

Hourly solar power forecasting using ARMA models

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Abstract

We describe a succinct methodology to develop hourly auto-regressive moving average (ARMA) models to forecast solar power. We illustrate how to use statistical tests to validate the model and construct hourly samples. These samples can be used as scenarios for energy planning or in stochastic optimization models.

Keywords: ARMA, solar energy, forecasting, scenario generation

1. Introduction

Increasing penetration of renewable energy sources, such as wind and solar, in the electricity grid requires good day-ahead power forecasts. Solar power differs from wind power due to its diurnal nature, and can have much greater ramps than wind [1]. In this article, we focus on forecasting
5 hourly solar power generation.

Forecasting methods for solar power are broadly divided into two categories: (i) physics-based models—these models predict solar power from numerical weather predictions and solar irradiation data, and (ii) statistical models—these models forecast solar power directly from historical data. Comparisons of these two methods are also available; see, e.g., [2, 3]. There are other approaches
10 available as well which combine these two methods [4]. In this article we center on statistical methods alone, and specifically the use of auto-regressive moving average (ARMA) models to develop our forecasts. ARMA models are widely used for forecasting many economic and planning processes; see, e.g., [5]. They have also been used to forecast wind power [6, 7], as well as solar power [8, 9]. Yet, accurate and fast methods to generate solar power scenarios are often unavailable, and nor-
15 mal approximations are often used; see, e.g., [10]. Here, we describe an in-depth summary of the

methodology to forecast solar power using ARMA models. The presented models can be applied either to a local photo-voltaic generating plant or at the regional level.

2. Methods

We take hourly year-long historical solar power output from [11]. We use approximately nine months of data for training. The data does not have any solar power for the ten hours [20:00-5:00], and hence we restrict the forecasts in these hours to be zero as well. For each of the remaining 14 hours of the day, we build an ARMA(p, q) model. Further, for each hour, we verify the stationarity of the time series. For each hour, we test a number of ARMA(p, q) models and find the best one. We use statistical tests on the residuals to validate the model. Finally, we use Monte Carlo sampling from the best ARMA model, for each hour, to create hourly scenarios. Below we provide more details.

2.1. Stationarity

An ARMA model may be suitable if a series is stationary. We test the hourly data for stationarity using the Augmented Dickey-Fuller (ADF) test [12]. The ADF test has a null hypothesis that the series includes a unit root (or, is non-stationary). We reject the null hypothesis at a level 0.05 if the test-statistic exceeds its 0.95 level quantile. For all the 14 hours of the day, the null hypothesis is rejected suggesting the series may be stationary, and hence an ARMA model may be suitable. If the series were not stationary, an ARIMA model may be suitable.

2.2. Selecting parameters of the ARMA model

Next, we estimate the parameters of the ARMA model— p , the order of the autoregressive part and, q , the order of the moving average part. For each hour, we construct 16 models with both p and q between one and four, and compute the log-likelihood objective function value. Next, for each hour, we calculate the Bayesian information criteria (BIC) for the 16 models using $p + q + 1$ parameters. The BIC penalizes for models with more parameters, and the smallest value of the BIC gives the best model, for each hour. Table 1 provides our estimated p and q values for the 14 hours of the day. We note that none of the hours have an order value exceeding two.

Table 1: Estimated p and q values for ARMA(p, q) models for 14 hours of the day

Hour	6:00	7:00	8:00	9:00	10:00	11:00	12:00	13:00	14:00	15:00	16:00	17:00	18:00	19:00
p	1	1	1	1	2	1	1	1	1	1	1	1	1	2
q	1	1	1	1	1	1	2	1	1	1	1	1	2	1

