

# Precise Control of Organic LED Emission Through Optically-Resonant Microcavity Confinement

An Honors Thesis Presented

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# Abstract

The ability to change the emission spectrum of an LED device has traditionally only been possible through chemical changes to the emissive material or the addition of dopants. Both of these techniques have significant disadvantages due to the limited range of changes possible and the difficulty of precisely controlling these changes. We present a technique of precisely controlling the emission spectrum of a device through modification of device thickness alone. By placing reflective electrodes on either side of an LED device, we generate an optically resonant microcavity whose properties impact the emission profile of the device. The direct relationship between the cavity thickness and the peak emission wavelength allows for tuning of the peak emission to within the resolution of our ability to deposit films. The resonance cavity amplification also significantly narrows the emission spectra of OLED devices. We additionally explore the impacts of stacking multiple microcavities on top of one another in the emission profile in the hopes of generating devices with the potential of reaching the lasing threshold through electrical pumping.

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# Chapter 1

## Introduction

### 1.1 Organic Light Emitting Diodes

Light emitting diodes (LEDs) have become prevalent in everyday life in applications ranging from displays to the headlights on cars. They have widely replaced the more traditional incandescent bulbs due to increased power efficiency, longevity, and compact size when compared to other luminescent devices. However, many LEDs require hazardous semiconductors such as gallium doped silicon.[8] In order to mitigate this, LEDs based off of organic materials, called OLEDs, have come into fruition, with the first OLEDs being demonstrated by Tang and VanSlyke in 1987.[14] OLEDs have advantages over conventional LEDs due to the fact that the emission spectrum of an OLED is determined almost entirely by the chemical structure of the emitter molecule, making tuning of OLEDs significantly easier. OLEDs are usually made from a transparent conductive oxide (TCO) as a transparent electrode, a metal for the non-transparent electrode, and three organic materials. These organic materials are used as a hole transport material (HTM), electron transport material(ETM), and an emissive material.[11] The emissive material has a band structure suitable for electron and hole recombination and the release of a photon in the visible spectrum. When the device is operated, current is injected through the device, with electrons being transferred through the ETM and holes through the HTM. The electrons and holes recombine in the emission material, and release a photon. By surrounding the emissive material with selective transport layers, it is ensured that the vast majority of charge recombination occurs within the emissive material, maximizing power conversion efficiency. Although TCOs generally have a higher resistance than pure metals, they are used to maximize the outcoupling of light. Currently, OLED technology falls behind its inorganic counterparts in power conversion efficiency, due in part to the low carrier

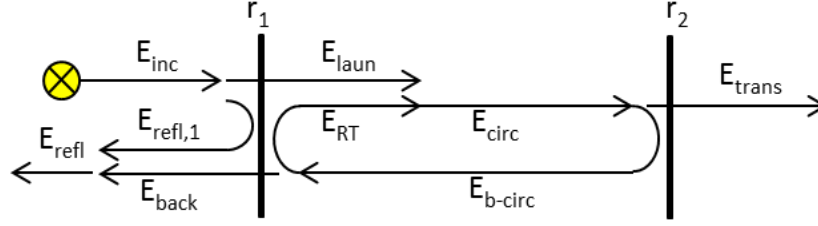


Figure 1.1: Schematic of the Fabry-Pérot etalon. The steady state solutions for wave propagation in the normal mode of the etalon are shown.[7]

mobilities in organic bulk.[11] Conventionally, the output intensity of an LED could be increased by thickening the recombination region, providing more recombination sites. With the limited mobility of carriers in organic materials, however, a thicker emission region makes effective charge injection into the recombination sites difficult. To mitigate this, a method of stacking multiple OLEDs on top of one another with a shared electrode has been previously demonstrated[5], although this device structure was mainly focused on the applications in stacked pixel OLED displays.

## 1.2 Waveguides and the Fabry-Pérot Etalon

In electromagnetism, a waveguide is defined as a surface or set of surfaces made of a conductor such that the electric and magnetic fields within the conductor are restricted to zero. These waveguides provide boundary conditions to Maxwell's equations, such that only specific modes of propagation can occur within the waveguide. These allowed modes are generally categorized as the transverse electric (TE) mode, the transverse magnetic (TM) mode, and in the special case of both TE and TM, the TEM mode.[4] One special form of waveguide, called the Fabry-Pérot etalon, is characterized by two conducting planes with a transparent material in between. Due to the structure of the etalon, certain wavelengths of light resonate in the etalon, while others destructively interfere with their reflections and are eliminated.[7] In particular, the condition for resonance is that the frequency  $\nu$  and wave number  $k$  obey:

$$\nu_q = \frac{qc}{2dn} \text{ and } k_q = \frac{\pi q}{l} \quad (1.1)$$

for the  $q$ th resonant mode. Here  $c$  is the speed of light,  $d$  is the geometric thickness of the etalon, and  $n$  is the index of refraction for the material inside.[10] In the case of light propagating normal to the two planes, this condition can be intuitively understood as standing waves that have zero amplitude at the metal surfaces. The selectivity of light through the Fabry-Pérot etalon is given

by:

$$T(\phi) = \frac{I_{trans}}{I_{inc}} = \frac{(1 - R_1)(1 - R_2)}{(1 - \sqrt{R_1 R_2})^2 + 4\sqrt{R_1 R_2} \sin^2(\phi)} \quad (1.2)$$

where  $\phi$  describes the phase shift between forward and backward propagating waves inside the etalon. In the special case of the resonant mode,  $\phi = 0$ , the selectivity is given by:

$$T(\nu_q) = \frac{(1 - R_1)(1 - R_2)}{(1 - \sqrt{R_1 R_2})^2} \quad (1.3)$$

where  $R_1$  and  $R_2$  are the reflectivities of the conductive planes.[12]

