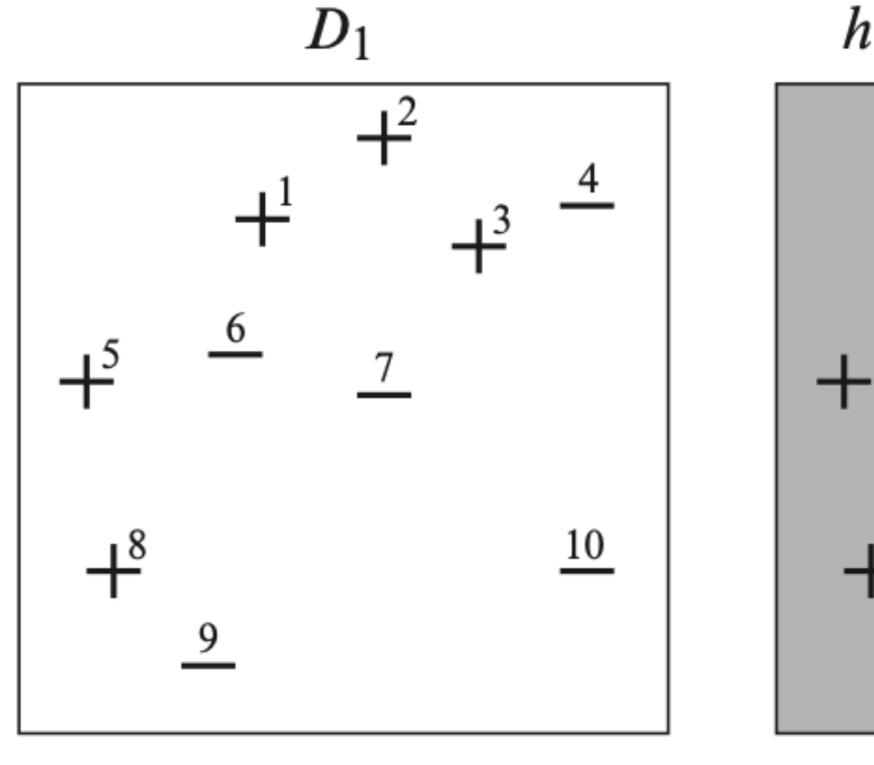
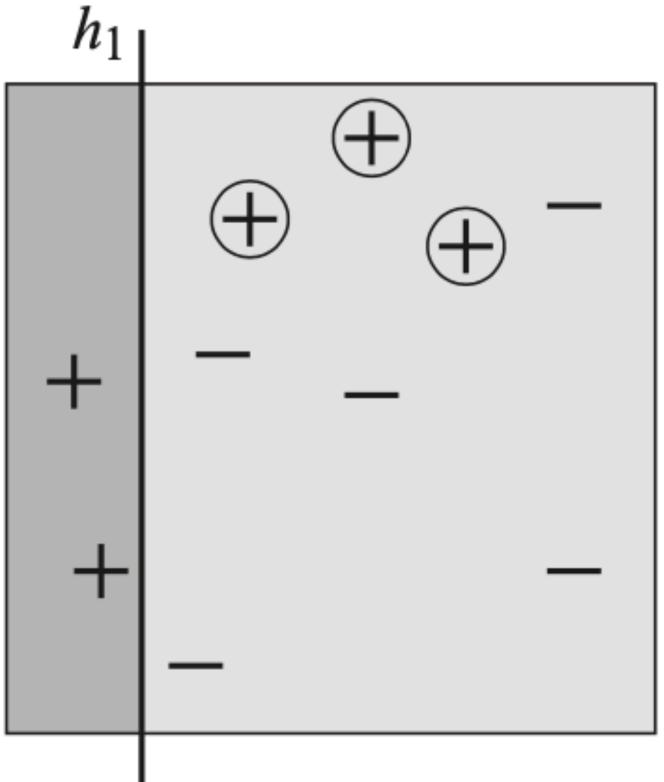
