



### CSCE 580: Introduction to Al

### Week 10 - Lectures 18 and 19: Adversarial Search; Constraints & Optimization

PROF. BIPLAV SRIVASTAVA, AI INSTITUTE 21<sup>ST</sup> AND 23<sup>RD</sup> OCT 2025

Carolinian Creed: "I will practice personal and academic integrity."

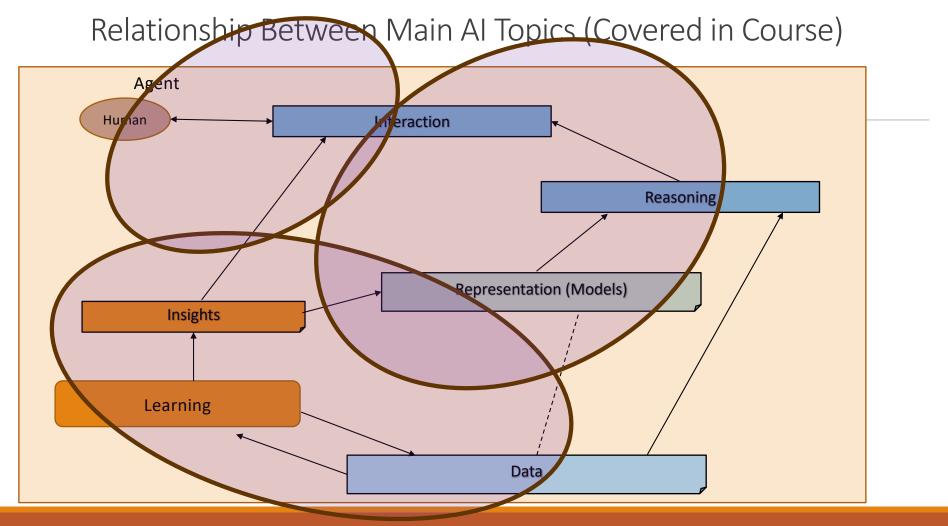
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### Organization of Week 10 - Lectures 18, 19

- Introduction Section
  - Recap from Week 9 (Lectures 16 and 17)
  - Al news
- Main Section
  - Lecture 18: Adversarial and Game Search
    - Games
    - Prisoner's Dilemma
  - Lecture 19: Optimization
    - Constraints
    - Optimization
- Concluding Section
  - About next week W11: Lectures 20, 21
  - Ask me anything

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## Recap of Week 9

#### We discussed

- Informed search
- Local search

- Week 1: Introduction, Aim: Chatbot / Intelligence Agent
- Weeks 2-3: Data: Formats, Representation and the Trust Problem
- Week 3: Machine Learning Supervised (Classification)
- Week 4: Machine Learning Unsupervised (Clustering) -
- Topic 5: Learning neural network, deep learning, <u>Adversarial attacks</u>
- Week 6: <u>Large Language Models</u> Representation and Usage issues
- Weeks 7-8: Search, Heuristics Decision Making
- Week 9: Constraints, Optimization Decision Making
- Topic 10: Markov Decision Processes, Hidden Markov models -Decision making
- Topic 11-12: Planning, Reinforcement Learning Sequential decision making
- Week 13: <u>Trustworthy Decision Making</u>: <u>Explanation</u>, AI testing
- Week 14: Al for Real World: Tools, Emerging Standards and Laws; Safe Al/ Chatbots

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## Upcoming Evaluation Milestones

• Projects B: Sep 30 – Nov 20

• Quiz 2: Oct 7

• Quiz 3: Nov 11

• Paper presentation (grad students only): Nov 18

• Finals: Dec 11

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### Al News

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### $\#1~{ m NEWS}-{ m Deloitte}$ to pay money back to Australia's government after using AI in \$440,000 report

• Link: <a href="https://www.theguardian.com/australia-news/2025/oct/06/deloitte-to-pay-money-back-to-albanese-government-after-using-ai-in-440000-report">https://www.theguardian.com/australia-news/2025/oct/06/deloitte-to-pay-money-back-to-albanese-government-after-using-ai-in-440000-report</a>

"Deloitte has a human intelligence problem. This would be laughable if it wasn't so lamentable. A partial refund looks like a partial apology for substandard work"