### 1.3 Optically Resonant OLED Microcavities

In the traditional Fabry-Pérot etalon, the light source is located outside of the conductor planes, and the spectrum is collected on the opposite side of the conductor planes. In a traditional OLED, an emitting material is located between a conductive electrode and a transparent electrode. By replacing the transparent electrode of an OLED with a partially reflective, partially transmissive film, the two devices can be combined to form Fabry-Pérot etalon with an emissive source inside of it. This device would filter from the broadband emission of the OLED all wavelengths except the resonant modes, forming much narrower emission peaks.[6] In this project, devices of this form were fabricated so that the emission of the OLED device underwent filtration by this optically resonant microcavity and the dependence of the emission spectrum on physical properties of the microcavity were explored. By narrowing the emission peak and increasing the optical path, we hope to move towards the lasing threshold for electrically pumped organic diodes. The stacking of several cavities on top of one another can also contribute to lengthening the optical path while maintaining relatively small electrical path length in each device, potentially bringing these devices closer to the lasing threshold.

## Chapter 2

# Experimental Methods

### 2.1 OLED Materials

A tris-(8-hydroxyquinoline)aluminum ( $\text{Alq}_3$ ) emissive material, along with bathophenanthroline (BPhen) as an electron transport material and N,N-Di(1-naphthyl)-N,N-diphenyl-(1,1-biphenyl)-4,4-diamine (NPB) as a hole transport material, were chosen due to their reported use in green OLED devices.[3, 9] Silver and molybdenum oxide ( $\text{Ag}/\text{MoO}_3$ ) were used for the anode, while aluminum and lithium fluoride ( $\text{Al}/\text{LiF}$ ) were used for the cathode. The organics were purchased from Sigma-Aldrich and purified through sublimation.

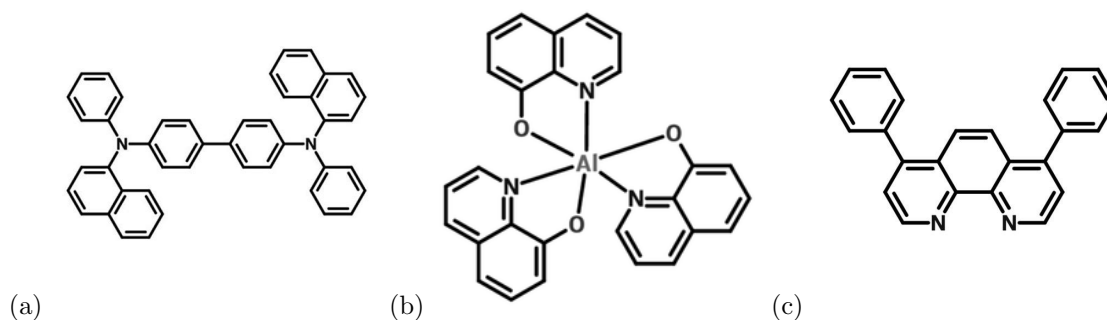


Figure 2.1: Chemical structures of (a) the NPB hole transport material, (b) the  $\text{Alq}_3$  emitter material, and (c) the BPhen electron transport material.

## 2.2 Device Fabrication

In order to generate optically resonant microcavities, a standard OLED recipe[3, 9] was used with the substitution of a 30 nm semitransparent metal electrode in the place of a transparent electrode. In particular, an oxidized silicon substrate had a 100 nm bottom electrode of silver, followed by 1 nm of molybdenum oxide,  $x$  nm of NPB, 20 (single cavity devices) or 26 nm (multi-cavity devices) of Alq<sub>3</sub>,  $x$  nm of BPhen, 1 nm of lithium fluoride, and 30 nm of aluminum deposited onto it through sequential thermal evaporation. For multi-cavity devices, this same structure was replicated in the following cavity, but inverted, as shown in Figure 2.2. The thickness  $x$  of the NPB and BPhen layers was modified to generate the desired cavity thickness. In all multi-cavity devices, a transport layer thicknesses of  $x = 40$  nm was used. All depositions were performed under a pressure of  $10^{-7}$  torr and vacuum was not broken during processing.



Figure 2.2: Schematic of a two-cavity device and the  $\lambda/2$  resonant mode.

## 2.3 Angle-Resolved Electroluminescence Spectroscopy

Devices were stored and tested in a nitrogen glovebox with  $< 0.1\text{ppm O}_2$  and  $< 0.5\text{ppm H}_2\text{O}$  to avoid degradation of devices. Emission spectra were collected using an OceanOptics HDX visible and near-IR spectrometer with a fiber optic feedthrough to the glovebox. The emission of the devices was passed through an iris to minimize the collection angle, then reflected off of a parabolic mirror to focus the emission into the fiber. Devices were mounted on a rotating stage so that the angle-resolved electroluminescence spectroscopy (ARES) pattern could be collected at 2.5 degree intervals from 0 to 90 degrees.



