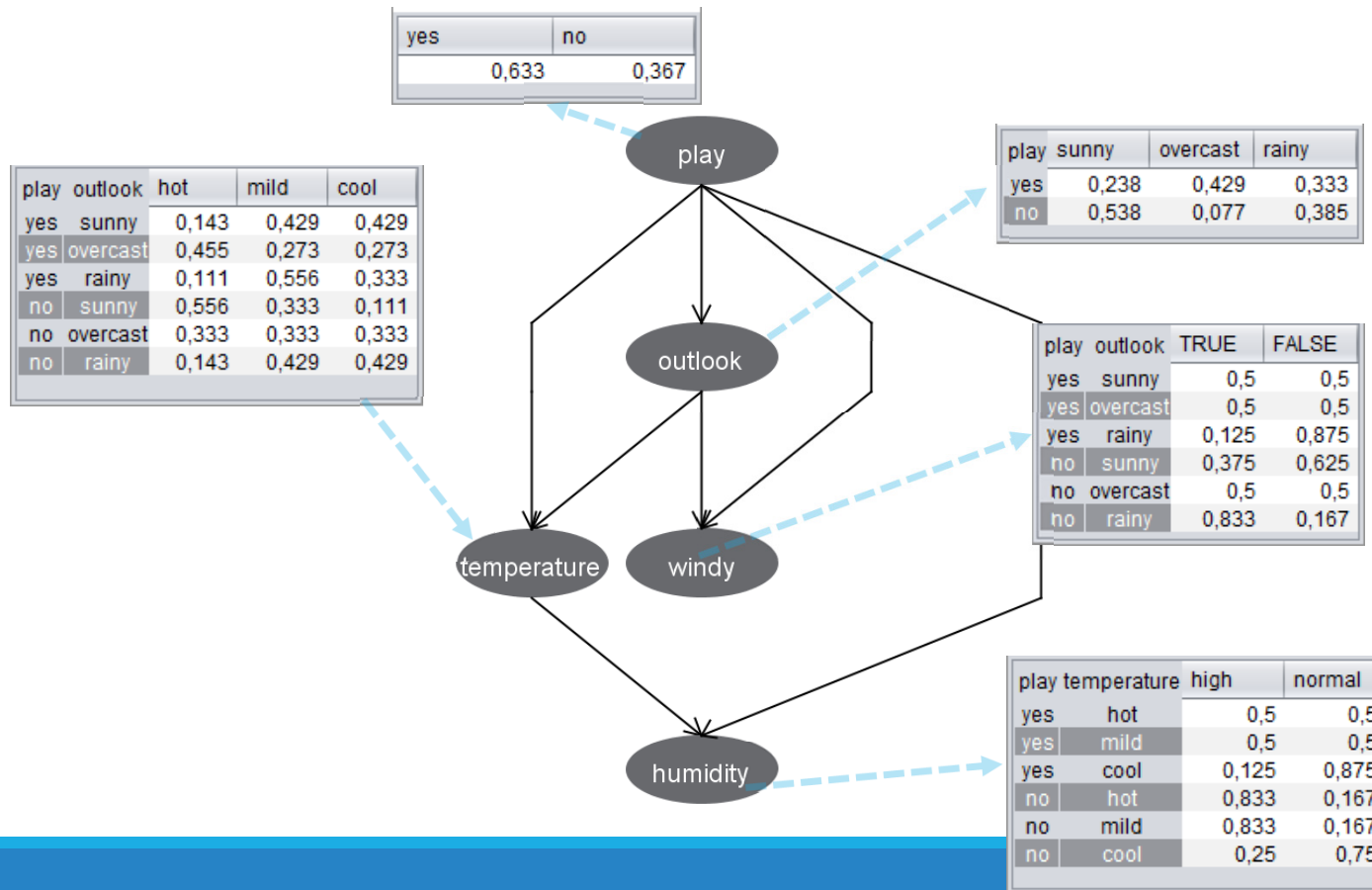
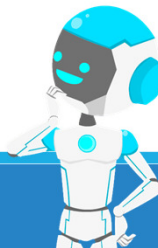


