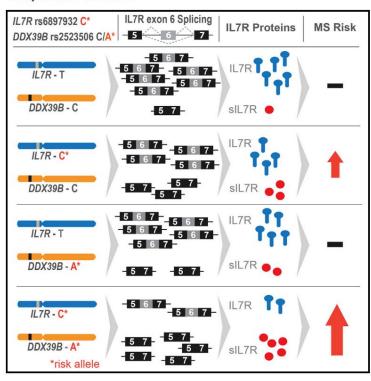
Lectures 6-7: robust statistical approaches for RNAseq

- RNA-seq is biased but quantitative: what are semi-parametric approaches for analyzing expression?
- How to test genetic interactions w/ RNA-expression

Splicing pinpointed as 'causal factor' in MS

Graphical Abstract



IL7R splicing changes its interaction with the immune system

The splicing factor has a mutant with epistatic control over this variant

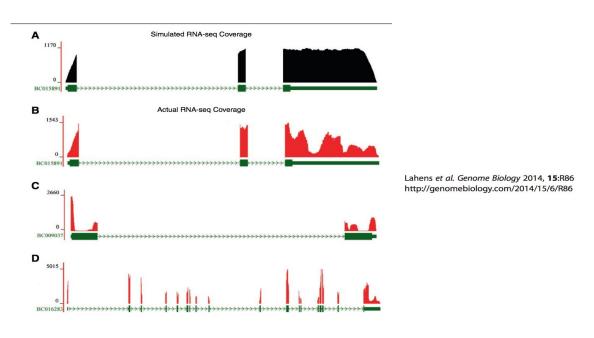
The facebook profile of RNA-seq: perfect statistical models

- Many models assume each RNA isoform is sampled at Poisson(a \lambda_i) where a is a bias constant proportional to the abundance of the transcript
- 2. Modified models use the negative binomial
- 3. These assumptions doesn't hold, as we will see
- 4. (similar problems with DNA)

Testing for differential expression of RNA requires non-parametric approaches

Why we need robustness: motivation by GTEx and IVT-Seq

Exon level data-- discovering relationships and isoforms?



Extreme biases in RNA-seq: no theoretical null

Lahens et al. Genome Biology 2014, **15**:R86 http://genomebiology.com/2014/15/6/R86

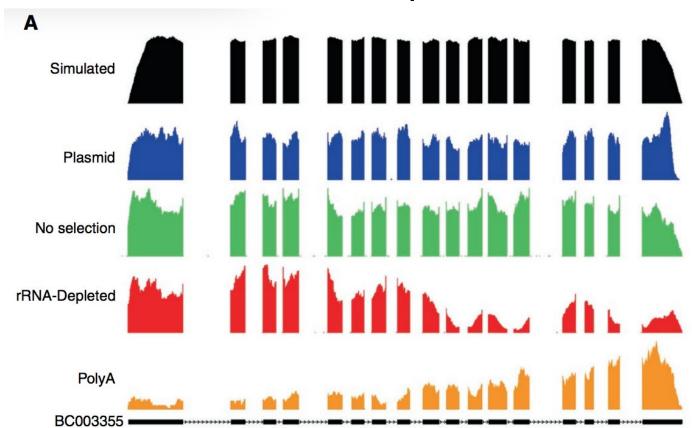


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IVT-seq reveals extreme bias in RNA sequencing

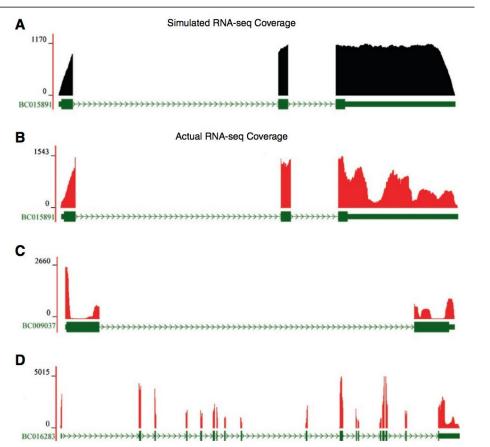
Nicholas F Lahens¹, Ibrahim Halil Kavakli^{2,3}, Ray Zhang¹, Katharina Hayer⁴, Michael B Black⁵, Hannah Dueck⁶, Angel Pizarro⁷, Junhyong Kim⁶, Rafael Irizarry⁸, Russell S Thomas⁵, Gregory R Grant^{4,9} and John B Hogenesch^{1*}

Extreme bias in RNA-seq



Lahens et al. Genome Biology 2014, **15**:R86 http://genomebiology.com/2014/15/6/R86

