Depolarization BB84

October 26, 2021

```
[2]: import numpy as np
      # Importing standard Qiskit libraries
      from qiskit import QuantumCircuit, transpile, Aer, IBMQ
      from qiskit.tools.jupyter import *
      from qiskit.visualization import *
      from ibm_quantum_widgets import *
      from qiskit.providers.aer import QasmSimulator
      # Loading your IBM Quantum account(s)
      provider = IBMQ.load_account()
 [3]: from qiskit.providers.aer.noise import NoiseModel
      from qiskit.providers.aer.noise.errors import pauli_error, depolarizing_error
      from qiskit import *
      from qiskit.visualization import plot_histogram
      import matplotlib.pyplot as plt
      import numpy as np
      %matplotlib inline
 [4]: def get_noise_dep(p_m, p_g):
          error_m = pauli_error([('X',p_m),('I',1-p_m)])
          error_g1 = depolarizing_error(p_g,1)
          error_g2 = error_g1.tensor(error_g1)
          noise_model = NoiseModel()
          # measurement error is applied to measurements
          noise_model.add_all_qubit_quantum_error(error_m, "measure")
          # single qubit gate error is applied to x gates
          noise_model.add_all_qubit_quantum_error(error_g1, ["h", "x", "id"])
          # two qubit gate error is applied to cx gates
          noise_model.add_all_qubit_quantum_error(error_g2, ["cx"])
          return noise model
[48]:
          bob_bits=[]
          from qiskit.tools.monitor import backend_monitor
```

```
import matplotlib.pyplot as plt
from qiskit.tools.visualization import circuit_drawer
from qiskit import *
from qiskit.visualization import plot_histogram
from random import randrange, seed, sample
from sys import argv, exit
import random
#data = int(input('ENTER LENGTH OF BIT STREAM (example 5 For 10110):'))
data=50
h=0
#h=int(input())
def bit_stream(p):
   key1 = ""
   for i in range(p):
      temp = str(random.randint(h,h))
      key1 += temp
   return(key1)
bitstream= bit_stream(data)
digits = [int(x) for x in str(bitstream)]
print(digits)
#print('List of Bit Stream to transfer over Quantum Channel')
#print(digits)
print('\n')
#n = len(digits)
bob_bits=[]
from random import choice
m=0
n = 50
for i in range(n):
   m=m+10
   print("No of identity Gate:",m)
   if digits[i] == 0:
      q = QuantumRegister(1, 'q')
      c = ClassicalRegister(1, 'c')
      qc = QuantumCircuit(q, c)
      qc.barrier()
      qc.h(0)
      qc.barrier()
      for j in range(m):
         qc.id(0)
         qc.barrier()
      qc.h(0)
```

```
qc.barrier()
          qc.measure(q[0], c[0])
          #print(qc)
          # Perform a noise simulation
          counts = execute(qc,Aer.
 →00036),shots=1000).result().get_counts()
          #counts = result.get_counts(qc)
          %matplotlib inline
          #print(qc)
          #qc.draw(output='mpl')
          #plt.show()
          #print(counts)
          #plot_histogram(counts)
          itemMaxValue = max(counts.items(), key=lambda x : x[1])
          print(itemMaxValue)
          # Iterate over all the items in dictionary to find keys with max_
 \rightarrow value
          for key, value in counts.items():
             if value == itemMaxValue[1]:
                 bob_bits.append(value)
   print(bob_bits)
No of identity Gate: 10
('0', 978)
No of identity Gate: 20
('0', 977)
No of identity Gate: 30
('0', 964)
No of identity Gate: 40
('0', 961)
No of identity Gate: 50
('0', 966)
No of identity Gate: 60
('0', 958)
No of identity Gate: 70
('0', 956)
No of identity Gate: 80
('0', 979)
No of identity Gate: 90
('0', 966)
```

No of identity Gate: 100

('0', 970)

No of identity Gate: 110

('0', 959)

No of identity Gate: 120

('0', 967)

No of identity Gate: 130

('0', 968)

No of identity Gate: 140

('0', 964)

No of identity Gate: 150

('0', 964)

No of identity Gate: 160

('0', 976)

No of identity Gate: 170

('0', 955)

No of identity Gate: 180

('0', 954)

No of identity Gate: 190

('0', 967)

No of identity Gate: 200

('0', 974)

No of identity Gate: 210

('0', 964)