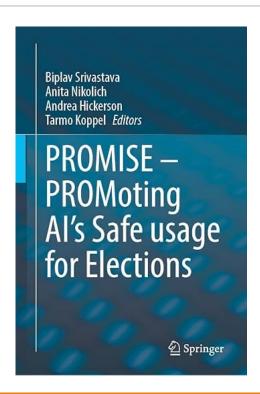
- Deloitte was contracted to do consulting for Australia's federal government Department of Employment and Workplace Relations (DEWR)
  - Contracted by department to review the targeted compliance framework and its IT system in December 2024
    - Used to automate penalties in the welfare system if mutual obligations were not met by jobseekers
    - The subsequent report found widespread issues, including a lack of "traceability" between the rules of the framework and the legislation behind it, as well as "system defects". It said an IT system was "driven by punitive assumptions of participant non-compliance".
- Deloitte will provide a partial refund to the federal government over a \$440,000 report that contained several errors, after admitting it used generative artificial intelligence to help produce it.
- University of Sydney academic, Dr Christopher Rudge, who first highlighted the errors, said the report contained "hallucinations" where AI models may fill in gaps, misinterpret data, or try to guess answers.
- Deloitte added reference to the use of generative AI in its appendix. It states that a part of the report "included the use of a generative artificial intelligence (AI) large language model (Azure OpenAI GPT 40) based tool chain licensed by DEWR and hosted on DEWR's Azure tenancy.

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### #2 NEWS - PROMISE Book - PROMoting Al's Safe usage for Elections

• Link: <a href="https://www.linkedin.com/posts/biplav-srivastava">https://www.linkedin.com/posts/biplav-srivastava</a> promise-promoting-ais-safe-usage-for-elections-activity-7377405499815911424-nlgU

• Press: https://www.nbcnews.com/tech/security/hacker-used-ai-automate-unprecedented-cybercrime-spree-anthropic-says-rcna227309



- It is an edited book based on four years of work that explores Al's role in enhancing credible, data-driven electoral processes.
- This all started with a few of us brainstorming on how AI could make elections better that lead to academic workshops at Neurips 2021, AAAI 2023, AAAI 2024, a special issue of the AI Magazine on the topic, and a blue-sky paper at AAAI 2025.
- The book has contributions from over 30 authors that are drawn from academia, industry, non-profits, and government, from around the world. They bring and combine technical perspectives from the lens of computer science and AI, security, journalism, law, and political science, and consider elections in all continents Asia (India), Africa (Ghana, Nigeria, Kenya), Europe (Estonia, UK), North America (Canada, US) and Latin America (Brazil).
- The book consists of a mix of article types research papers, interviews and essays, touching on impact potentials of AI technologies like chatbots, large language models, game theory and machine learning, for voters, candidates, and election commissions, and ends with a code of ethics for those working in AI and election space using relevant guidance from computing and journalism fields.
- It offers practical guidelines for researchers, teachers, practitioners, students and government officials.

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### Introduction Section

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### Main Section

## Lecture 18: Adversarial and Game Search

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### Offline and Online Search

- All search studied until now were offline search
  - Solution found and then agent executed
- Online search
  - Interleave solution finding and execution
  - · Cannot guarantee solution, unless actions have inverse-actions to undo state change

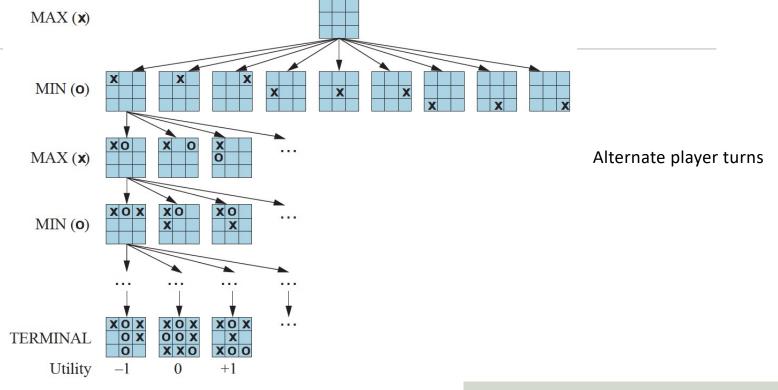
### Games and Search

- Common setting
  - Two players
    - One human, one automated [Common case]
    - Both automated
  - Perfect information (fully observable)
  - Zero-sum if one wins, another looses
- Captures many types of games
  - Tic-tac-toe, chess, Go, backgammon, ...

