

Recommender Systems

Electronic Business Technologies



Recommender Systems

- In e-markets there is too much information available, and consumers have an overwhelming number of alternatives
- Would be helpful:
 - narrow down users' choices
 - make choices without having sufficient personal experience or information
- Recommender System (RS)
system that provides recommendations to a user
 - Amazon.com makes use of a recommendation system when you select an item *X*, (Amazon provides a list of items that have been purchased by other users who have also purchased item *X*)



Recommender Systems

- Information used by RSs:
 - Purchase data
 - purchase history of users
 - Feedback provided by users
 - feedback can be provided explicitly or implicitly (ex: playlist)
 - Textual comments
 - Browsing and searching data
 - observe user's behaviour and infer their preferences
 - Expert recommendations
 - Demographic data
 - age, gender, education, geographical location, ...
 - ...



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Recommendation

- Recommendation problem
 - Problem of estimating *ratings* for the items that have not been seen by a user

$$\forall c \in C, \quad s'_c = \max_{s \in S} u(c, s)$$

C – set of all users

S – set of all possible items that can be recommended

$u(c, s)$ – utility function (usefulness of item s to user c)

- Recommender systems predict:
 - absolute values of ratings that users would give to items → *rating-based systems*
 - the relative preferences of users → *preference-based filtering*



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Recommendation

- Each element of the user space C can be defined with a profile
 - user characteristics, such as age, gender, income, ...
 - user preferences and needs
 - can be elicited explicitly (questionnaires) or implicitly (behavior over time)
- Each element of the item space S can be defined with a set of characteristics:
 - domain-dependent attributes



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Recommender Systems

- Classified into:
 - *Content-based recommendations*
recommend items based on the ones the user preferred in the past and user profile
 - *Collaborative recommendations*
recommend items that people with similar tastes and preferences liked in the past
 - *Hybrid approaches*
combine collaborative and content-based methods



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Content-based recommendation

$u(c,s)$ estimated based on $u(c,s_i)$

$u(c,s_i)$: utility assigned by user c to items s_i

$s_i \in S$ and s_i is similar to item s

$$u(c,s) = \text{score}(\text{ContentBasedProfile}(c), \text{Content}(s))$$

$\text{ContentBasedProfile}(c)$: user c profile

$\text{Content}(s)$: item s profile

ex: a movie recommender will probably recommend a new Woody Allen film to a Woody Allen fan



Property: Do not depend on having other users in the system (do not need a critical mass)

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Content-based recommendation (1)

$u(c,s)$ can be estimated by the cosine distance between user's and item's profile vectors

Consider a movie recommender system

M1 profile = (1,0,1,0,1) % actors: Julia, Peter, Mark, Jennifer, Tom

utility matrix (if not boolean, we can normalize it)

	M1	M2	M3	M4	...	avg
A	3	4	5		...	3
B	2	3		5	...	4

M1, M2, M3, M4 have Julia as actress

UserA profile = (1,...) % (likelihood of movies with Julia, ...)

UserB profile = (-2/3, ...)



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Content-based recommendation (1)

User profile:

- positive values in components related to actors that appear in movies the user likes
- negative values in components related to actors that appear in movies he doesn't like

Consider a movie M_n

- M_n profile = (1,0,1,1,1) % with many actors the user X likes
cosine of the angle (UserA, M_n) will be a large positive fraction (angle close 0)
- M_n profile = (0,0,1,1,1) % with mostly actors the user X doesn't like
cosine of the angle (UserA, M_n) will be a large negative fraction (angle around 180)
- M_n profile = (1,0,1,0,1) % with as many actors the user X likes as doesn't like
cosine of the angle (UserA, M_n) is around 0 (angle around 90)



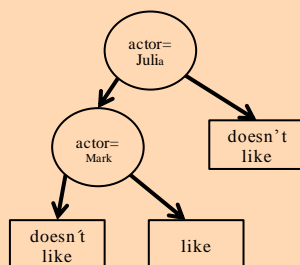
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Content-based recommendation (2)

$u(c,s)$ can be estimated using machine learning

- the given data is the training set
- for each user, build a classifier that predicts the rating of all items

Possible classifiers: *decision tree*, *neural network*, ...



