# Motifs, Modules and Pathways

**Proteomes Interactomes and Biological Networks** 

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http://biofold.org/

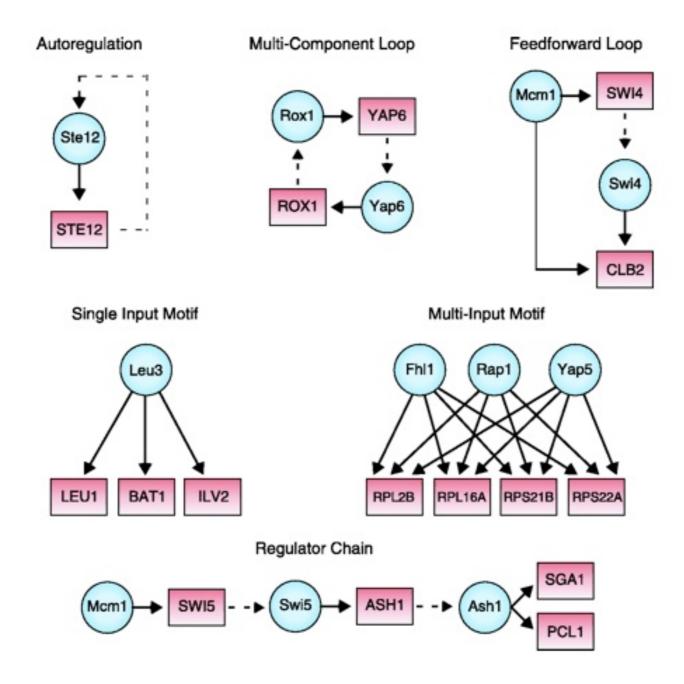


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#### **Network Motifs**

Network analysis is important for detecting network motifs, which are recurrent and statistically significant sub-graphs or patterns.



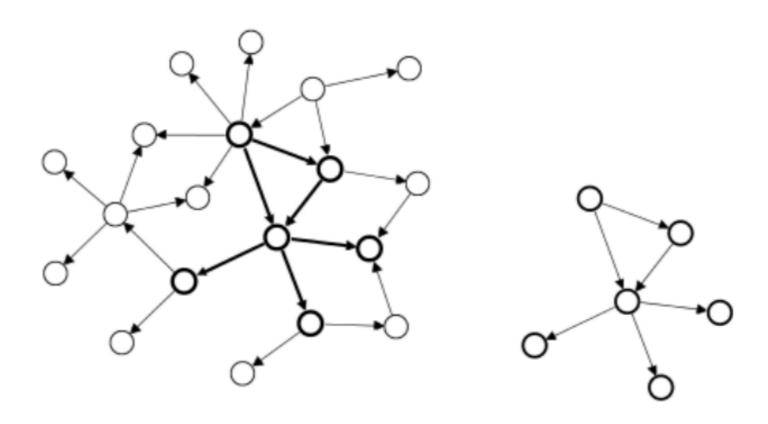
http://compbio.pbworks.com/

# **Motif Matching**

A match of a motif G' in the target graph G = (V, E) is a subgraph G'' = (V'', E'') which is isomorphic to motif G'

Two graphs G' and G" are isomorphic if there is a bijective mapping between the edge and vertex identities

i.e. G' is transformed to G" by changing the vertex and edge identities



# **Problem Complexity**

The complexity of graph isomorphism is in the 'grey area' of complexity:

- It belongs to NP class of problems (problems where solution is easy to verify once found)
- if the correspondence is known, the graph isomorphism belongs to P class of problems (problems that can be solved efficiently)
- f the correspondence is not known, the graph isomorphism is NP-complete (problems that are believed to be hard to solve but easy to verify)
- Subgraph isomorphism, checking if a subgraph G" that is isomorphic to given graph G' exists in a larger graph G, is known to be NPcomplete
- No hope for really fast algorithms for finding motifs.

