ADAMAS UNIVERSITY

END-SEMESTER EXAMINATION: MAY 2021

UNIVERSITY PURSUE EXCELLENCE	(Academic Session: 2020 – 21)		
Name of the Program:	B.Tech. (CE/ME/EE)	Semester:	IV
Paper Title :	Engineering Mathematics-IV (Numerical Techniques)	Paper Code:	SMA42116
Maximum Marks :	40	Time duration:	3 hrs.
Total No of questions:	8	Total No of Pages:	2

Instructions:

- At top of Answer Sheet, clearly mention Name, Roll No., Enrolment No., Paper Name & Code, and Date of Exam.
- 2. Assumptions made if any, should be stated clearly at the beginning of your answer.
- 3. All parts of a Question should be answered consecutively.

Answer all the Groups Group A Answer all the questions of the following

 $5 \times 1 = 5$

- **1.** a) How many significant figures are there in the number 0.00100500.
 - b) Is the matrix $\begin{pmatrix} 9 & -5 & 2 \\ -5 & 10 & 3 \\ 1 & 4 & 6 \end{pmatrix}$ strictly diagonally dominant? Justify.
 - c) What is the order of convergence of Newton-Rapson method?
 - d) Define degree of precision of a quadrature formula.
 - e) What is the relation between Euler's method and R-K method?

GROUP-B Answer any three of the following

 $3 \times 5 = 15$

- 2. Using Regula-falsi method, find the real root of the equation $x^3 5x 7 = 0$ correct to 3 decimal places. Assume that the root lies between 2 and 3. [5]
- **3.** Solve the following system of equations by Gauss-elimination method. [5]

$$2x+3y-z=5$$
$$4x+4y-3z=3$$
$$2x-3y+2z=2$$

- **4.** Use Simpson's $1/3^{\text{rd}}$ rule to evaluate $\int_{0}^{6} \frac{dx}{(1+x)^2}$ taking six sub-intervals. [5]
- 5. Use R-K method of order two to find y(0.2) and y(0.4) given that [5]

$$y \frac{dy}{dx} = y^2 - x$$
, $y(0) = 2$, taking h=0.2.

GROUP –CAnswer *any two* of the following

 $2 \times 10 = 20$

6. (a) Use the LU decomposition method to solve the following system of equations:

$$x+3y+z=3$$

 $x+4y+2z=3$
 $x+2y-3z=6$ [7]

- (b) Evaluate $\int_{-1}^{0} xe^{x} dx$ by using Trapezoidal rule taking n=6. [3]
- 7. (a) Find the equation of the curve which passes through the points (4, -43), (7, 83), (9,327) and (12,1053) by Newton's forward interpolation formula. [3]
 - (b) Using the Gauss-Seidal method find the solution of the following system of linear equation up to fourth iteration: [7]

$$10x + y - 2z = 7.74$$
$$x + 12y + z = 39.66$$
$$3x + 4y + 15z = 54.8$$

- **8.** (a) Find the percentage error if 625.483 is approximated to 3 significant figures. [2]
 - (b) Find the value of $(\nabla + \Delta)^2 (x^2 + x)$. [3]
 - (c) Use Euler method to find the value of y when x=0.5, if [5]

 $\frac{dy}{dx} = x^2 - y$, y(0) = 1, taking h=0.1.