

$$R = \begin{matrix} & \begin{matrix} i_1 & i_2 & i_3 & i_4 \end{matrix} \\ \begin{matrix} u_1 \\ u_2 \\ u_3 \end{matrix} & \begin{pmatrix} 3 & & 0 & \\ & 2 & & 1 \\ 1 & & \square & \end{pmatrix} \end{matrix}$$

Link prediction (centrality)

Collaborative filtering w/ context

Row or column

Low Rank Factorization by SVD

Rank deficient means:

- There are a "small" # of independent users or items.

By SVD: $R = U \Sigma V^T$

Assume R is of Rank $k \ll m$ or n

$$R = \begin{matrix} & k \\ \begin{matrix} \text{ } \end{matrix} & \begin{matrix} \text{ } \end{matrix} \end{matrix} = \begin{matrix} k \\ \begin{matrix} \text{ } \end{matrix} \end{matrix} \begin{matrix} \text{ } \\ U \end{matrix} \begin{matrix} k \\ \begin{matrix} \text{ } \end{matrix} \end{matrix} \begin{matrix} \text{ } \\ \Sigma \end{matrix} \begin{matrix} k \\ \begin{matrix} \text{ } \end{matrix} \end{matrix} \begin{matrix} \text{ } \\ V^T \end{matrix}$$

1. Choose Random $U_k \Sigma_k V_k^T$

2. Compute $\tilde{R} = U_k \Sigma_k V_k^T$

3. Compare R with \tilde{R} only w/ known entries

4. Update U_k, Σ_k, V_k^T