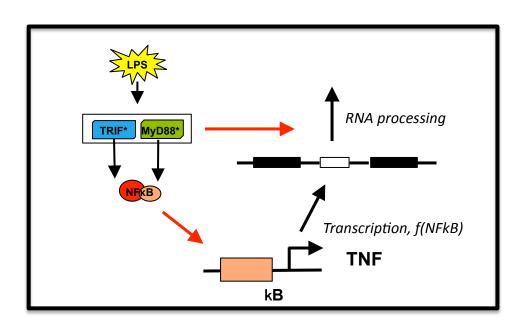
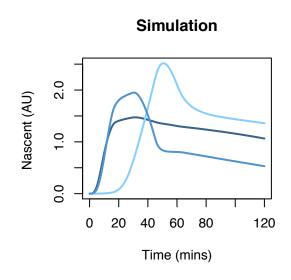
Module1: Transcription + RNA processing





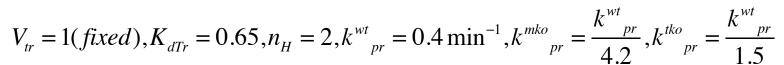
Equation

$$\frac{d[Nascent]}{dt} = V_{tr} \frac{[NF \kappa B_n]^{n_H}}{[NF \kappa B_n]^{n_H} + K_{dtr}^{n_H}} - k_{pr}[Nascent]$$

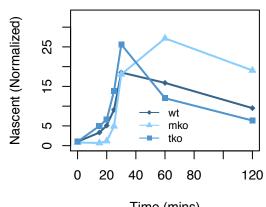
Initial condition

$$[Nascent]_{t=0} = \frac{V_{tr}}{k_{pr}} \frac{[NF \kappa B_n]_{t=0}^{n_H}}{[NF \kappa B_n]_{t=0}^{n_H} + K_{dtr}^{n_H}}$$

Parameters $(n_p = 5)$

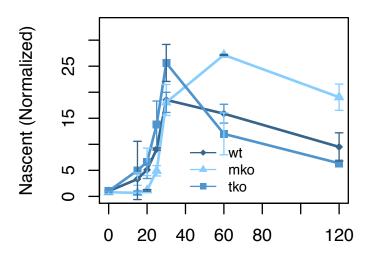


Experiment



Time (mins)

Experiment



Score function (modified chi square)

$$\chi_{\rm m}^2 = \frac{1}{n_F - n_p - 1} \sum_{i=1}^{n_F} \frac{(F_i^s - F_i^e)^2}{\sigma_i^2}$$

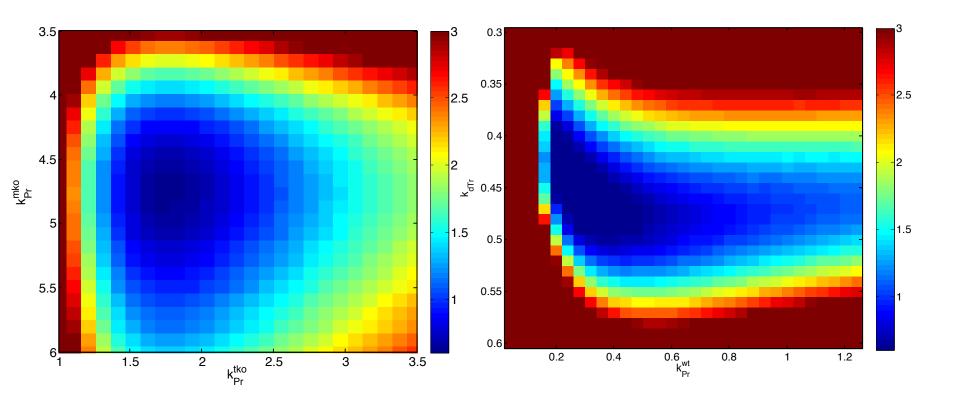
Time (mins)