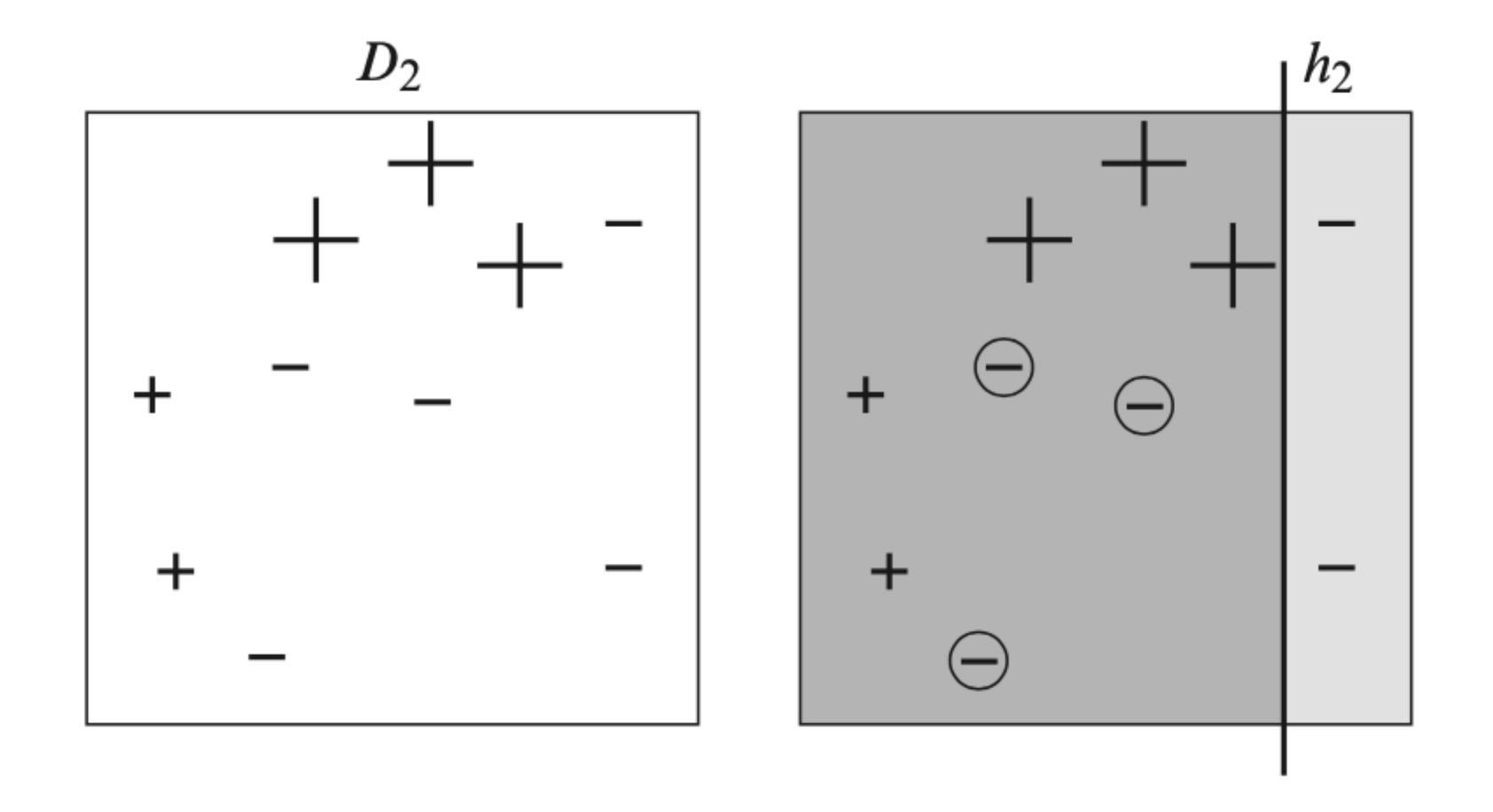
AdaBoost