# Redes Bayesianas



| outlook  | temperature | humidity | windy | play |
|----------|-------------|----------|-------|------|
| sunny    | hot         | high     | FALSE | no   |
| sunny    | hot         | high     | TRUE  | no   |
| overcast | hot         | high     | FALSE | yes  |
| rainy    | mild        | high     | FALSE | yes  |
| rainy    | cool        | normal   | FALSE | yes  |
| rainy    | cool        | normal   | TRUE  | no   |
| overcast | cool        | normal   | TRUE  | yes  |
| sunny    | mild        | high     | FALSE | no   |
| sunny    | cool        | normal   | FALSE | yes  |
| rainy    | mild        | normal   | FALSE | yes  |
| sunny    | mild        | normal   | TRUE  | yes  |
| overcast | mild        | high     | TRUE  | yes  |
| overcast | hot         | normal   | FALSE | yes  |
| rainy    | mild        | high     | TRUE  | no   |



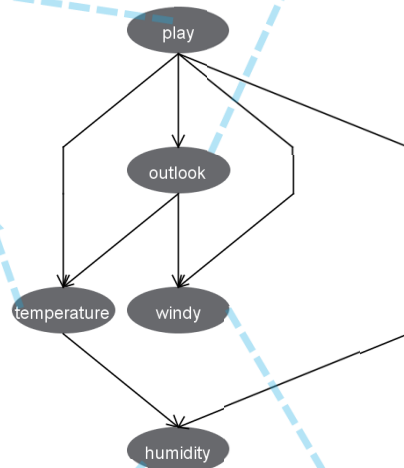
| play | sunny | overcast | rainy |
|------|-------|----------|-------|
| yes  | 0,238 | 0,429    | 0,333 |
| no   | 0,538 | 0,077    | 0,385 |

1: outlook 2: temperature 3: humidity 4: windy  
 Nominal Nominal Nominal Nominal  
 sunny hot high FALSE

| yes   | no    |
|-------|-------|
| 0,633 | 0,367 |

|        | Class | Outlook<br>P(outlook   Play) | Temperature<br>P(temperature   outlook, play) | Humidity<br>P(Humidity   tem<br>perature, Play) | Windy<br>P(Windy   outlook,<br>Play) |
|--------|-------|------------------------------|---|---|--------------------------------------|
| P(Yes) | 0,633 | 0,238                        | 0,143   | 0,5   | 0,5                                  |
| P(No)  | 0,367 | 0,538                        | 0,556   | 0,833   | 0,5                                  |

| play | outlook  | hot   | mild  | cool  |
|------|----------|-------|-------|-------|
| yes  | sunny    | 0,143 | 0,429 | 0,429 |
| yes  | overcast | 0,455 | 0,273 | 0,273 |
| yes  | rainy    | 0,111 | 0,556 | 0,333 |
| no   | sunny    | 0,556 | 0,333 | 0,111 |
| no   | overcast | 0,333 | 0,333 | 0,333 |
| no   | rainy    | 0,143 | 0,429 | 0,429 |



| play | temperature | high  | normal |
|------|-------------|-------|--------|
| yes  | hot         | 0,5   | 0,5    |
| yes  | mild        | 0,5   | 0,5    |
| yes  | cool        | 0,125 | 0,875  |
| no   | hot         | 0,833 | 0,167  |
| no   | mild        | 0,833 | 0,167  |
| no   | cool        | 0,25  | 0,75   |

| play | outlook  | TRUE  | FALSE |
|------|----------|-------|-------|
| yes  | sunny    | 0,5   | 0,5   |
| yes  | overcast | 0,5   | 0,5   |
| yes  | rainy    | 0,125 | 0,875 |
| no   | sunny    | 0,375 | 0,625 |
| no   | overcast | 0,5   | 0,5   |
| no   | rainy    | 0,833 | 0,167 |