## Chapter 3

# Results

### 3.1 Single Cavity Devices

In all single cavity devices, a 100 nm bottom electrode was used with a 30 nm top electrode to produce a resonant cavity of the desired size. The thickness of the organics was changed in order to maintain a 20 nm Alq<sub>3</sub> layer between the contact layers. In all devices except those described in section 3.1.3, a silver electrode with a MoO<sub>3</sub> cap was used as the bottom electrode and an aluminum electrode with a LiF cap was used for the top. As we increase the cavity thickness, the emission peak redshifts, until it shifts to the next resonant mode, returning to a blue color, as seen in Figure 3.1. Following each shift to the next resonant mode, the bandwidth of the emission narrows. The 182 nm device in Figure 3.3 shows a strong broadband emission along with the resonant mode. That is because the natural emission at the wavelength of the resonant mode is extremely weak, so the broadband leakage out of the cavity is on the same order as the resonant emission.

### 3.1.1 Peak Emission Wavelength

An analysis of the peak wavelength of emission for each cavity thickness reveals a very strong correlation. In particular, a linear relationship is observed between the peak wavelength and the resonance cavity thickness, as shown in Figure 3.1. This is logical as the wavelength of a resonant mode should be proportional to the width of the resonance cavity, with the constant of proportionality being the index of refraction for light in the organic materials. We do see some variation from the linear model, which is to be expected since the overall index of refraction in the cavity is not a constant across devices. Specifically, by not keeping the ratio of each organics layer the same, we inadvertently modified the index of refraction slightly, leading to small variations from the linear model.

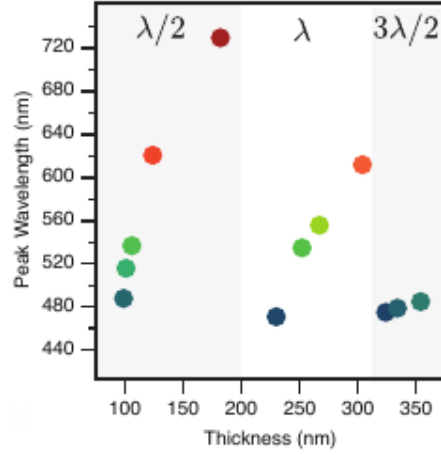


Figure 3.1: Peak emission wavelength as a function of thickness for various single cavity devices.

The linear model, however, is only valid for the regime of a single resonant mode. We see a break in the linearity of peak emission wavelength and cavity thicknesses at the points of transition from a half-integer resonance to the next. We have measured the transition from  $\lambda/2$  to  $\lambda$  and from  $\lambda$  to  $3\lambda/2$  at approximately 200 nm and 310 nm, respectively. This is as expected, as the resonant wavelength doubles when shifting from one half-integer mode to the next. We also notice that when the linear relationship picks up again on the other side of a transition to the next mode, the slope is decreased, indicating that the constant of proportionality discussed above is not just dependent on the index of refraction, but also which resonant mode is being described.

### 3.1.2 Band Narrowing

Analysis of the band width of the emission can be analyzed through the use of the quality factor. The quality factor is defined as:

$$Q = \frac{\nu_0}{\Delta\nu_{1/2}} \quad (3.1)$$

where  $\nu_0$  is the resonant frequency and  $\Delta\nu_{1/2}$  represents the full width at half maximum of the emission spectrum in Fourier space.[15] By solving for the steady state solutions of the Fabry-Pérot etalon, we find that  $\Delta\nu_{1/2}$  is given by:

$$\Delta\nu_{1/2} = \frac{c}{2nd} \frac{1 - \sqrt{R_1 R_2}}{\pi(R_1 R_2)^{1/4}} \quad (3.2)$$

where  $c$  is the speed of light in the organics,  $n$  is integer describing the mode, and  $d$  is the cavity thickness.[15] Then, taking the resonant frequency  $\nu_0$  to be the frequency of the peak intensity light:

$$\nu_0 = \frac{c}{\lambda_0} \quad (3.3)$$

We can obtain an expression for the quality factor of the device:

$$Q = \frac{\nu_0}{\Delta\nu_{1/2}} = \frac{c}{\lambda_0} \frac{2nd}{c} \frac{1 - \sqrt{R_1 R_2}}{\pi(R_1 R_2)^{1/4}} = \frac{2nd}{\lambda_0} \frac{1 - \sqrt{R_1 R_2}}{\pi(R_1 R_2)^{1/4}} \quad (3.4)$$

Now, by introducing  $q$  to be the number of half wavelengths in the cavity:

$$q = \frac{2nd}{\lambda_0} \quad (3.5)$$

We see that the quality factor depends only on  $q$  and the reflectivities of the metal electrodes:

$$Q = q \left\{ \frac{1 - \sqrt{R_1 R_2}}{\pi(R_1 R_2)^{1/4}} \right\} \quad (3.6)$$

Therefore, the steady state solutions of the Fabry-Pérot etalon predict the quality factor to be a step function in  $q$ , which is confirmed by the data displayed in Figure 3.2

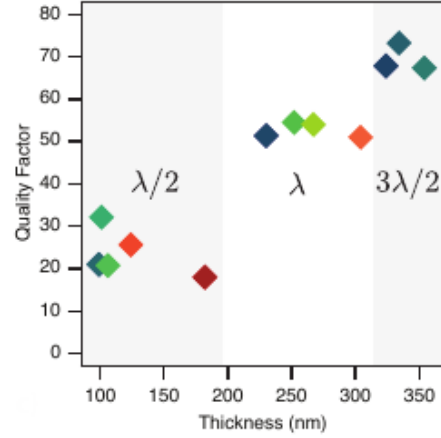


Figure 3.2: Quality factor as a function of cavity thickness for various single cavity devices.

