Introduction to Machine Learning and Artificial Neural Networks (CS554)

Osman Furkan KINLI – S002969 - Assignment-3 Non-Linear Dimensionality Reduction (Polynomial Regression & KNN Regression & MLP Regression)

1. Introduction

In this assignment, we test three different algorithms (polynomial regression, k-th nearest neighbor and multi-layer perceptron) on a custom data set. Training and test data contains 25 samples for each, and given in the CSV format where each line represent one sample, the first value is independent variable x, and the second one is dependent variable y.

2. Methodology

- Implement Polynomial Regressor where the degree is a hyper-parameter
- Implement KNN Regressor where K is a hyper-parameter
- Implement Multi-layer Perceptron where number of hidden units is a hyperparameter
- Train these 3 algorithms with train set
- Choose best model for each algorithm by using validation set
- Plot the best model for each algorithm with the test set
- Report mean-squared error of the best model for each algorithm on the test set
- For MLP case, with the best model, plot the learned lines, the output of each hidden unit and the actual output

3. Code

import csv

```
print("TASK: Polynomial Regression")
def vectorize_poly(x, degree):
   vector = \overline{list()}
   for d in range(degree, -1, -1):
       vector.append(x**d)
       # print(vector)
   return np.array(vector).transpose()
def poly reg lse solver(x, y):
    return np.dot(np.dot(np.linalq.inv(np.dot(x.transpose(), x)),
x.transpose()), y)
def mse loss(y true, y pred):
   return np.square(np.subtract(y true, y pred)).mean()
def validate(x, w, y):
   y hat = np.dot(x, w)
   return mse loss(y, y hat)
def cross validate(x train, y train, x val, y val, max degree=10):
    losses = list()
    for degree in range(1, max degree+1):
        vec x train = vectorize poly(x train, degree)
        vec x val = vectorize poly(x val, degree)
       assert vec x train.shape == (25, degree+1)
       assert vec x val.shape == (25, degree+1)
w hat = poly reg lse solver(vec x train, y train)
     losses.append((degree, validate(vec x val, w hat, y val), w hat))
   return losses
losses = cross validate(train x, train y, val x, val y)
best degree, , best w hat = min(losses, key=lambda\ l:\ l[1])
# print(best degree)
# print(best w hat)
vec x test = vectorize poly(test x, best degree)
best model = np.dot(vec x test, best w hat)
plt.plot(test x, test y, "b+", test x, best model, "r")
plt.xlabel("X")
plt.ylabel("Value")
# plt.savefig('./images/poly reg best model fit on test.png')
plt.show()
print("MSE Error on Test set: {}".format(validate(vec x test, best w hat,
test y)))
print("-----")
```

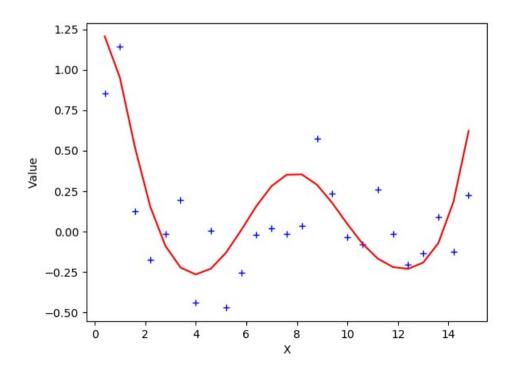
```
print("TASK: K-Nearest Neighbour Regression")
def calc dist(x1, x2):
   return (x1 - x2)**2
def knn regressor(k, x train, y train, x val):
   y pred = list()
    for x v in x val:
       distances = list()
        for x t, y t in zip(x train, y train):
           distances.append((v t, calc dist(x v, x t)))
       distances = sorted(distances, key=lambda d: d[1])
       distances = distances[:k]
       y pred.append(sum([d[0] for d in distances]) / k)
    return y pred
def find best k(x train, y train, x val, y val, max k=10):
    losses = list()
   for k in range(1, max k+1):
       y pred = knn regressor(k, x train, y train, x val)
       losses.append((k, mse loss(y val, y pred)))
   return min(losses, key=lambda l: l[1])[0]
best k = find best k(train x, train y, val x, val y)
y pred = knn regressor(best k, train x, train y, test x)
plt.plot(test x, test y, "b+", test x, y pred, "r")
plt.xlabel("X")
plt.ylabel("Value")
# plt.savefig('./images/knn reg best model fit on test.png')
plt.show()
print("MSE Error on Test set: {}".format(mse loss(test y, y pred)))
print("-----")
print("TASK: Multilayer Perceptron")
NUM EPOCH = 10
LR = 0.00001
def init weights(in channel, out channel):
   epsilon = np.sqrt(2.0 / (in channel * out channel))
   w = epsilon * np.random.randn(out channel, in channel)
   return w.transpose()
def init bias():
return 0
def run mlp(num hidden unit, X, y, weights=None, bias=None, is train=True):
   if weights is None:
       w1 = init weights(1, num hidden unit)
       w2 = init weights(num hidden unit, 1)
```