No of identity Gate: 220

('0', 963)

No of identity Gate: 230

('0', 959)

No of identity Gate: 240

('0', 968)

No of identity Gate: 250

('0', 964)

No of identity Gate: 260

('0', 976)

No of identity Gate: 270

('0', 962)

No of identity Gate: 280

('0', 962)

No of identity Gate: 290

('0', 970)

No of identity Gate: 300

('0', 959)

No of identity Gate: 310

('0', 960)

No of identity Gate: 320

('0', 965)

No of identity Gate: 330

('0', 958)

```
No of identity Gate: 340
('0', 965)
No of identity Gate: 350
('0', 966)
No of identity Gate: 360
('0', 966)
No of identity Gate: 370
('0', 953)
No of identity Gate: 380
('0', 951)
No of identity Gate: 390
('0', 962)
No of identity Gate: 400
('0', 963)
No of identity Gate: 410
('0', 970)
No of identity Gate: 420
('0', 956)
No of identity Gate: 430
('0', 962)
No of identity Gate: 440
('0', 962)
No of identity Gate: 450
('0', 973)
No of identity Gate: 460
('0', 970)
No of identity Gate: 470
('0', 958)
No of identity Gate: 480
('0', 963)
No of identity Gate: 490
('0', 954)
No of identity Gate: 500
('0', 970)
[978, 977, 964, 961, 966, 958, 956, 979, 966, 970, 959, 967, 968, 964, 964, 976,
955, 954, 967, 974, 964, 963, 959, 968, 964, 976, 962, 962, 970, 959, 960, 965,
958, 965, 966, 966, 953, 951, 962, 963, 970, 956, 962, 962, 973, 970, 958, 963,
954, 970]
```

0.1 20 time Average

```
y1=[969, 965, 960, 957, 967, 977, 964, 957, 953, 967, 960, 959, 966, 978, 967, u
 →973, 969, 958, 961, 974, 950, 965, 959, 962, 964, 960, 971, 960, 973, 953, U
\rightarrow 956, 968, 963, 972, 965, 961, 960, 958, 960, 960, 958, 965, 968, 962, 964, <math>\square
\rightarrow965, 973, 954, 958, 963]
y2=[959, 962, 964, 962, 950, 961, 966, 961, 963, 962, 956, 963, 965, 959, 967,<sub>U</sub>
\rightarrow968, 968, 970, 963, 964, 971, 964, 959, 973, 958, 964, 963, 947, 951, 964, 11
→956, 952, 963, 961, 964, 959, 962, 966, 973, 966, 968, 975, 962, 964, 958, U
→960, 970, 950, 958, 959]
y3=[965, 960, 963, 960, 960, 976, 966, 966, 969, 960, 974, 967, 966, 972, 962, u
\rightarrow960, 972, 963, 965, 955, 967, 966, 962, 968, 961, 966, 972, 945, 958, 967,
\rightarrow959, 959, 965, 964, 965, 970, 971, 965, 959, 963, 959, 962, 963, 968, 958, \Box
\rightarrow959, 966, 968, 963, 962]
y4=[963, 967, 971, 955, 966, 966, 968, 970, 960, 955, 958, 967, 952, 955, 964, u
959, 958, 971, 961, 964, 965, 973, 956, 954, 965, 958, 969, 970, 971, 960
\rightarrow974, 960, 963, 971, 962, 960, 953, 968, 959, 960, 965, 953, 962, 961, 961,
\rightarrow961, 969, 957, 954, 959]
y5=[969, 968, 959, 962, 965, 967, 964, 968, 966, 971, 964, 964, 966, 957, 958, u
 →959, 967, 953, 958, 969, 962, 965, 971, 962, 962, 958, 960, 957, 968, 958, U
→969, 961, 971, 969, 973, 971, 965, 953, 972, 956, 955, 972, 975, 959, 958, u
\rightarrow 973, 959, 957, 963, 968]
y6=[970, 965, 969, 965, 963, 967, 972, 964, 966, 961, 965, 968, 961, 974, 959,<sub>U</sub>
954, 964, 966, 957, 963, 971, 972, 952, 962, 971, 964, 964, 967, 972, 957,
→964, 965, 969, 957, 972, 964, 970, 957, 969, 973, 970, 948, 964, 967, 959, U
\rightarrow965, 961, 974, 966, 972]
y7=[967, 971, 967, 974, 962, 957, 961, 970, 962, 951, 964, 966, 973, 966, 958, u
→967, 962, 961, 962, 970, 963, 964, 966, 958, 963, 970, 959, 967, 958, 968, U
→966, 972, 965, 969, 963, 976, 952, 967, 969, 965, 968, 975, 959, 968, 962, u
\rightarrow952, 962, 963, 962, 960]
y8=[963, 967, 959, 961, 969, 968, 966, 963, 962, 974, 963, 970, 968, 960, 965, u
\rightarrow961, 964, 961, 955, 967, 959, 967, 966, 970, 960, 958, 963, 953, 958, 964,
→972, 961, 967, 963, 963, 964, 973, 971, 952, 960, 959, 965, 952, 960, 963, ⊔
\rightarrow959, 962, 964, 966, 961]
y9=[967, 959, 959, 956, 961, 961, 971, 965, 955, 962, 970, 962, 965, 962, 963,<sub>U</sub>
→959, 955, 956, 964, 964, 963, 959, 964, 962, 966, 970, 966, 962, 963, 967, U
→968, 954, 966, 966, 962, 956, 966, 957, 955, 986, 955, 959, 961, 961, 968, U
\hookrightarrow952, 962, 962, 962, 974]
y10=[960, 968, 957, 969, 969, 970, 964, 963, 960, 956, 952, 974, 962, 959, 967,<sub>U</sub>
→958, 960, 966, 961, 964, 974, 971, 966, 961, 962, 964, 951, 959, 968, 956, U
→974, 964, 971, 964, 972, 963, 965, 959, 967, 941, 960, 969, 965, 964, 963, U
\rightarrow972, 971, 962, 965, 965]
y11=[972, 952, 963, 967, 959, 957, 963, 966, 967, 964, 968, 962, 960, 962, 955, u
→973, 965, 959, 969, 961, 969, 972, 963, 959, 962, 969, 970, 975, 967, 960, U
→967, 958, 956, 962, 962, 967, 970, 965, 957, 966, 972, 962, 958, 962, 966, ⊔
\rightarrow960, 961, 970, 961, 971]
```

