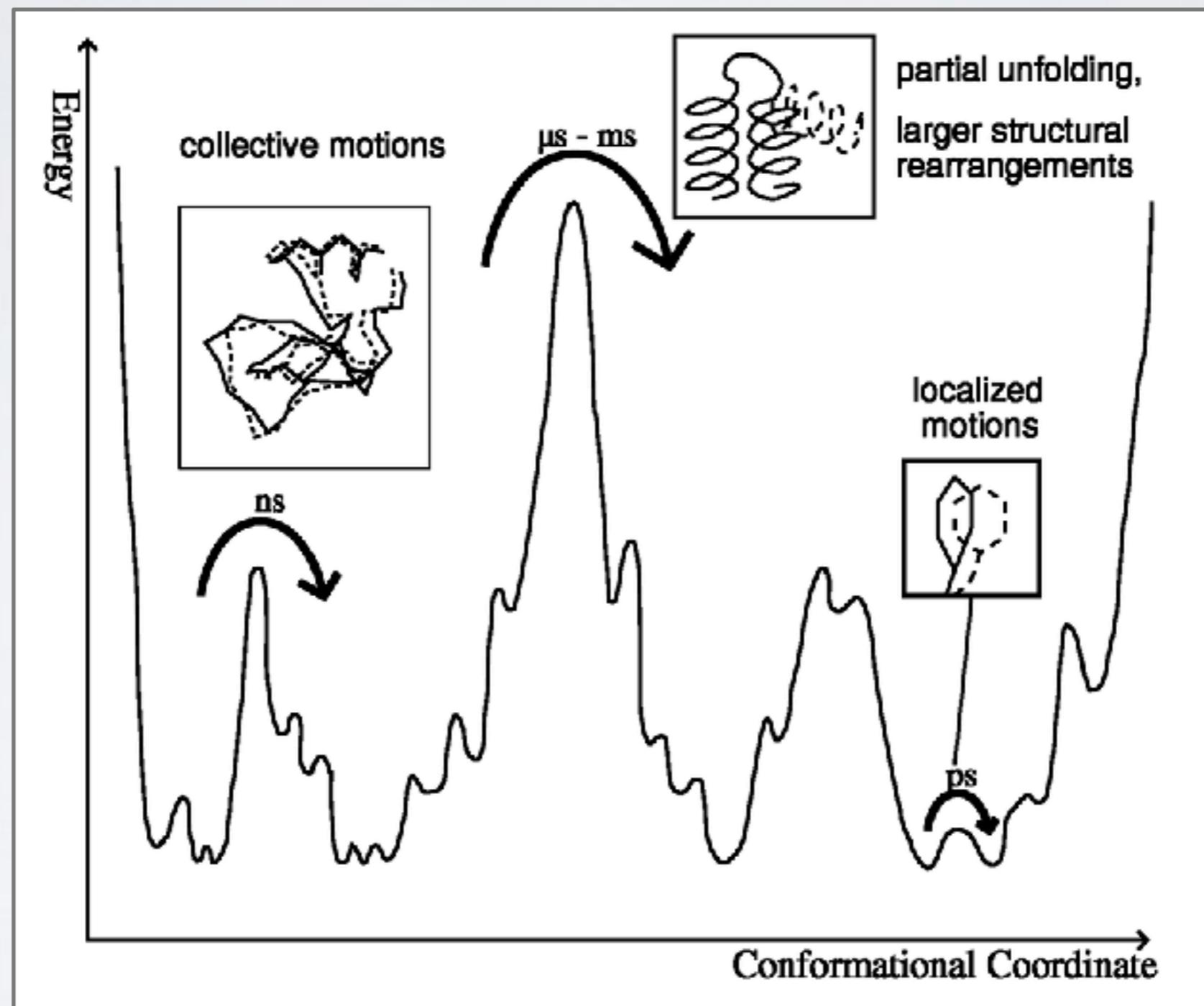
# Simulations Identify Key Residues Mediating Dynamic Activation



# EXAMPLE APPLICATION OF MOLECULAR SIMULATIONS TO GPCRS



# PROTEINS JUMP BETWEEN MANY, HIERARCHICALLY ORDERED “CONFORMATIONAL SUBSTATES”



H. Frauenfelder et al., *Science* **229** (1985) 337

# MOLECULAR DYNAMICS IS VERY

**Example:** F<sub>1</sub>-ATPase in water (183,674 atoms) for 1 nanosecond:

- => 10<sup>6</sup> integration steps
- => 8.4 \* 10<sup>11</sup> floating point operations/step  
[n(n-1)/2 interactions]