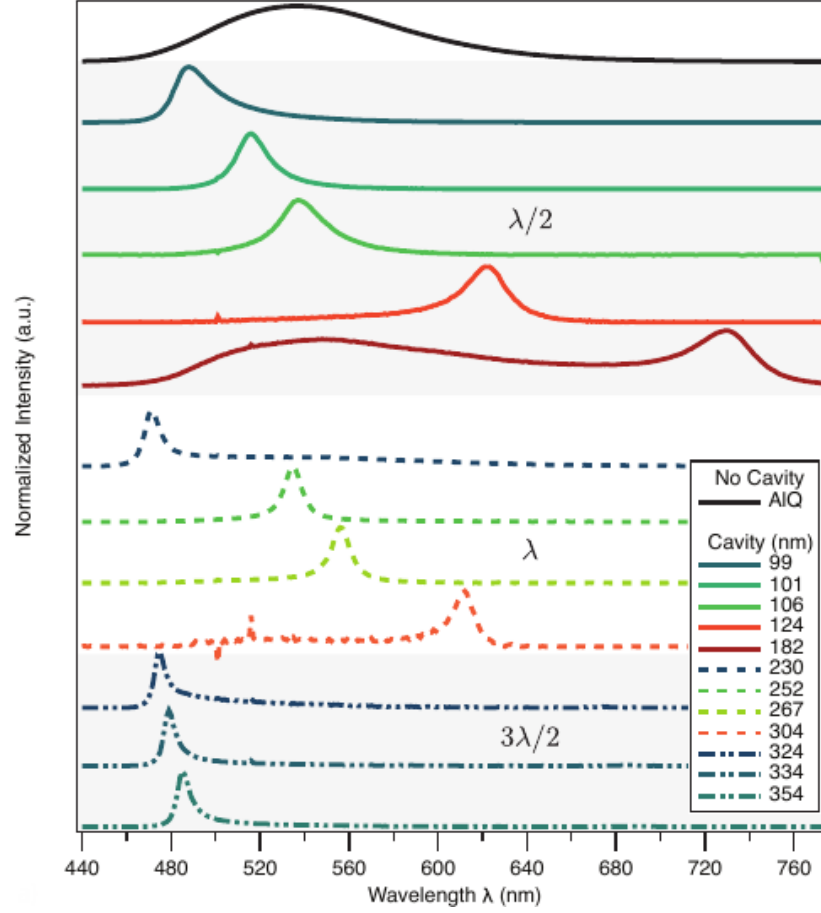


Figure 3.3: Emission spectra of single cavity devices of various cavity thicknesses, along with the natural emission spectrum of the Alq<sub>3</sub> emitter.

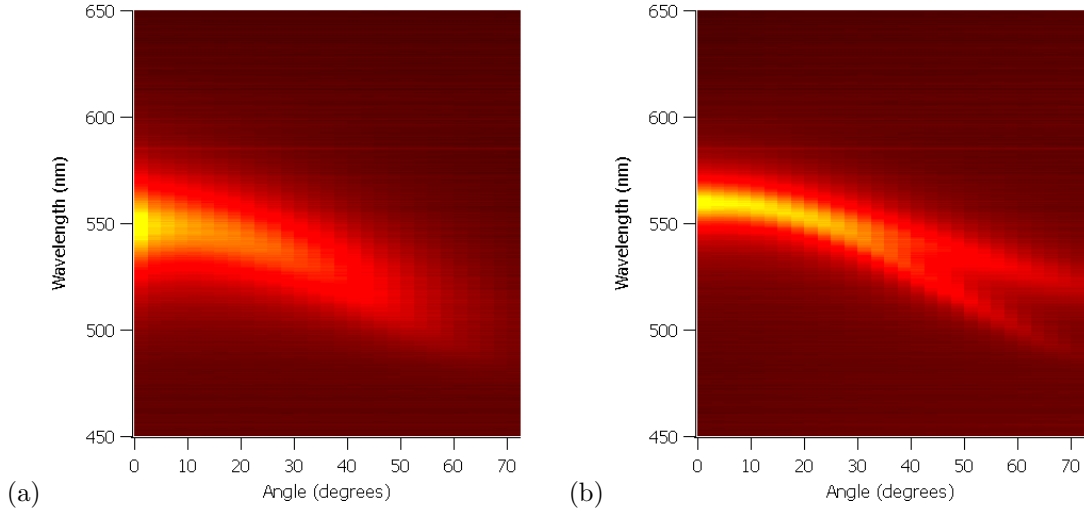


Figure 3.4: ARES profile of single cavity devices topped with a silver electrode (a), and with an aluminum electrode (b). The aluminum topped device shows a much narrower emission peak than the silver topped device due to differences in optical properties of the metals.

### 3.1.3 Effect of Top Electrode Material

As fabrication of the multi-cavity devices requires both regular and inverted devices, two devices were fabricated in identical conditions except that they were inverted with respect to each other. Each has a 100 nm bottom electrode, 1 nm capping layer, followed by a 40/26/40 set of organics layers, with a 1 nm cap and 30 nm top electrode, as was done with the multi-cavity devices. In comparing the emission spectra of the two devices, we see a significant difference. In particular, the aluminum topped device has a much narrower emission spectrum than the silver topped device. The contrast in emission spectra is due to the differing optical properties of silver and aluminum. While both have similar transmissivities, aluminum absorbs a significant amount more than silver, and reflects significantly less.[13] In the aluminum topped device, almost all light that travels towards the bottom electrode is reflected by the 100 nm silver electrode, strongly pinning that light to the resonant wavelength, which can then be partially transmitted through the top aluminum electrode. In the case of the silver topped device, however, the lower reflectivity on the bottom electrode gives a weaker resonant mode to be transmitted through the top electrode.

