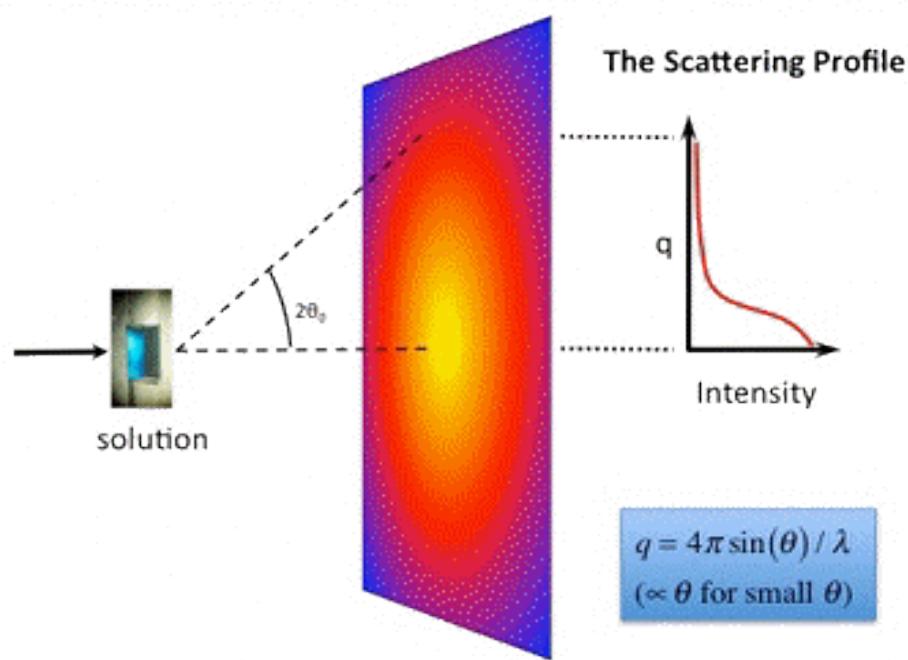
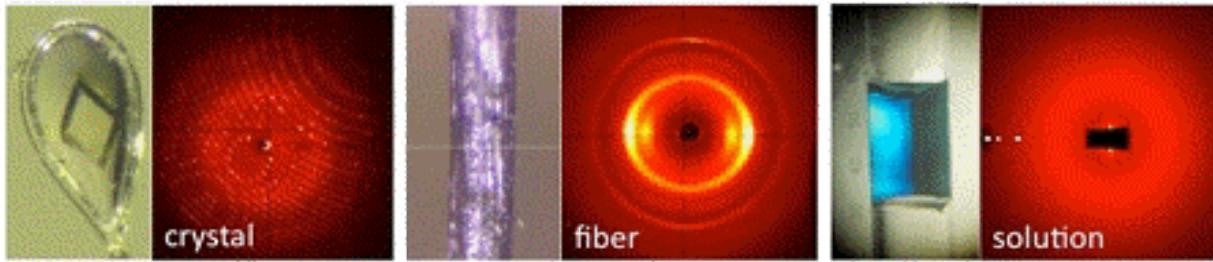
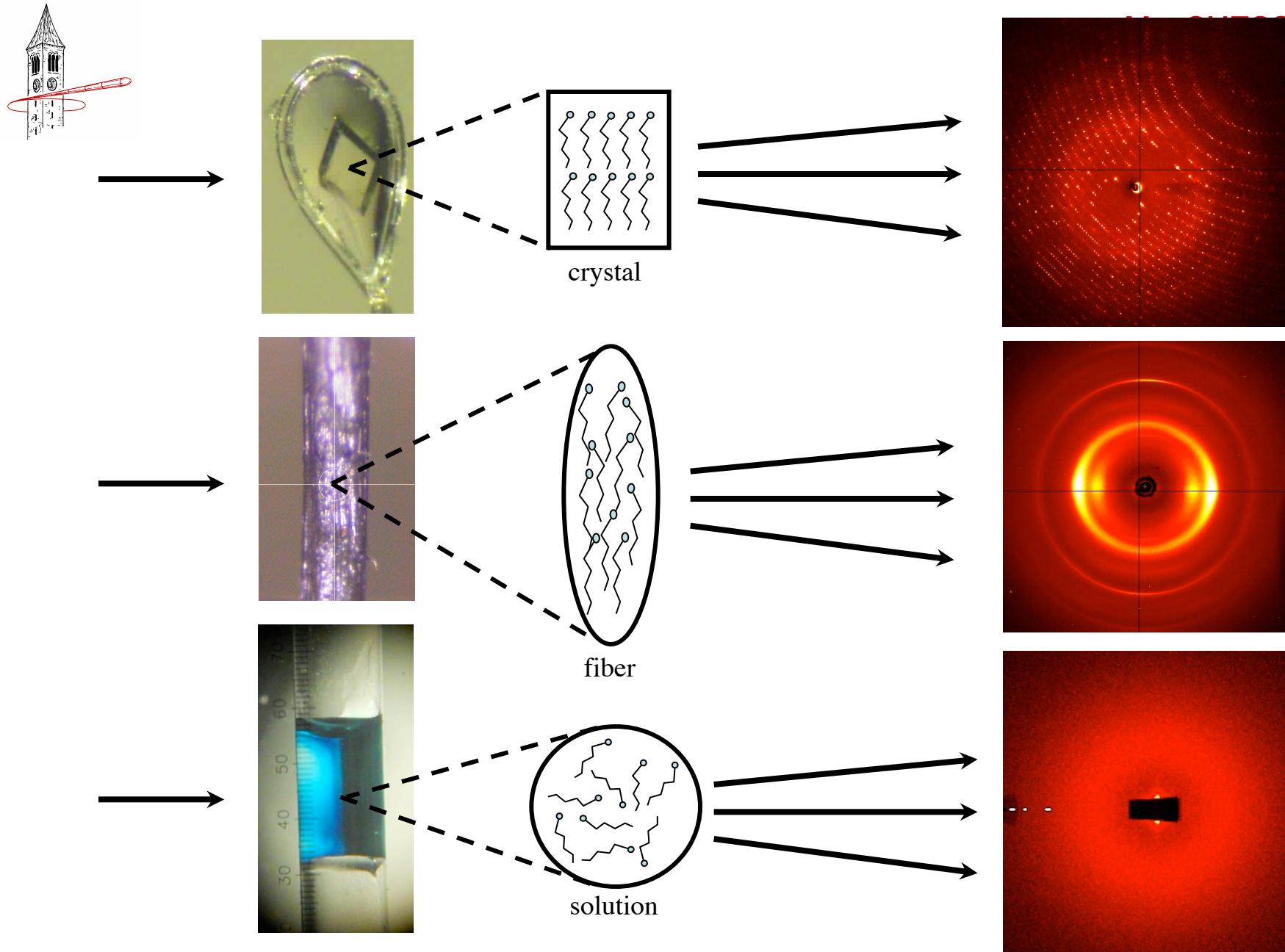
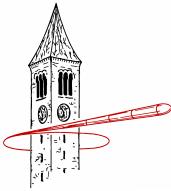


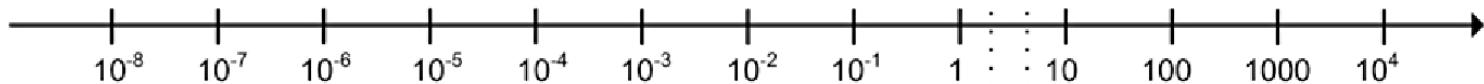
BioSAS Overview and Applications



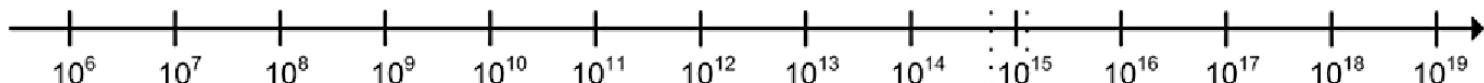




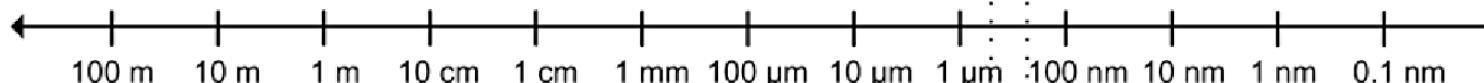
Energy of one photon (electron volt)



Frequency (Hz)



Wavelength



AM radio

VHF TV & FM radio

Radar
Microwaves
Mobile phones
UHF TV

Infra-red

Visible light

Ultra violet

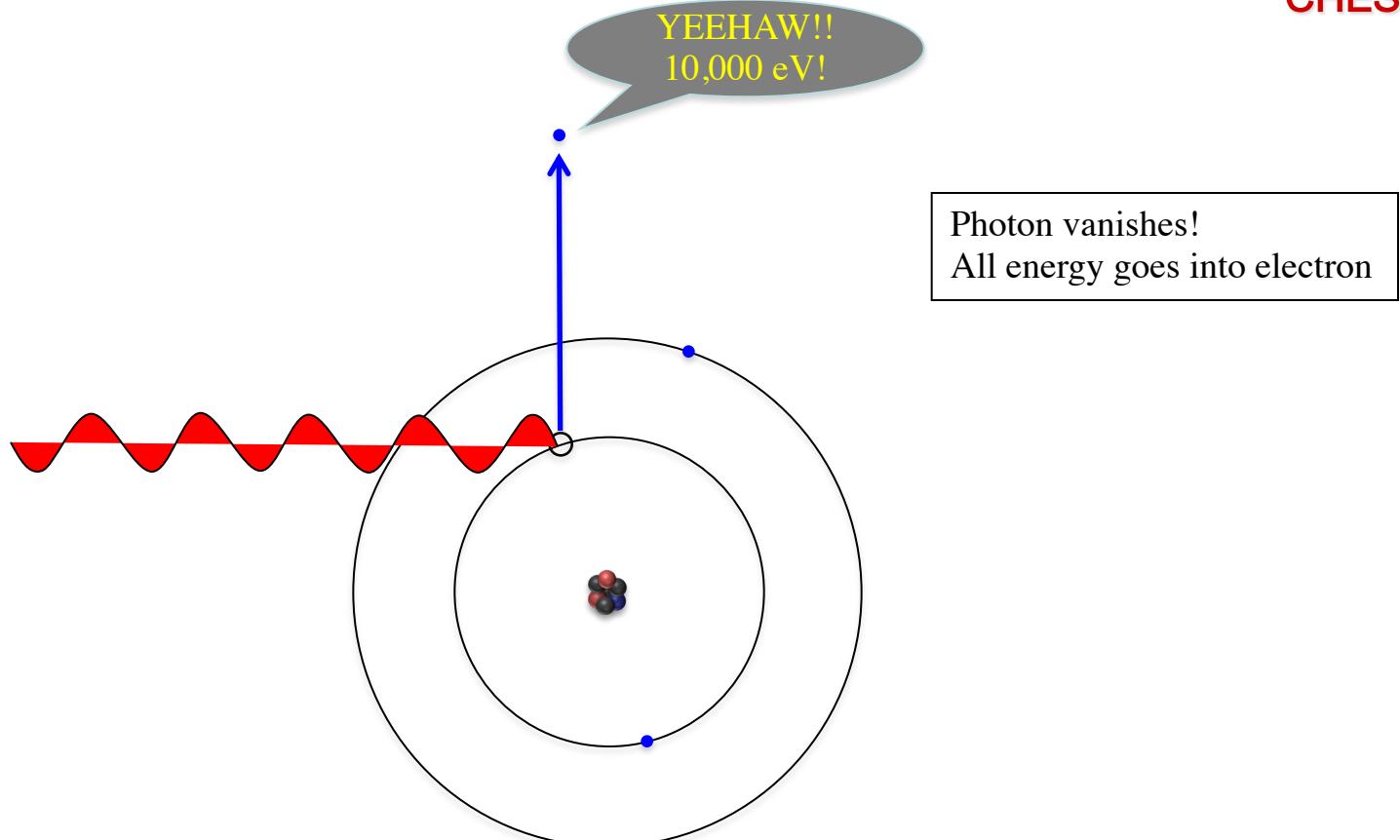
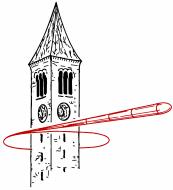
X-rays