24-Period Solar Power Forecasts and Approximate 95% Confidence Intervals

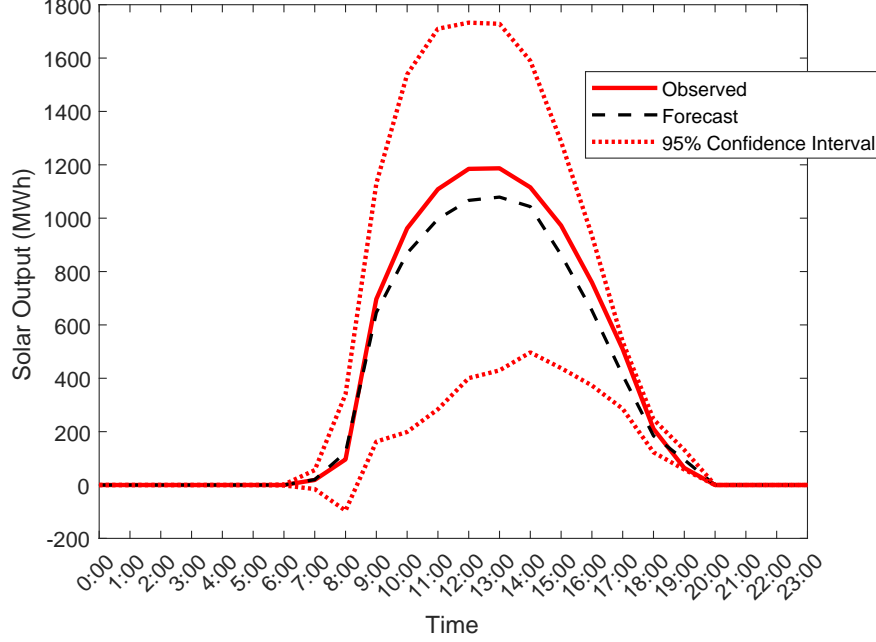


Figure 1: Day-ahead actual and predicted values using ARMA models from Table 1

2.3. Prediction

Figure 1 plots a day-ahead prediction using the above constructed ARMA models; i.e., one hour ahead predictions from the 14 ARMA models. The mean absolute error between the actual and the predicted series is 39.6, or 3.3% of the maximum actual value. The root mean square error between the actual and the predicted series is 61.0, or 5.1% of the maximum actual value.

We further verify autocorrelation in the series, for each hour, using the Ljung-Box test [13] on the residuals for lags of 5, 10, and 15. The Ljung-Box test has a null hypothesis that the residuals are uncorrelated up to a given lag. We reject the null hypothesis at a level 0.05 if its test-statistic exceeds its 0.95 level quantile. For all the 14 hours of the day, the null hypothesis is not rejected suggesting a zero autocorrelation in the series, or the model choice may be appropriate.