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Content-based recommendation

Limitations:

- Items profiles should contain a sufficient set of features
 - IR techniques work well in extracting features from text documents, but other domains are much harder (multimedia data, ...)
- Over-specialization
 - limited to recommend items that are similar to those already rated
res: often addressed by introducing some randomness
- New items
 - The user has to rate a sufficient number of items before the system can really understand its preferences



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Collaborative recommendation

$u(c,s)$ estimated based on $u(c',s)$

$u(c',s)$: utility assigned by user c' to items s
 $c' \in C$, and c' is similar to c

Two general classes:

- *Memory-based (heuristic-based)*:
heuristics that make rating predictions based on previously rated items by the users
- *Model-based*
use previous ratings to learn a *model*, which is then used to make rating predictions



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Collaborative recommendation (memory-based)

Let be $r_{c,s}$ the unknown rating for user c and item s

$r_{c,s}$ computed as an aggregation of the ratings of some other users (usually, the N most similar) for item s

$$r_{c,s} = \text{aggr}_{c' \in C_s} r_{c',s}$$

C_s : set of N most similar users to c who have rated s

$\text{sim}(c, c')$: similarity between users c and c'

is a distance measure, and is used as a weight



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Collaborative recommendation (memory-based)

– Some examples of aggregation functions:

$$\text{i) } r_{c,s} = \frac{1}{N} \sum_{c' \in C_s} r_{c',s}$$

$$\text{ii) } r_{c,s} = k \sum_{c' \in C_s} \text{sim}(c, c') \times r_{c',s}$$

k is a normalizing factor, $k = 1 / \sum_{c' \in C_s} |\text{sim}(c, c')|$

$$\text{iii) } r_{c,s} = \bar{r}_c + k \sum_{c' \in C_s} \text{sim}(c, c') \times (r_{c',s} - \bar{r}_{c'})$$

$$\bar{r}_c = (1/|S_c|) \sum_{s \in S_c} r_{c,s}, \quad S_c = \{s \in S \mid r_{c,s} \neq \emptyset\}$$



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Colaborative recommendation (memory-based)

- **Similarity** (some approaches):
 - **Correlation**: uses the Pearson correlation coefficient

$$sim(c, c') = \frac{\sum_{s \in S_{cc'}} (r_{c,s} - \bar{r}_c)(r_{c',s} - \bar{r}_{c'})}{\sqrt{\sum_{s \in S_{cc'}} (r_{c,s} - \bar{r}_c)^2 \sum_{s \in S_{cc'}} (r_{c',s} - \bar{r}_{c'})^2}}$$

$S_{cc'}$: set of all items corated by c and c'

can also be used to compute
similarity between items

- **Cosine-based**: cosine of the angle between vectors that represent the 2 users in m-dimensional space ($m = |S_{cc'}|$)

$$sim(c, c') = \cos(\vec{c}, \vec{c'}) = \frac{\sum_{s \in S_{cc'}} r_{c,s} r_{c',s}}{\sqrt{\sum_{s \in S_{cc'}} r_{c,s}^2} \sqrt{\sum_{s \in S_{cc'}} r_{c',s}^2}}$$

- **Clustering**



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Colaborative recommendation (memory-based)