Gamma rays

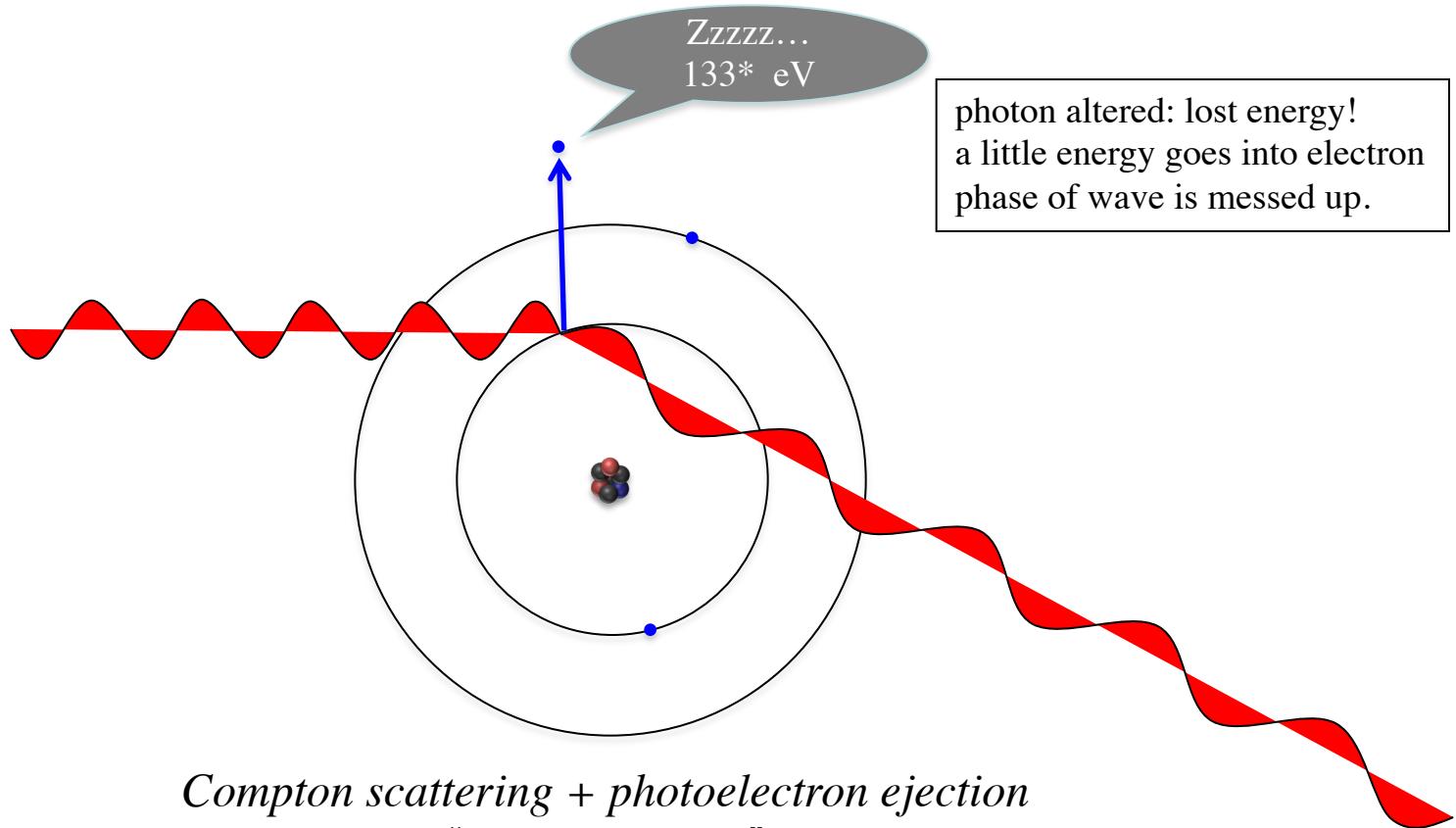
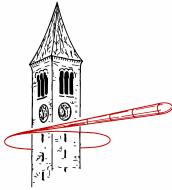


Useful: Energy (keV) = 12.4/wavelength (Angstroms)

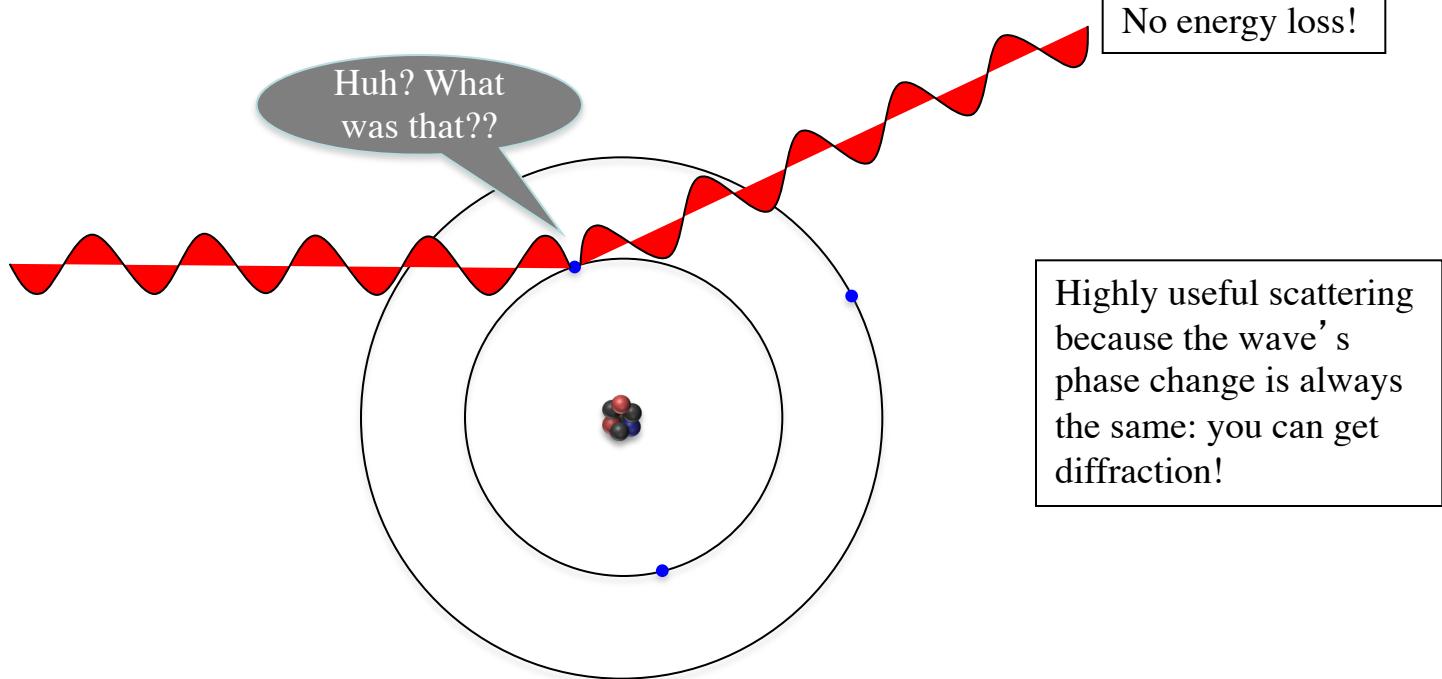
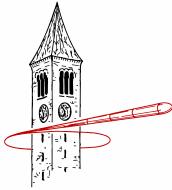
* From <http://what-when-how.com/wp-content/uploads/2012/07/tmp26dc54.png>



Photoabsorption → photoelectron ejection → fluorescence



* Compton ΔE @ 90° = 188 eV
Lithium 1s binding = 54.7 eV
 $188 \text{ eV} - 54 \text{ eV} = 133 \text{ eV}$

