

a)

- Sort the set of points P along x -axis into $\boxed{O(n \log n)}$ with mergesort.
- a BST, P. Use x as a key and y as a value.

- initialize 'layers' a 2D list

- While P is not empty:

 - Start from rightmost in P

$\boxed{\text{It is sorted and keyed by } X \text{ so can be reached } O(1)}.$

 - Add to layer

 - save y -value as \max_y

 - For point in P :

 - If $\text{point}_y > \max_y$:

 - add point y to layer $\leftarrow O(1)$

 - pop point from P $\leftarrow O(\log n)$

Complexity:

- Sorting $O(n \log n)$

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- Each point is visited only once because they are removed when visited.
- Delete on every traversal $O(n \log(n))$
- Add to list on every traversal $O(n)$

$$O(n \log n + n \log n + n)$$

$$O(2n \log n)$$

$$\underline{O(n \log n)}$$

b)