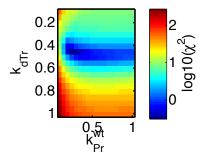
Table of features (n_F=9)

| Index(i) | Feature | Value(F ^e _i) | Error(σ _i) |
|----------|------------------|-------------------------------------|------------------------|
| 1 | Peak time (wt) | 30 min | 5 min |
| 2 | Peak time (mko) | 60 min | 10 min |
| 3 | Peak time (tko) | 30 min | 5 min |
| 4 | Peak_wt/Peak_mko | 0.68 | 0.11 |
| 5 | Peak_wt/peak_tko | 0.75 | 0.22 |
| 6 | Wt(60)/tko(60) | 1.55 | 0.67 |
| 7 | Wt(60)/mko(60) | 0.59 | 0.07 |
| 8 | Wt(120)/mko(120) | 0.52 | 0.21 |
| 9 | Wt(120)/tko(120) | 1.49 | 0.43 |

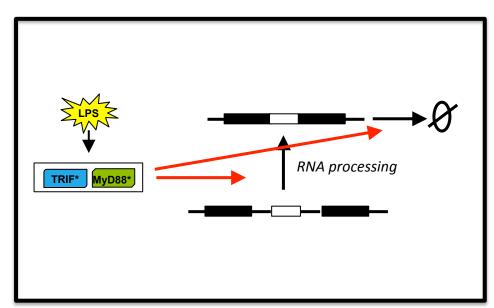
How well the model capture the features.

Score heat map for different parameters.





Module 2: RNA processing + stabilization



Equation

$$\frac{d[mRNA]}{dt} = k_{pr}[Nascent] - k_{\deg mRNA}[mRNA]$$

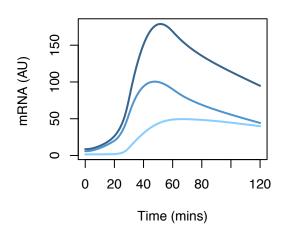
Initial condition

$$[mRNA]_{t=0} = \frac{k_{pr}}{k_{\deg mRNA}} [nascent]_{t=0}$$

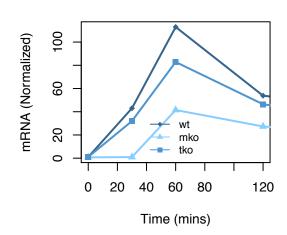
Parameters $(n_p = 5)$

$$k^{wt}_{pr} = 0.6 \,\text{min}^{-1}, k^{mko}_{pr} = \frac{k^{wt}_{pr}}{4.5}, k^{tko}_{pr} = \frac{k^{wt}_{pr}}{1.5}, k^{tko}_{deg mRNA} = 0.07 \,\text{min}^{-1}, k^{wt/mko}_{deg mRNA} = \begin{cases} -\frac{1}{30}t + 0.07 \,\text{min}^{-1}(0.5t < 50 \,\text{min}) \\ \frac{0.05}{30}(t - 30) + 0.02 \,\text{min}^{-1}(30 \,\text{min} \le t < 60 \,\text{min}) \end{cases}$$

Simulation



Experiment

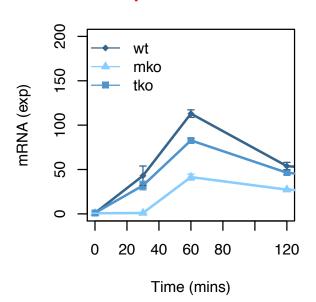


$$-\frac{0.05}{30}t + 0.07 \,\text{min}^{-1}(0 \le t < 30 \,\text{min})$$

$$\frac{0.05}{30}(t - 30) + 0.02 \,\text{min}^{-1}(30 \,\text{min} \le t < 60 \,\text{min})$$

$$0.07 \,\text{min}^{-1}(60 \,\text{min} \le t)$$

Experimental data



Score function (modified chi square)