Boosting: a toy example

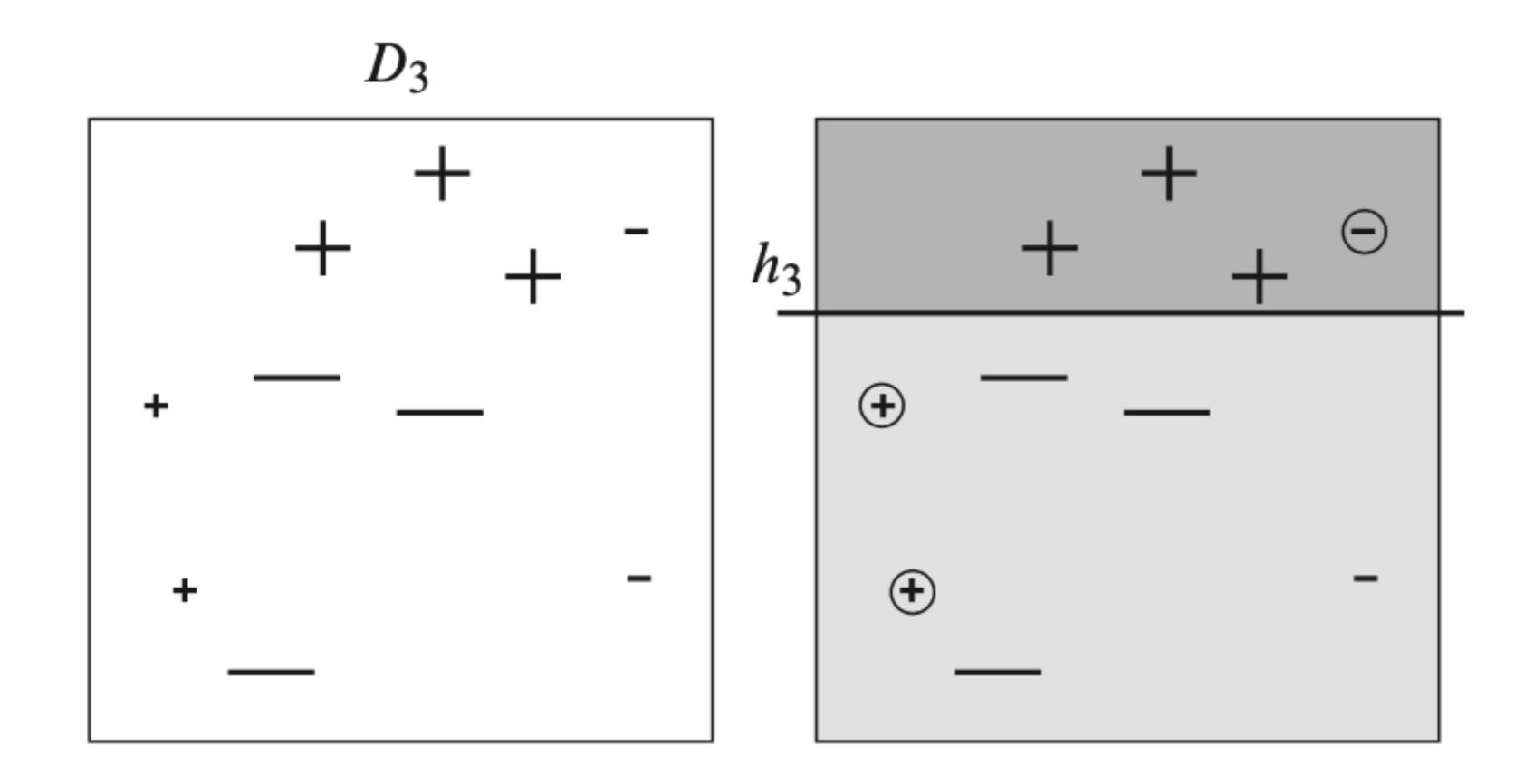




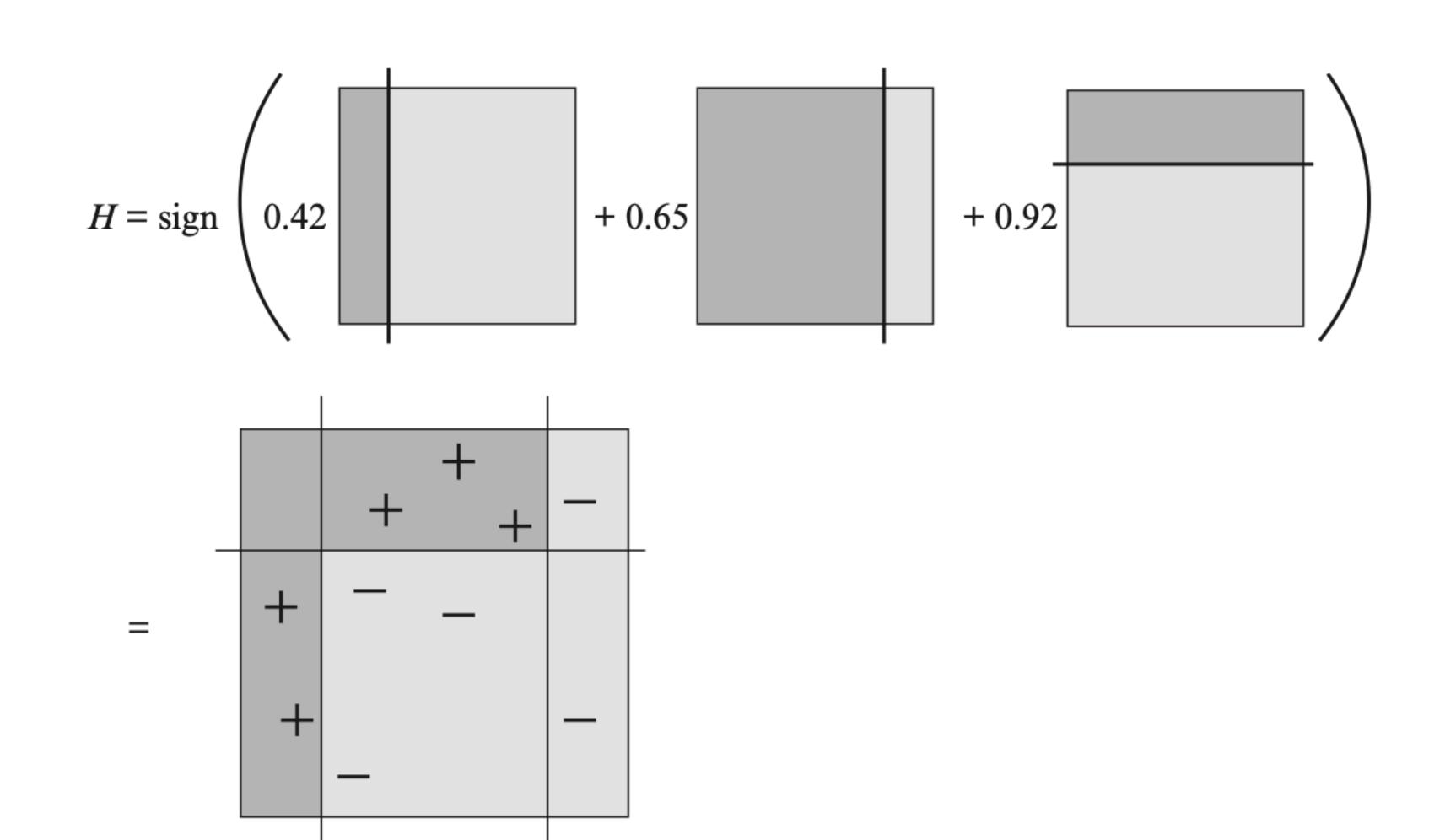
Boosting: a toy example (cont.)



Boosting: a toy example (cont.)



Boosting: a toy example (cont.)



Source: Schapire and Freund, Boosting: Foundations and Algorithms, Section 1.2

AdaBoost

Given: $(x_1, y_1), ..., (x_m, y_m)$ where $x_i \in \mathcal{X}, y_i \in \{-1, +1\}$. Initialize: $D_1(i) = 1/m$ for i = 1, ..., m. For t = 1, ..., T:

- Train weak learner using distribution D_t .
- Get weak hypothesis $h_t: \mathcal{X} \to \{-1, +1\}$.
- Aim: select h_t to minimalize the weighted error:

$$\epsilon_t \doteq \mathbf{Pr}_{i \sim D_t}[h_t(x_i) \neq y_i].$$

- Choose $\alpha_t = \frac{1}{2} \ln \left(\frac{1 \epsilon_t}{\epsilon_t} \right)$.
- Update, for $i = 1, \ldots, m$:

$$D_{t+1}(i) = \frac{D_t(i)}{Z_t} \times \begin{cases} e^{-\alpha_t} & \text{if } h_t(x_i) = y_i \\ e^{\alpha_t} & \text{if } h_t(x_i) \neq y_i \end{cases}$$
$$= \frac{D_t(i) \exp(-\alpha_t y_i h_t(x_i))}{Z_t},$$

where Z_t is a normalization factor (chosen so that D_{t+1} will be a distribution).

Output the final hypothesis:

$$H(x) = \operatorname{sign}\left(\sum_{t=1}^{T} \alpha_t h_t(x)\right).$$