

Many Operations Faster via Vectorization	Vectorization Ubiquitos
<pre>system.time(1:100000+1) # user system elapsed # 0 0 0 system.time({ x<-1:100000 for(i in x) x[i]<-x[i] +1 }) # user system elapsed # 0.231 0.002 0.233</pre>	<pre>dnorm(5, mean = 1:10, sd = 1) # [1] 1.338e-04 4.432e-03 5.399e-02 2.420e-01 3.989e-01 # [6] 2.420e-01 5.399e-02 4.432e-03 1.338e-04 1.487e-06</pre>
Vectorization Ambiguous in Many Instances	How to Vectorize Ambiguous Functions

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[1] 3.0 2.5 2.0 3.0 3.0

Many Operations Factor via Vactorization

The Guts of Vectorize	Minimizing Code for Mapping Functions: the Apply Family
<pre>sampMeanV # function (vec, size) # { args <-lapply(as.list(match.call())[-IL], eval, parent.frame()) names <- if (is.mull(names(args))) # character(length(args)) # dovec <- names (IM, wectorize.args) # dovec <- names (IM, wectorize.args) # do.call("mapply", c(FUM = FUM, args[dowec], MoreArgs = list(args[!dowec]) # SIMPLIFY = SIMPLIFY, USE.NAMES = USE.NAMES)) # Senvironment: 0x2305f5c></pre>	Take an object type - vector, matrix, list, etc., and map a function to every element, cleanly and quickly.
sapply for Vectors	Anonymous Functions and sapply
<pre>f <- function(x) x+1 # sapply(1:5,f)</pre>	<pre>sapply(1:5, function(x) x+1) # [1] 2 3 4 5 6</pre>

[1] 2 3 4 5 6

```
Lots of Possibilities with sapply
Apply Statements Faster than For Loops
   system.time({
    x<-1:100000
    for(i in x) x[i] <-x[i] +1
                                                             sapply(1:5, function(x) sampMean(1:5, x))
     user system elapsed
                                                             # [1] 1 3 2 3 3
     0.220 0.001 0.221
   system.time(sapply(1:100000, f))
       user system elapsed
     0.180 0.002 0.182
Many Output Types with sapply
                                                          apply for Matrices
                                                             m <- matrix( c(1, 2,
                                                                           3, 4), ncol=2)
   sapply(1:5, function(x) return( c(x+2, x^2) ) )
                                                             apply(m, 1, sum)
         [.1] [.2] [.3] [.4] [.5]
   #[1,] 3 4 5 6
                                                             # [1] 4 6
   # [2,] 1 4 9 16 25
                                                             apply(m, 2, sum)
                                                             # [1] 3 7
```

apply for Matrices

apply(m, c(1,2), sum)

```
[.1] [.2]
#[1,] 1 3
# [2,] 2
```

logic = c(TRUE, FALSE, FALSE, TRUE)) # compute the list mean for each list element lapply(x,mean) # \$a # [1] 5.5

lapply for Lists - mclapply to use multiple cores

beta = exp(-3:3).

x <- list(a = 1:10.

Exercise: Apply Yourself!

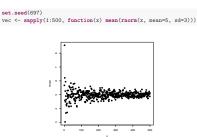
\$beta # [1] 4.535 # \$logic # [1] 0.5

Exercise: Apply Yourself!

1. Using sapply, write a short script to show the relationship between n and estimated mean for a normally distributed population with a mean of 5 and SD of 3.

2. Challenge: What is the bootstrapped SE at each sample size? 50 hoots!

hint: 2 lines with bootstrap, 3-4 with nested sapply



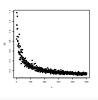
Exercise: Apply Yourself!

```
seVec <- sapply(1:500, function(x){
   mvec<- sapply(1:50, function (i) mean(rnorm(x, mean=5, sd=3)))
    return(sd(mvec))
```



Exercise: Apply Yourself!

library(bootstrap) seVec2 <- sapply(1:500, function(x) sd(bootstrap(rnorm(x, mean=5, sd=3), 50, mean)\$thetastar))



Application of Iterative Solutions: Likelihood

given hypothesis.

Likelihood: how well data support a

Note: Each and every parameter choice IS a hypothesis

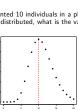


Where D is the data and θ is some choice of parameter values

 $L(\theta|D) = p(D|\theta)$

Example of Maximum Likelihood

Let's say we have counted 10 individuals in a plot. Given that the population is Poisson distributed, what is the value of λ ?



Maximum Likelihood

Enter Iteration

I did this by searching all values of λ using sapply

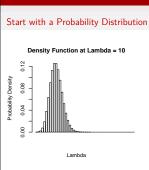
The Maximum Likelihood Estimate is the value at which $p(D|\theta)$ is highest.

count <- 10
#
1 <- sapply(0:20, function(x) dpois(count, lambda=x))
#
plot(0:20, 1, ylab="likelihood", xlab="lambda", pch=19)
abline(y=10, col="red", lud=2, lty=2)</pre>

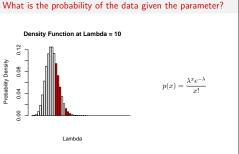


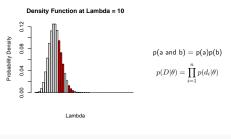
We often maximize log-likelihood because of the more well behaved properties of Log-Likelihood values

What about Many Data Points?



Log-Likelihood





What is the probability of the data given the parameter?

Can Compare p(data — H) for alternate H Lambda = 10 Lambda = 15 Lambda = 15 Lambda = 15 Lambda = 15

Compare $p(D|\theta_1)$ versus $p(D|\theta_2)$

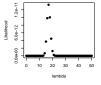


[1] 1.332e-11

[1] 17

lambdaVals[which(lik==max(lik))]

Likelihood and Log-Likelihood of a Data Set

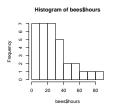




Exercise: Likelihood and Bees!

- ▶ Load the Bee Lifespan Data
- $\begin{tabular}{ll} \bf & Model \ Bee \ Lifespans \ as \ a \ Gamma \ Distribution \ with \ shape = 1 \\ \hline (1 \ bee \ per \ death) \\ \end{tabular}$
- ► What is the ML estimate of a Bee's Lifespan?

Exercise: Likelihood and Bees!



Exercise: Likelihood and Bees!

```
scaleVals <- seq(0.2, 80, 0.2)

s
beeD <- function(x) sum(dgamma(bees%hours, shape=1, scale=x, log=TRUE))
mll <- sapply(scaleVals, beeD)

s scaleVals[which(mll==max(mll))]

s [1] 27.8
```