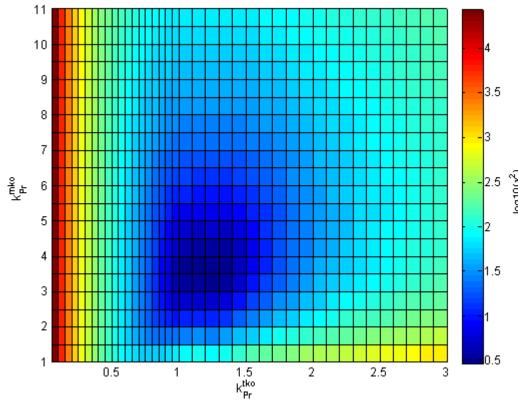
$$\chi_{\rm m}^2 = \frac{1}{n_F - n_p - 1} \sum_{i=1}^{n_F} \frac{(F_i^s - F_i^e)^2}{\sigma_i^2}$$

Table of features $(n_F=7)$

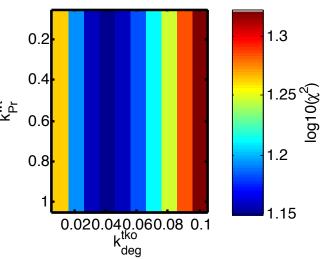
| Index(i) | Feature | Value(Fs _i) | Error(σ _i) |
|----------|-------------------|-------------------------|------------------------|
| 1 | Peak time (wt) | 60 min | 10 min |
| 2 | Peak time (mko) | 60 min | 10 min |
| 3 | Peak time (tko) | 60 min | 10 min |
| 4 | Peak_tko/Peak_wt | 0.73 | 0.05 |
| 5 | Peak_mko/peak_tko | 0.50 | 0.06 |
| 6 | wt_120/mko_120 | 1.98 | 0.23 |
| 7 | Wt_120/tko_120 | 1.17 | 0.14 |

How well the model capture the features.

Score heat map for different parameters.



As long as keep the same ratios of processing rate between wt, mko and tko, the fit doesn't depend on the processing rate.



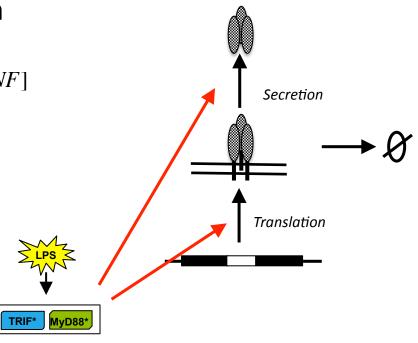
Module 3: Translation + Secretion

$$\frac{d[proTNF]}{dt} = k_{tt}[mRNA] - k_{\deg P}[proTNF] - k_{\sec}[proTNF]$$

$$[\sec TNF](t) = \int_{0}^{t} k_{\text{sec}}[proTNF]dt$$

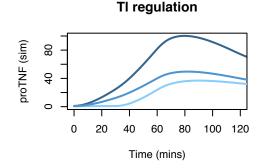
$$k_{tl}^{wt/mko} = 0.05 \,\mathrm{min}^{-1}, k_{tl}^{tko} = \frac{k_{tl}^{wt}}{1.5}, k_{\deg P} = 0.07 \,\mathrm{min}^{-1},$$

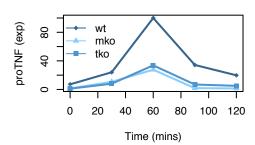
$$k_{\text{sec}}^{wt/mko} = 0.07 \,\text{min}^{-1}, k_{\text{sec}}^{tko} = \frac{k_{tl}^{wt}}{5}$$



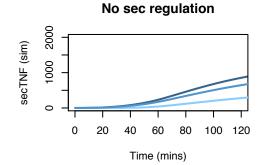
(Eis) 08 - 0 20 40 60 80 100 120 Time (mins)

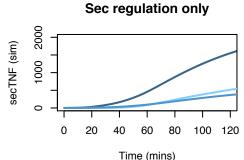
No tl regulation

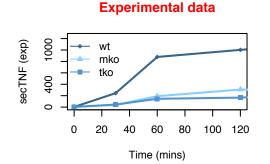




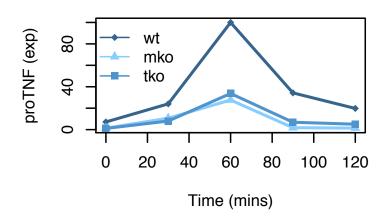
Experimental data



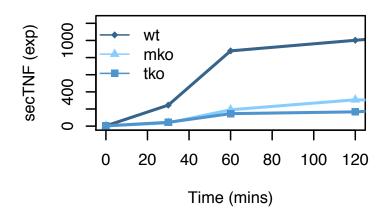




Experimental data



Experimental data

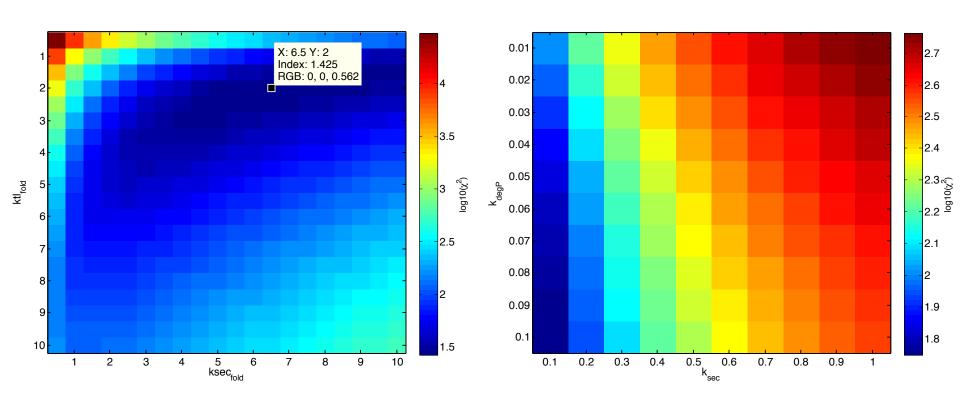


| Index(i) | Feature | Value(F ^s _i) | Error(σ _i) |
|----------|-------------------|-------------------------------------|------------------------|
| 1 | Peak time (wt) | 60 min | 10 min |
| 2 | Peak time (mko) | 60 min | 10 min |
| 3 | Peak time (tko) | 60 min | 10 min |
| 4 | Peak_tko/Peak_wt | 0.34 | 0.06 |
| 5 | Peak_mko/peak_tko | 0.82 | 0.14 |
| 6 | wt_120/Peak_wt | 0.20 | 0.04 |
| 7 | Wt_120/tko_120 | 3.9 | 0.65 |
| 8 | wt_120/mko_120 | 14 | 2.3 |
| 9 | Tko_30/mko_30 | 0.75 | 0.12 |

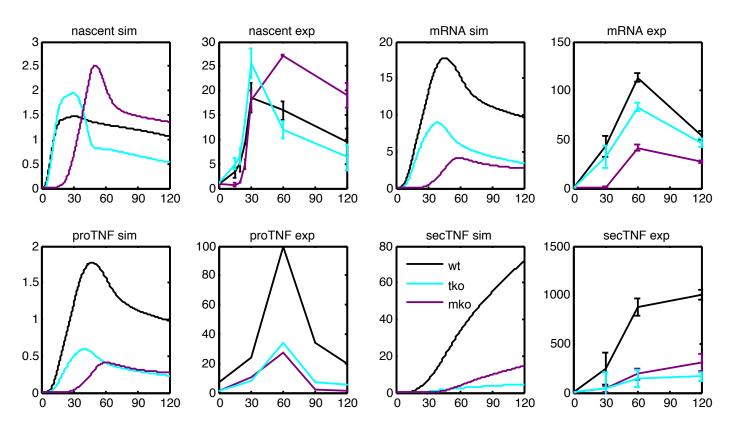
| Index(i) | Feature | Value(F ^s _i) | Error(σ _i) |
|----------|-----------------|-------------------------------------|------------------------|
| 1 | tko_60/wt_60 | 0.17 | 0.03 |
| 2 | Mko_60/tko_60 | 1.4 | 0.54 |
| 3 | Tko_120/wt_120 | 0.17 | 0.03 |
| 4 | Mko_120/tko_120 | 1.9 | 0.76 |
| 5 | wt_120/wt_60 | 1.2 | 0.16 |

How well the model capture the features.

