Started on	Wednesday, 23 November 2022, 11:25 PM
State	Finished
Completed on	Wednesday, 23 November 2022, 11:29 PM
Time taken	4 mins 29 secs
Grade	**1.49** out of 1.50 (**99**%)

Question **1**

Correct

Mark 0.75 out of 0.75

Use Pollard's ρ method with $x_0 = 2$ and $f(x) = x^2 + 1$ to determine the decomposition of the number $n = 9553$ into two factors.

Important note: All answer boxes should be filled in using the convention that those not applicable must be filled in with x.
All numbers must be filled in as positive numbers mod n.

Solution.

Iterations (results mod n):

$x_1 =$ 5 $x_2 =$ 26 $(|x_2 - x_1|, n) =$ 1

$x_3 =$ 677 $x_4 =$ 9339 $(|x_4 - x_2|, n) =$ 1

$x_5 =$ 7585 $x_6 =$ 4060 $(|x_6 - x_3|, n) =$ 1

$x_7 =$ 4676 $x_8 =$ 7713 $(|x_8 - x_4|, n) =$ 1

$x_9 =$ 3839 $x_{10} =$ 7196 $(|x_{10} - x_5|, n) =$ 1

$x_{11} =$ 5157 $x_{12} =$ 8651 $(|x_{12} - x_6|, n) =$ 1

$x_{13} =$ 1600 $x_{14} =$ 9350 $(|x_{14} - x_7|, n) =$ 41

$x_{15} =$ x $x_{16} =$ x $(|x_{16} - x_8|, n) =$ x

$x_{17} =$ x $x_{18} =$ x $(|x_{18} - x_9|, n) =$ x

$x_{19} =$ x $x_{20} =$ x $(|x_{20} - x_{10}|, n) =$ x

Conclusion:

The obtained two factors of n are (in increasing order!) 41 ✔ and 233 ✔ .

Question **2**

Partially correct

Mark 0.74 out of 0.75

Use Fermat's method to determine the decomposition of the number $n = 9231$ into two factors.

Important note: All answer boxes should be filled in using the convention that those not applicable must be filled in with x.

Solution.

Initialization:

$t_0 = [\sqrt{n}]$= 96 ✔

Iterations:

$t = t_0 + 1$: $t^2 - n$= 178 ✔ perfect square (yes/no) no ✔

$t = t_0 + 2$: $t^2 - n$= 373 ✔ perfect square (yes/no) no ✔

$t = t_0 + 3$: $t^2 - n$= 570 ✔ perfect square (yes/no) no ✔

$t = t_0 + 4$: $t^2 - n$= 769 ✔ perfect square (yes/no) no ✔

$t = t_0 + 5$: $t^2 - n$= 970 ✔ perfect square (yes/no) no ✔

$t = t_0 + 6$: $t^2 - n$= 1173 ✔ perfect square (yes/no) no ✔

$t = t_0 + 7$: $t^2 - n$= 1378 ✔ perfect square (yes/no) no ✔

$t = t_0 + 8$: $t^2 - n$= 1585 ✔ perfect square (yes/no) no ✔

$t = t_0 + 9$: $t^2 - n$= 1794 ✔ perfect square (yes/no) no ✔

$t = t_0 + 10$: $t^2 - n$=	2005 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 11$: $t^2 - n$=	2218 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 12$: $t^2 - n$=	2433 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 13$: $t^2 - n$=	2650 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 14$: $t^2 - n$=	2869 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 15$: $t^2 - n$=	3090 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 16$: $t^2 - n$=	3313 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 17$: $t^2 - n$=	3538 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 18$: $t^2 - n$=	3765 ✔	perfect square (yes/no)	no ✔
$t = t_0 + 19$: $t^2 - n$=	3394 ✖	perfect square (yes/no)	no ✔
$t = t_0 + 20$: $t^2 - n$=	4225 ✔	perfect square (yes/no)	yes ✔

Values:

s= 65 ✔ t= 116 ✔

Conclusion:

The obtained two factors of n are (in increasing order!) 51 ✔ and 181 ✔ .

◄ Assignment A (to submit by Week 8)

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Assignment B (to submit by Week 10) ►