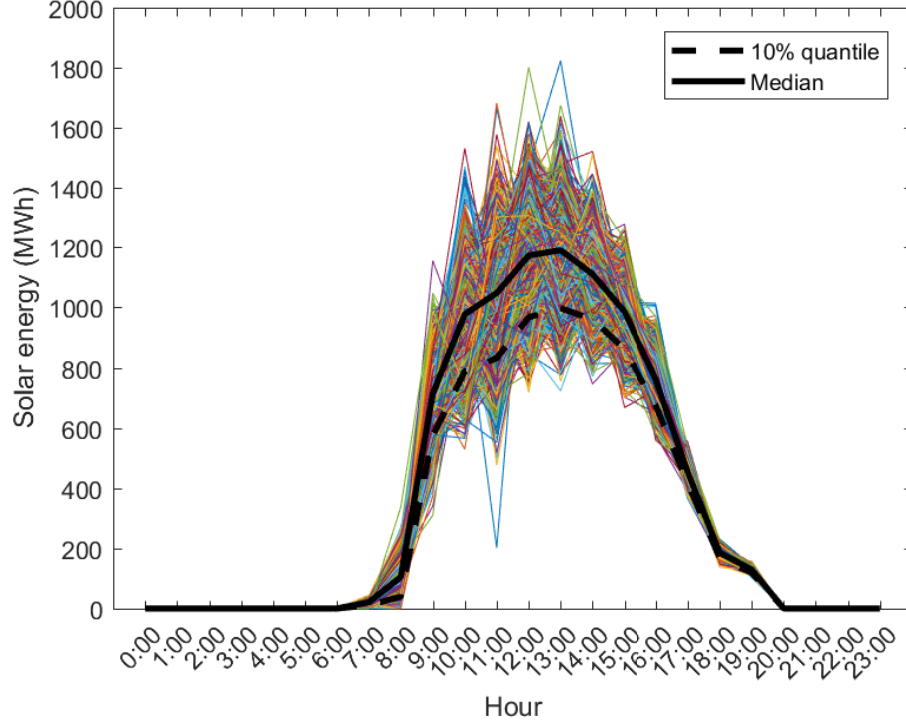


Figure 2: 2000 hourly scenarios for solar power generated using the ARMA models from Table 1. The dashed black line is the median hourly value, and the solid black line is the 10 percentile solar energy value.

Finally, we use Monte Carlo sampling to generate 2000 hourly solar power scenarios. The output from an ARMA model is real valued, and hence can be negative. We truncate the negative powered outputs to 0. For the 14 hours of the day, the sampling resulted in 1.6% of the outputs with estimated power output below -5MWh. Figure 2 plots the 2000 day-ahead scenarios as well as the median and 10 percentile values.

Conclusions

We present a step-by-step methodology for fitting an ARMA model to historical solar power data, and use it to forecast future hourly scenarios. We present statistical tests to check the applicability of the model and investigate the fit, at each step. This methodology can be directly applied to historical data to analyze if an ARMA model might be suitable, and can be used to

create future scenarios for use in a stochastic model.

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References

- 70 [1] I. Graabak, M. Korpås, Variability characteristics of european wind and solar power resources—
A review, *Energies* 9 (6) (2016) 449.
- [2] Y. Huang, J. Lu, C. Liu, X. Xu, W. Wang, X. Zhou, Comparative study of power forecasting
methods for PV stations, in: *Power System Technology (POWERCON), 2010 International
Conference on*, IEEE, 2010, pp. 1–6.
- 75 [3] R. H. Inman, H. T. Pedro, C. F. Coimbra, Solar forecasting methods for renewable energy
integration, *Progress in energy and combustion science* 39 (6) (2013) 535–576.
- [4] C. Chen, S. Duan, T. Cai, B. Liu, Online 24-h solar power forecasting based on weather type
classification using artificial neural network, *Solar Energy* 85 (11) (2011) 2856–2870.
- [5] G. Box, G. Jenkins, G. Reinsel, G. Ljung, *Time Series Analysis*. Hoboken (2008).
- 80 [6] B. G. Brown, R. W. Katz, A. H. Murphy, Time series models to simulate and forecast wind
speed and wind power, *Journal of climate and applied meteorology* 23 (8) (1984) 1184–1195.
- [7] M. J. Duran, D. Cros, J. Riquelme, Short-term wind power forecast based on ARX models,
Journal of Energy Engineering 133 (3) (2007) 172–180.
- [8] L. Mora-Lopez, M. Sidrach-de Cardona, Multiplicative ARMA models to generate hourly series
85 of global irradiation, *Solar Energy* 63 (5) (1998) 283–291.

- [9] R. Huang, T. Huang, R. Gadh, N. Li, Solar generation prediction using the ARMA model in a laboratory-level micro-grid, in: Smart Grid Communications (SmartGridComm), 2012 IEEE Third International Conference on, IEEE, 2012, pp. 528–533.
- [10] W. Su, J. Wang, J. Roh, Stochastic energy scheduling in microgrids with intermittent renewable energy resources, IEEE Transactions on Smart Grid 5 (4) (2014) 1876–1883.
- [11] F. Golestaneh, H. B. Gooi, P. Pinson, Generation and evaluation of space–time trajectories of photovoltaic power, Applied Energy 176 (2016) 80–91.
- [12] D. A. Dickey, W. A. Fuller, Distribution of the estimators for autoregressive time series with a unit root, Journal of the American Statistical Association 74 (366a) (1979) 427–431.
- [13] G. M. Ljung, G. E. Box, On a measure of lack of fit in time series models, Biometrika 65 (2) (1978) 297–303.