

Algorithms: Design and Implementation

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7th April, 2025

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1 Algorithms: Design and Implementation

Correct Thinking leads to correct Code!

Algorithms, even the ones that seem simple, can be very difficult to design and implement. Purely technical algorithms frequently have mistakes in them until they have been debugged over a significant period of time. Business Logic algorithms are unique to the domain and there is little guidance there to help the developer.

The biggest failing is not one of coding, but rather a failure of imagination, to conceive of all the scenarios that the algorithm is executed in. Not realizing that a list might be empty, or a input not supplied can wreck an algorithm.

We will go through a systematic process that is a discovery process, finding all the ways the algorithm will be used and stretched. The code is intuitive once all the facets of the problem domain have been discovered.

2 Requirements

State & Clarify – Deep Comprehension Modeling

Study the given requirements with deep comprehension, looking to find a singular explanation model for how the results can be reached from the description details. Make sure that every word or apparent quirk, ambiguity, anomaly, or lack of clarity in your understanding of the domain is worked out for every part of the model.

Use the domain terminology exclusively for reading, writing, and modeling the requirements.

Model every entity in the description carefully, being very wary of premature optimization. This initial model is for proving correctness, and will be used to verify correctness of optimizations further in the development process.

3 Definition

Refine your domain model into a computational model, using computational terms with entities transformed into data structures or objects having one or more invariants, types, and operations.

Define your goals in terms of metrics, and clearly state your assumptions.

Your requirements and definition process is foundational to your success, and the remaining process is more derivative than architectural. Your code reflects these assumptions more than your skill in most cases.

4 SCENARIOS

State & Clarify – CASES and EXPECTATIONS

(Contexts & Inputs, Expectations & Qualifications, Outputs).

CASES are Contexts and Inputs. Contexts are factors or constraints in the case that shape the case beyond the simple action or input that is fed into the algorithm. Inputs are events or data that are fed into the algorithm.

The combination of Context and Inputs allow the algorithm designer to craft an effective expectation of BEHAVIOR that is complete and satisfies the CASE.

Expectations and Qualifications are the definition of BEHAVIOR that that correctly solve the CASE. The Expectations are what the algorithm should compute, do, or return. The Qualifications are constraints on the behavior such as how fast it must solve the problem, or how many solutions it should produce.

The outputs are what the algorithm should return. Even if the algorithm is entirely side-effects it should probably return an error code. Defining what the algorithm returns clearly is vital to understanding the problem, documenting, and testing it.

4.1 BEHAVIOR

State & Clarify

BEHAVIOR is the actions that lead to the EXPECTATIONS being met by the algorithm. It is vital to clarify the behavior and make sure it covers all facets of the environment, cases, and results.

It is important to clarify behavior because if behavior doesn't thread through the scenarios it will result in a broken implementation.

4.2 INPUTS?

State & Clarify - Types and Scale

The type, scale, and possible anomalies in the inputs to the algorithm have a huge impact on the algorithm. Designing something for one thousand elements is a very different from designing for one million elements. A thousand will fit easily to memory, a million elements is a different design entirely.

4.3 RETURN?

State & Clarify - Types and Scale

The types and results that EXPECTATIONS requires are crucial to the design process. Early in the computation the assembly of output should begin.

4.4 CHANGE?

State & Clarify - Before and After

Sometimes the algorithm must make a change in the environment. This is less-desirable from a design and implementation standpoint but if it is the EXPECTATION then it must be done well.

If a change must be made it is best to make the algorithm idempotent, or where repeated calls have the same result. For example: a light button as a toggle will alternate on/off the lights every time it's pressed. This is confusing since the initial state determines the result. A switch instead, will turn the light off every time it is pressed in the off direction. That is idempotent.

5 Sketch the Code

Sketch the code in functions, loops, with comments on purpose and O-notation complexity

1. **Initialize:** establish a return value, empty containers over nulls
2. **Terminate:** determine the base case. When is it done?
3. **First, Common, Last Cases:** The basic sequence of the algorithm
4. **Corner:** cases
5. **Input Validation:** System errors, stale state, deadlocks, and sync errors, timeouts

6. **State:** initialize, update, delete [1]

6 Design (Iteration)

6.1 CASES and Experiments

Brainstorm the different CASES in the context of an environment. Conduct thought experiments, Give up on bad ideas quickly. See if the CASES enumerate all the scenarios, how common they are: common case, corner case.

6.2 Isolate Operations

Maximize Idempotent side-effect free operations [1]

Breakdown the cases into functions, and try and maximize side-effect free idempotent functions. Where there is state handle it carefully defining the entire life-cycle of the state.

6.3 Message Passing (API)

APIs are message passing between functionally isolated components (API)

Modules are data coupled, or related functions. API's pass abstract messages between modules that are declarative or events in nature that execute operations without knowledge of how those operations are built.