## 3.2 Multi-cavity Devices

In all multi-cavity devices, a 100 nm silver bottom electrode was used, with all subsequent electrodes at a thickness of 30 nm. The cavities were created using a 26 nm film of the Alq<sub>3</sub> emitter with 40 nm transport layers on either side. This generates 126 nm cavities for all multi-cavity devices.

### 3.2.1 Behavior at Large Angles

In the ARES profile, we see that the emission spectrum of the resonance cavities are highly dependent on the viewing angle. The peak emission blueshifts parabolically with increasing angle, and the emission splits into two distinctive peaks that separate as the angle increases. This is as would be predicted by the theory of wave propagation in a Fabry-Pérot etalon.[8] The modal splitting is the separation of the transverse electric (TE) and transverse magnetic (TM) modes diverging from the superposition of them at  $\theta = 0$ , called the transverse electric and magnetic (TEM) mode.

### 3.2.2 Number of Resonant Modes

We additionally see that a more complex modal structure can be generated with multi-cavity devices, even in forward emission. We see the first transition from one to two forward emission

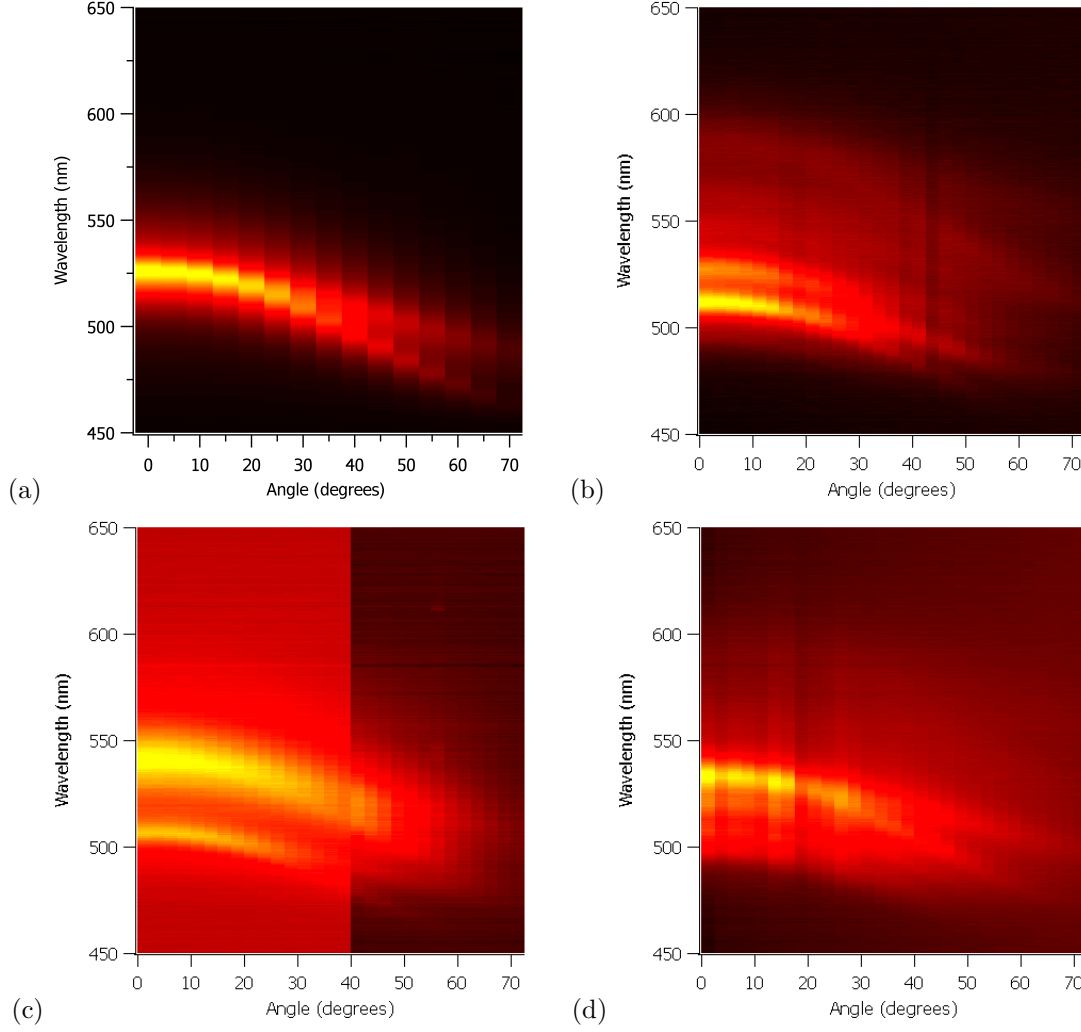


Figure 3.5: ARES profile of devices with two (a), three (b), four (c), and five (d) cavities. The modal splitting of TE and TM modes can be seen along with the increase in emission modes at higher numbers of resonant cavities. The change in background intensity in the four cavity device (c) is due to a change in the iris size during data collection to maintain a strong signal.