# Statistical Significance

A motif is a statistically overrepresented pattern of local interactions in the network

 Overrepresentation = occurring more frequently than expected by chance

 The motif has emerged several times therefore it has been conserved in the evolution of the network

 The rationale is that overrepresentation may denote possible conservation of the function

# Significance tests

The statistical significance can be tested calculating the z-score of the presence of the motif on a set of randomly generated graphs obtained with

Generation of random networks with the Erdos-Renyi algorithm

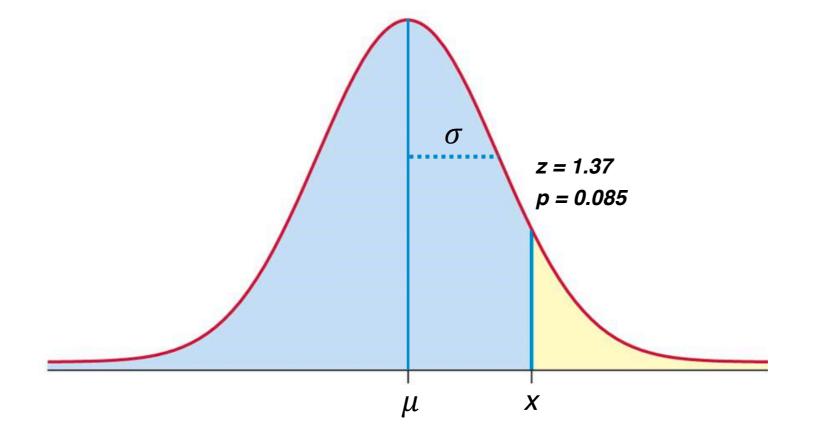
Random shuffling of the edges

#### **Z-score**

The z-score represents the distance of a number x from the mean value  $(\mu)$  of a distribution in terms of standard deviations  $(\sigma)$ 

$$z = \frac{X - \mu}{\sigma}$$

Assuming a normal distribution of the data the probability p(t>x) can be calculated as a function of the z-score



# **Empirical probability**

If the distribution of data can not be fitted to any known distribution, the empirical probability is estimated based on the fraction of the events.

Given a sorted list of measures

$$M = \{ t_1, t_2, \ldots, t_i, \ldots, t_N \}$$

being  $t_i$  the lowest measure with  $t_i > x$  the empirical probability f(t > x) can be calculates as

$$f(t>x) = \frac{N-i+1}{N} \quad \text{with } N \to \infty \quad f(t>x) \to p(t>x)$$

#### **Detection of Motifs**

Networkx allow to select a subgraph of a the whole graph and verify if two graphs are isomorphic

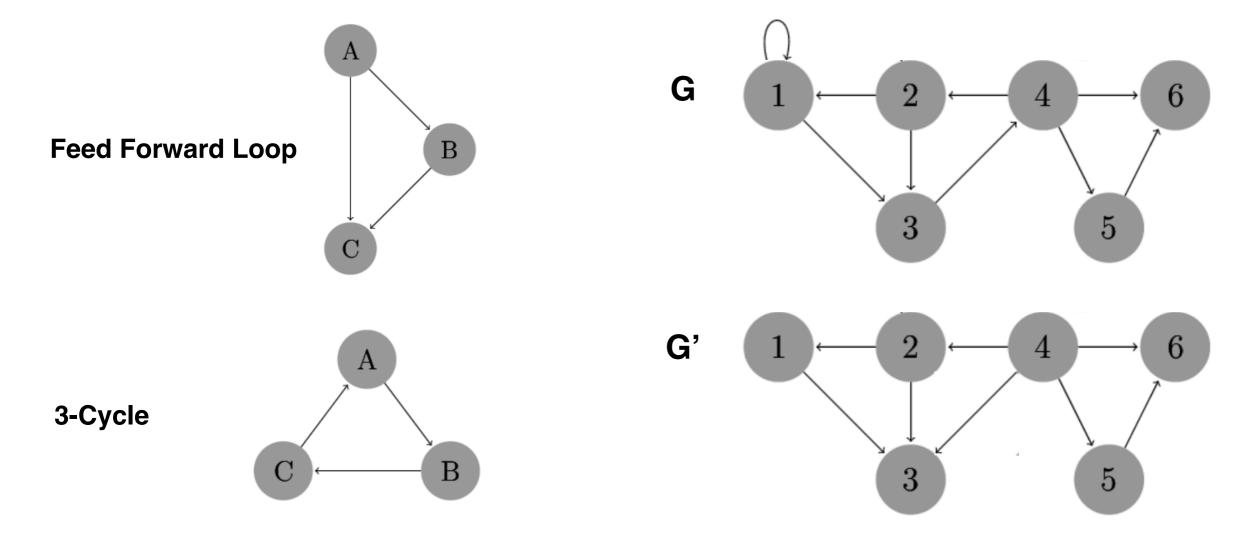
```
>>> g = nx.Graph()
>>> g.add_edges_from([(1,2),(1,3)])
>>> mot = nx.Graph()
>>> mot.add_edges_from([("A","B")])
>>> g1 = g.subgraph([1,2])
>>> nx.is_isomorphic(g1,mot)
```