### Games and Search

- Setup
  - So: the initial state
  - TO-MOVE(s): the player to play in state s
  - ACTIONS(s): the set of legal actions at state s
  - **RESULT (s, a):** transition model
  - IS-TERMINAL (s): terminal test to determine if game is over
  - UTILITY (s, p): utility or objective function. Numeric value capturing value of state s to player p

### Tic-Tac-Toe — Game Tree



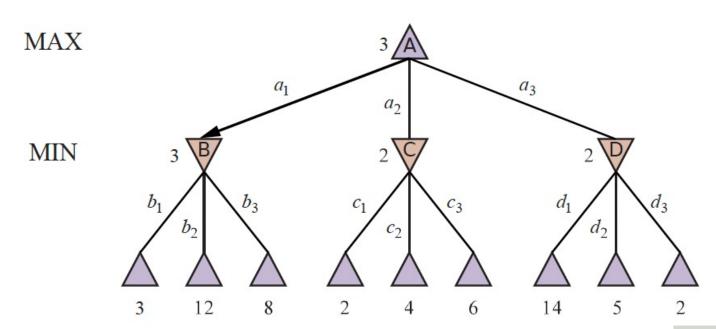
Adapted from:

Russell & Norvig, Al: A Modern Approach

## MiniMax Utility

#### MINMAX(s) =

- UTILITY(s, MAX) if IS-TERMINAL(s)
- Max a in ACTIONS(S) MINIMAX(RESULT(s, a)) if TO-MOVE(s) = MAX
- Min a in ACTIONS(S) MINIMAX(RESULT(s, a)) if TO-MOVE(s) = MIN



Adapted from:

Russell & Norvig, AI: A Modern Approach

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### Minimax Search Algorithm

```
function MINIMAX-SEARCH(qame, state) returns an action
  player \leftarrow qame.To-MovE(state)
  value, move \leftarrow MAX-VALUE(qame, state)
  return move
function MAX-VALUE(game, state) returns a (utility, move) pair
  if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
  v \leftarrow -\infty
  for each a in game.ACTIONS(state) do
    v2, a2 \leftarrow MIN-VALUE(game, game.RESULT(state, a))
    if v2 > v then
       v, move \leftarrow v2, a
  return v, move
function MIN-VALUE(game, state) returns a (utility, move) pair
  if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
  v \leftarrow +\infty
  for each a in game.ACTIONS(state) do
    v2, a2 \leftarrow MAX-VALUE(game, game.RESULT(state, a))
    if v2 < v then
       v, move \leftarrow v2, a
  return v, move
```

Starts from a Max node
Recursively does min on children,
who in-turn does max on children
to get value and corresp. action

Adapted from:

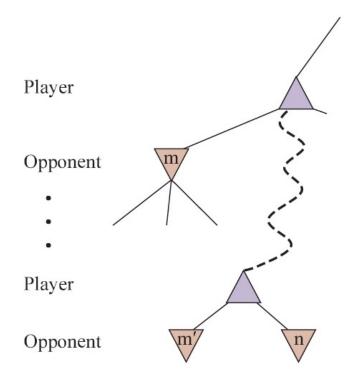
Russell & Norvig, AI: A Modern Approach

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## Multi-player (>2) Games

- Possible to extend MINMAX, algorithm is more complex
  - Extend values with vectors, corresponding to per player
  - Levels increase (per turn)
- In real games, players can often form alliances
  - Hard to model

# Alpha-Beta Pruning

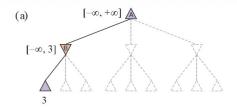


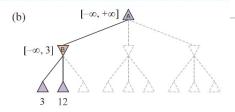
If m or m' is better than n for Player, search will never get to n

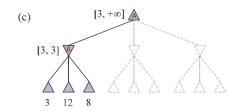
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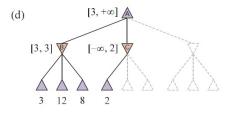
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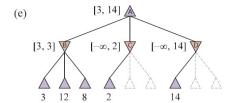
## Alpha-Beta Pruning

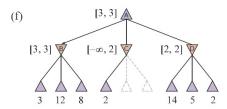












The first leaf below C has the value 2. Hence, C, which is a MIN node, has a value of at most 2. But we know that B is worth 3, so MAX would never choose C.