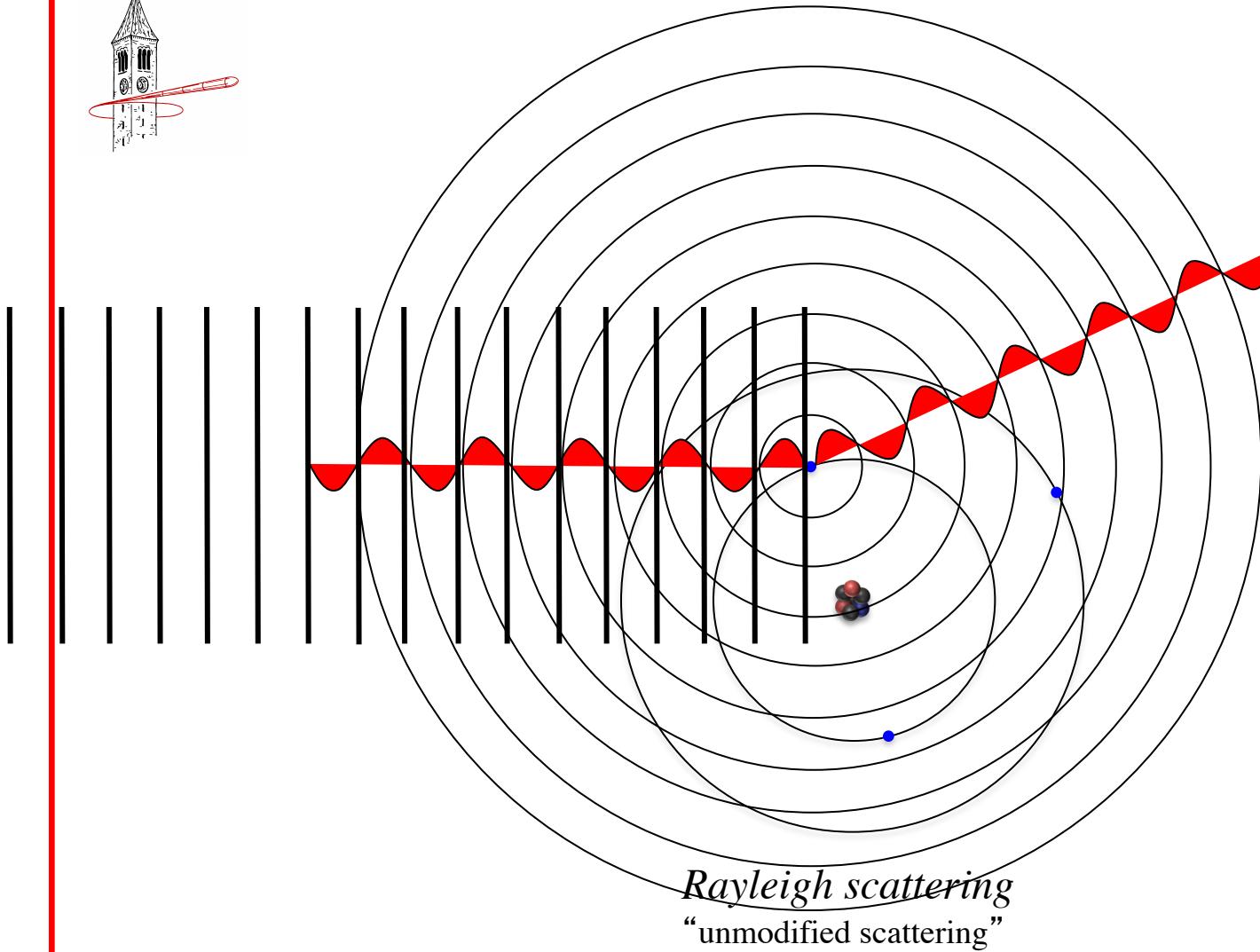
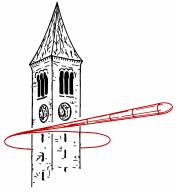


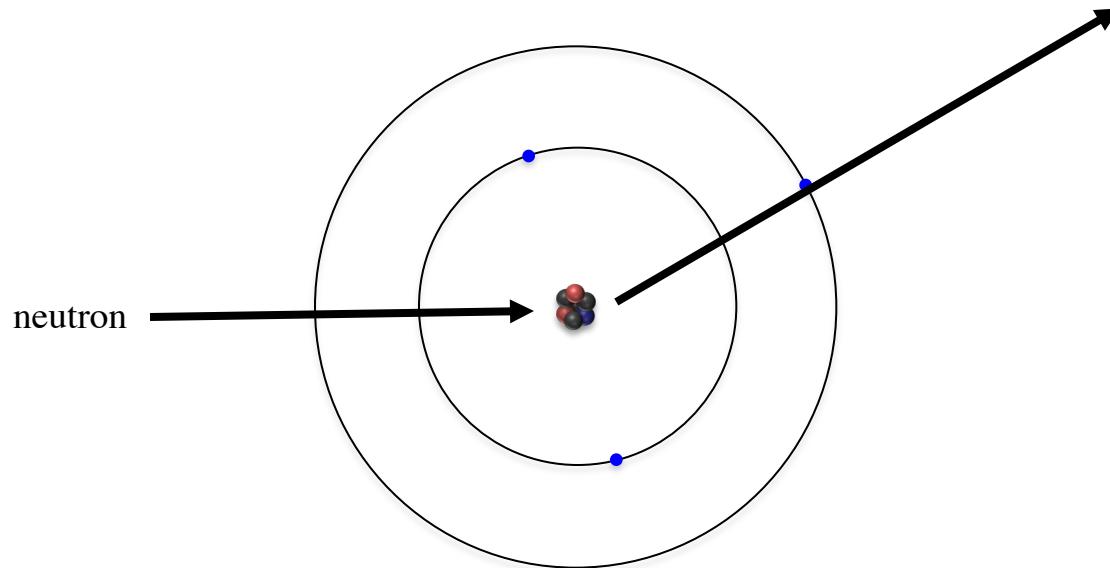
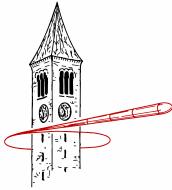
Rayleigh scattering
“unmodified scattering”

Rayleigh scattering = bound electron

Thomson scattering = free electron

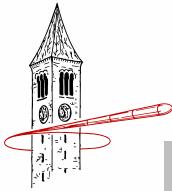
To hard X-rays, everything looks like a free electron anyhow!





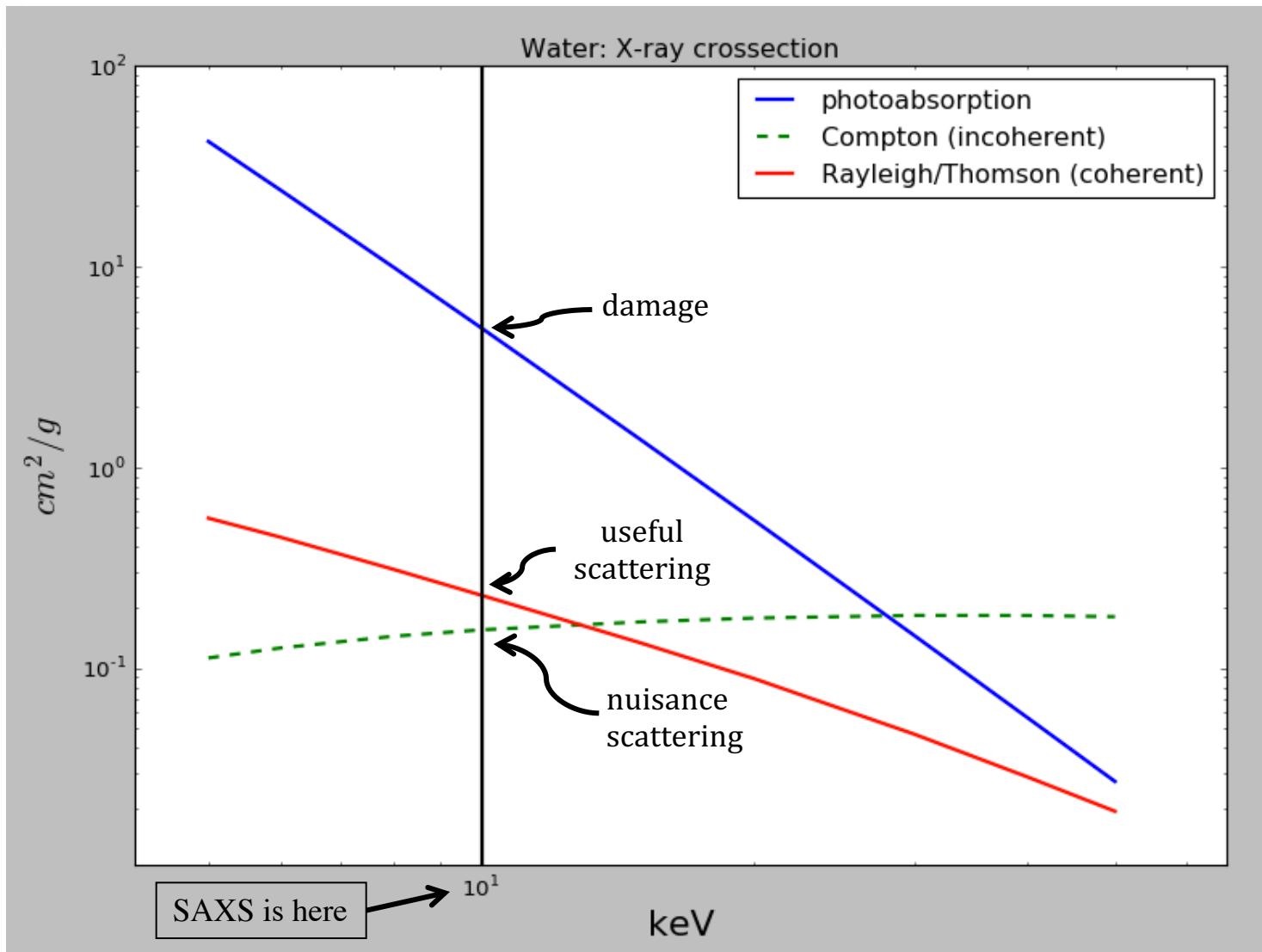
Scattering of **photons** by the nucleus does happen, it's just far too weak to observe.
Neutrons, on the other hand, are scattered by the nucleus very effectively: SANS!

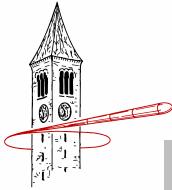
*when photon Energy > 1 MeV: photonuclear effects, pair production, Delbrück scattering etc.



Energy and X-ray Damage

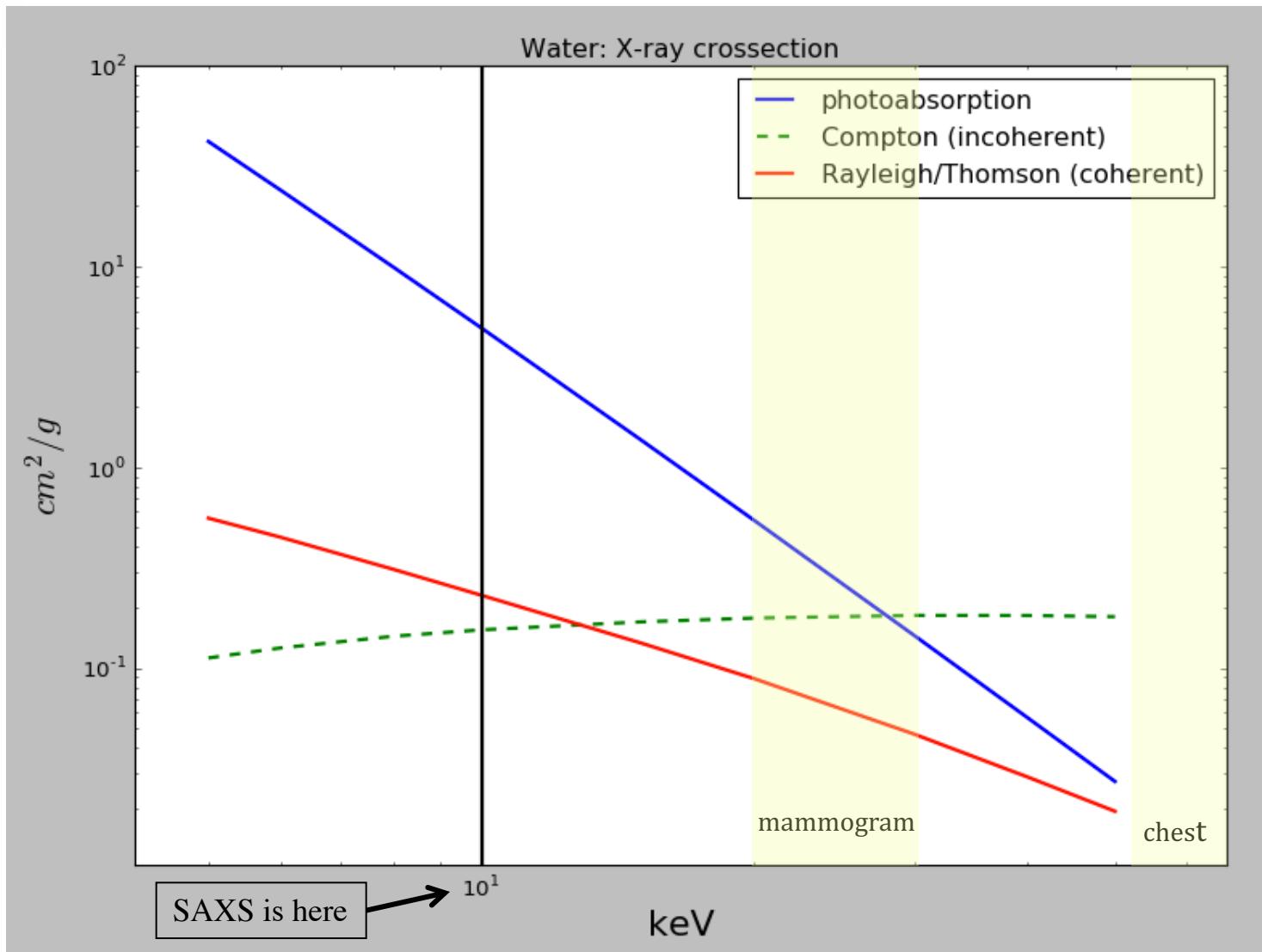
MacCHESS
CHESS

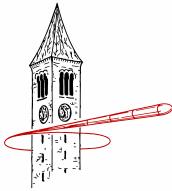




The sad reality of biology with X-rays

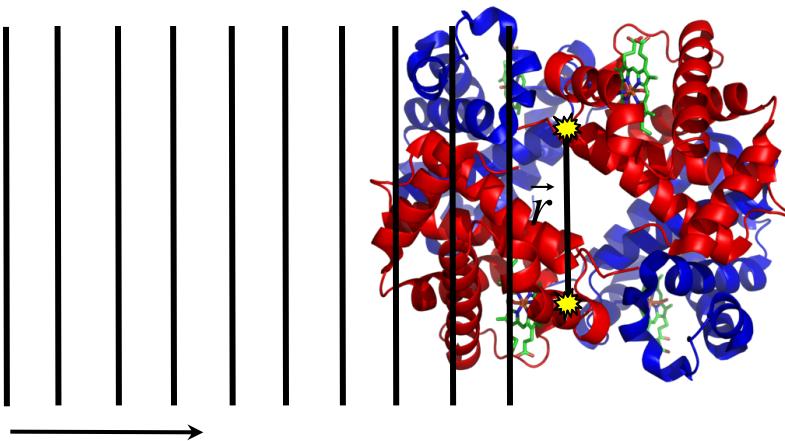
MacCHESS
CHESS



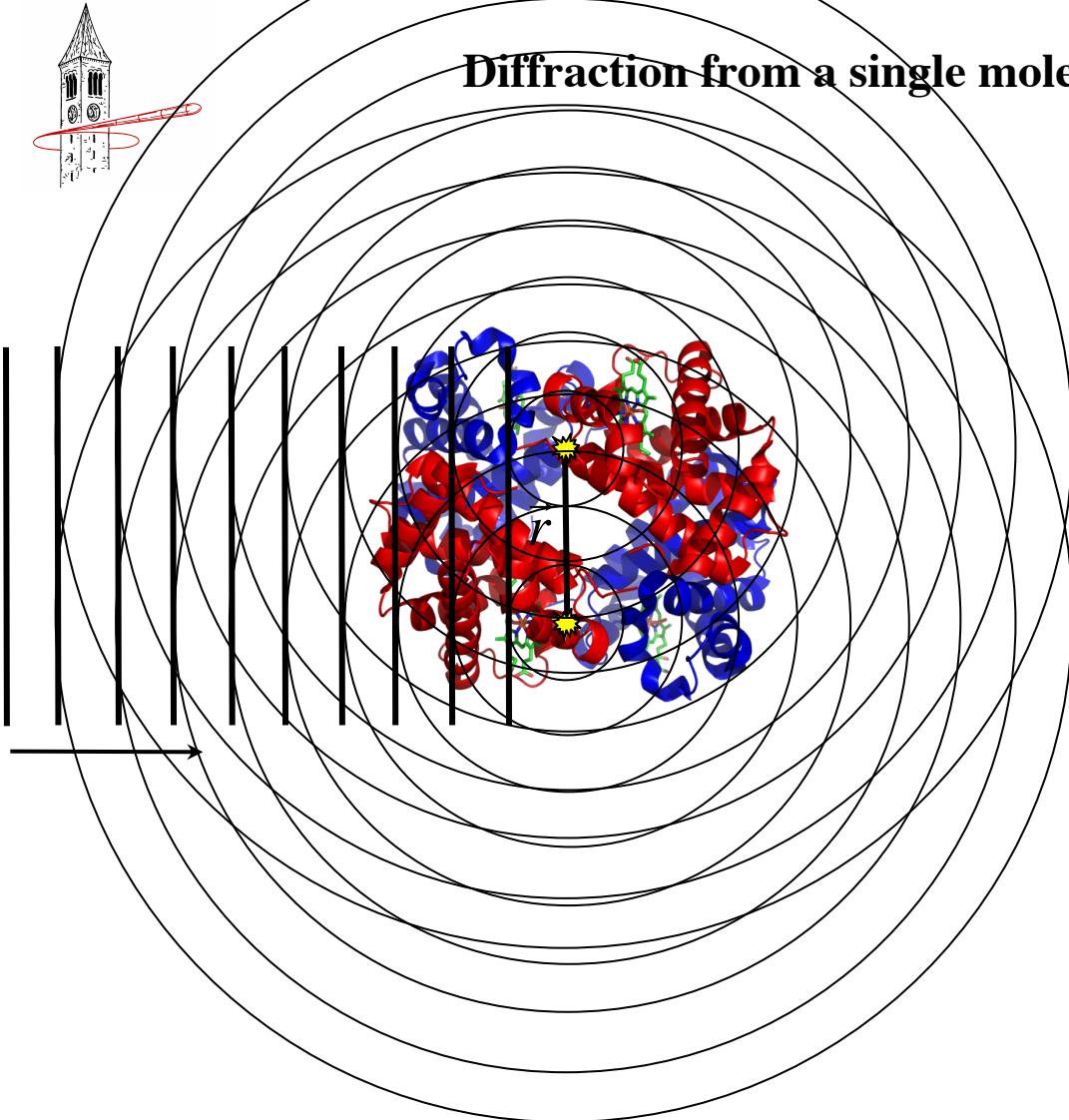


Diffraction from a single molecule

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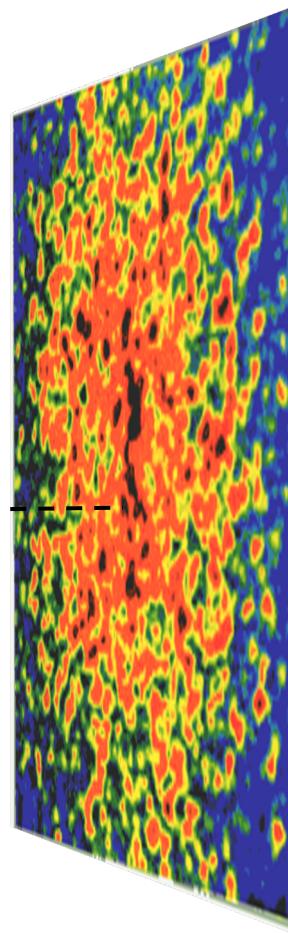
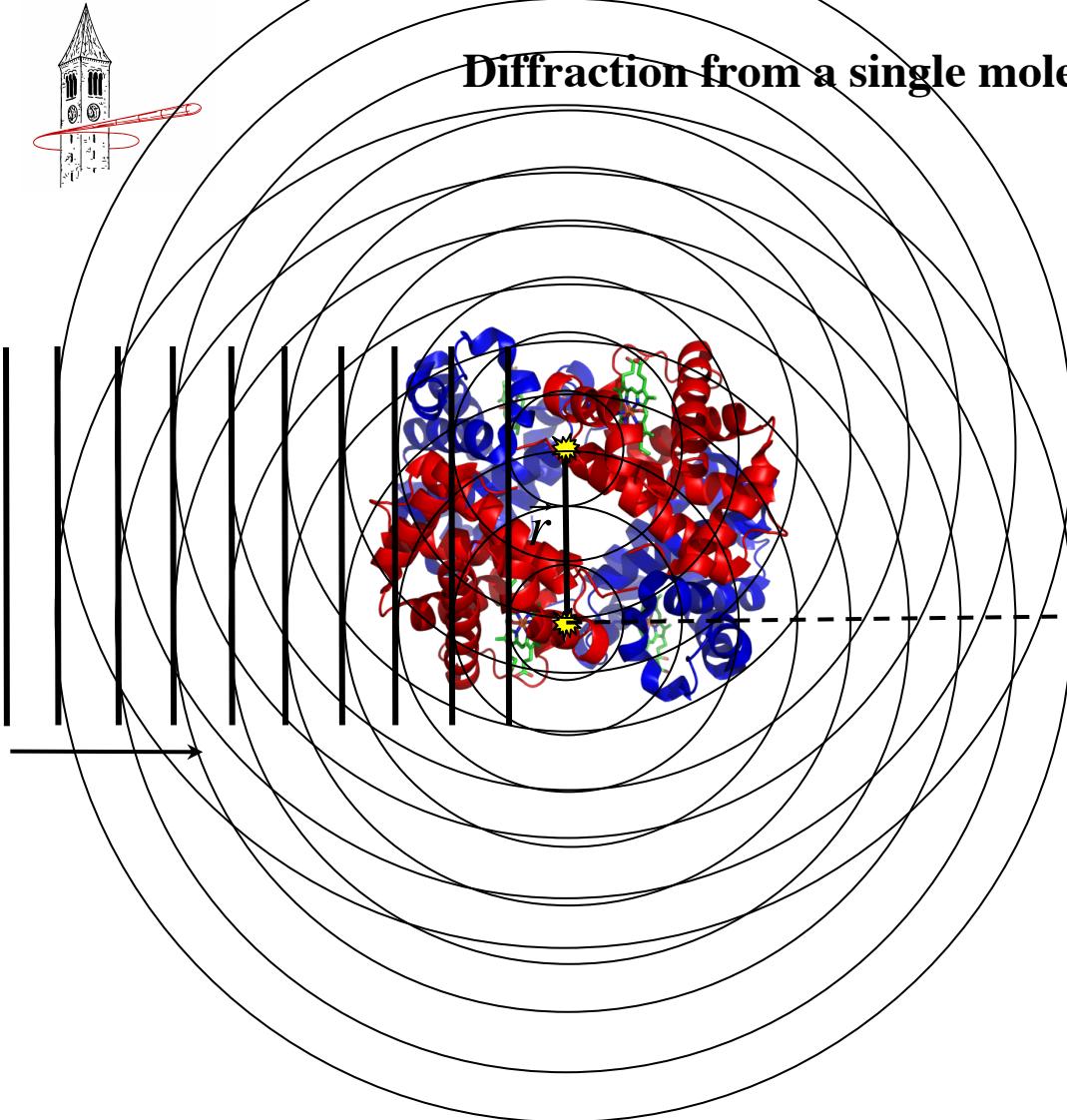


Diffraction from a single molecule



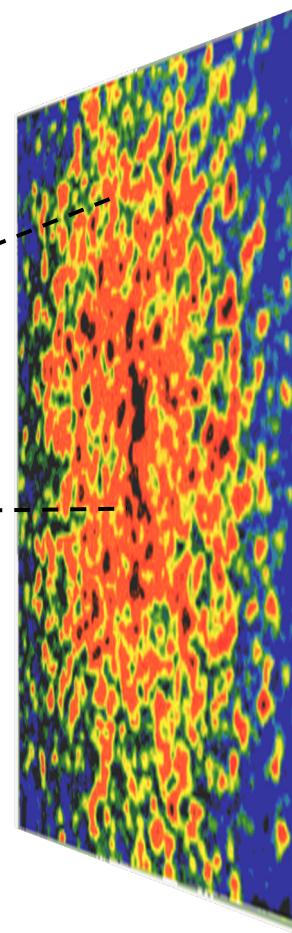
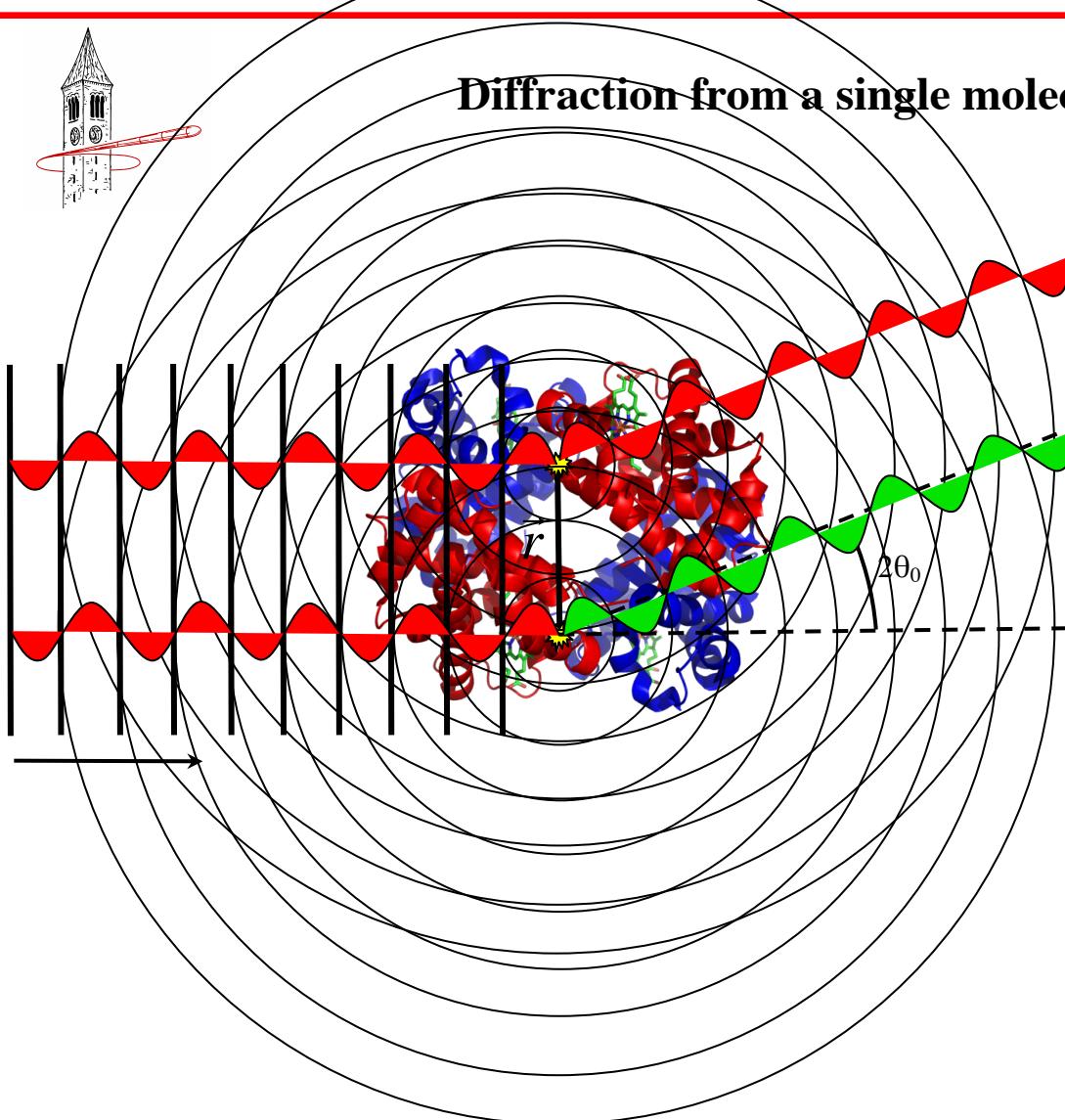
MacCHESS
CHESS

Diffraction from a single molecule



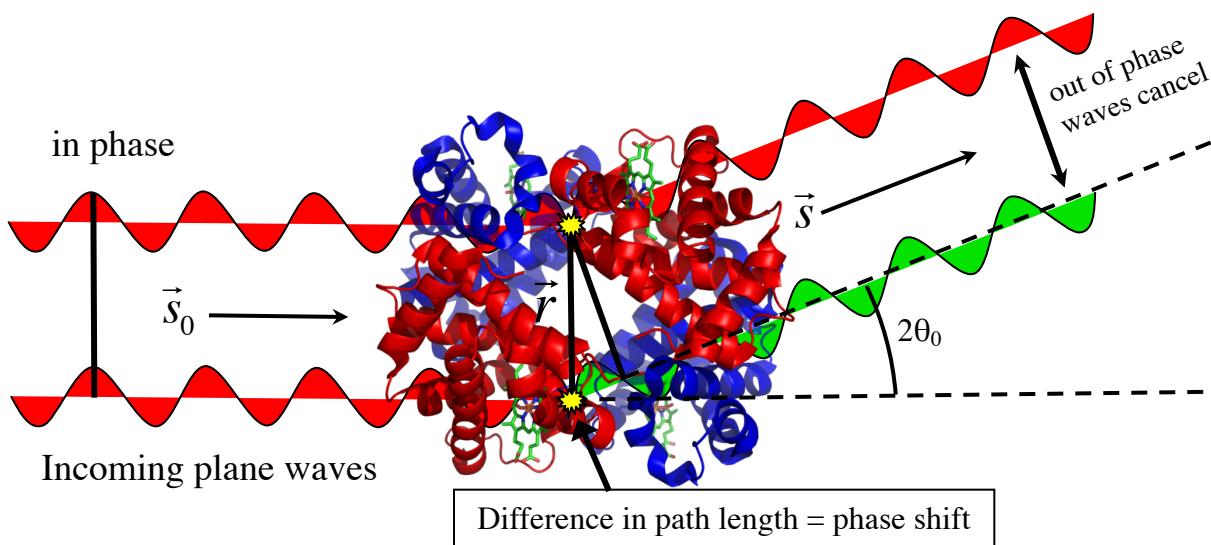
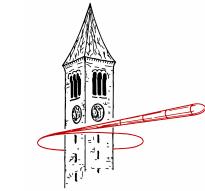


Diffraction from a single molecule

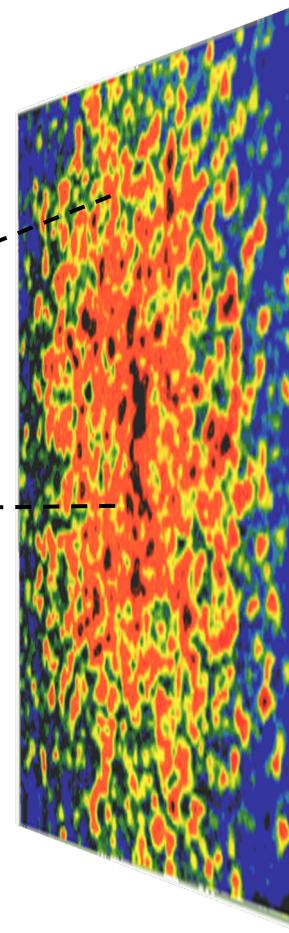


MacCHESS
CHESS

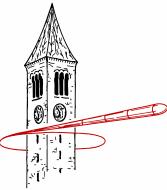
Diffraction from a single molecule



Waves scattered from different parts of the molecule result in phase shifts – a speckled intensity pattern on detector