#### Exercise

Given the Feed Forward Loop (FFL) and 3-Cycle write the code to detect the motif in the graph G with 6 nodes and 8 edges.

Calculate occurrences on random networks and the z-score.

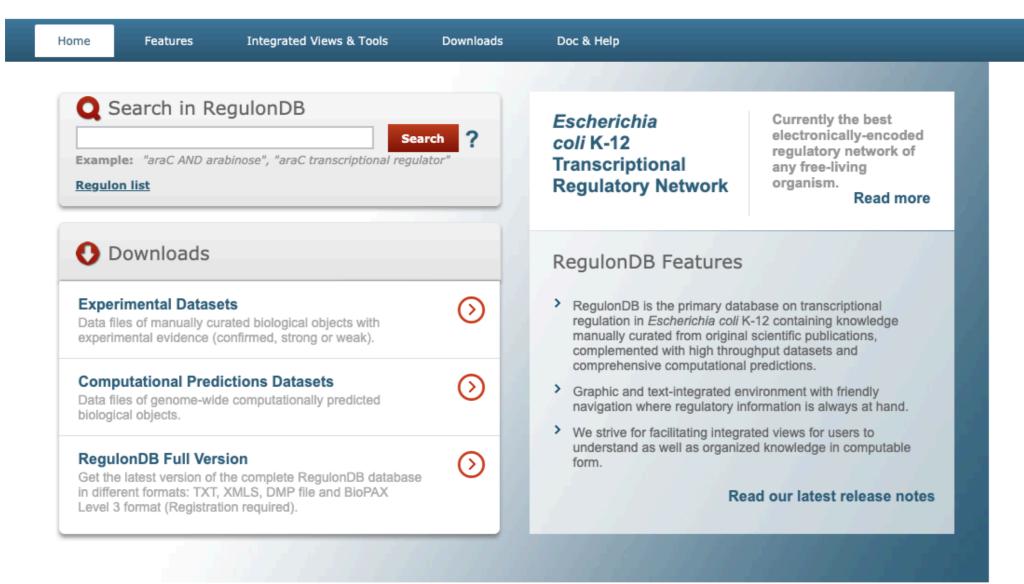
What is the difference the the FFL is matched on G'?



