

Q Show $-\boxed{X}- = -\boxed{H}-\boxed{Z}-\boxed{H}-$
 $-\boxed{Z}- = -\boxed{H}-\boxed{X}-\boxed{H}-$

Ans:

$$HXH = \frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix} \begin{vmatrix} 0 & 1 \\ 1 & 0 \end{vmatrix} \frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix}$$

$$= \begin{vmatrix} 1 & 0 \\ 0 & -1 \end{vmatrix}$$

$$= Z$$

Given,

$$H = \frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix}$$

$$X = \begin{vmatrix} 0 & 1 \\ 1 & 0 \end{vmatrix}$$

$$HZH = \frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix} \begin{vmatrix} 1 & 0 \\ 0 & -1 \end{vmatrix} \frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix}$$

$$= \begin{vmatrix} 0 & 1 \\ 1 & 0 \end{vmatrix}$$

$$= X$$

proved