Application of the Neumann's problem



where are the unit vectors 📙 and 🕻

this function is equivalent to the vertical component of the

gravitational attraction produced by a source with positive density Hence, the scalar magnetic potential can be rewritten as follows:

$$V(x_0, y_0, y_0) = -\nabla \Theta(x_0, y_0, y_0)^{T} \hat{h}$$

$$= -\left[(\cos I \cos S) \right] \int_{-\infty}^{\infty} P(x_1, y_1, y_0) dx + dx dy + (\cos I \sin D) \int_{-\infty}^{\infty} P(x_1, y_1, y_0) dx + dx dy + (\sin I) \int_{-\infty}^{\infty} P(x_1, y_1, y_0) dx + dx dy + (\sin I) \int_{-\infty}^{\infty} P(x_1, y_1, y_0) dx + dx dy$$

$$= -\int_{-\infty}^{\infty} P(x_1, y_1, y_0) \nabla \frac{1}{x_0} \nabla \frac{1}$$

In this case, the $\, lpha \,$ -component of the magnetic induction can be defined by the following integral:

$$B_{\alpha}(x_{0}, y_{0}, y_{0}) = -\partial_{\alpha}V(x_{0}, y_{0}, y_{0}, y_{0})$$

$$= \int_{00}^{00} P(x_{0}, y_{0}, y_{0}) \left[\partial_{\alpha}x + \partial_{\alpha}y + \partial_{$$

By using this integral, we can define the approximated total-field anomaly as follows:

$$\Delta T (x_0, y_0, z_0) = \int_{-\infty}^{\infty} P(x, y, z_0) \hat{\mathbf{F}}_{0}^{T} (\nabla^{2} \frac{1}{r}) \hat{\mathbf{h}} dxdy$$

$$\Delta T = \hat{\mathbf{F}}_{0}^{T} \hat{\mathbf{B}}$$

Note that this equation represents the approximated total-field anomaly produced by a continuous layer of dipoles with total-magnetization direction equal to

approximated total-field anomaly produced by a dipole

Note that the surface integrals defining the scalar magnetic potential, magnetic induction and approximated total-field anomaly were deduced by considering that the continuous layer of dipoles the same total magnetization direction as that of the true magnetic source.

Equivalent layers

All these quantities associated with the magnetic field depend on the same physical property!

The dipoles are the equivalent sources!

In this case, the physical property جنج کر) is a positive function proportional to the vertical derivative of (جریری) -

It is worth noting that the physical property distribution $\mathcal{P}^{(\varkappa, y, z^{\circ})}$ is positive at all points $(\varkappa, y, z^{\circ})$ on the plane z° and does not depend on the unit vectors z° and defining, respectively, the directions of the main field and total-magnetization direction.

t means that, by determining $\mathcal{P}^{(x,y)}$ 3c), it is possible to determine the approximated total-field anomaly, scalar magnetic potential and magnetic induction that would be produced by the source if the main field and/or the total magnetization had different directions.

For example, if we determine P(x,y,3c), we can compute the approximated total-field anomaly that would be produced by the source if both β and β were vertical, i.e.:

In this case, the approximated total-field anomaly assumes the form:

$$\Delta T_{RTP}(x_0, y_0, 3_0) = \int_{-\infty}^{\infty} P(x, y, 3_0) dy = \partial_{33} + \partial_{x} dy = \partial_{33} + \partial_{x} dy = \partial_{33} + \partial_{x} dy$$

which is similar to the zz-derivative of the gravitational potential produced by a source with positive density. Transforming an observed total-field anomaly into this simpler anomaly is called "reduction to the pole". This transformation was proposed by Baranov (1957) and is valid for the case in which the sources have a uniform magnetization direction.

It is possible to determine a continuous layer of dipoles that (i) has a uniform magnetization direction different from that of the true sources and (ii) exactly reproduces the observed total-field anomaly. In this case, however, there is no guarantee that the physical property distribution is positive at all points on the layer and it is not possible to compute the reduction to the pole.

References:

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