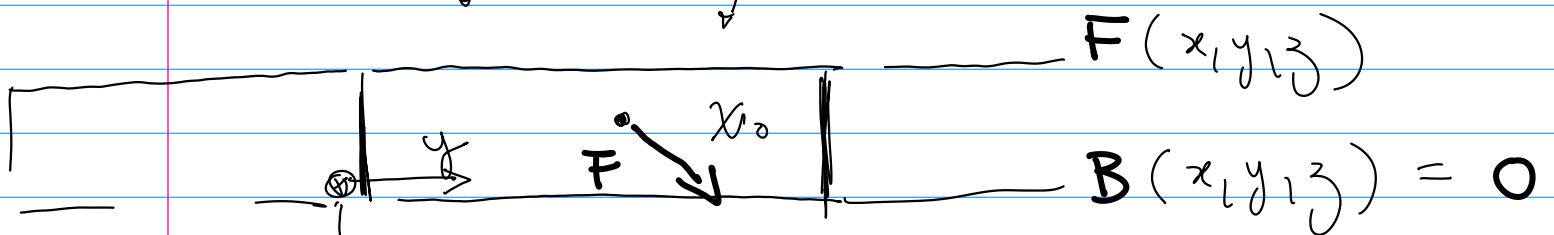
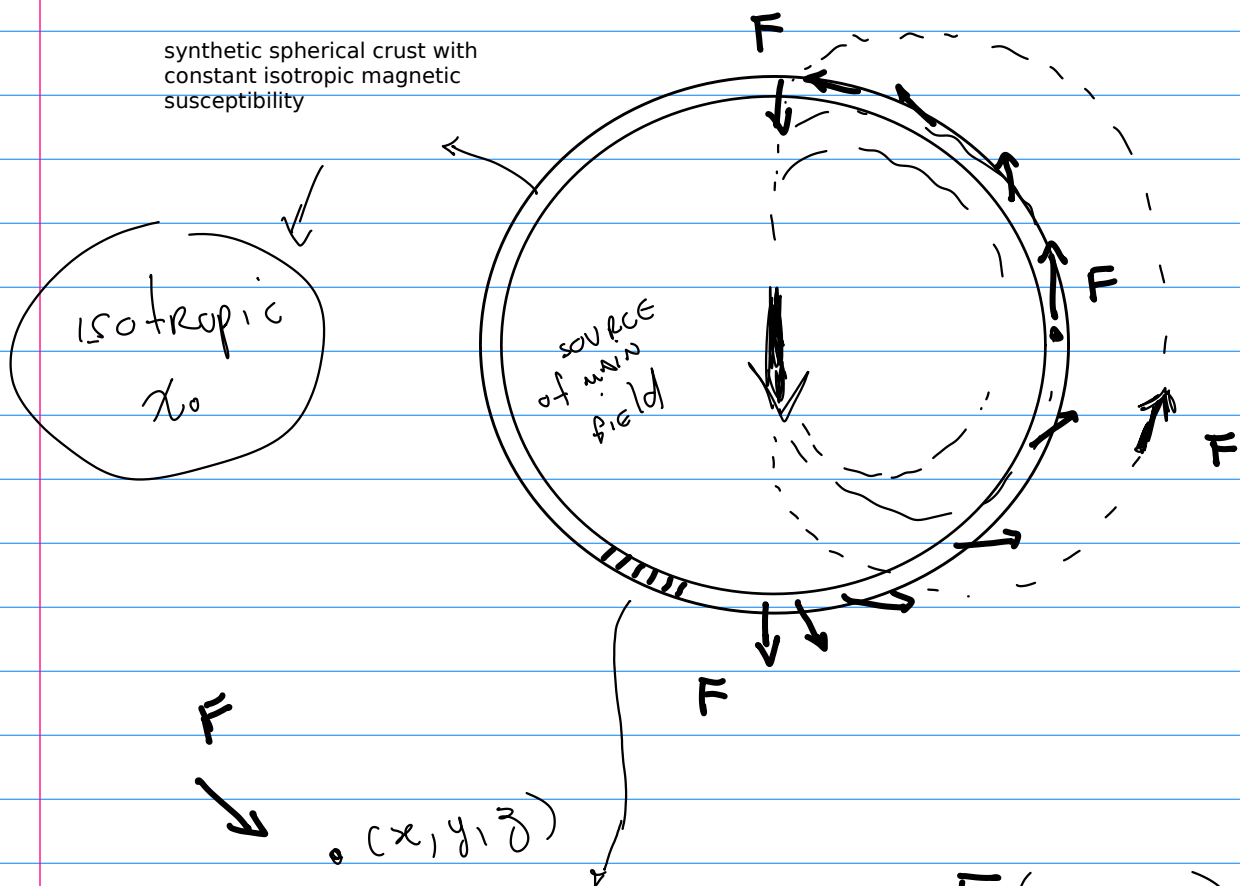


synthetic spherical crust with  
constant isotropic magnetic  
susceptibility



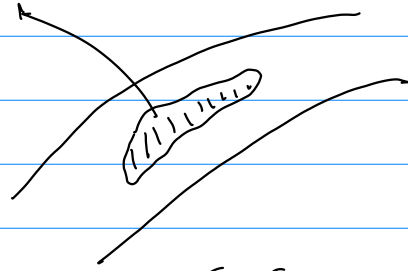
(Runcorn theorem)

$$h = \chi_0 H \neq 0$$

$$\frac{F}{\mu_0}$$

$$B(x, y, z) = \mu_0 \iiint_{V_c} \nabla^2 \frac{1}{r} (\chi_0 H) dV = 0$$

$$\chi = \chi_0 + \Delta\chi$$



$$\mathcal{B}(x, y, z) =$$

$$= \underbrace{\mu_0 \chi_0 \iiint_{\mathcal{V}_c} \nabla^2 \frac{1}{r} H \, d\mathcal{V}}_{=0 \text{ (Runcorn)}} + \mu_0 \Delta\chi \iiint_{\mathcal{V}_c} \nabla^2 \frac{1}{r} H \, d\mathcal{V} \neq 0$$

$$h = \chi H + P$$

$$\chi = \chi_0 \mathbf{I} + \Delta\chi$$

$$= (\chi_0 \mathbf{I} + \Delta\chi) H + P$$

$$h^* = \Delta\chi H + P$$

$$\mathcal{B}(x, y, z) = \mu_0 \iiint_{\mathcal{V}_c} \nabla^2 \frac{1}{r} (\Delta\chi H + P) \, d\mathcal{V}$$

Runcorn Theorem, in: David Gubbins, Emilio Herrero-Bervera (eds.),  
 Encyclopedia of Geomagnetism and Paleomagnetism, 2007, Springer, p. 888  
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