



A system  $f(x)$  is linear iff

$$p(a) = 3a + 2$$

$$f(kx) = kf(x)$$

$$p(a)$$

$$f(x_1 + x_2) = f(x_1) + f(x_2)$$

$$p(2) = 8$$

$$p(3 \times 2) = 3p(2)$$

$$= 3(8) = 24$$

$$f(k_1x_1 + k_2x_2) = k_1f(x_1) + k_2f(x_2)$$

$$p(6+2) = p(6) + p(2)$$

Is  $f(x) = 3x^2$  linear? NO

$$f(kx) = 3(kx)^2 = 3k^2x^2$$

$$kf(x) = 3kx^2$$

Is  $f(x) = 3x + 2$  <sup>affine</sup> linear?

$$f(kx) = 3(kx) + 2$$

$$= 3kx + 2$$

$$kf(x) = k(3x + 2)$$

$$= 3kx + 2k$$