peaks in the transition from  $N=2$  to  $N=3$ . The  $N=3$  device has a narrow and intense emission peak at approximately 510 nm with a slightly wider and weaker peak around 525 nm. In the  $N=4$  device, we also see two forward emission peaks, but the one around 510 nm is significantly narrower and less intense with a broader, more intense peak occurring around 540 nm. In the transition from  $N=4$  to  $N=5$ , we see almost perfect preservation of the modal structure of  $N=4$ , with an additional peak superimposed between the two existing peaks. Although the cause of these additional peaks is not immediately clear, the existence of two modes, one narrower than the other, is logical. For example, in the  $N=4$  device, the narrow peak could be generated by a resonant mode stretching across the bottom three devices, while the broad peak is generated from resonances off of both the

inner and outer interfaces of the top metal electrode. However, more experimentation would be necessary to confirm this theory.

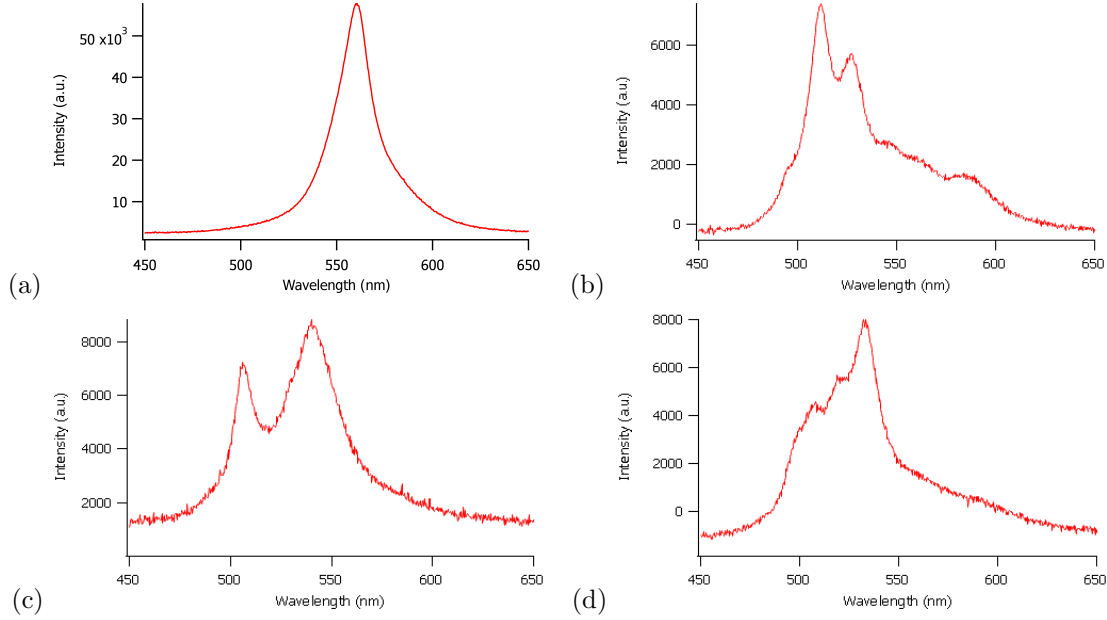


Figure 3.6: Forward emission spectra of devices with two (a), three (b), four (c), and five (d) cavities. The transition from two to three cavities shows the introduction of an additional resonance mode, as does the transition from the four to the five cavity device. Additionally, the width of resonant peaks shrinks as more cavities are introduced.

### 3.2.3 Bandwidth of Resonant Modes

By fitting with Lorentzian functions, the full width at half maximum (FWHM) can be found for each emission peak. By analyzing the FWHM for the emission peaks, we find a definite correlation between bandwidth and number of cavities. The emission bands narrow significantly as the number of cavities increases. This is expected for modes that form a resonant standing wave across several cavities for reasons similar to those presented in Section 3.1.2. In Equation 3.6, the value  $q$  representing the number of half wavelengths in the device will be proportional to the number of cavities as well as the number of waves in each cavity. Thus, the quality factor will be a step function in both number of cavities and the mode of each cavity.

## Chapter 4

# Conclusion

In this project, we have demonstrated a technique for controlling the bandwidth and peak emission wavelength of an OLED device, as well as generating more complex emission profiles. This technique utilizes device design alone, rather than chemical changes to the emitter materials. The relationships of both peak emission wavelength and bandwidth with the thickness of the cavity allows for the ability to design and fabricate a device to match any desired single peak emission profile, provided an emissive material with a sufficiently wide broadband emission spectrum is used. However, the same level of control can not yet be exerted over the complex emission spectra of multi-cavity devices.

In the future, we hope to study the multi-cavity emission in more detail. In particular, a collection of emission spectra from multi-cavity devices with a different cavity thickness could contribute to a better understanding of the relationship of the emission peaks and the cavity properties. Also, polarization analysis of the emission spectra of multi-cavity devices could lead to a stronger understanding of the modal structure of these devices. Additionally, more exploration into the band narrowing of multi-cavity devices could lead to the ability to make extremely narrow emission devices.