# RegulonDB

Database of Escherichia coli K-12 Transcriptional Regulatory Network





# Regulation Data

The regulation data includes information about the transcription factors (TF) that activate or repress the expression of the genes with associated supporting evidences.

```
# Release: 10.6.2 Date: 10-04-2019
# Columns:
# (1) Transcription Factor (TF) name
 (2) Gene regulated by the TF (regulated gene)
  (3) Regulatory effect of the TF on the regulated gene (+ activator, - repressor, +- dual, ? unknown)
  (4) Evidence that supports the existence of the regulatory interaction
                        [BCE, BPP, GEA, HIBSCS] Strong
AcrR
        acrA
                        [BCE, BPP, GEA, HIBSCS] Weak
AcrR
        acrB
                        [AIBSCS, BCE, BPP, GEA, HIBSCS] Weak
AcrR
        acrR
       flhC
                        [GEA, HIBSCS]
AcrR
                                         Weak
       flhD
                        [GEA, HIBSCS]
AcrR
                                        Weak
                        [BPP, GEA, HIBSCS]
AcrR
       marA
                                                Strong
                        [BPP, GEA, HIBSCS]
AcrR
       marB
                                                Strong
                        [BPP, GEA, HIBSCS]
        marR
                                                 Strong
AcrR
        micF
                        [AIBSCS]
AcrR
                                        Weak
AcrR
                        [BPP, GEA, HIBSCS]
        soxR
                                                 Strona
```

# Nodes ad Edges

With networkx we can assign attributes to nodes and edges

```
>>> G=nx.DiGraph()
>>> G.add_node(1, color='blue')
>>> G.add_node(2, color='red')
>>> G.add_edge(1, 2, sign='+')
>>> G.node[1]
>>> G[1][2]
```

### Matches Node and Edges

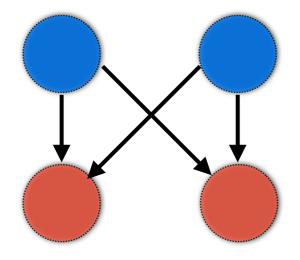
Matches can be performed based on node and edges attributes

```
>>> import networkx.algorithms.isomorphism as iso
>>> em=iso.categorical_edge_match('sign','+')
>>> nm=iso.categorical_node_match('color','red')
>>> nx.is_isomorphic(G1,G2,edge_match=em, node_match=nm)
```

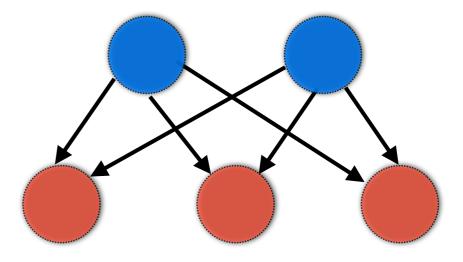
#### **Exercise**

Write a program to analyze the RegulonDB network considering only data with strong supporting information.

- Find the TF that regulates more genes (activation and suppression)
- Find the gene that is regulated by more TFs
- Find the Double-Positive Feedback loop and Multi-Input module