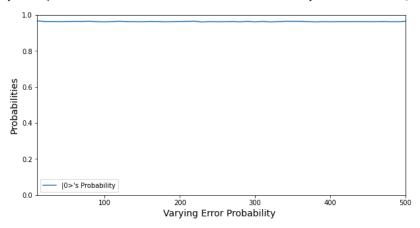
```
y12=[980, 966, 957, 965, 961, 966, 957, 967, 965, 965, 966, 960, 963, 967, 968, u
957, 961, 957, 964, 955, 959, 969, 957, 965, 959, 964, 962, 955, 972, 960,
\rightarrow962, 961, 965, 958, 957, 960, 978, 957, 968, 957, 970, 966, 956, 955, 968,
\rightarrow961, 960, 955, 966, 962]
y13=[966, 953, 954, 966, 964, 960, 964, 971, 958, 964, 965, 962, 978, 967, 957, u
959, 970, 965, 964, 967, 966, 955, 961, 958, 962, 961, 967, 969, 966, 962,
→965, 964, 959, 960, 967, 964, 968, 963, 968, 964, 971, 952, 968, 977, 966, U
→965, 971, 962, 970, 969]
y14=[971, 966, 969, 958, 972, 965, 965, 962, 961, 958, 966, 968, 954, 963, 961, u
\rightarrow967, 966, 970, 967, 957, 972, 962, 951, 962, 958, 960, 963, 965, 968, 970,
\rightarrow963, 961, 964, 963, 958, 971, 961, 970, 963, 961, 964, 965, 970, 960, 964,
\rightarrow958, 969, 969, 957, 969]
y15=[971, 968, 971, 957, 971, 959, 969, 964, 971, 962, 970, 960, 953, 959, 962, u
\rightarrow962, 967, 967, 961, 960, 961, 973, 958, 958, 969, 956, 958, 971, 970, 963,
4961, 953, 964, 976, 968, 969, 963, 970, 958, 956, 956, 963, 961, 965, 964, 10
\rightarrow962, 954, 969, 953, 962]
y16=[971, 959, 971, 964, 961, 968, 963, 965, 965, 967, 955, 981, 961, 948, 964, u
 \rightarrow969, 970, 959, 963, 964, 965, 967, 957, 961, 950, 972, 967, 965, 966, 949, \Box
\rightarrow960, 960, 967, 971, 969]
y17=[952, 962, 963, 976, 970, 952, 968, 956, 964, 958, 964, 960, 970, 966, 966, u
\rightarrow965, 963, 963, 958, 960, 959, 963, 957, 966, 962, 961, 965, 959, 961, 969,
→967, 964, 956, 954, 967, 963, 959, 955, 963, 964, 962, 966, 963, 971, 945, U
\rightarrow 972, 961, 954, 964, 967]
y18=[962, 965, 970, 959, 970, 975, 966, 966, 959, 958, 966, 959, 958, 963, 965, u
→970, 956, 965, 977, 965, 970, 956, 968, 971, 972, 955, 964, 957, 957, 966, U
\rightarrow 969, 958, 964, 973, 959]
y19=[976, 958, 968, 969, 953, 962, 954, 964, 969, 952, 962, 967, 958, 960, 955, u
→968, 966, 957, 962, 967, 962, 962, 970, 968, 954, 954, 963, 970, 960, 961, U
→967, 963, 961, 973, 965, 958, 952, 953, 961, 965, 966, 959, 971, 958, 967, ⊔
\rightarrow960, 974, 962, 965, 963]
y20=[978, 977, 964, 961, 966, 958, 956, 979, 966, 970, 959, 967, 968, 964, 964, u
→976, 955, 954, 967, 974, 964, 963, 959, 968, 964, 976, 962, 962, 970, 959, U
\rightarrow960, 965, 958, 965, 966, 966, 953, 951, 962, 963, 970, 956, 962, 962, 973,
→970, 958, 963, 954, 970]
avagarge = [967.55,963.9,963.9,963.15,963.95,964.6,964.35,965.35,963.05,961.
→85,963.35,965.3,963.35,963.05,962.35,964.2,963.9,962.05,962.95,964.2,964.
\rightarrow6,965.4,961.1,963.4,962.2,963,963.95,961.75,964.85,961.65,964.85,961.45,963.
-05,965,964.9,964.75,963.5,961.6,963.1,962.25,963.35,963,963.4,963.35,962.
 \rightarrow 8,962.75,964.05,962.3,962.55,965.2
```