Adapted from:

Russell & Norvig, AI: A Modern Approach

### Alpha-Beta Pruning

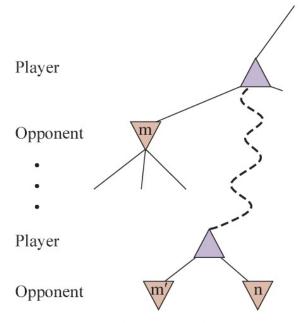
```
function ALPHA-BETA-SEARCH(game, state) returns an action
   player \leftarrow qame.To-MovE(state)
   value, move \leftarrow \text{MAX-VALUE}(game, state, -\infty, +\infty)
   return move
function MAX-VALUE(game, state, \alpha, \beta) returns a (utility, move) pair
   if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
   v \leftarrow -\infty
   for each a in game.ACTIONS(state) do
     v2, a2 \leftarrow \text{MIN-VALUE}(game, game. \text{RESULT}(state, a), \alpha, \beta)
     if v2 > v then
        v, move \leftarrow v2, a
        \alpha \leftarrow \text{MAX}(\alpha, v)
     if v \geq \beta then return v, move
   return v, move
function MIN-VALUE(game, state, \alpha, \beta) returns a (utility, move) pair
  if game.IS-TERMINAL(state) then return game.UTILITY(state, player), null
   v \leftarrow +\infty
  for each a in game.ACTIONS(state) do
     v2, a2 \leftarrow \text{MAX-VALUE}(game, game. \text{RESULT}(state, a), \alpha, \beta)
     if v2 < v then
        v, move \leftarrow v2, a
        \beta \leftarrow \text{MIN}(\beta, v)
     if v < \alpha then return v, move
   return v, move
```

Alpha: the best (highest, at least) value Beta: the best (lowest, at most) value

Adapted from: Russell & Norvig, AI: A Modern Approach

### Impact of Alpha Beta

- MINIMAX(O (b ^ m)
- Cuts down on size of game tree searched
  - Reduction depends on order of nodes traversed
  - Assuming order of nodes is random, expect to prune after exploring half the branches
  - Best case: O (b ^ (m/2)), where b is branching factor and m is depth



## Game Setting

- Gaming strategies
  - Random
  - Minimax
  - alphabeta
- two automated players
  - First: random
  - Second: alphabeta
  - Code Example: <a href="https://github.com/aimacode/aima-python/blob/master/games4e.ipynb">https://github.com/aimacode/aima-python/blob/master/games4e.ipynb</a>
- one human, one automated
  - First: human
  - Second: minimax

### Heuristic Alpha Beta Tree Search

#### H-MINIMAX(s) =

```
• Eval(s, MAX) if IS-CUTOFF(s, d)
```

- Max a in ACTIONS(S) H-MINIMAX(RESULT(s, a), d+1) if TO-MOVE(s) = MAX
- Min a in ACTIONS(S) H-MINIMAX(RESULT(s, a), d+1) if TO-MOVE(s) = MIN

#### Useful when

- Depth is very high, example Chess
- Good (informative) eval functions exists

Adapted from:

Russell & Norvig, AI: A Modern Approach

<sup>\*</sup> Cut-off search at depth d

<sup>\*</sup> Estimate utility of a state to player just like a heuristic function UTILITY(loss, p) <= EVAL (s, p) <= UTILITY(win, p)

# Coding Example

- 2-party games code notebook
  - <a href="https://github.com/aimacode/aima-python/blob/master/games4e.ipynb">https://github.com/aimacode/aima-python/blob/master/games4e.ipynb</a>
  - Has
    - Minimax
    - Alphabeta
    - Heuristic alpha beta

### Searching in Larger Games

#### Game characteristics

- large branching factor Go (361)
- difficult to get a meaningful evaluation function (heuristics)

#### Key Idea

- Value of a state is estimated as the average utility over a number of simulations of complete games from that state
- Get information of good plays by self-play and learning using neural networks

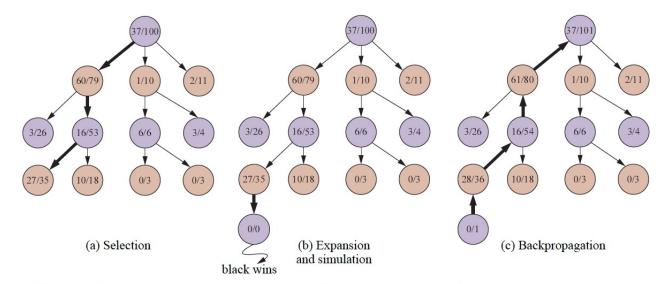
### Monte Carlo Tree Search (MTCS)

```
function Monte-Carlo-Tree-Search(state) returns an action tree \leftarrow \text{Node}(state)
while Is-Time-Remaining() do leaf \leftarrow \text{Select}(tree)
child \leftarrow \text{Expand}(leaf)
result \leftarrow \text{Simulate}(child)
Back-Propagate(result, child)
return the move in Actions(state) whose node has highest number of playouts
```

Adapted from:

Russell & Norvig, AI: A Modern Approach

### Monte Carlo Tree Search (MCTS)



**Figure 5.10** One iteration of the process of choosing a move with Monte Carlo tree search (MCTS) using the upper confidence bounds applied to trees (UCT) selection metric, shown after 100 iterations have already been done. In (a) we select moves, all the way down the tree, ending at the leaf node marked 27/35 (for 27 wins for black out of 35 playouts). In (b) we expand the selected node and do a simulation (playout), which ends in a win for black. In (c), the results of the simulation are back-propagated up the tree.

function MONTE-CARLO-TREE-SEARCH(state) returns an action
tree ← NODE(state)
while Is-TIME-REMAINING() do
leaf ← SELECT(tree)
child ← EXPAND(leaf)
result ← SIMULATE(child)
BACK-PROPAGATE(result, child)
return the move in ACTIONS(state) whose node has highest number of playouts

Adapted from:

Russell & Norvig, Al: A Modern Approach

# Coding Example

- MCTS code notebook
  - https://pypi.org/project/mcts-simple/
  - <a href="https://colab.research.google.com/drive/1uYCDn\_lymEhexepKfBXcMqiHquyhZpZ5?usp=sharing">https://colab.research.google.com/drive/1uYCDn\_lymEhexepKfBXcMqiHquyhZpZ5?usp=sharing</a>

#### References:

- https://deepmind.google/technologies/alphago/
- https://deepmind.google/technologies/alphazero-and-muzero/
- https://en.wikipedia.org/wiki/AlphaGo
- https://deepmind.google/discover/blog/alphastar-grandmaster-level-instarcraft-ii-using-multi-agent-reinforcement-learning/

### AlphaGo

Search with neural network based estimation

Alpha Solvers

- Two NNs: first "policy network" selects the next move to play, second the "value network" predicts the winner of the game.
- Developed for Go; learned from human players and self-play

#### AlphaZero

- Given rules of the game (in mathematical form)
- · Uses reinforcement learning
- Plays multiple games (Go, Chess, Shogi), learned from self-play
- · Developed newer methods for faster sorting, hashing, and matrix multiplication algorithms

#### MuZero

- Models three aspects of its environment how good is the current position? Which action is the best to take? And how good was the last action?
- Plays multiple games (Go, Chess, Shogi, Atari family), learned from self-play

#### AlphaDev

- · self-play via reinforcement learning, multi-agent learning, and imitation learning
- Example: self-play with a group of players (league)

## Lecture 18: Summary

- We talked about
  - Games and Search
  - Minimax
  - Alphabeta
  - Monte Carlo Tree Search

# Lecture 19: Optimization

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### Lecture 19: Outline

#### We will discuss

- Constraints Satisfaction Problems
- Optimization

### Constraint Satisfaction Problems (CSPs)

- X A set of variables {X<sub>1</sub>, ..., X<sub>n</sub>}
- D A set of domains {D<sub>1</sub>, ..., D<sub>n</sub>}, for each variable
- C set of constraints specifying allowed combinations of values for variables

#### Example

```
• X_1 = \{1,2,3\}, X_2 = \{1,2,3\}
```

• Here, 
$$D_1 = D_2 = \{1,2,3\}$$

• 
$$C = \langle (X_1, X_2), X_1 > X_2 \rangle$$

Solutions = Assignments to  $(X_1, X_2) = \{(3,1), (3,2), (2,1)\}$ 

### Example: Map-Coloring



Variables WA, NT, Q, NSW, V, SA, T

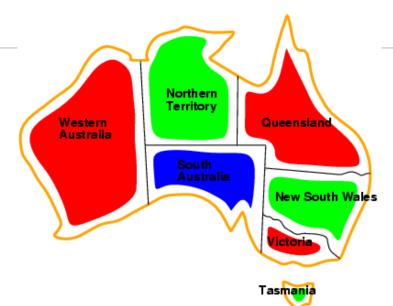
Domains  $D_i$  = {red, green, blue}

Constraints: adjacent regions must have different colors

e.g., WA ≠ NT, or (WA,NT) in {(red,green),(red,blue),(green,red), (green,blue),(blue,red),(blue,green)}

Adapted from: Tuomas Sandholm's CSP Lecture Russell & Norvig, AI: A Modern Approach