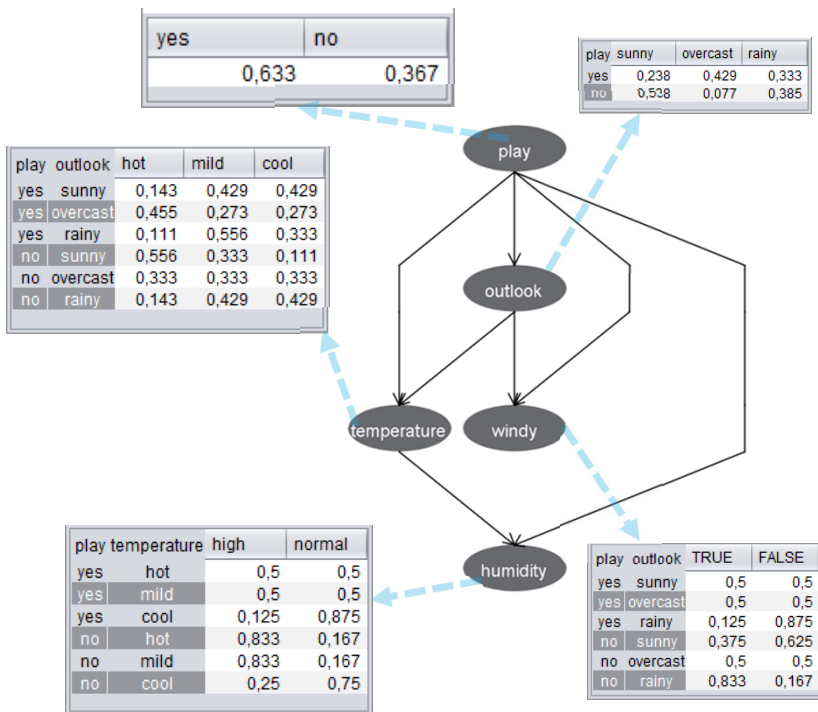
$$P(\text{yes}) = 0,633 * 0,238 * 0,143 * 0,5 * 0,5 = 0,00538588$$

$$P(\text{no}) = 0,367 * 0,538 * 0,556 * 0,833 * 0,5 = 0,045723$$



# Classificador de Rede Bayesiana

## Tabelas de distribuição de probabilidade



## Calculando uma Previsão

### Dados

| Outlook | Temperature | Humidity | Windy |
|---------|-------------|----------|-------|
| sunny   | hot         | high     | FALSE |

### Probabilidades

|        | Class | Outlook<br>P(outlook   Play) | Temperature<br>P(temperature   outlook, play) | Humidity<br>P(Humidity   temperature, Play) | Windy<br>P(Windy   outlook, Play) |
|--------|-------|------------------------------|---|---|-----------------------------------|
| P(Yes) | 0,633 | 0,238                        | 0,143   | 0,5   | 0,5                               |
| P(No)  | 0,367 | 0,538                        | 0,556   | 0,833                                       | 0,5                               |

### Cálculos

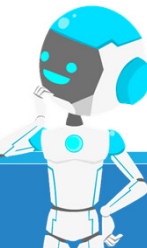
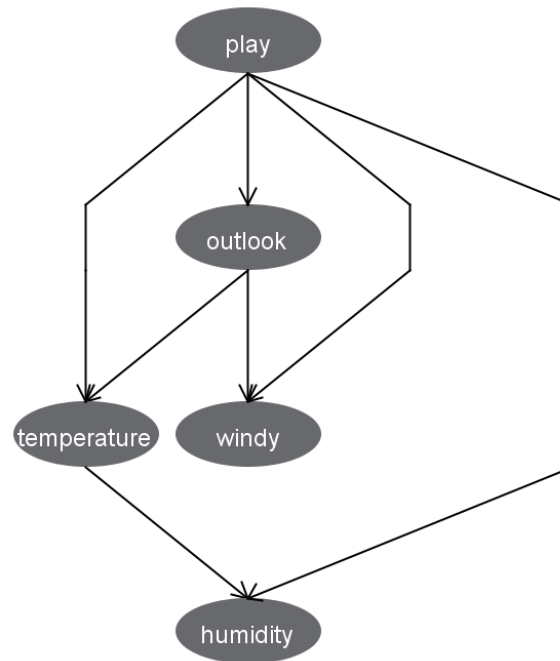
$$P(\text{yes}) = 0,633 * 0,238 * 0,143 * 0,5 * 0,5 = 0,00538588$$

