Poisson's relation

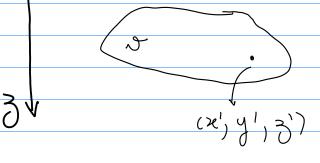
scalar magnetic potetial produced by a source with constant total magnetization

$$(x,y,z) = Cmh \int \int d\sigma$$

$$\hat{\Lambda} = \begin{bmatrix} \cos I \cos D \\ \cos I \sin D \end{bmatrix}$$

$$\sin I$$





$$V(x,y,3) = -\begin{bmatrix} \partial_x \oplus \\ \partial_y \oplus \\ \\ \partial_3 \oplus \end{bmatrix}^{T} \qquad A \oplus = \underbrace{\partial \oplus (x,y,3)}_{\partial \alpha} = \underbrace{\Box (x,y,3)}_{\gamma 3} = \underbrace{\Box (x,y,3)}_{\gamma$$

gravitational potential produced by a source with constant density

alfa-component of the gravitational acceleration

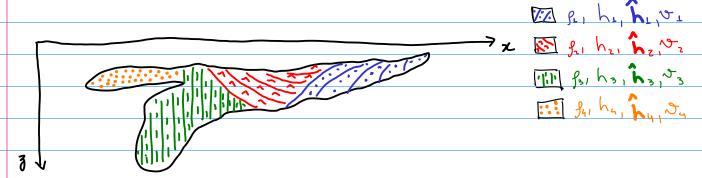
$$\partial_{\alpha}U = \frac{\partial U(x,y,3)}{\partial \alpha} = G_{\beta} \iiint \frac{\alpha'-\alpha}{r^3} dv, \quad \alpha = x,y,3$$

$$\partial_{\alpha} \Theta = \frac{cmh}{Gp} \partial_{\alpha} O \qquad V(x_1y_1z_1) = \frac{cmh}{Gp} \nabla U(x_1y_1z_1)^T$$

$$\nabla \Theta(x,y,z) = \frac{cmh}{G\beta} \nabla O(x,y,z)$$

According to the conditions specified above, the scalar magnetic potential represents the directional derivative of the gravitational potential along the total-magnetization direction of the source. This equation is known as Poisson's relation (Blakely, 1996, p. 91).





$$V(x,y,z) = V_{*}(x,y,z) + V_{2}(x,y,z) + V_{3}(x,y,z) + V_{4}(x,y,z)$$

$$V_{\perp}(x,y,z) = \frac{cmh_{\perp}}{G_{\beta}} \nabla U_{\perp}(x,y,z)^{\top} \hat{h}_{\perp} \quad V_{z}(x,y,z) = \frac{cmh_{z}}{G_{\beta}z} \nabla U_{z}(x,y,z)^{\top} \hat{h}_{z}$$

$$V_{3}(x,y,3) = \frac{cm h_{3}}{G f_{3}} \nabla U_{3}(x_{1}y_{1}3)^{T} \hat{h}_{3} \qquad V_{4}(x,y,3) = \frac{cm h_{4}}{G f_{4}} \nabla U_{4}(x_{1}y_{1}3)^{T} \hat{h}_{4}$$

Poisson's relation for a heterogeneous body

$$V(x_{1}y_{1}z) = \frac{cmh_{1}}{G_{1}} \nabla U_{1}(x_{1}y_{1}z)^{T} \hat{h}_{1} + \frac{cmh_{2}}{G_{2}} \nabla U_{2}(x_{1}y_{1}z)^{T} \hat{h}_{2} + \frac{cmh_{3}}{G_{3}} \nabla U_{3}(x_{1}y_{1}z)^{T} \hat{h}_{3} + \frac{cmh_{4}}{G_{3}} \nabla U_{4}(x_{1}y_{1}z)^{T} \hat{h}_{4}$$

Ex: Deduce the relation between the magnetic induction and derivatives of the gravitational potential.

Ex: Deduce the relation between the approximated total-field anomaly and derivatives of the gravotational potential.