Optically resonant microcavity confined OLEDs could see many applications, such as in low cost displays or optics. In the fabrication of displays, these devices could replace the traditional three emitter materials with a single emitter material deposited over a patterned substrate to generate pixels with different colors while only requiring a single emitter deposition. The ability to generate narrow bandwidth light from tunable organic materials could also be beneficial in optical applications. If the bandwidth continues to narrow with more cavities, it is also possible that a multi-cavity stacked device could reach the lasing threshold through electrical pumping.[1, 2]



## Chapter 5

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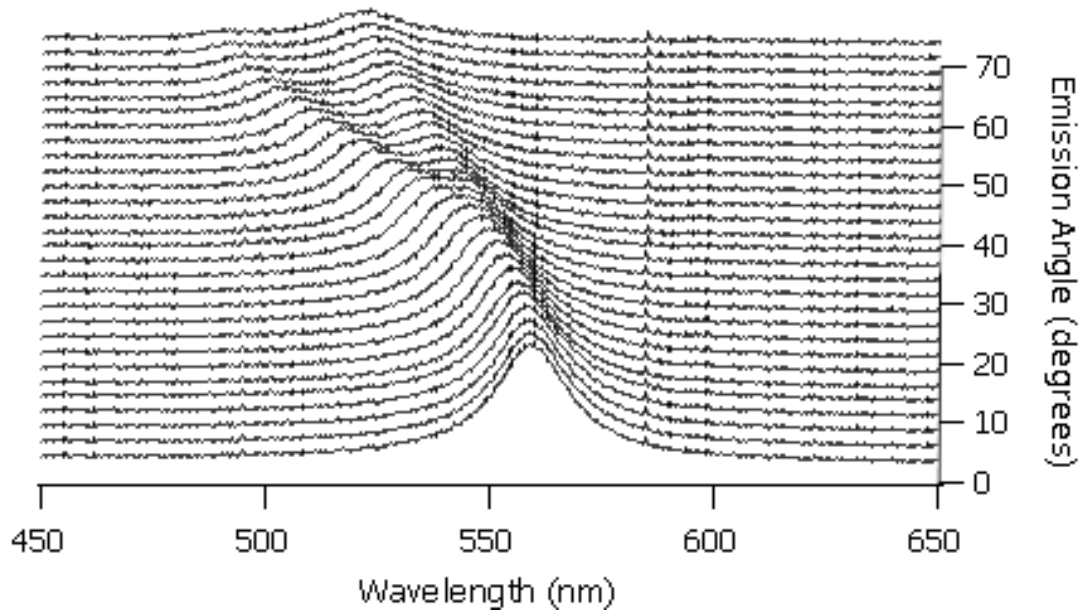
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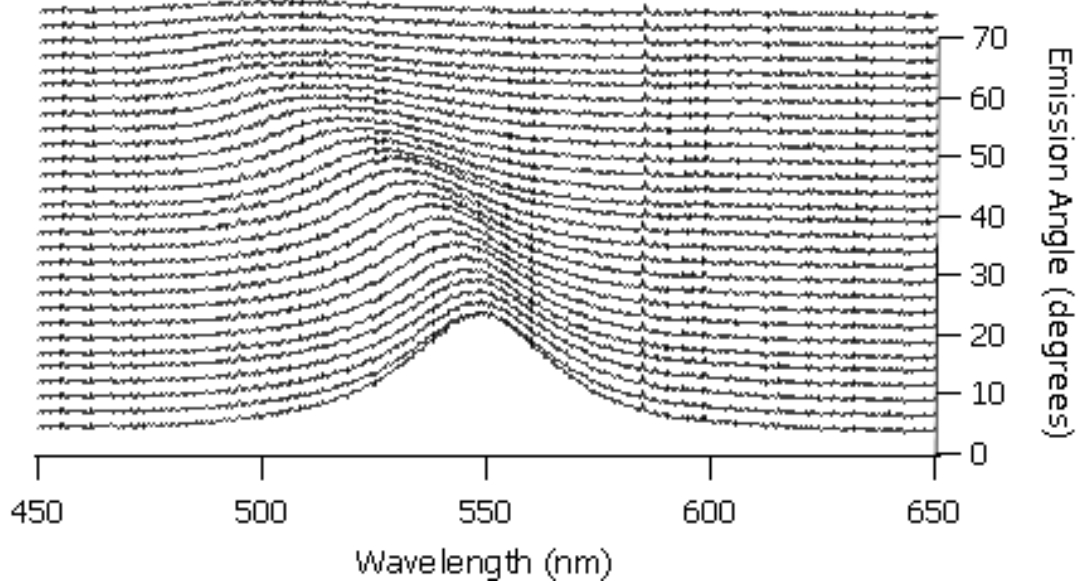
## Appendix A