0.2 Map Plotting

```
[61]: | %config InlineBackend.print figure kwargs={'facecolor' : "w"}
                      import matplotlib.pyplot as plt
                      from matplotlib.ticker import (AutoMinorLocator, MultipleLocator)
                      fig, ax = plt.subplots(figsize=(10, 5))
                      fig.suptitle('|O> probability for Depolarisation error BB84 Protocol with ⊔
                        →variable Identity Gate number as Quantum Channel',fontsize=15)
                      # naming the x axis
                      plt.xlabel('Varying Error Probability ',fontsize=14)
                      # naming the y axis
                      plt.ylabel('Probabilities',fontsize=14)
                      # giving a title to my graph
                      # Set axis ranges; by default this will put major ticks every 25.
                      #ax.set xlim(0, 300)
                      #ax.set_ylim(0, 1)
                      ax.set_xlim(10, 500)
                      ax.set_ylim(0,1)
                      fig = plt.figure(figsize=(8,5))
                      # line 2 points
                      v1 = [0.96755, 0.9639, 0.9639, 0.96315, 0.96395, 0.9646, 0.96435, 0.96535, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96305, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505, 0.96505
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                         \rightarrow 9642,0.9646,0.9654,0.9611,0.9634,0.9622,0.963,0.96395,0.96175,0.96485,0.
                         \rightarrow 96165, 0.96485, 0.96145, 0.96305, 0.965, 0.9649, 0.96475, 0.9635, 0.9616, 0.9631, 0.
                         496225,0.96335,0.963,0.9634,0.96335,0.9628,0.96275,0.96405,0.9623,0.96255,0.
                         <del>→</del>9652]
                      x1 = [10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 130, 140, 150, 160]
                         →170, 180, 190, 200, 210, 220, 230, 240, 250, 260, 270, 280, 290, 300, 310, U
                         →320, 330, 340, 350, 360, 370, 380, 390, 400, 410, 420, 430, 440, 450, 460, u
                        470, 480, 490, 500
                      # plotting the line 2 points
                      ax.plot(x1, y1, label = "|0>'s Probability")
                      #ax.axes.xaxis.set_ticks([])
                      # show a legend on the plot
                      ax.legend()
```

