Motifs in Biological Networks

Proteomes Interactomes and Biological Networks

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http://biofold.org/

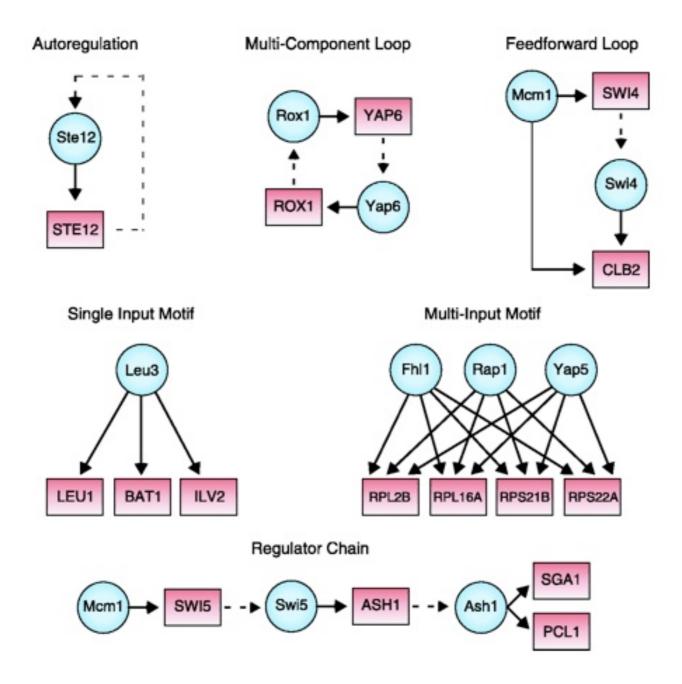


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Network Motifs

Network analysis is important for detecting network motifs, which are recurrent and statistically significant sub-graphs or patterns.



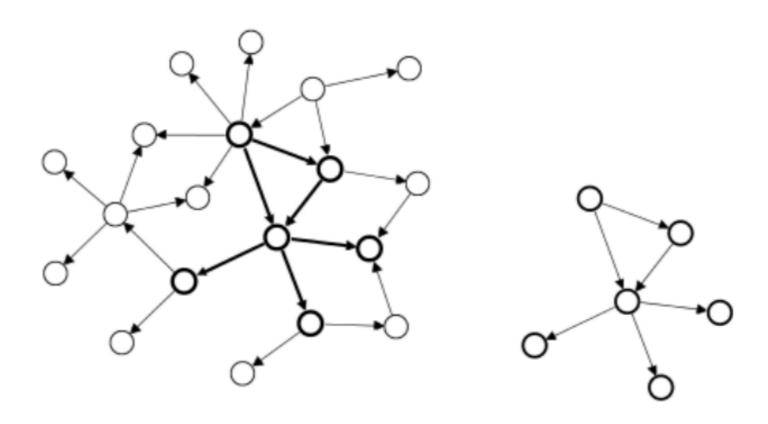
http://compbio.pbworks.com/

Motif Matching

A match of a motif G' in the target graph G = (V, E) is a subgraph G'' = (V'', E'') which is isomorphic to motif G'

Two graphs G' and G" are isomorphic if there is a bijective mapping between the edge and vertex identities

i.e. G' is transformed to G" by changing the vertex and edge identities



Problem Complexity

The complexity of graph isomorphism is in the 'grey area' of complexity:

- It belongs to NP class of problems (problems where solution is easy to verify once found)
- It is not known if graph isomorphism belongs to P class of problems (problems that can be solved efficiently)
- It is not known if graph isomorphism is NP-complete (problems that are believed to be hard ot solve but easy to verify)
- Subgraph isomorphism, checking if a subgraph G" that is isomorphic to given graph G' exists in a larger graph G, is known to be NPcomplete
- No hope for really fast algorithms for finding motifs.

Statistical Significance

A motif is a statistically overrepresented pattern of local interactions in the network

 Overrepresentation = occurring more frequently than expected by chance

 The motif has emerged several times therefore it has been conserved in the evolution of the network

 The rationale is that overrepresentation may denote possible conservation of the function

Significance tests

The statistical significance can be tested calculating the z-score of the presence of the motif on a set of randomly generated graphs obtained with

Generation of random networks with the Erdos-Renyi algorithm

Random shuffling of the edges

Detection of Motifs

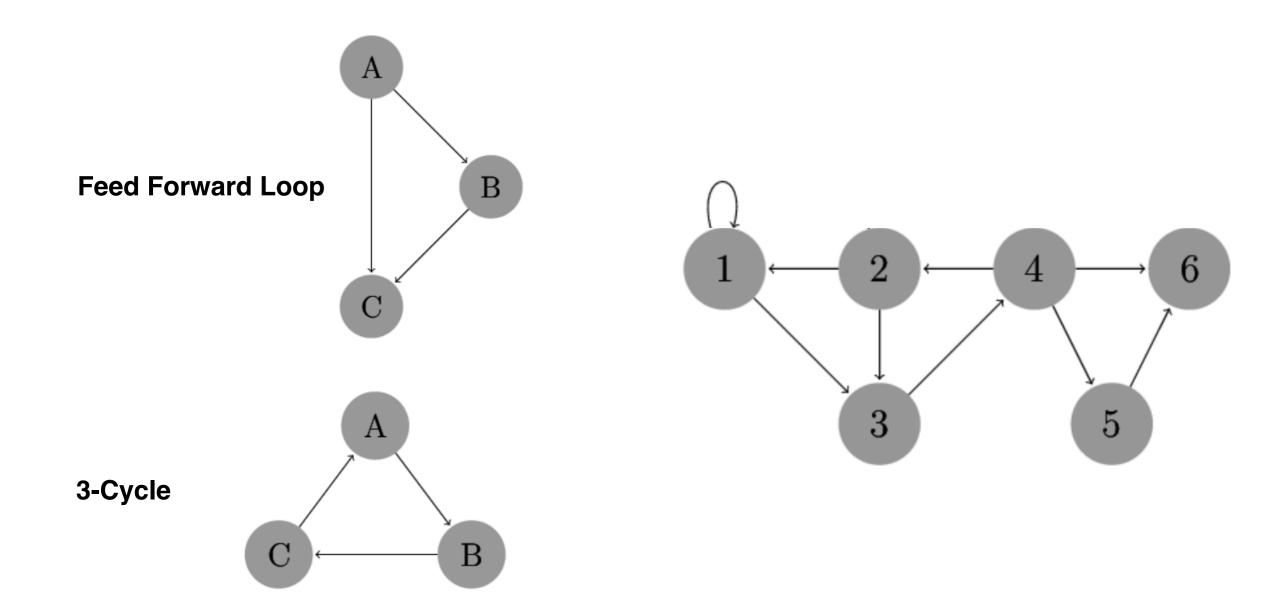
Networkx allow to select a subgraph of a the whole graph and verify if two graphs are isomorphic

```
>>> g = nx.Graph().add_nodes_from([(1,2),(1,3)])
>>> mot = nx.Graph().add_nodes_from([("A","B")])
>>> g1 = g.subgraph([1,2])
>>> nx.is_isomorphic(g1,mot)
```

Exercise

Given the Feed Forward Loop (FFL) and 3-Cycle write the code to detect the motif in the graph with 6 nodes and 8 edges.