	Item1	Item2	Item3	Item4	Item5	
User A	4	4	1	4	3	$\bar{r}_D = 3.5$
User B	2	1	4	2	5	$\bar{r}_A = 3$
User C	3	1	3	2	1	$\bar{r}_B = 3$
User D	5	4	2		3	$\bar{r}_C = 2$

using Pearson correlation:

$$sim(D,A)=0.9 ; sim(D,B)=-0.7 ; sim(D,C)=0$$

using aggregate funtion: $r_{c,s} = \bar{r}_c + k \sum_{c' \in C_S} sim(c, c') \times (r_{c',s} - \bar{r}_{c'})$

$$\bar{r}_{D,4} = 3.5 + 0.625 * (0.9 * (4 - 3) - 0.7 * (2 - 3)) = 4.5$$

$$k = 1/(0.9 + 0.7 + 0) = 0.625 \text{ (using all neighbours)}$$



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Colaborative recommendation (model-based)

Uses the collection of ratings to learn a *model*, which is then used to predict ratings

- Probabilistic approach:

$$r_{c,s} = E(r_{c,s}) = \sum_{i=0}^n i \times \Pr(r_{c,s} = i | r_{c,s'}, s' \in S_c)$$

- *Pr* can be estimated by: cluster models, Bayesian networks

- Machine learning approach:

- Neural networks, Decision trees, ...



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Collaborative recommendation

Limitations

- New user problem
 - The user has to rate a sufficient number of items before the system can really understand its preferences
 - res*: use item popularity ; item entropy ; user personalization ; hybrid recommendation
- New item problem
 - New item needs to be rated by a substantial number of users
 - res*: hybrid recommendation
- Sparsity
 - Recommendation depends on the availability of a critical mass of users
 - res*: use user profile information for $\text{sim}(c, c')$; SVD (Singular Value Decomposition) for sparse ratings matrices



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Collaborative recommendation

Limitations

- Reliability
 - Ratings can be artificially inflated by phantom users
- Users' privacy
 - The more information a system has about users' preferences and tastes, the better it can provide recommendation. But users may not want their habits known

res: anonymous participation



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Hybrid methods

Combine *collaborative* and *content-based* methods:

- 1) Combining separate recommenders
 - Combine the outputs (ratings) from individual RSs using a linear combination or a voting scheme
 - Use one of the individual RSs, one that is “better” (higher level of confidence, more consistent with past ratings of the user, ...)



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Hybrid methods

Combine *collaborative* and *content-based* methods:

- 2) Adding content-based characteristics to collaborative methods
 - for instance, include content-based profiles for each user
 - > used to calculate $\text{sim}(c, c')$
 - > recommend item that scores highly against the user's profile
- 3) Adding collaborative characteristics to content-based methods
 - Create a collaborative view of a collection of content-based profiles (for instance, user profiles)



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Hybrid methods

Combine *collaborative* and *content-based* methods:

- 4) Developing a single unifying recommendation model
 - for instance, use the profile information of users and items in a single statistical model that estimates unknown ratings:

$$r_{cs} = x_{cs}\mu + z_c\gamma_s + \omega_s\phi_c + e_{cs}$$



- Use of *case-based reasoning* to improve recommendation accuracy

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RSs and e-commerce

Recommender Systems used in e-commerce

- Helping users find products/services
- Cross-selling
 - suggesting additional products for the user to purchase
- Personalization
 - Enables vendors to offer personalized products
- Keeping users informed
 - Keep users up-to-date on current offers and new products
- Retaining user loyalty
 - RSs create a value-added relationship between the site and the user.



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Recommender Systems

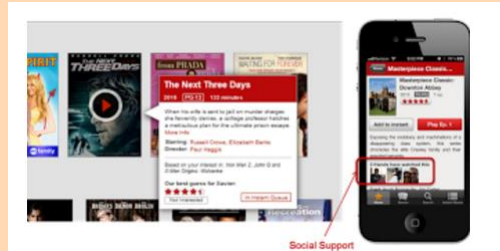
Some examples:

- LinkedIn
 - Recommendations for people, jobs, groups or companies (collaborative filtering)
- Amazon
 - Recommends items other users purchased (collaborative filtering)
- Netflix
 - Video rental and streaming service (content-based and collaborative filtering)



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Recommender System - Netflix



Promotes trust by
provide explanations

Ranking =
Predicted rating + Popularity