## Example: Map-Coloring



Solutions are complete and consistent assignments

e.g., WA = red, NT = green, Q = red, NSW = green, V = red, SA = blue,T = green

Adapted from: Tuomas Sandholm's CSP Lecture Russell & Norvig, AI: A Modern Approach

### Varieties of CSPs

#### Discrete variables

- finite domains:
  - n variables, domain size  $d \rightarrow O(d^n)$  complete assignments
  - e.g., Boolean CSPs, includes Boolean satisfiability (NP-complete)
- infinite domains:
  - integers, strings, etc.
  - e.g., job scheduling, variables are start/end days for each job
  - need a constraint language, e.g.,  $StartJob_1 + 5 \le StartJob_3$

#### Continuous variables

- e.g., start/end times for Hubble Space Telescope observations
- linear constraints solvable in polynomial time by LP

Adapted from: Tuomas Sandholm's CSP Lecture Russell & Norvig, AI: A Modern Approach

### Varieties of constraints

Unary constraints involve a single variable,

• e.g., SA ≠ green

Binary constraints involve pairs of variables,

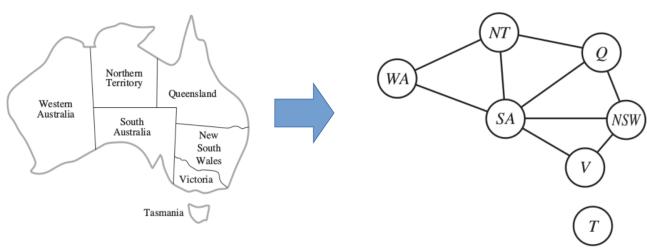
• e.g., SA ≠ WA

Higher-order constraints involve 3 or more variables,

• e.g., cryptarithmetic column constraints

Adapted from: Tuomas Sandholm's CSP Lecture Russell & Norvig, AI: A Modern Approach

### The constraint graph



Binary CSP: each constraint relates at most two variables

Constraint graph: nodes are variables, arcs show constraints

General-purpose CSP algorithms use the graph structure to speed up search

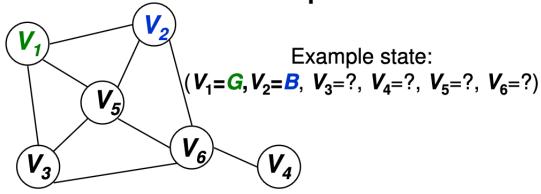
E.g., Tasmania is an independent subproblem!

### Adapted from:

- https://www.khoury.northeastern. edu/home/camato/5100/csp.pdf
- https://www.cs.cmu.edu/afs/cs/ac ademic/class/15381s07/www/slides/020107CSP.pdf

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## Search Space



- State: assignment to k variables with k+1,..,N unassigned
- Successor. The successor of a state is obtained by assigning a value to variable k+1, keeping the others unchanged
- Start state: (V<sub>1</sub>=?, V<sub>2</sub>=?, V<sub>3</sub>=?, V<sub>4</sub>=?, V<sub>5</sub>=?, V<sub>6</sub>=?)
- Goal state: All variables assigned with constraints satisfied
- No concept of cost on transition → We just want to find a solution, we don't worry how we get there

### Adapted from:

- Tuomas Sandholm's CSP Lecture
- <a href="https://www.khoury.northeastern.">https://www.khoury.northeastern.</a>
   edu/home/camato/5100/csp.pdf
- https://www.cs.cmu.edu/afs/cs/ac ademic/class/15381s07/www/slides/020107CSP.pdf

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### Example: Cryptarithmetic

- VariablesD, E, M, N, O, R, S, Y
- Domains{0, 1, 2, 3, 4, 5, 6, 7, 8, 9}
- Constraints

$$M \neq 0$$
,  $S \neq 0$  (unary constraints)  
 $Y = D + E$  OR  $Y = D + E - 10$ .  
 $D \neq E$ ,  $D \neq M$ ,  $D \neq N$ , etc.



### Adapted from:

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### A harder CSP to represent: Cryptarithmetic

### Variables:

$$F T U W R O X_1 X_2 X_3$$

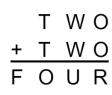
Domains:

$$\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

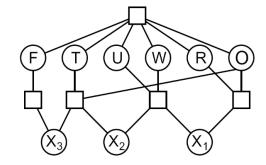
#### Constraints:

$$O + O = R + 10 \cdot X_1$$

. . .







### Adapted from:

- https://www.khoury.northeastern.edu/home/camato/5100/csp.pdf
- https://www.cs.cmu.edu/afs/cs/ac ademic/class/15381s07/www/slides/020107CSP.pdf

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### Example: N-Queens

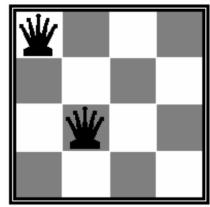
Variables: Q<sub>i</sub>

• Domains:  $D_i = \{1, 2, 3, 4\}$ 

Constraints

-Q<sub>i</sub>≠Q<sub>i</sub> (cannot be in same row)

 $-|\mathbf{Q}_{\mathbf{i}} - \mathbf{Q}_{\mathbf{j}}| \neq |\mathbf{i} - \mathbf{j}|$  (or same  $Q_1 = 1$   $Q_2 = 3$ diagonal)



$$Q_1 = 1$$
  $Q_2 = 3$ 

 Valid values for (Q<sub>1</sub>, Q<sub>2</sub>) are (1,3) (1,4) (2,4) (3,1) (4,1)(4,2)

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# Constraint Propagation

- Node Consistency: a variable (node in CSP graph) is node—consistent of all the values in the variable's domain satisfy variable's unary constraints
- Arc Consistency: every variable in its domain satisfies binary constraints

```
function AC-3(csp) returns false if an inconsistency is found and true otherwise
  queue \leftarrow a queue of arcs, initially all the arcs in csp
  while queue is not empty do
     (X_i, X_i) \leftarrow POP(queue)
     if REVISE(csp, X_i, X_i) then
       if size of D_i = 0 then return false
       for each X_k in X_i. NEIGHBORS - \{X_i\} do
          add (X_k, X_i) to queue
  return true
function REVISE(csp, X_i, X_i) returns true iff we revise the domain of X_i
  revised \leftarrow false
  for each x in D_i do
     if no value y in D_i allows (x,y) to satisfy the constraint between X_i and X_i then
       delete x from D_i
        revised \leftarrow true
  return revised
```

Adapted from:

Russell & Norvig, AI: A Modern Approach

## Constraint Propagation

- Path Consistency: A two variables set  $\{X_i, X_j\}$  is path-consistent with respect to a third variable  $X_m$  if, for every assignment  $\{X_i = a_i, X_j = a_j\}$  consistent with constraints on  $\{X_i, X_j\}$ , there is an assignment to  $X_m$  which is consistent with  $\{X_i, X_m\}$  and  $\{X_m, X_i\}$
- **k-consistency**: A CSP is k-consistent if for any set of (k-1) variables and their consistent assignments, a consistent value can always be assigned for the k<sup>th</sup> variable.

# CSP: Coding Example

- CSP code notebook
  - https://github.com/aimacode/aima-python/blob/master/csp.ipynb/

# Making Optimal Decisions

# Optimal Decision

- What is it? There is no absolute answer. In AI, there is the concept of a rational agent.
- Acting rationally: acting such that one ca achieve one's goals given one's beliefs (and information)
  - But what are one's goals
  - Are the always of achievement?

#### Some options

- Perfect rationality: maximize expected utility at every time instant
  - Given the available information; can be computationally expensive
  - "Doing the right thing"
- Bounded optimality: do as well as possible given computational resources
  - Expected utility as high as any other agent with similar resources
- · Calculative rationality: eventually returns what would have been the rational choice

### What Is It?

- As a working principle
  - Bounded or Calculative Rationality
- In observable and deterministic scenarios
  - Maximize utility: (benefit cost)
- In scenarios with uncertainty and/ or unobservable
  - Maximize expected utility: (benefit cost)

# Example Situation – Course Selection

- A person wants to pass an academic program in two majors: A and B
- There are three subjects: A, B and C, each with three levels (\*1, \*2, \*3). There are thus 9 courses: A1, A2, A3, B1, B2, B3, C1, C2, C3
- To graduate, at least one course at beginner (\*1) level is needed in major(s) of choice(s), and two courses at intermediate levels (\*2) are needed
- Optimality considerations in the problem
  - Least courses, fastest time to graduate, class size, friends attending together, ...
- Answer questions
  - Q1: How many minimum courses does the person have to take?
  - Q2: Can a person graduate in 2 majors studying 3 courses only?
  - ...

