# **Examples of simulation in JSim**

## Dynamics of fish in a tank

Fishes are growing in a tank that has specific carrying capacity (k).

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- Fishes are regularly removed from tank at a fixed rate.
- No death

The model:

$$\frac{dx}{dt} = r.x.(1 - \frac{x}{k}) - d$$

*r* = rate constant for growth *k* = carrying capacity d = rate of removal of fish from tank

A JSim model is made of nested components.

Here, **fish\_model** is the top level component. You can give any name for this.

This component is of math type. Declaring this is essential.

Top component **fish\_model** is composed of other components, declared within the parentheses [ { } ]. These parentheses are must.

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
        real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45; \}
  // ODEs
         x:t = r*x*(1-x/k) - d;
```

A **realDomain** represents an independent variable. Here it is t.

Each **realDomain** must have a minimum value, maximum value, and step size.

For t, these are written here as t.min, t.max and t.delta.

You have to provide specific numerical values for each of these.

Each statement ends with a semicolon.

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
        real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45; \}
  // ODEs
         x:t = r*x*(1-x/k) - d;
```

x is a dependent variable that varies with t. So it is written as x(t).

It is a **real** variable. A "real" variable represents a either constant or a dependent variable.

// is used to mark annotation

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
        real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45; \}
  // ODEs
         x:t = r*x*(1-x/k) - d;
```

**r**, **k**, and **d** are parameters or constants. We have to provide numerical values for each.

These parameters/constants are **real** variables.

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
        real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45; \}
  // ODEs
        x:t = r*x*(1-x/k) - d;
```

To solve the ODE we have to specify the initial value.

Initial time is zero. In other words

```
t = t.min
```

Value of x at that time is x = 45

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
       real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45;\}
  // ODEs
         x:t = r*x*(1-x/k) - d;
```

Finally we have to declare the ODE.

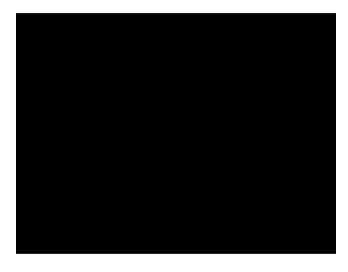
```
In JSim, dx/dt = x : t
```

So the ODE is declared as:

```
x:t = r*x*(1-x/k) - d;
```

```
math fish model
{ realDomain t;
       t.min = 0; t.delta = 0.01; t.max = 100;
  //Define dependent variable
        real x(t);
  //Define parameters
       real r = 1;
        real k = 100;
        real d = 20;
  // Initial value
        when (t = t.min) \{x = 45; \}
  // ODEs
         x:t = r*x*(1-x/k) - d;
```

# Simulating the model in JSim



## Model with two dependent variables

Predator-prey ecosystem:

Prey population grows by new birth and decreases as predators eat them

Predators eat prey. Population growth of predator depends upon how much they eat. Predators have death.

$$\frac{dx}{dt} = k_1.x - k_2.x.y$$

$$\frac{dy}{dt} = k_2.x.y - k_3.y$$

x = number of prey

y = number of predator

 $k_1$  = rate constant for growth of prey population

 $k_2$  = rate constant for consumption of prey by predator

 $k_3$  = rate constant for death of predators

## **Coding in JSim**

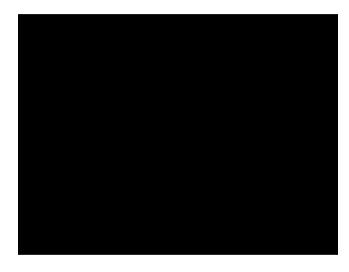
Two dependent variables are declared.

Initial values of two dependent variables declared

Two ODEs defined

```
math predator prey model
{ realDomain t :
        t.min=0; t.delta=0.1; t.max=100;
  //Define dependent variables
        real x(t), y(t);
  //Define parameters
        real k1 = 0.2;
        real k2 = 0.001;
        real k3 = 0.5;
  // Initial values
        when (t=t.min) \{x=200; y=5; \}
  // ODEs
        x:t = k1*x - k2*x*y;
        v:t = k2*x*v - k3*v;
```

## Simulating the model in JSim



#### **Key points:**

- 1. JSim code has different components nested one within other.
- 2. Key components of a ODE model:

```
Time: realDomain t

Dependent variables: real x(t), y(t)

Parameter values: real k1 = 0.2

Initial conditions: when (t=t.min) {x=200; y=5;}

ODE: x:t = k1*x - k2*x*y;
```

- 3. Define the main component (model name) as math
- 4. Be careful of proper use of semicolon(;) and curly bracket ( { } )