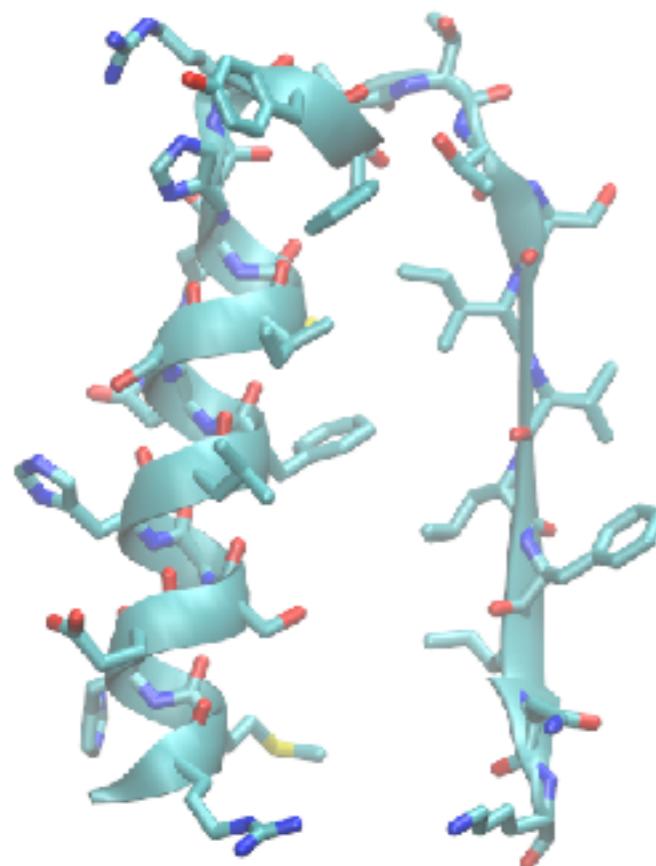
Total: 8.4 \* 10<sup>17</sup> flop  
(on a 100 Gflop/s cpu: **ca 25 years!**)

**... but performance has been improved by use of:**

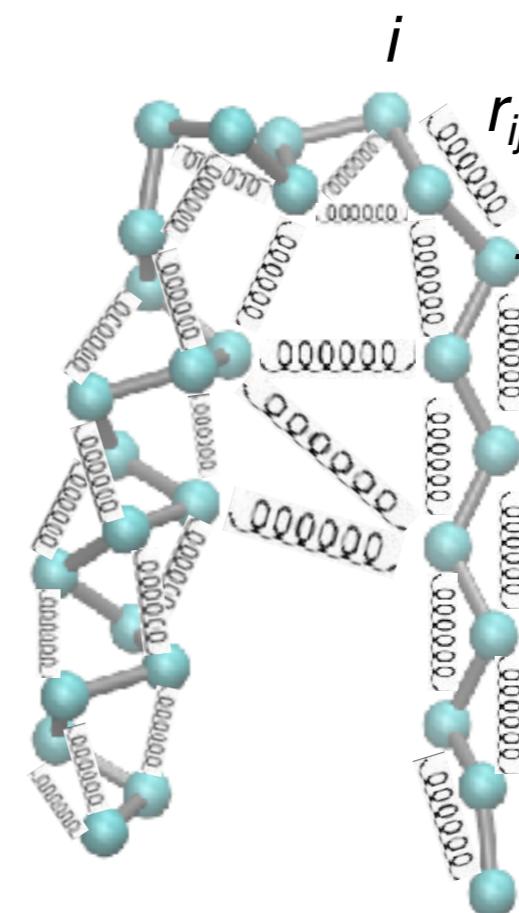
multiple time stepping	ca. 2.5 years
fast multipole methods	ca. 1 year
parallel computers	ca. 5 days
modern GPUs	ca. 1 day
<b>(Anton supercomputer</b>	<b>ca. minutes)</b>

# COARSE GRAINING: **NORMAL MODE ANALYSIS** (NMA)

- MD is still time-consuming for large systems
- Elastic network model NMA (ENM-NMA) is an example of a lower resolution approach that finishes in seconds even for large systems.