# Component Spectra of Angular Resolved Graphs

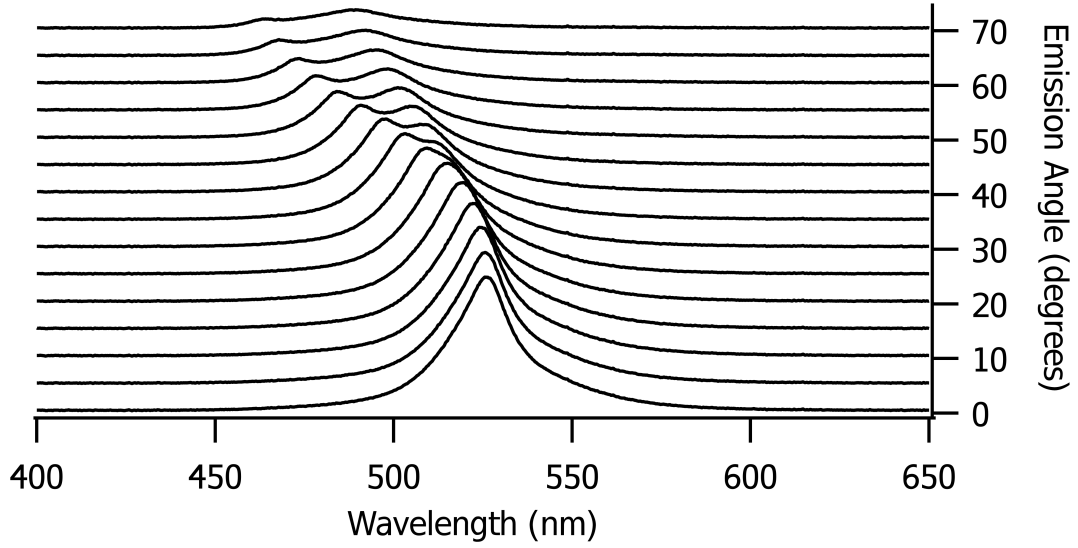
Single Cavity Aluminum Topped Device



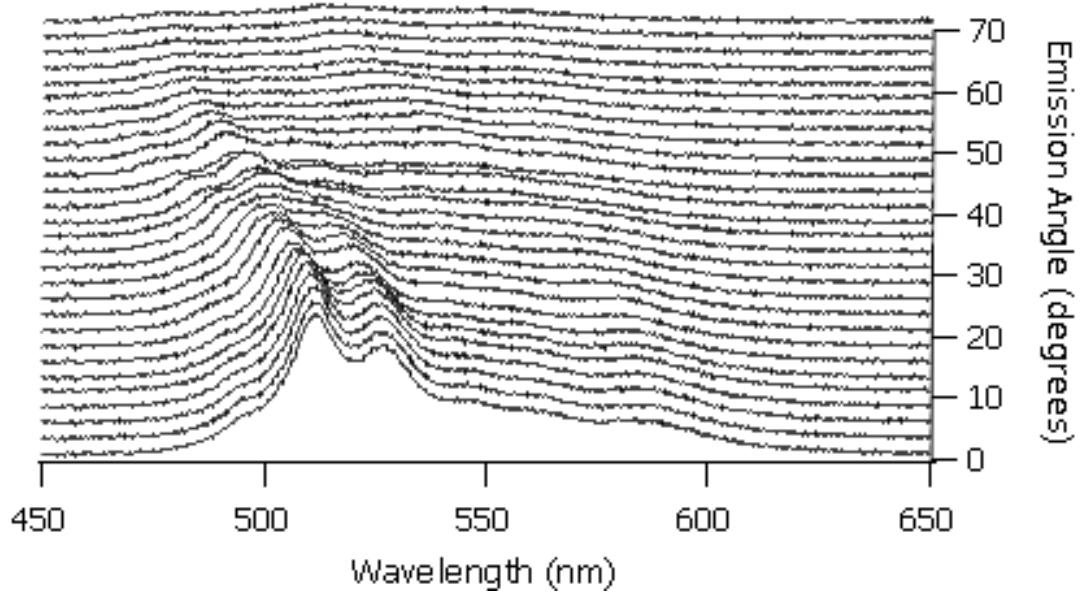
### Single Cavity Silver Topped Device



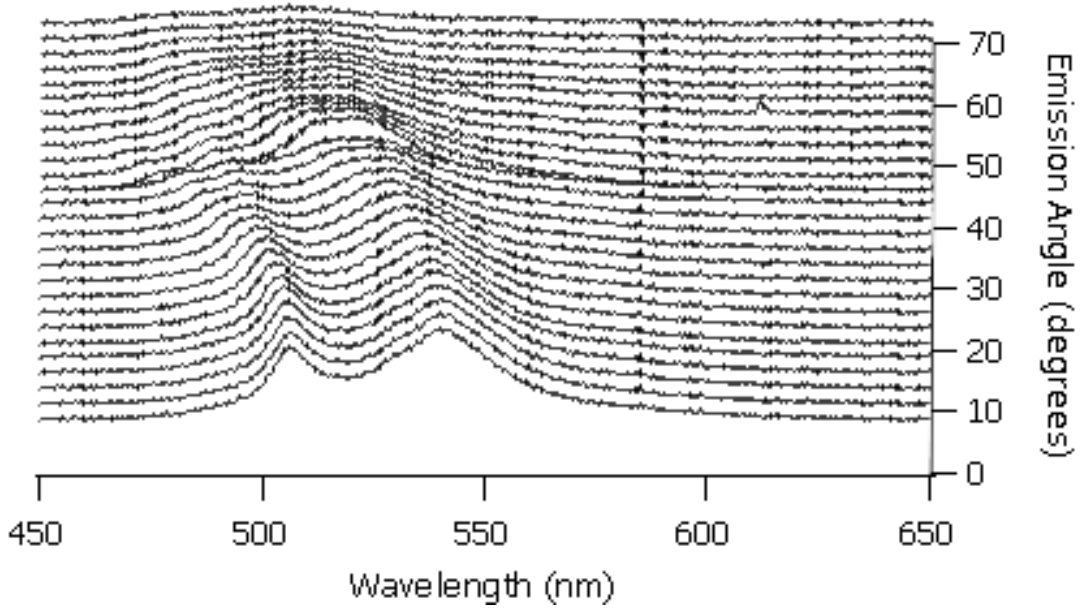
### Two Cavity Device



### Three Cavity Device



### Four Cavity Device



## Five Cavity Device