$$P(\text{no}) = 0,367 * 0,538 * 0,556 * 0,833 * 0,5 = 0,045723$$

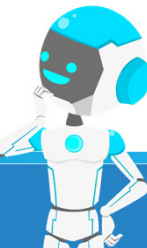
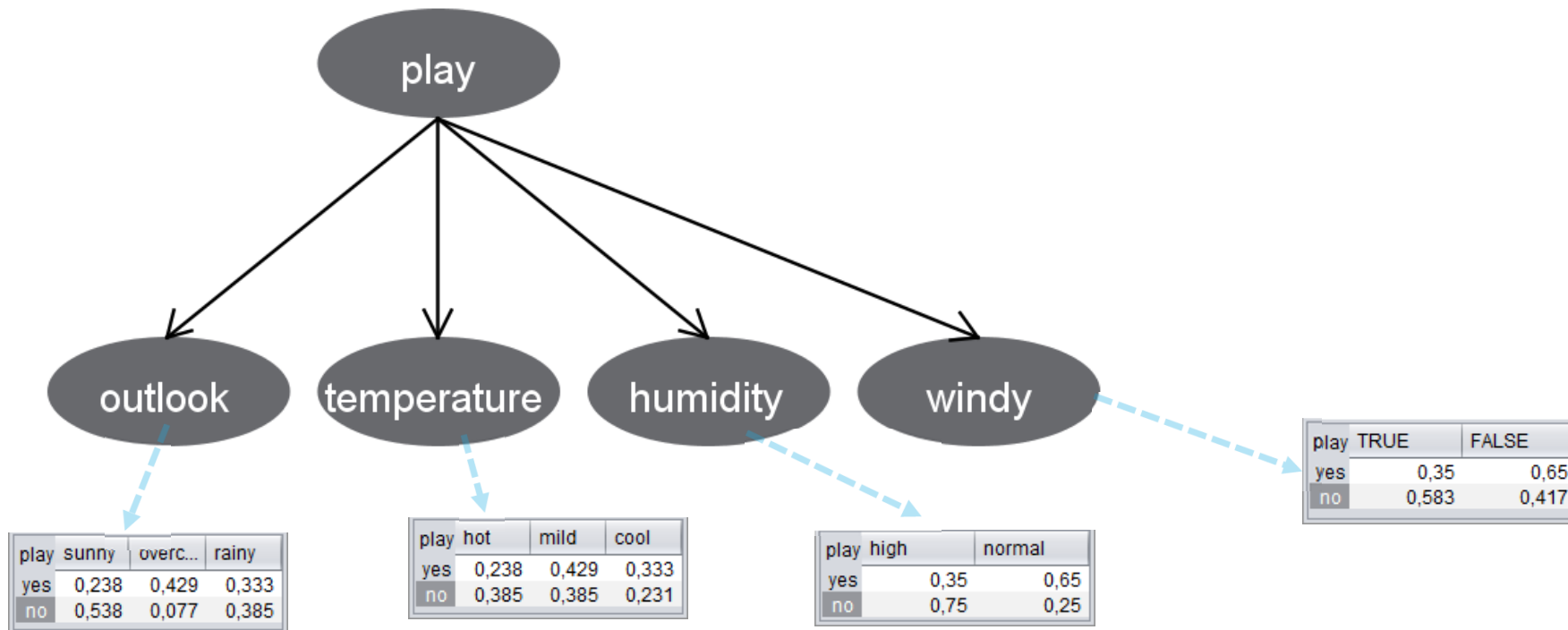
**Resultado: no**

# Dois pais

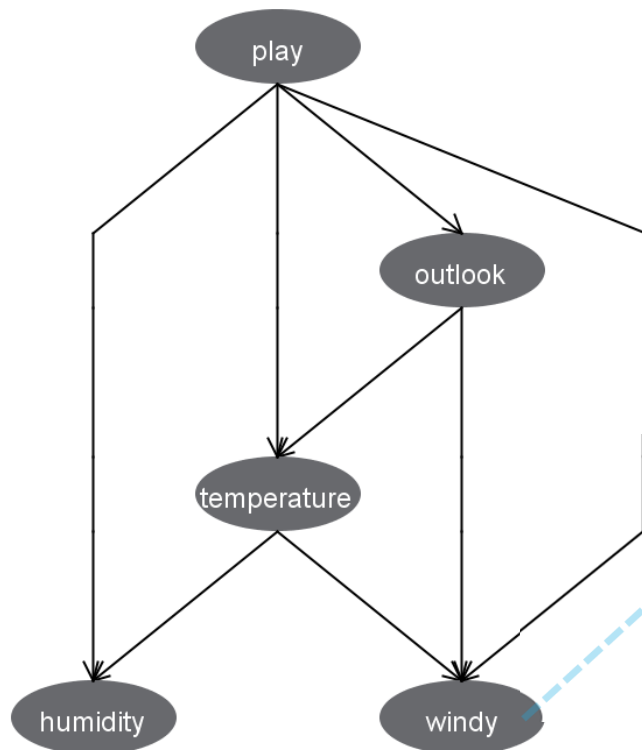
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# Redes Bayesianas com 1 pai apenas



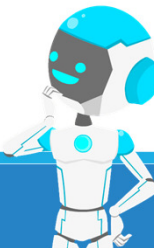
# Aumentando o número de pais



| play | outlook  | temperature | TRUE  | FALSE |
|------|----------|-------------|-------|-------|
| yes  | sunny    | hot         | 0,5   | 0,5   |
| yes  | sunny    | mild        | 0,75  | 0,25  |
| yes  | sunny    | cool        | 0,25  | 0,75  |
| yes  | overcast | hot         | 0,167 | 0,833 |
| yes  | overcast | mild        | 0,75  | 0,25  |
| yes  | overcast | cool        | 0,75  | 0,25  |
| yes  | rainy    | hot         | 0,5   | 0,5   |
| yes  | rainy    | mild        | 0,167 | 0,833 |
| yes  | rainy    | cool        | 0,25  | 0,75  |
| no   | sunny    | hot         | 0,5   | 0,5   |
| no   | sunny    | mild        | 0,25  | 0,75  |
| no   | sunny    | cool        | 0,5   | 0,5   |
| no   | overcast | hot         | 0,5   | 0,5   |
| no   | overcast | mild        | 0,5   | 0,5   |
| no   | overcast | cool        | 0,5   | 0,5   |
| no   | rainy    | hot         | 0,5   | 0,5   |
| no   | rainy    | mild        | 0,75  | 0,25  |
| no   | rainy    | cool        | 0,75  | 0,25  |

Dois pais (anterior)

| play | outlook  | TRUE  | FALSE |
|------|----------|-------|-------|
| yes  | sunny    | 0,5   | 0,5   |
| yes  | overcast | 0,5   | 0,5   |
| yes  | rainy    | 0,125 | 0,875 |
| no   | sunny    | 0,375 | 0,625 |
| no   | overcast | 0,5   | 0,5   |
| no   | rainy    | 0,833 | 0,167 |



# Todas as possibilidades

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$$3 \times 3 \times 2 \times 2 \times 2 = 72$$

| outlook  | temperature | humidity | windy | play |
|----------|-------------|----------|-------|------|
| sunny    | hot         | high     | FALSE | no   |
| sunny    | hot         | high     | TRUE  | no   |
| overcast | hot         | high     | FALSE | yes  |
| rainy    | mild        | high     | FALSE | yes  |
| rainy    | cool        | normal   | FALSE | yes  |
| rainy    | cool        | normal   | TRUE  | no   |
| overcast | cool        | normal   | TRUE  | yes  |
| sunny    | mild        | high     | FALSE | no   |
| sunny    | cool        | normal   | FALSE | yes  |
| rainy    | mild        | normal   | FALSE | yes  |
| sunny    | mild        | normal   | TRUE  | yes  |
| overcast | mild        | high     | TRUE  | yes  |
| overcast | hot         | normal   | FALSE | yes  |
| rainy    | mild        | high     | TRUE  | no   |

# Como construir um modelo?

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Estrutura de rede - Número de pais

- Algoritmo de busca: hill climber, tabu search etc.

Tabelas de distribuição de probabilidade

- Estimador