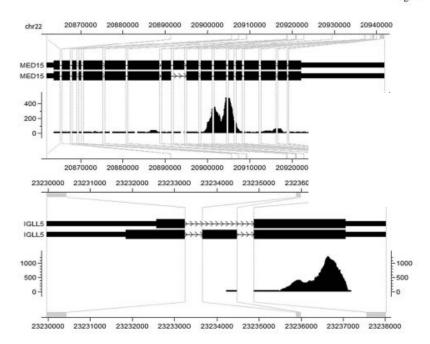
Simulations and intuition don't match real data



Lahens et al. Genome Biology 2014, **15**:R86 http://genomebiology.com/2014/15/6/R86

Model based approaches

Jiang and Salzman Page 15



$$= \sum_{j=1}^{J} \left\{ n_j \ln \left(\sum_{i=1}^{I} \theta_i a_{ij} e^{b_j} \right) - \sum_{i=1}^{I} \theta_i a_{ij} e^{b_j} \right\} - \lambda \sum_{j=1}^{J} |b_j|$$
 (2.3)

Genes discovered by non-parametric analysis

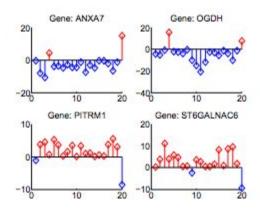


Figure 4: Count difference of the top four genes discovered only by the sign test. X-axis: sample index; Y-axis: gene expression level.

https://arxiv.org/pdf/1801.04005.pdf

Opportunities for discovery using robust statistics and massive data

Motivation by Gtex

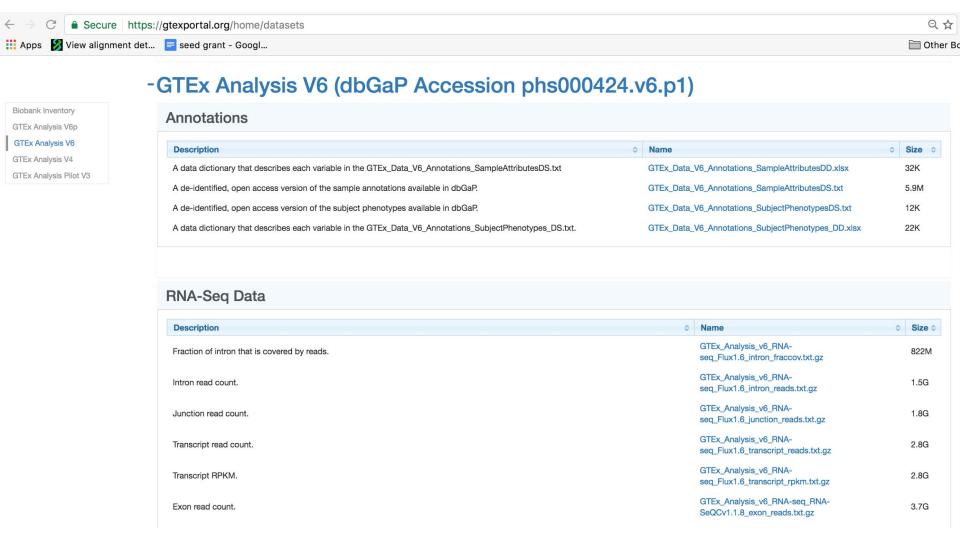
Describe data: clinical data https://gtexportal.org/home/datasets

And a great deal of information on genotype/RNA expression

https://gtexportal.org/home/tissueSummaryPage#cause

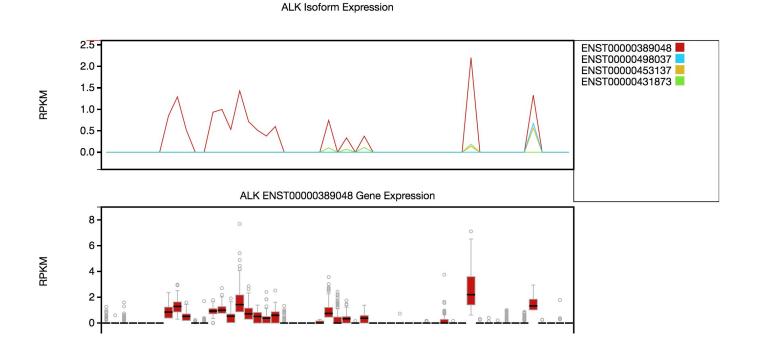
https://gtexportal.org/home/gene/SMN2

But, statistics are not interpretable



Motivation by Gtex

Question: differential isoform expression: example-- real differences, or artifacts?



How do we overcome these problems?

- Learn statistical theory and methods
- Designing our own custom test that captures intuition, then analyze its properties

Does the bootstrap or permutation test break down?

FDR control by knockoffs (Candes')

Bootstrap breakdown (Lehman and Romano)