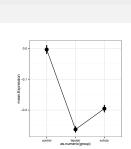
After the ANOVA

# Myrain shauth nated

Disorders

Categorical Predictors: Gene Expression and Mental

The Data



Fit the Data with a Linear Model

bg.sub.lm <- lm(PLP1.expression ~ group, data=brainGene)

### F-Test to Compare Variation Within versus Between Groups

 $SS_{Total} = SS_{Between} + SS_{Within}$ 

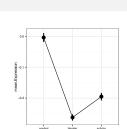
$$SS_{Between} = \sum_{i} \sum_{j} (\bar{Y}_{i} - \bar{Y})^{2}$$
, df=k-1

 $SS_{Within} = \sum_{i} \sum_{j} (Y_{ij} - \bar{Y}_{i})^{2}$ , df=n-k

$$MS = SS/DF, e.g. \ MS_W = \frac{SS_W}{2}$$

 $F = \frac{MS_B}{MS_W}$  with DF=k-1,n-k

### The Data



# **ANOVA**

anova (bg.sub.lm)

# Analysis of Variance Table

# group

# Response: PLP1.expression 2 0.54 0.2701

Df Sum Sq Mean Sq F value Pr(>F) 7.82 0.0013 # Residuals 42 1.45 0.0345

Which groups are different from one another?

### The Coefficients

```
summary(bg.sub.lm)
# Call:
# Residuals:
      Min
# -0.2960 -0.1273 -0.0347 0.0753 0.4840
```

# lm(formula = PLP1.expression ~ group, data = brainGene) 1Q Median 30

# Coefficients: Estimate Std. Error t value Pr(>|t|) # (Intercept) -0.0040 0.0480 -0.08 0.93395 # groupbipolar -0.2587 0.0678 -3.81 0.00044 # groupschizo -0.1913 0.0678 -2.82 0.00730

# Residual standard error: 0.186 on 42 degrees of freedom # Multiple R-squared: 0.271, Adjusted R-squared: 0.237

### Default "Treatment" Contrasts

contrasts(brainGene\$group)

# control

# bipolar
# schizo

bipolar schizo

Ω

### The Coefficients

# Call:
# Lafformula = FLP1.expression ~ group - 1, data = brainGene)
# sesiduals:
# Min 10 Median 30 Max
# -0.2960 -0.1273 -0.0347 0.0753 0.4840
# Coefficients:
# Estimate Std. Error t value Pr(>|t|)
# groupcontrol -0.004 0.048 -0.08 0.9340
# groupbipolar -0.263 0.048 -5.47 2.3e-06
# groupbipolar -0.195 0.048 -4.07 0.0002
# Residual standard error: 0.186 on 42 degrees of freedom
# Multiple R-squared: 0.526, Adjusted R-squared: 0.492

summary(lm(PLP1.expression ~ group -1, data=brainGene))

### OK. but WHICH GROUPS ARE DIFFERENT?

### Remember your Null:

ANOVA is an Omnibus Test

$$H_0 = \mu_1 = \mu_2 = \mu_3 = ...$$

This had nothing to do with specific comparisons of means.

### A priori contrasts

### Specific sets of a priori null hypotheses:

$$\mu_1 = \mu_2$$

$$\mu_1 = \mu_3 = ...$$

Use t-tests

### A priori contrasts

```
contrast(bg.sub.lm, list(group="control"),
        list(group=c("schizo", "bipolar")))
# lm model parameter contrast
```

Contrast S.E. Lower Upper t df Pr(>|t|) 0.1913 0.06785 0.0544 0.3283 2.82 42 0.0073 # 0.2587 0.06785 0.1217 0.3956 3.81 42 0.0004

Note: can only do k-1, as each takes 1df

### A priori contrasts

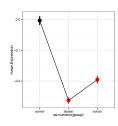
### library(contrast)

contrast(bg.sub.lm, list(group="control"), list(group="schizo"))

# 1m model parameter contrast

# Contrast S.E. Lower Upper t df Pr(>|t|) # 1 0.1913 0.06785 0.0544 0.3283 2.82 42 0.0073

### The Data



# Orthogonal A priori contrasts

structure of your groups

# Control v. Disorders # Bipolar v. Schizo

Note: can only do k-1, as each takes 1df

Sometimes you want to test very specific hypotheses about the

control bipolar schizo 1 -0.5 -0.5

1.0 -1.0

library(multcomp)

summary(bg\_orthogonal)

Note adjusted p-value is set to none...