C. G.

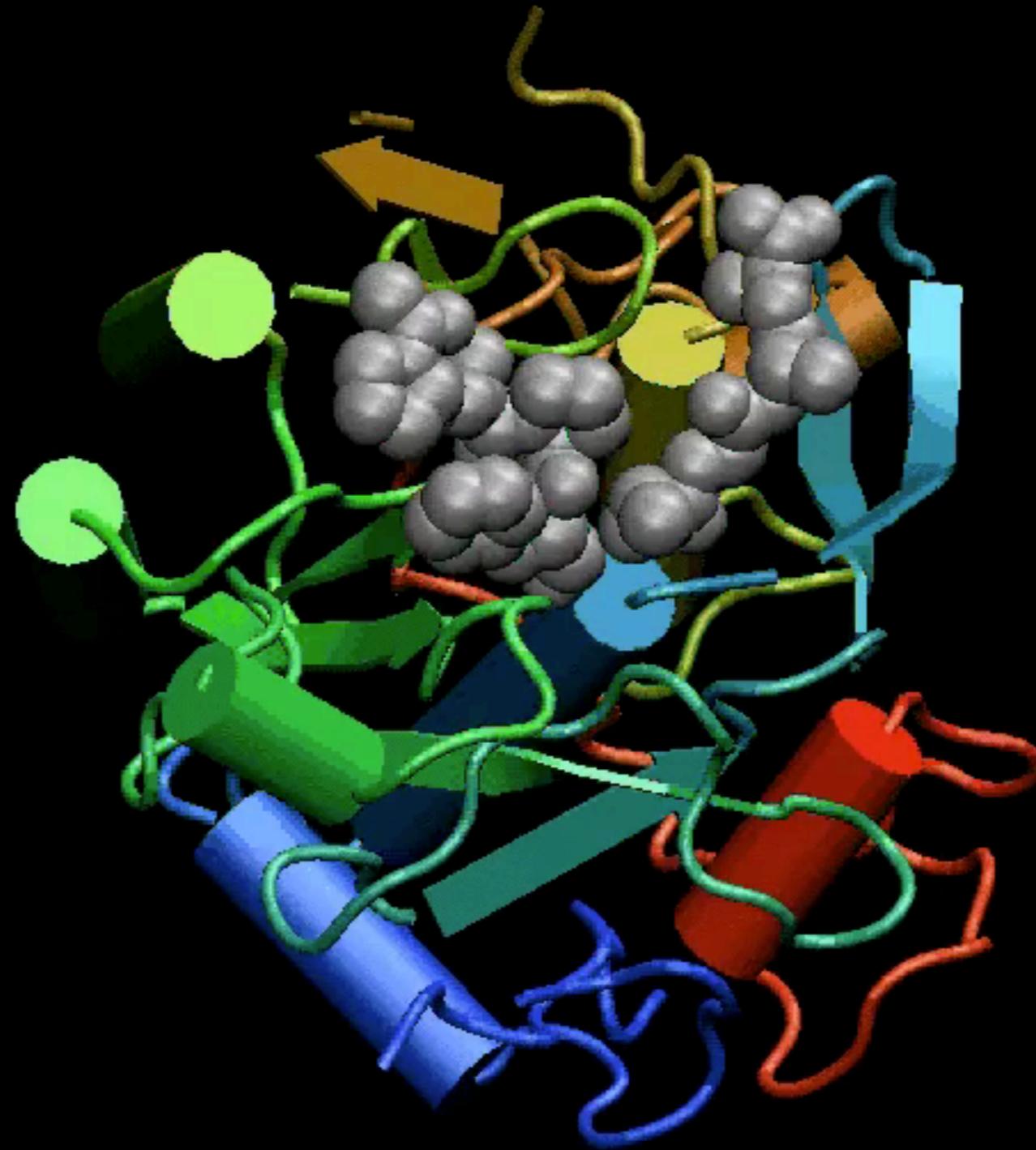


Atomistic

Coarse Grained

- 1 bead /  
1 amino acid
- Connected by  
springs

NMA models the protein as a network of elastic strings



Proteinase K

Do it Yourself!

# Hand-on time!

[https://bioboot.github.io/bimm143\\_S18/lectures/#11](https://bioboot.github.io/bimm143_S18/lectures/#11)

Focus on **section 6** to **7**

# SUMMARY

- Structural bioinformatics is computer aided structural biology
- Described major motivations, goals and challenges of structural bioinformatics
- Reviewed the fundamentals of protein structure
- Introduced both physics and knowledge based modeling approaches for describing the structure, energetics and dynamics of proteins computationally