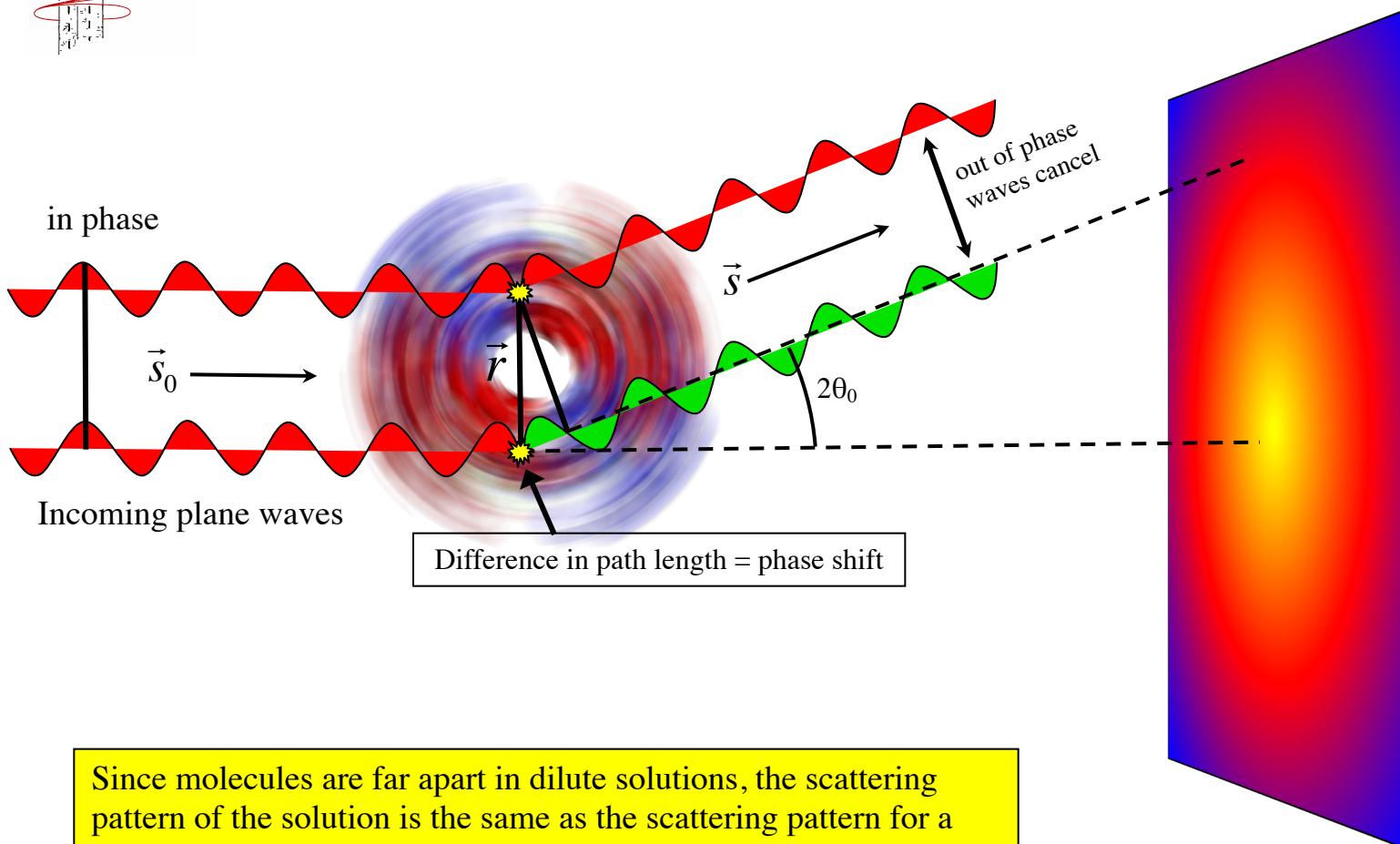


Far-field diffraction pattern



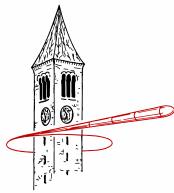
Diffraction from a rotationally-averaged molecule

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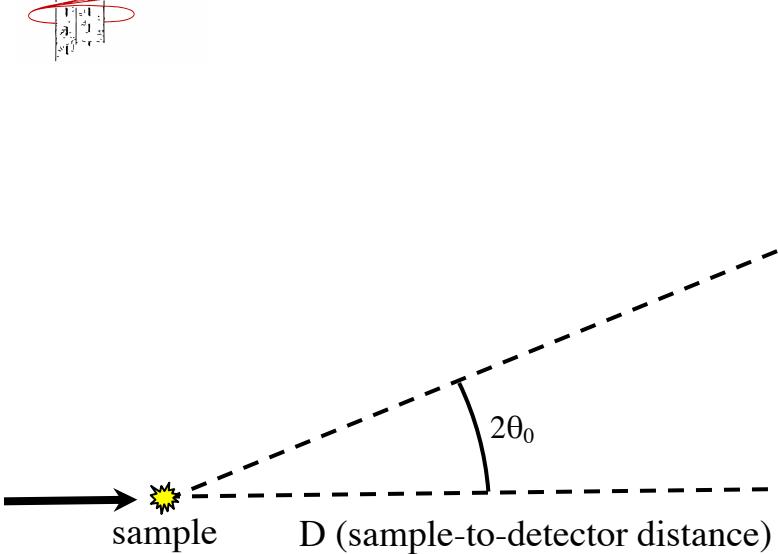


Since molecules are far apart in dilute solutions, the scattering pattern of the solution is the same as the scattering pattern for a single rotationally-averaged molecule.

Far-field diffraction pattern



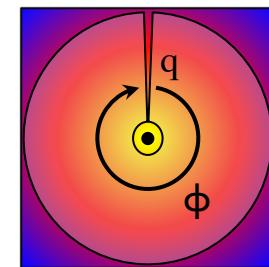
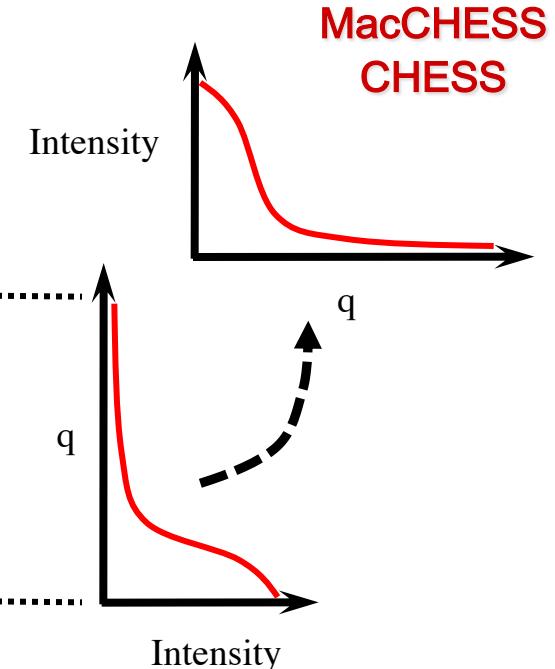
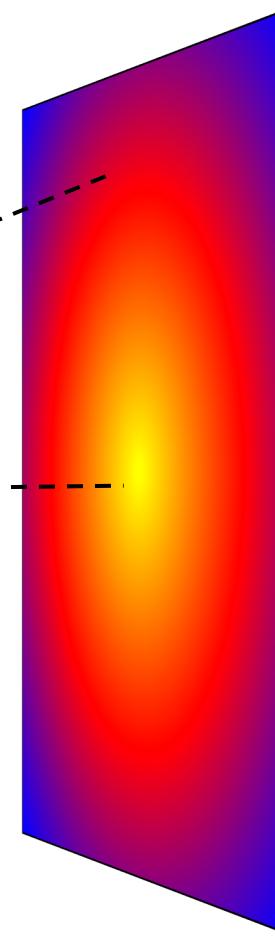
The Scattering Profile



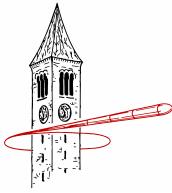
The *scattering profile* is the intensity as a function of “q”, the special reciprocal space coordinate that is proportional scattering angle at small angles. $I(q)$

$$q = 4\pi \sin(\theta) / \lambda \quad (\propto \theta \text{ for small } \theta)$$

Far-field diffraction pattern

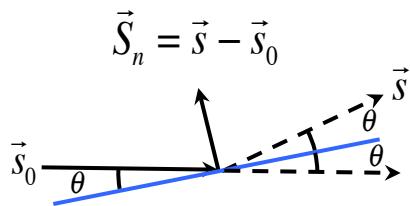
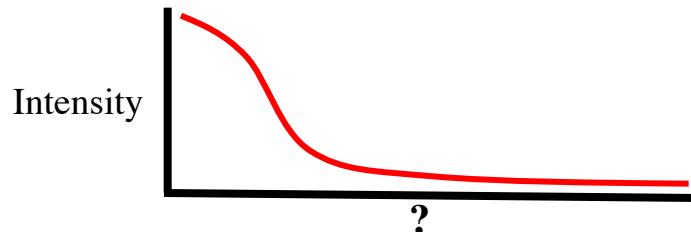


$I(q)$ is obtained by integrating around the circle. For detectors, the standard deviation of signal $\sigma(q)$ is also calculated.



Most important variable in SAXS: \mathbf{q} , \mathbf{s} , or ... \mathbf{h} ??

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Can be viewed as light S_0 reflecting off a fictitious **mirror plane**. Normal vector to plane, \vec{S}_n , is the momentum transferred.

$$\|\vec{S}\|^2 = (\vec{s} - \vec{s}_0) \cdot (\vec{s} - \vec{s}_0) = 2 - 2\cos(2\theta) = (2\sin(\theta))^2^*$$

$$\frac{2\pi\|\vec{S}_n\|}{\lambda} = \frac{4\pi\sin(\theta)}{\lambda} = \text{Oscillations of radiation (in radians) per unit length}$$

Sometimes called **momentum transfer**. Can have units of \AA^{-1} , or sometimes nm^{-1} .

$h = 4\pi \sin(\theta)/\lambda$ [Guinier & Fournet (1955); Glatter & Kratky (1982)]

$s = 4\pi \sin(\theta)/\lambda$ [Feigin & Svergun (1987)]

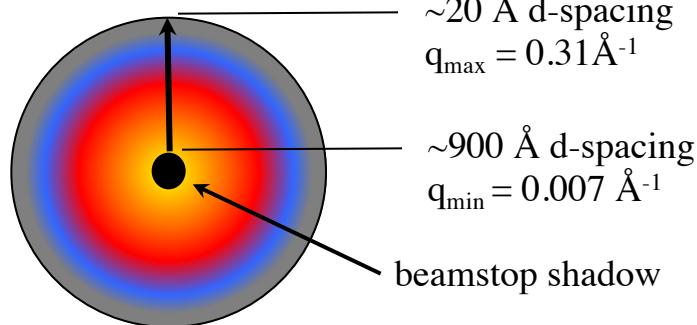
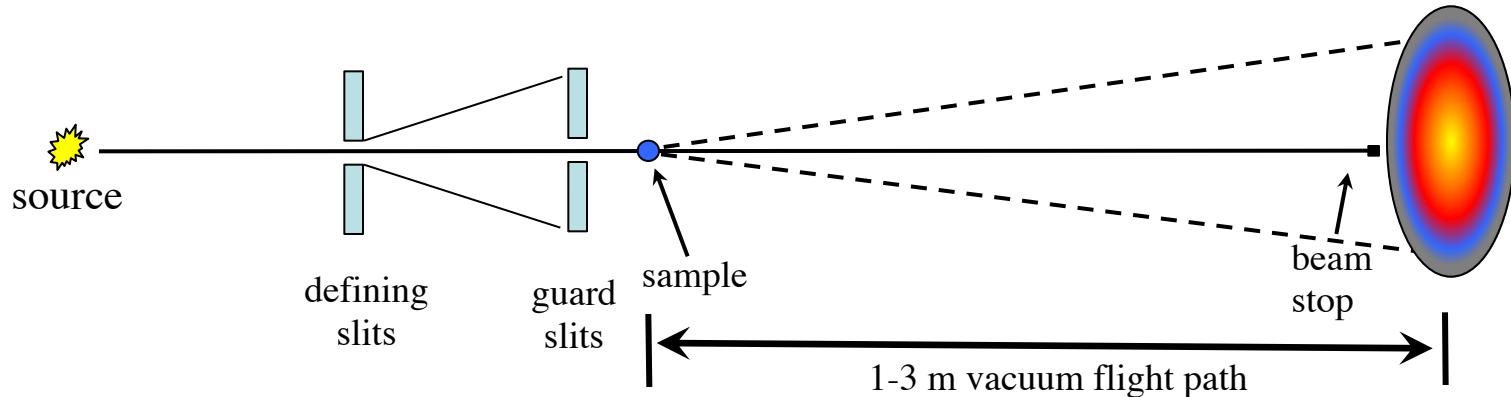
$q = 4\pi \sin(\theta)/\lambda$ [Putnam, Hammel, Hura & Tainer (2007); Jacques & Trehewella (2010)]

Sometimes you will see $s = 2\sin(\theta)/\lambda$ because $1/s = \text{"d-spacing"}$ (resolution in crystallography).