6.4 Paradigm

Solution Comprehension

At this point you should have a collection of functions, with a description of the part they play in the algorithm. Next is paradigm.

Paradigm is what model best describes the problem (dynamic greedy, lazy, streams, Relational, divide and conquer) and most efficiently produces an answer.

Spot check the paradigm against the CASES to see if it adequately describes the problem. Find the right paradigm.

6.4.1 Recursion

$$\theta(\log_n) \tag{1}$$

Recursion is elegant and compact. In languages that support it it is practical as well as simple and transparent.

1. recurrence

Distill the problem down into a solution that can be applied to all the elements.

2. termination

Define the base case or **termination** as return of the solution that unwinds the recursion.

6.4.2 Divide & Conquer

$$\theta(n * \log_n) \tag{2}$$

Divide and Conquer is a technique where the problem is dived into parts, each part is solved, and then the sub-solutions are combined into the complete solution.

1. Divide the problem into n/x parts.

Decide the granularity of the division.

2. Solve each part

Solve the sub-problem. The reduced scale of n reduces the complexity or run time of the solution.

3. Combine the solutions for the final solution

With each sub-problem solved combine the solutions into a final solution.

6.4.3 Dynamic

Dynamic Programming uses a technique of caching answers to frequently computed problems.

Memoization [5] is a powerful technique and in Python the "functools" package has a LRU [6]

6.4.4 Linguistic (DSL)

DSL stands for Domain Specific Languages. These can be simple declarative language processors, or full blown domain specific languages like "R" [10]. They can be used to define complex problems and organize the problem into something more easily solved, like a parse tree.

6.4.5 Query

Query Languages like SQL can go beyond transactional into the space of analytical queries either providing processing of data, or even computations such as "GROUP BY" and MIN and MAX in SQL [11].

The underlying model behind relational databases is the Relational Algebra [4]

6.4.6 Logic

Logic systems are basically rule systems like Prolog [9] They are used in mathematical and logic applications. Their solution finding approach can also be useful in solving difficult problems like cross-wiring network links for redundancy and expert systems.

6.4.7 Single Pass

Single pass approaches are significant when the data set is so large it cannot be contained in memory. These kinds of problems are becoming more important as the size of data in general skyrockets.

6.4.8 Multi-Pass

Sometimes huge gains can be made by making multiple passes. This is basically a variant on Dynamic Programming. Database Indexes. When data is queried the location can be found quickly in the index instead of a full table scan.

Sorting ahead of time is another example, making possible a Binary Search technique.

6.4.9 Pre-Compute

Pre-Computing unlike multi-pass where the complete problem set is traversed, is instead the compilation of tables that are expensive to compute.

In the early days of computing the computation of sine/cosine and other graphic operations were prohibitively expensive.

Since the answers were a small table pre-computing the equations greatly sped up programs. Bitmaps were even compiled to machine code for faster rendering.

6.4.10 Multi-Process

There is an entire field of programming dedicated to multi-process computing. It is based upon parallel computation which is currently in vogue, due to the large number of cores on CPU's and the use of massively parallel dedicated chips like video cards.

It's even possible to crack passwords, do machine learning, and mine crypto currencies on dedicated chips.

6.4.11 Dynamic Programming

Applied to recursion is (descent + memoization) recursively can be no cycles in the DAG of the recursion, or it will get into an infinite loop. It is fundamentally a brute force approach, good for computing min/max style answers.

6.4.12 Greedy Programming

Greedy algorithms, like the parser compiler packer function I wrote in my Emacs Parser Compiler used a greedy technique with push back to maximally fill functions with code [8].

6.4.13 Lazy Programming

When the computation may not be needed or when the problem cannot fit into memory it can be lazy loaded, or lazy computed.

6.4.14 Streams

Streams [2] are a finite sequence of discrete elements of the same type processed in a linear sequence of operations. They are produced by a generator function which allows a subset of the stream to be computed.

7 Data Structures

7.1 Array

Typed and indexed they are extremely fast with $O(1)$ read/write for any element. Insert is very slow as the array elements have to be copied to make room for each insertion. The equal cost of access to any element makes algorithms like binary search, and some sorting algorithms possible.

7.2 List

Single or Double Linked lists have efficient inserts but perform poorly in most cases.

Counting length or adding to end is $\theta(n)$

7.3 Trees

Good for storing hierarchal data and a natural fit for recursive algorithms, trees require only $\theta \log_n$ to find an element.

Performance is maintained only when the tree is balanced, re-balancing on insert can be an expensive operation.

7.4 Stack/LIFO

Last In First Out

Stacks are an excellent structure for back-tracking problems. They are LIFO, or Last In First Out. They can be used as a substitute for recursion, and generally for back-tracking.

7.5 QUEUE FIFO

First In First Out

Good for processing in chronological order. It can also be used for a breadth traversal of a tree.

7.6 Hashes

A bread and butter data structure used pervasively to look up non-integer keys in $\theta(1)$ complexity.

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