Score heat map for different parameters.

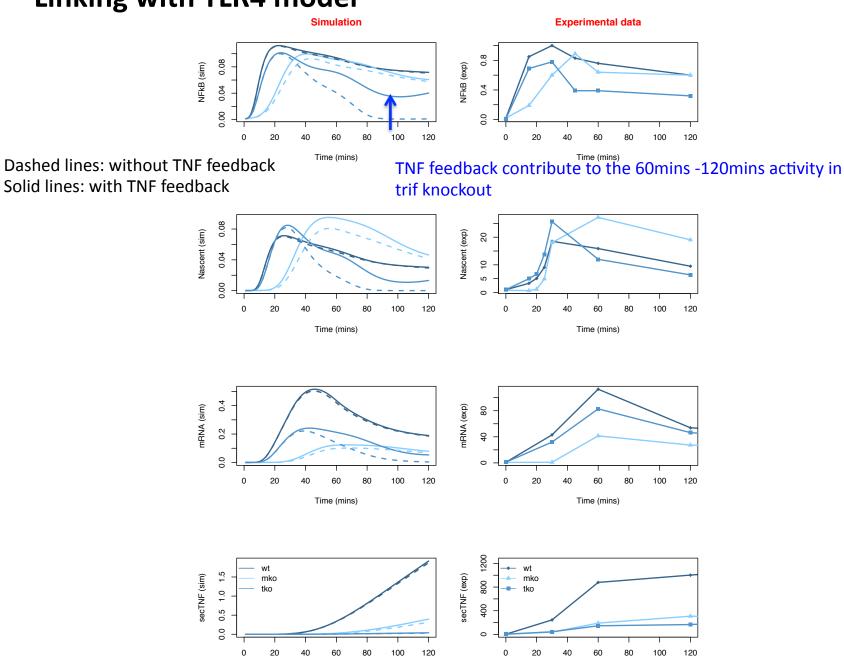


Module 1 to 3, together (NFkB as input)



| ID | Name | Values |
|----|-------------|--------|
| | | 0.65 |
| | Km_tr | 0.03 |
| 2 | Km_tr_fold | 2 |
| 3 | V_tr | 1 |
| 4 | k_pr | 0.4 |
| 5 | k_sec | 0.07 |
| 6 | k_tl | 0.05 |
| 7 | kdeg_m | 0.02 |
| 8 | kdeg_p | 0.07 |
| 9 | n | 2 |
| 10 | pr_fold_mko | 4.2 |
| 11 | pr_fold_tko | 1.5 |
| 12 | sec_fold | 5 |
| 13 | tl_fold | 1.5 |

Linking with TLR4 model

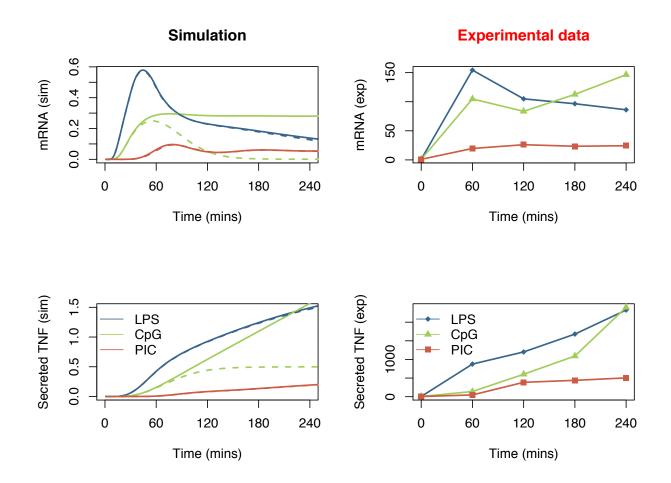


Time (mins)

Time (mins)

CpG and **PIC** stimulation (with / without TNF feedback)

Feedback toggled by TNFR synthesis



CpG and PIC stimulation (with / without TNF feedback)