[61]: <matplotlib.legend.Legend at 0x7f2392b2aa90>

|0> probability for Depolarisation error BB84 Protocol with variable Identity Gate number as Quantum Channel



<Figure size 576x360 with 0 Axes>

```
[53]: from statistics import mean
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       →953, 956, 968, 963, 972, 965, 961, 960, 958, 960, 960, 958, 965, 968, 962, □
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       \rightarrow974, 960, 963, 971, 962, 960, 953, 968, 959, 960, 965, 953, 962, 961, 961,
       \rightarrow961, 969, 957, 954, 959],
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\rightarrow961, 964, 961, 955, 967, 959, 967, 966, 970, 960, 958, 963, 953, 958, 964, \square
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\rightarrow 968, 954, 966, 966, 962, 956, 966, 957, 955, 986, 955, 959, 961, 961, 968, \Box
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print(*map(mean, zip(*a)))
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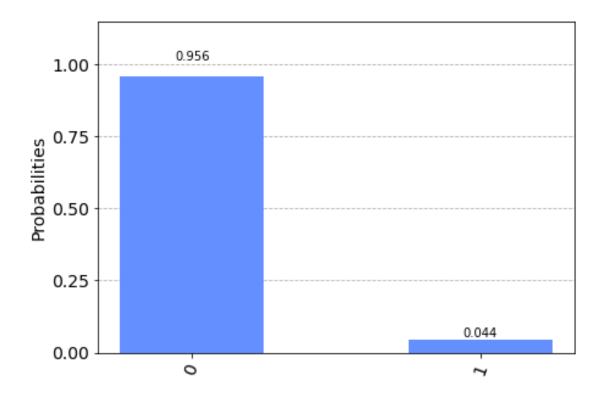
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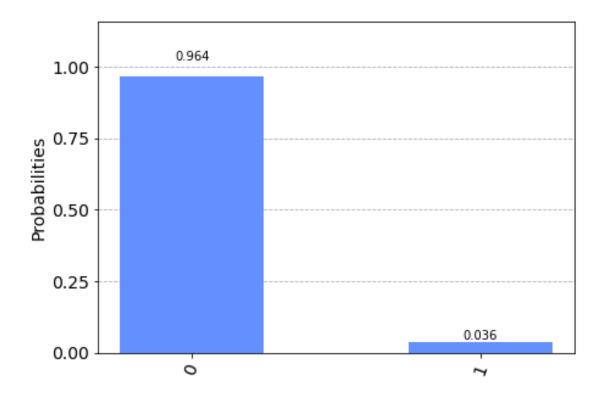
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0.3 Sir's Code

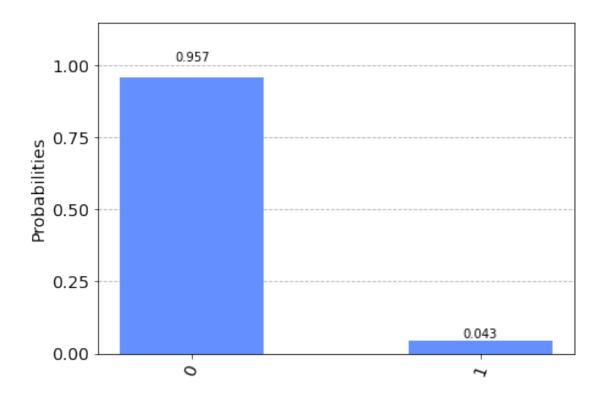
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[58]:
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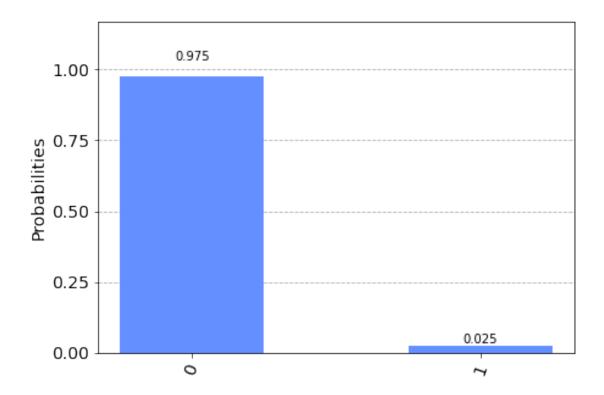
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[5]:



[6]:



[]: