Poisson's relation

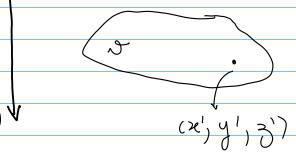
scalar magnetic potetial produced by a source with constant total magnetization

$$(x,y,z) = Cmh \iint_{\mathcal{A}} \frac{L}{r} dr$$

$$\hat{\Lambda} = \begin{bmatrix} \cos I \cos D \\ \cos I \sin D \end{bmatrix}$$

$$= \begin{bmatrix} \cos I \sin D \\ \sin I \end{bmatrix}$$





$$V(x_{1}y_{1}z) = -\begin{bmatrix} \partial_{x} \oplus \\ \partial_{y} \oplus \\ \\ \partial_{z} \oplus \end{bmatrix}^{T} \qquad \lambda_{x} \oplus = \underbrace{\partial \oplus (x_{1}y_{1}z)}_{\partial x} = cm h \underbrace{\int \int \alpha' - \alpha d\alpha'}_{T^{2}} d\alpha'$$

$$\alpha = x_{1}y_{1}z_{2}$$

gravitational potential produced by a source with constant density

alfa-component of the gravitational acceleration

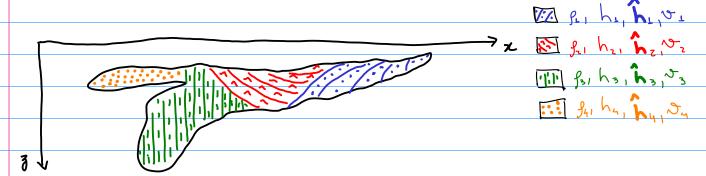
$$\partial_{\alpha}U = \frac{\partial U(x,y,3)}{\partial \alpha} = G_{\beta} \iiint \frac{\alpha'-\alpha}{r^3} dv, \quad \alpha = x,y,3$$

$$\partial_{\alpha} \Theta = \frac{cmh}{GP} \partial_{\alpha} O \qquad V(x,y,z) = -\frac{cmh}{GP} \nabla U(x,y,z)^{T}$$

$$\nabla \Theta(x,y,z) = \frac{cmh}{G\beta} \nabla O(x,y,z)$$

According to the conditions specified above, the scalar magnetic potential represents the directional derivative of the gravitational potential along the total-magnetization direction of the source. This equation is known as Poisson's relation (Blakely, 1996, p. 91).

(x, h, z)



$$V(x,y,z) = V_1(x,y,z) + V_2(x,y,z) + V_3(x,y,z) + V_4(x,y,z)$$

$$U(x_1,y_1,z) = U_1(x_1,y_1,z) + U_2(x_1,y_1,z) + U_3(x_1,y_1,z) + U_4(x_1,y_1,z)$$

$$V_{3}(x,y,3) = -\frac{cm h_{3}}{G f_{3}} \nabla U_{3}(x_{1}y_{1}3)^{T} \hat{h}_{3} \qquad V_{4}(x,y,3) = -\frac{cm h_{4}}{G f_{4}} \nabla U_{4}(x_{1}y_{1}3)^{T} \hat{h}_{4}$$

Poisson's relation for a heterogeneous body

$$\frac{V(x_1y_13) = -(\frac{cmh_1}{G_{11}} \nabla U_1(x_1y_13)^{T} \hat{h}_1 + \frac{cmh_2}{G_{12}} \nabla U_2(x_1y_13)^{T} \hat{h}_2 + \frac{cmh_3}{G_{13}} \nabla U_3(x_1y_13)^{T} \hat{h}_3 + \frac{cmh_4}{G_{13}} \nabla U_4(x_1y_13)^{T} \hat{h}_4}{G_{13}}$$

B

Ex: Deduce the relation between the magnetic induction and derivatives of the gravitational potential.

NT = P'B

Ex: Deduce the relation between the approximated total-field anomaly and derivatives of the gravotational potential.