* $\|\mathbf{S}\| = \|\mathbf{S}_0\| = 1$ $\vec{S} \cdot \vec{S}_0 = \cos(2\theta)$ $1 - \cos(2\theta) = 2\sin^2(\theta)$ (*double-angle formula*)

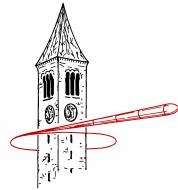
Simplified diagram of SAXS setup

typically 7-12 keV (1.7 Å - 1.0 Å). - practical high-energy limit ~20 keV

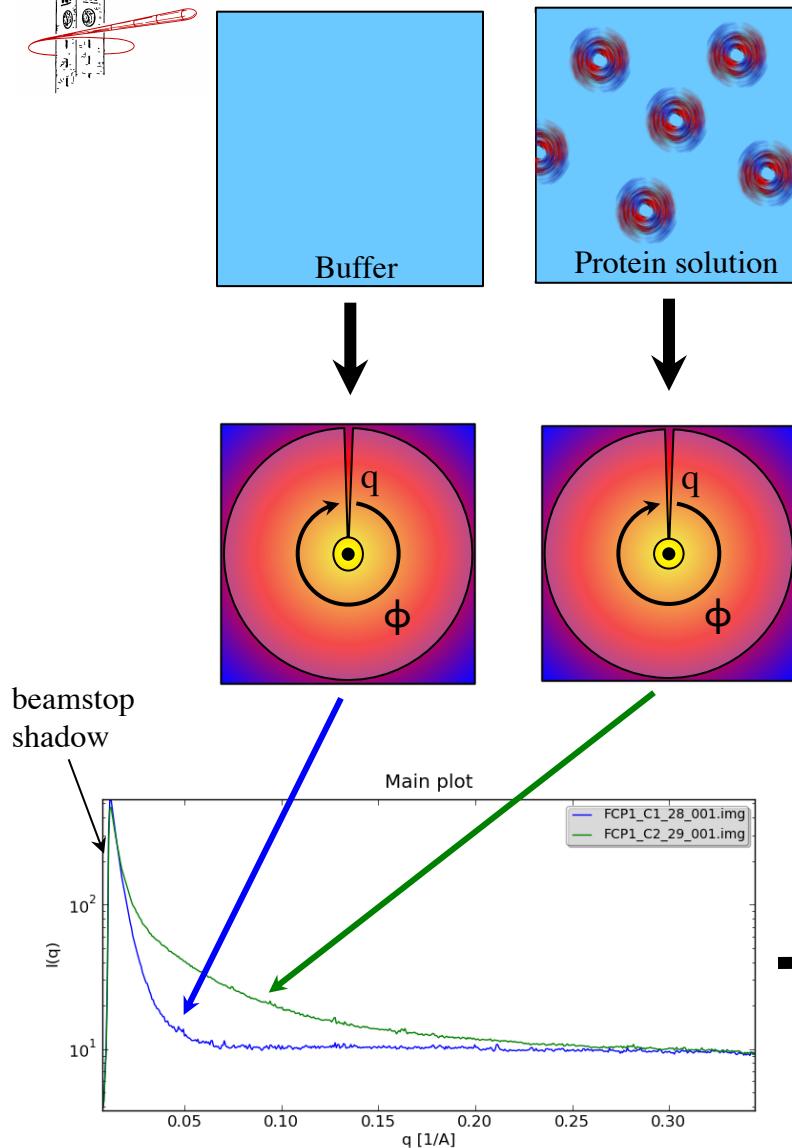


$$q = 4\pi \sin(\theta)/\lambda$$

As you get lower in scattering angle (smaller q), the background scatter gets VERY high – this ultimately limits how low you can go and how large of molecules you can study.



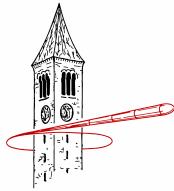
Real protein signal is obtained by buffer subtraction



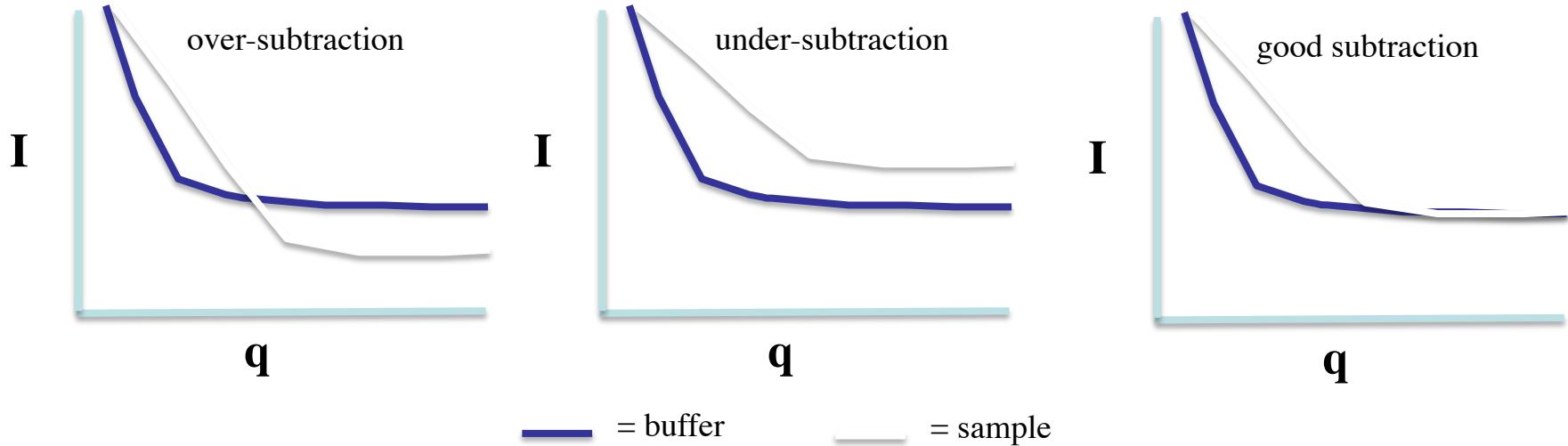
$$I_{protein} = I_{solution} - \alpha I_{buffer}$$

Scattering pattern for protein in vacuum is obtained by subtracting separate images normalized to the same exposure. The normalization constant α can be obtained in several ways:

1. Assume no beam decay: $\alpha = 1$
2. Average before and after buffers
3. Scale so that tails of protein and buffer meet
4. Use transparent beamstop to integrate direct beam
- 5. Integrate beamstop diode readings**



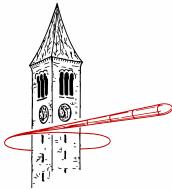
Perfect “buffer match” is everything in BioSAXS



Small changes in concentration of salts and additives can result in change of baseline scattering level

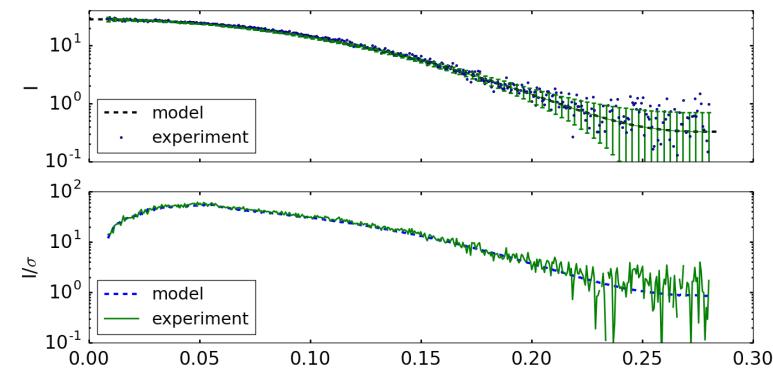
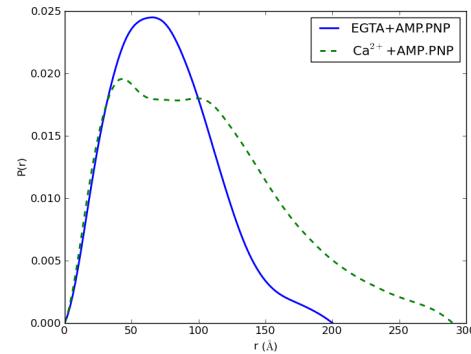
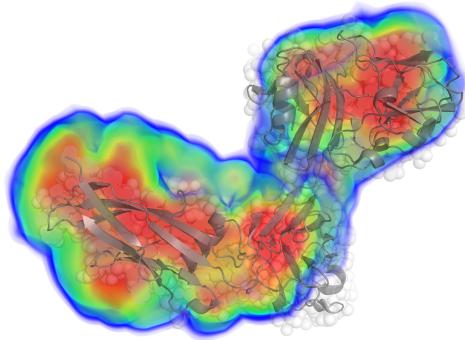
How to get matching buffer:

1. Use buffer from a size-exclusion chromatography run
2. Change to known buffer using centrifugal concentrator
3. Change buffer using dialysis
4. Use a “desalting” spin column



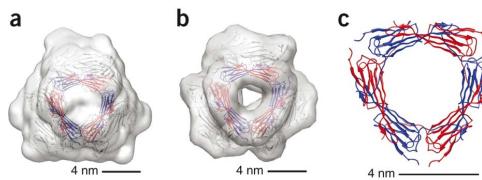
BioSAS tells you about how biomolecules behave in solution!

- quantifying **flexibility**, **disorder**, and **unfolding** in biomolecules.
- tracking of **time-resolved** structural changes (sub-milliseconds and longer)
- study of molecular crowding and **high-concentration** samples
- determination of **conformational changes** induced by binding ligands etc.
- characterizing the **ensembles** of conformations **in solution**.
- measurement of molecular weight, radius of gyration, and maximum length
- identification of physiological **oligomeric states**
- determination of structural **stability limits**
- **verification** of proposed molecular **models**
- **assembly of complexes** from known domain structures (pseudoatomic)
- calculation of true low-resolution **electron density** *in solution*.