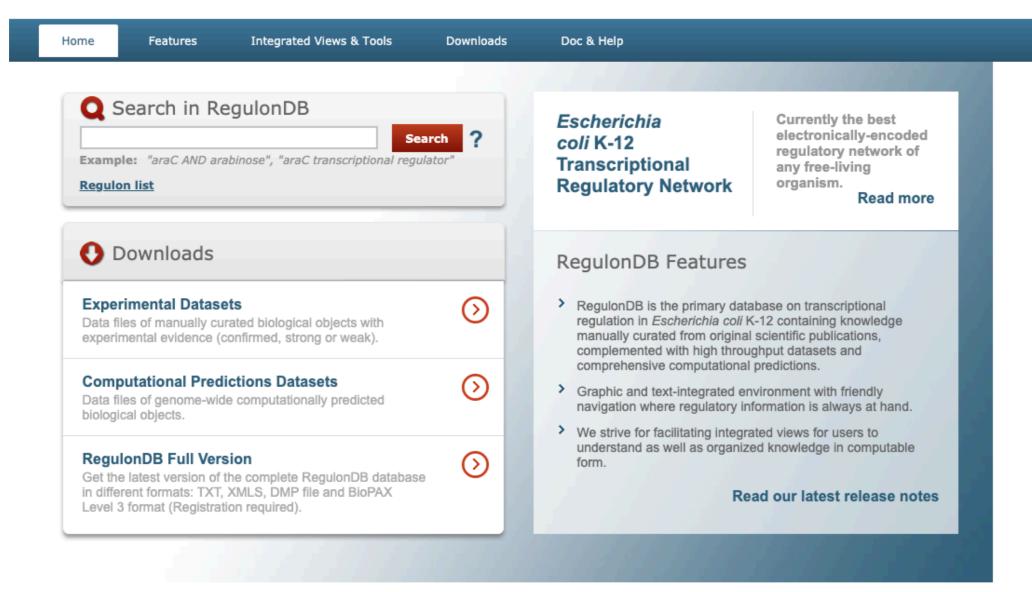
Calculate occurrence on random network and the z-score.



RegulonDB

Database of Escherichia coli K-12 Transcriptional Regulatory Network





Regulation Data

The regulation data includes information about the transcription factors (TF) that activate or repress the expression of the genes with associated supporting evidences.

```
# Release: 10.6.2 Date: 10-04-2019
# Columns:
# (1) Transcription Factor (TF) name
# (2) Gene regulated by the TF (regulated gene)
# (3) Regulatory effect of the TF on the regulated gene (+ activator, - repressor, +- dual, ? unknown)
 (4) Evidence that supports the existence of the regulatory interaction
                      [BCE, BPP, GEA, HIBSCS] Strong
AcrR
       acrA
       acrB
                      [BCE, BPP, GEA, HIBSCS] Weak
AcrR
       acrR
                      [AIBSCS, BCE, BPP, GEA, HIBSCS] Weak
AcrR
       flhC
AcrR
                      [GEA, HIBSCS] Weak
       flhD
                      [GEA, HIBSCS]
                                   Weak
AcrR
                      [BPP, GEA, HIBSCS]
AcrR
                                            Strong
       marA
                                          Strong
       marB -
                      [BPP, GEA, HIBSCS]
AcrR
       marR -
                      [BPP, GEA, HIBSCS]
                                             Strong
AcrR
AcrR
       micF
                      [AIBSCS]
                                     Weak
AcrR
                      [BPP, GEA, HIBSCS] Strong
       soxR
```

http://regulondb.ccg.unam.mx/menu/download/datasets/files/network_tf_gene.txt

Nodes ad Edges

With networkx we can assign attributes to nodes and edges

```
>>> G=nx.DiGraph()
>>> G.add_node(1, color='blue')
>>> G.add_node(2, color='red')
>>> G.add_edge(1, 2, sign='+')
>>> G.node[1]
>>> G.edge[1][2]
```

Matches Node and Edges

Matches can be performed based on node and edges attributes

```
>>> import networkx.algorithms.isomorphism as iso
>>> em=so.categorical_edge_match('sign'='+')
>>> nm=iso.categorical_node_match('color'='red')
>>> nx.is_isomorphic(G1,G2,edge_match=em, node_match=nm)
```

Exercise

Write a program to analyze the RegulonDB network considering only data with strong supporting information.

- Find the TF that regulates more genes (activation and suppression)
- Find the gene that is regulated by more TFs
- Match a graph that contains a TF activating three genes.