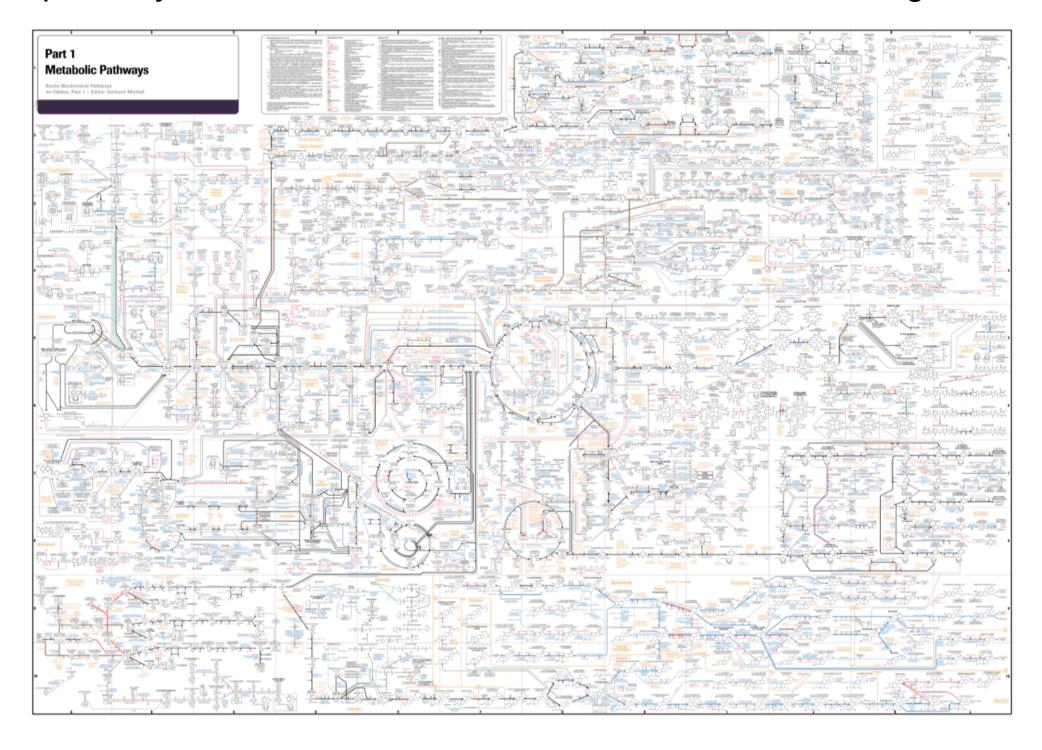
**Double-Positive Feedback loop** 



**Multi-Input module** 

# Metabolic Pathway

Metabolic pathway is a linked series of chemical reactions occurring within a cell.



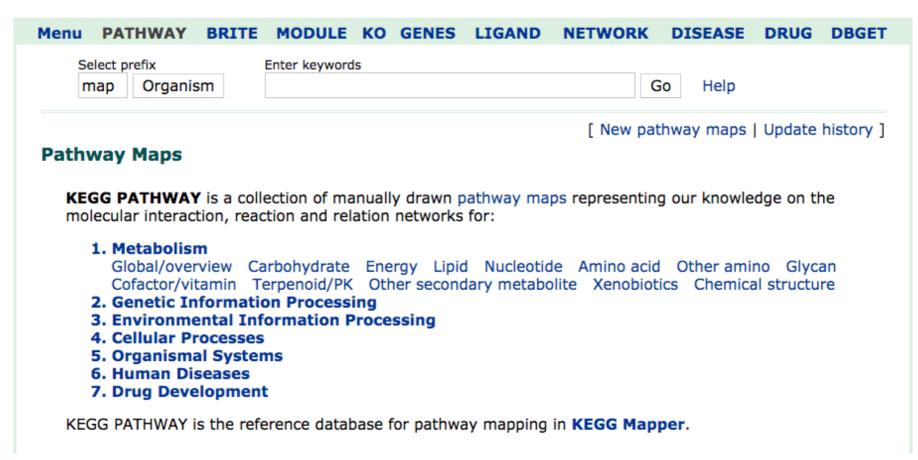
#### **KEGG Database**

It is the Kyoto Encyclopedia of Genes and Genomes. It collects many databases the most important one is KEGG Pathway which contains maps divided in 7 groups