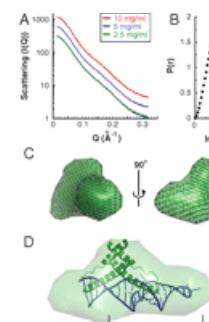


Specific Applications of BioSAXS

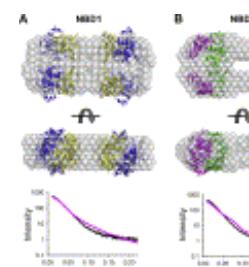
- combining NMR with SAXS to build oligomers from monomers
- **are some parts of the protein extended or disordered in solution?**
- comparing Lit vs. dark states of photoactive proteins
- comparing ligand-induced conformational changes
- adding and refining loops to homology models
- determining spatial distributions of domains connected by flexible linkers
- modeling changes in protein interaction with salt concentration and cation type
- determine fractions of monomer and dimer with change in ionic strength/additives
- categorizing discrete folded and unfolded states
- monitoring changes in protein stability with additives (stabilization due to binding)
- combining computational docking with SAXS data to improve hit rate
- building pseudoatomic models from known fragments and homology models



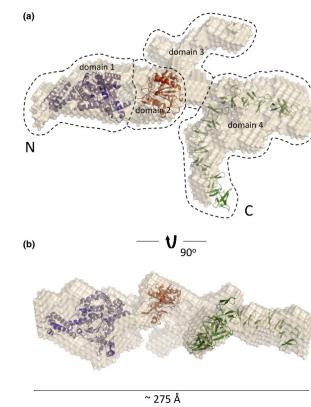
Jehle S, et al. Nat Struct Mol Biol. 2010 Sep;17(9):1037-42.



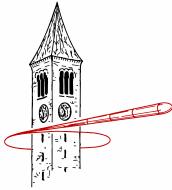
Daugherty MD, et al. Proc Natl Acad Sci U S A. 2010 Jul 13;107(28):12481-6



Park S, et al. J Struct Biol 2010 Feb; 169(2):243-51



Albesa-Jove D, et al. J Mol Biol. 2010 Mar 12;396(5):1260-70.



Sample characteristic

Purity
(monodispersity)

Oligomeric State

Shape/anisometry

Flexibility
Folded/Non-folded

Interparticle
Interactions

Conformation

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141

Sample characteristic

Basic parameter/data

Purity
(monodispersity)

Guinier plot

Oligomeric State

Particle volume,
Molecular Mass

Shape/anisometry

Envelope, R_g ,
 $P(r)$ function

Flexibility
Folded/Non-folded

Porod exponent,
Kratky plot

Interparticle
Interactions

Concentration
Series

Conformation

$I(q)$

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141

Sample characteristic

Basic parameter/data

Program/method

Purity
(monodispersity)

Guinier plot

Mixture analysis
OLIGOMER, SVD,
EFA

Oligomeric State

Particle volume,
Molecular Mass

Docking: CORAL,
FoXSdock

Shape/anisometry

Envelope, R_g ,
 $P(r)$ function

Ab initio modelling
DAMMIF, DENSS

Flexibility
Folded/Non-folded

Porod exponent,
Kratky plot

Mult. conformations
SCATTER, EOM

Interparticle
Interactions

Concentration
Series

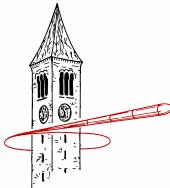
Interaction
potentials

Conformation

$I(q)$

Compare to model
Crysol, FoxS

Based on H.D.T. Mertens, D.I. Svergun / Journal of Structural Biology 172 (2010) 128–141



Example of SAXS titration and model validation

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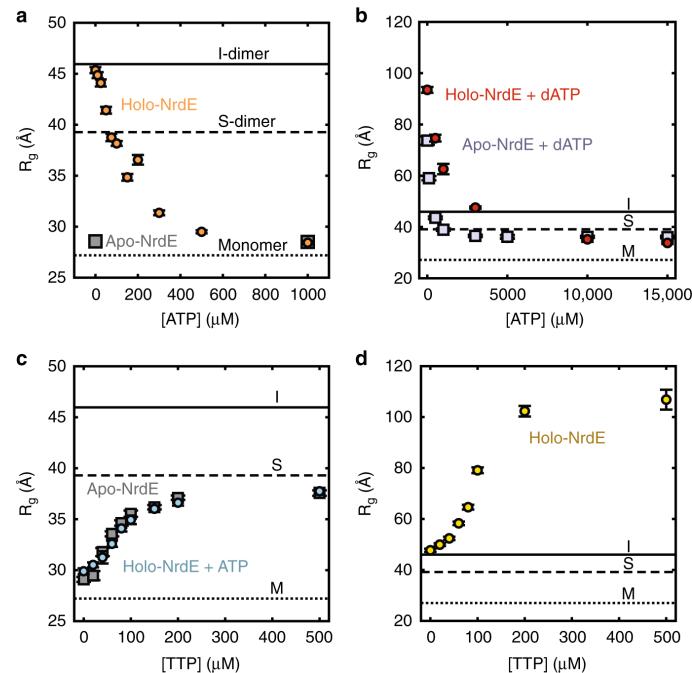
Thomas, W.C., Brooks, F.P., Burnim, A.A. et al. Convergent allosteric in ribonucleotide reductase. *Nat Commun* **10**, 2653 (2019).
<https://doi.org/10.1038/s41467-019-10568-4>

Study combines:

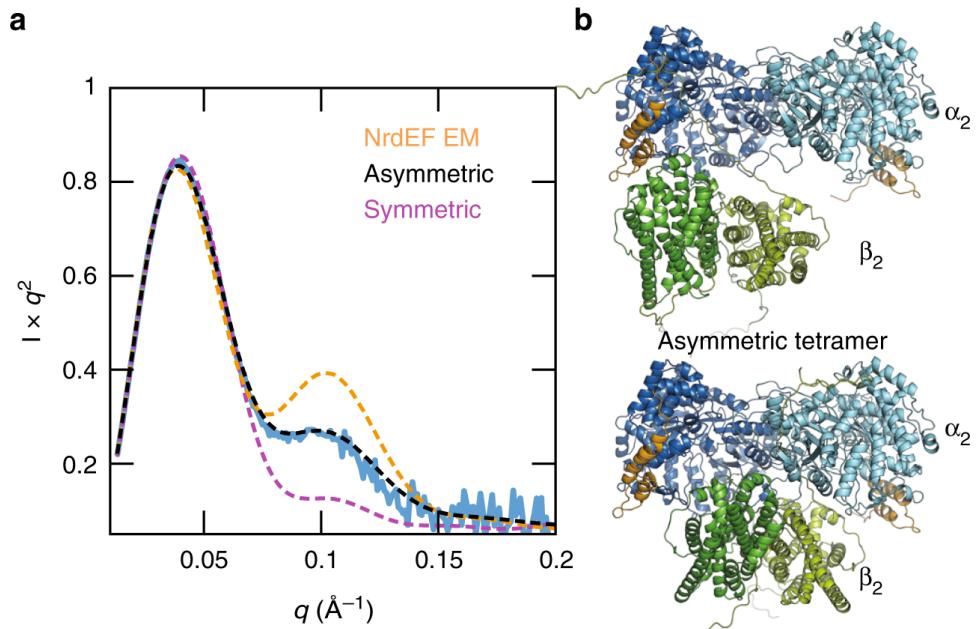
- SAXS
- cryoEM
- crystallography

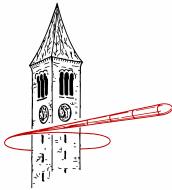
“Reversible interconversion of six unique structures ...
conformational gymnastics necessary for RNR activity”

Watching R_g of a complex change while titrating in ATP:



Comparing models to data:





Example of how basic SAXS data complement a larger study

[BMC Biol.](#) 2018 Jul 11;16(1):76.

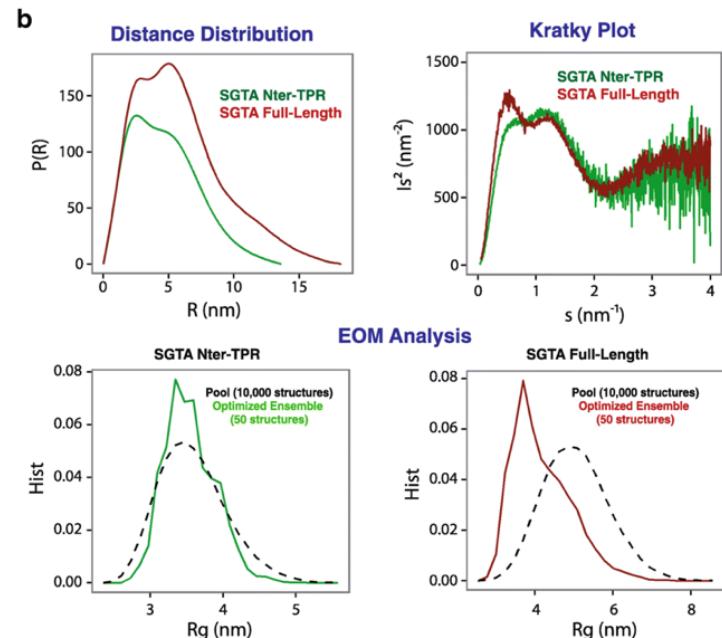
Structural complexity of the co-chaperone SGTA: a conserved C-terminal region is implicated in dimerization and substrate quality control.

[Martínez-Lumbreras S¹](#), [Krysztofinska EM¹](#), [Thapaliya A¹](#), [Spilotros A²](#), [Matak-Vinkovic D³](#), [Salvadori E^{4,5}](#), [Roboti P⁶](#), [Nyathi Y^{6,7}](#), [Muench JH¹](#), [Roessler MM⁴](#), [Svergun DI²](#), [High S⁶](#), [Isaacson RL⁸](#).

- Confirmed dimeric state
- P(r) function confirms domains with 5 nm separation
- P(r) also confirms full-length protein is more compact than truncated
- Kratky indicates moderate flexibility
- EOM also shows how full-length construct is more compact

SAXS combined with

- Native mass spectrometry (shows dimer in solution)
- NMR
- EPR spectroscopy (DEER)
- DLS
- CD



Example of sophisticated pseudoatomic homology model building and refinement

oxygen-sensing FixL-FixJ

(Wright et al. Sci. Signal. 11 10 April 2018)

Data from:

- crystallography
- SEC-SAXS
- Existing fragments from PDB
- homology modeling
- Validation of part of model via SAXS on truncated protein

Software:

- JPred, Coils (which parts are helices vs coils)
- PEP-FOLD generate models of linkers
- Torsion angle MD in CNS to refine positions of domains and loops
- SWISS-MODEL to generate homology model
- HADDOCK to refine and dock domains
- pyDockSAXS and FoXS-Dock for placement of domains
- FTDock/Crysol and PatchDock/FoXS