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else:
       w1, w2 = weights
    if bias is None:
        b1 = init bias()
       b2 = init bias()
    else:
       b1, b2 = bias
    def sigmoid(x):
        return 1 / (1 + np.exp(-x))
    def derivative sigmoid(x):
       return x * (1 - x)
    def forward(X ):
        z1 = np.dot(X , w1) + b1
        a1 = sigmoid(z1)
        z2 = np.dot(a1, w2) + b2
        return z1, z2
    def step(X_, y_, z1_, z2_, w1_, w2_): # TODO
        layer2_error = y_ - z2_
        layer2 delta = layer2 error * derivative sigmoid(z2)
        layer1 error = np.dot(layer2 delta, w2 .transpose())
        layer1 delta = layer1 error * derivative sigmoid(z1 )
        layer1 adjustment = np.dot(X .transpose(), layer1 delta)
        layer2 adjustment = np.dot(z1 .transpose(), layer2 delta)
       # Adjust the weights.
       w1_ += LR * layer1 adjustment
          += LR * layer2 adjustment
        return w1 , w2
    if is train:
        losses = list()
        for _ in range(NUM EPOCH):
            z1, z2 = forward(X)
            losses.append(0.5 * np.square(y - z2).mean())
            w1, w2 = step(X, y, z1, z2, w1, w2)
        final loss = losses[-1]
    else:
        , z2 = forward(X)
        final loss = 0.5 * np.square(y - z2).mean()
return (w1, w2), (b1, b2), final_loss, z2
model lst = list()
for i in range(1, 101):
    weights, bias, _, _ = run_mlp(i, np.expand_dims(train_x, axis=-1),
np.expand_dims(train_y, axis=-1))
    _, _, val_loss, _ = run_mlp(i, np.expand_dims(val x, axis=-1),
                            np.expand_dims(val_y, axis=-1),
weights=weights, bias=bias, is train=False)
   model lst.append((i, weights, bias, val loss))
best_mlp_model = min(model lst, key=lambda m: m[3])
```

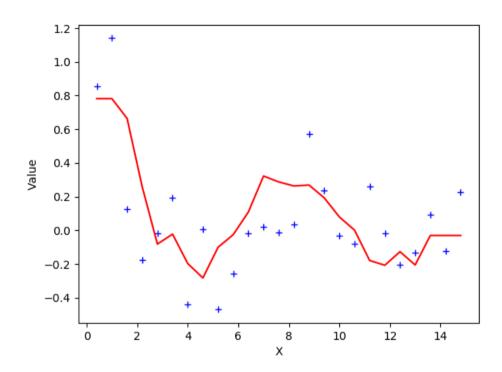
```
best num hidden unit, best weights, best bias, = best mlp model
, , test loss, y pred = run mlp(best num hidden unit,
np.expand dims(test x, axis=-1),
                               np.expand dims(test y, axis=-1),
weights=best weights,
                           bias=best bias, is train=False)
plt.plot(test x, test y, "b+", test x, y pred, "r")
plt.xlabel("X")
plt.ylabel("Value")
# plt.savefig('./images/mlp_best_model fit on test.png')
plt.show()
print("MSE Error on Test set: {}".format(test loss))
print("-----")
# plt.plot(train x, train y, "b+", train x, y pred, "r")
# plt.xlabel("X")
# plt.ylabel("Value")
# # plt.savefig('./images/mlp best model fit on test.png')
# plt.show()
# print("MSE Error on Test set: {}".format(test_loss))
# print("------
```

4. Results

• Best model fitted on test set for Polynomial Regression



• Best model fitted on test set for KNN Regression



• Best model fitted on test set for MLP Regression