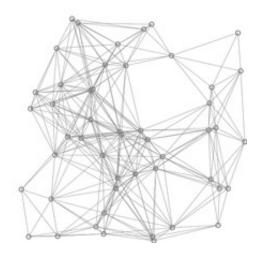
# Algorithms for Optimality

- Problem specific methods
  - Path finding
  - Linear programming
  - Constraint satisfaction and optimization
- General-purpose methods for optimality using search

# Optimality: Example - Path Finding

#### Main steps

- Mark all nodes unvisited. Create a set of all the unvisited nodes called the unvisited set.
- 2. Assign to every node a tentative distance value: set it to zero for our initial node and to infinity for all other nodes. Set the initial node as current.
- 3. For the current node, consider all of its unvisited neighbors and calculate their tentative distances through the current node. Compare the newly calculated tentative distance to the current assigned value and assign the smaller one.
- 4. When we are done considering all of the unvisited neighbors of the current node, mark the current node as visited and remove it from the *unvisited set*. A visited node will never be checked again.
- If the destination node has been marked visited or if the smallest tentative distance among the nodes in the *unvisited set* is infinity, then stop. The algorithm has finished.
- 6. Otherwise, select the unvisited node that is marked with the smallest tentative distance, set it as the new "current node", and go back to step 3.



A demo of Dijkstra's algorithm based on Euclidean distance

Djikstra's Algorithm with positive numbers or labels that are monotonically non-decreasing.

Source: https://en.wikipedia.org/wiki/Dijkstra%27s\_algorithm

### Exercise and Code

- Linear Programming Methods
  - Link <a href="https://github.com/biplav-s/course-d2d-ai/blob/main/sample-code/l16-optimal/Optimization.ipynb">https://github.com/biplav-s/course-d2d-ai/blob/main/sample-code/l16-optimal/Optimization.ipynb</a>

# OR and N- Queens

• Code sample: <a href="https://developers.google.com/optimization/cp/queens">https://developers.google.com/optimization/cp/queens</a>

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# Lecture 19: Summary

- We talked about
  - Constraint Satisfaction Problem
  - Optimization Problems

# Week 10: Concluding Comments

#### We talked about

- Lecture 18: Adversarial and Game Search
- Lecture 19: Optimization

- Week 1: Introduction, Aim: Chatbot / Intelligence Agent
- Weeks 2-3: Data: Formats, Representation and the Trust Problem
- Week 3: Machine Learning Supervised (Classification)
- Week 4: Machine Learning Unsupervised (Clustering) -
- Topic 5: Learning neural network, deep learning, <u>Adversarial attacks</u>
- Week 6: <u>Large Language Models</u> Representation and Usage issues
- Weeks 7-8: Search, Heuristics Decision Making
- Week 9: Constraints, Optimization Decision Making
- Topic 10: Markov Decision Processes, Hidden Markov models -Decision making
- Topic 11-12: Planning, Reinforcement Learning Sequential decision making
- Week 13: <u>Trustworthy Decision Making</u>: <u>Explanation</u>, AI testing
- Week 14: <u>AI for Real World: Tools, Emerging Standards and Laws;</u>
   Safe AI/ Chatbots

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## Projects B: Sep 30 - Nov 20 (7 weeks; 400 points)

- End date: Thursday, Nov 20
  - Remember to update spreadsheet on data/ time when finished (Column I)
- Choices
  - Given by instructor
  - Defined by student using project-b teamplate; reviewed and approved by instructor

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# Upcoming Evaluation Milestones

• Projects B: Sep 30 – Nov 20

• Quiz 2: Oct 7

• Quiz 3: Nov 11

Paper presentation (grad students only): Nov 18

• Finals: Dec 11

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# About Week 11 – Lectures 20, 21

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# Week 11 – Lectures 20, 21

- Lecture 18: Making Decisions -Simple
- Lecture 19: Making Decisions -Complex

- Week 1: Introduction, Aim: Chatbot / Intelligence Agent
- Weeks 2: Data: Formats, Representation, ML Basics
- Week 3: Machine Learning Supervised (Classification)
- Week 4: Machine Learning Unsupervised (Clustering) -
- Topic 5: Learning neural network, deep learning, <u>Adversarial attacks</u>
- Week 6: Large Language Models Representation and Usage issues
- Weeks 7-8: Search, Heuristics Decision Making
- Week 9: Constraints, Optimization Decision Making
- Topic 10: Markov Decision Processes, Hidden Markov models -Decision making
- Topic 11-12: Planning, Reinforcement Learning Sequential decision making
- Week 13: <u>Trustworthy Decision Making</u>: <u>Explanation</u>, AI testing
- Week 14: <u>AI for Real World: Tools, Emerging Standards and Laws;</u>
   <u>Safe AI/ Chatbots</u>

**Note**: exact schedule changes slightly to accommodate for exams and holidays.

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