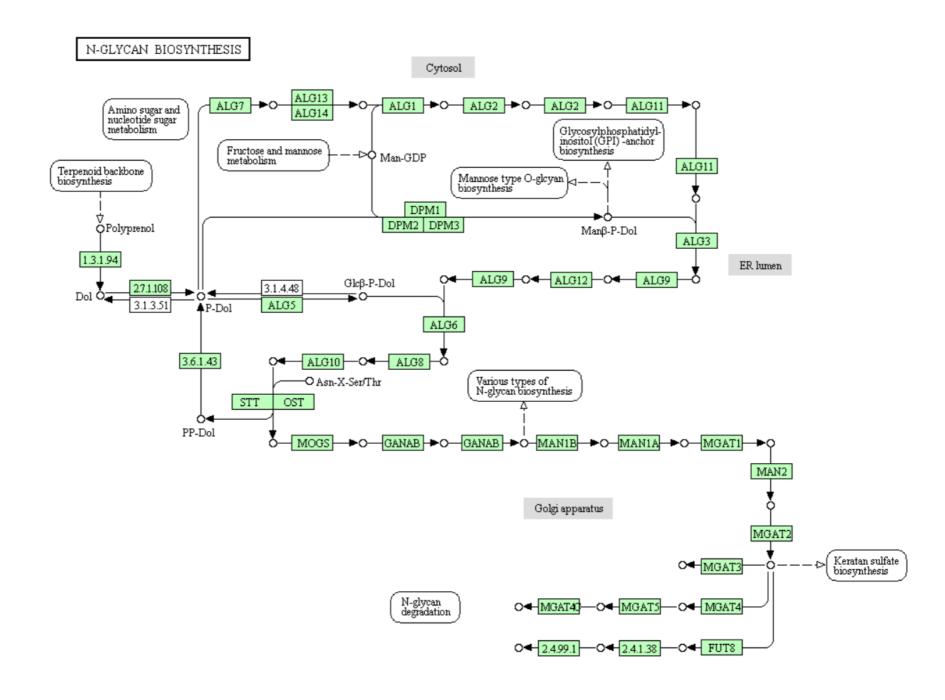
#### **KEGG PATHWAY Database**

Wiring diagrams of molecular interactions, reactions and relations



# Pathway Map

It is a representation of a set of reactions in which the reactants, products, and intermediates of an enzymatic reaction, known as metabolites, are modified by a sequence of reactions catalyzed by enzymes.



#### **KEGG Data**

Given a pathway KEGG provide several information about the genes, the metabolites and the enzymes involved in the series of reactions

KFGG	
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PATHWAY: map00510

Help Entry map00510 Pathway N-Glycan biosynthesis Name Description N-glycans or asparagine-linked glycans are major constituents of glycoproteins in eukaryotes. N-glycans are covalently attached to asparagine with the consensus sequence of Asn-X-Ser/Thr by an Nglycosidic bond, GlcNAc b1- Asn. Biosynthesis of N-glycans begins on the cytoplasmic face of the ER membrane with the transferase reaction of UDP-GlcNAc and the lipid-like precursor P-Dol (dolichol phosphate) to generate GlcNAc a1- PP-Dol. After sequential addition of monosaccharides by ALG glycosyltransferases [MD:M00055], the N-glycan precursor is attached by the OST (oligosaccharyltransferase) complex to the polypeptide chain that is being synthesized and translocated through the ER membrane. The protein-bound N-glycan precursor is subsequently trimmed, extended, and modified in the ER and Golgi by a complex series of reactions catalyzed by membrane-bound glycosidases and glycosyltransferases. N-glycans thus synthesized are classified into three types: high-mannose type, complex type, and hybrid type. Defects in N-glycan biosynthesis lead to a variety of human diseases known as congenital disorders of glycosylation [DS:H00118 H00119]. Metabolism; Glycan biosynthesis and metabolism Class BRITE hierarchy

#### All links Pathway (5) KEGG MODULE (5) Disease (2) KEGG DISEASE (2) Chemical substance (38) KEGG COMPOUND (8) KEGG GLYCAN (30) Chemical reaction (72) KEGG ENZYME (35) KEGG REACTION (37) Gene (117824) KEGG ORTHOLOGY (45) RefGene (117779) Literature (6) PubMed (6) All databases (117947) Download RDF

#### KGML Format

The KEGG Markup Language (KGML) is an exchange format of the KEGG pathway maps.

The KGML files for metabolic pathway maps contain two types of graph object patterns:

- boxes (enzymes) are linked by "relations"
- circles (chemical compounds) are linked by "reactions".

The information are provided in xml format. Enzymes are always indicated with Enzyme Commission number (EC number).

The EC number is composed by four numbers separated by periods. Those numbers represent a progressively finer classification of the enzyme.

#### **Network Modules**

A module is a set of genes/proteins performing a distinct biological function are characterized by coherent behavior with respect to certain biological property.