Orthogonal A priori contrasts

Simultaneous Tests for General Linear Hypotheses # Fit: lm(formula = PLP1.expression ~ group, data = brainGene) # Linear Hypotheses: Estimate Std. Error t value # Control v. Disorders == 0 0.2210 0.1018 2.17 # Bipolar v. Schizo == 0 0.0679 -0.99 -0.0673 Pr(>|t|) # Control v. Disorders == 0 0.07 # Bipolar v. Schizo == 0 0.54 # (Adjusted p values reported -- single-step method)

Post hoc contrasts

I want to test all possible comparisons!

Orthogonal A priori contrasts with multcomp

bg\_orthogonal <- glht(bg.sub.lm, linfct=contrast\_mat,

test=adjusted("none"))

### Post hoc contrasts

Only to be done if you reject Ho

All possible comparisons via t-test

- ▶ But...with many comparisons, does type I error rate increase?
- Consider adjusted alpha
- ▶ But, adjusting alpha also may increase type II error rate!
- Additional multiple comparison methods calulate family-wise critical values of differences.

### All Possible T-Tests

```
with( brainGene, pairwise.t.test(PLP1.expression, group,
p.adjust.method = "none") )

# Pairwise comparisons using t tests with pooled SD
# data: PLP1.expression and group
# control bipolar
# bipolar 0.00044 -
# schizo 0.00730 0.32671
# P value adjustment method: none
```

### P-Value Adjustments

Bonferroni :  $\alpha_{adj} = \frac{\alpha}{m}$  where m = # of tests - VFRY conservative

5. 5. 5. 6.

False Discovery Rate:  $\alpha_{adj}=\frac{k\alpha}{m}$  - Order your p values from smallest to largest, rank = k,

- Adjusts for small v. large p values
- Less conservative

Other Methods: Sidak, Dunn, Holm, etc. We're very focused on p here!

### Bonferroni Correction

```
with( brainGene, pairwise.t.test(PLP1.expression, group,
p.adjust.method ="bonferroni") )

# Pairwise comparisons using t tests with pooled SD
# data: PLP1.expression and group
# control bipolar
# bipolar 0.0013 -
# schizo 0.0219 0.0801
# P value adjustment method: bonferroni
```

### False Discovery Rate

```
with( brainGene, pairwise.t.test(PLP1.expression, group, p.adjust.method ="fdr") )

# Pairwise comparisons using t tests with pooled SD

# data: PLP1.expression and group

# control bipolar

# bipolar 0.0013 -

# schizo 0.0110 0.3267

# P value adjustment method: fdr
```

Other Methods Use Critical Values

- ► Tukey's Honestly Significant Difference
  - Dunnet's Test for Comparison to Controls
     Ryan's Q (sliding range)
  - ► etc...

### Tukey Test

# \$group

```
bg.sub.aov <- aov(PLP1.expression ~ group, data=brainGene)
TukeyHSD(bg.sub.aov)

# Tukey multiple comparisons of means
# 95% family-wise confidence level
# Fit: aov(formula = PLP1.expression ~ group, data = brainGene)
```

lwr

upr p adj

diff

# bipolar-control -0.25867 -0.42351 -0.09382 0.0013 # schizo-control -0.19133 -0.35618 -0.02649 0.0196 # schizo-bipolar 0.06733 -0.09751 0.23218 0.5857

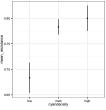
Final Notes of Caution

- ► Often you DO have a priori contrasts in mind
- Often you DO have a priori contrasts in mind
   If you reject Ho with ANOVA, differences between groups exist
- Consider Type I v. Type II error before correcting

## Exercise: Daphnia Resistance

Fit an ANOVAWhich groups are different?

Daphnia Data



### ANOVA shows an Effect

daphnialM <- lm(resistance - cyandensity, data-daphnia)
anova(daphnialM)

# Analysis of Variance Table
#
Response: resistance
# Df Sum Sq Mean Sq F value Pr(>F)
# cyandensity 20.0892 0.0446 6.69 0.0041

# Residuals 29 0.1933 0.0067

### High and Med Not Different

```
summary( glht(daphniaLM, linfct=mcp(cyandensity="Tukey")),
        test=adjusted("none"))
   Simultaneous Tests for General Linear Hypotheses
# Multiple Comparisons of Means: Tukey Contrasts
# Fit: lm(formula = resistance ~ cyandensity, data = daphnia)
# Linear Hypotheses:
                 Estimate Std. Error t value Pr(>|t|)
 med - low == 0
                   0.0997
                             0.0350
                                       2.85 0.0079
# high - low == 0
                  0.1167
                             0.0350
                                       3.34 0.0023
# high - med == 0 0.0170
                             0.0365
                                       0.47 0.6450
# (Adjusted p values reported -- none method)
```