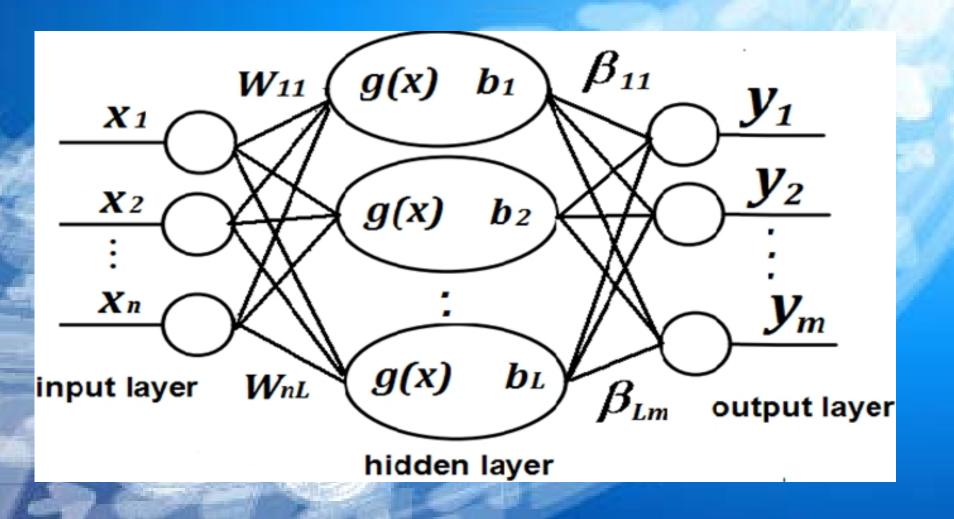




Artificial Neural Network



BP

$$E = \frac{1}{2}(d_i - y_i)^2$$

d_i desired outputy_i NN output

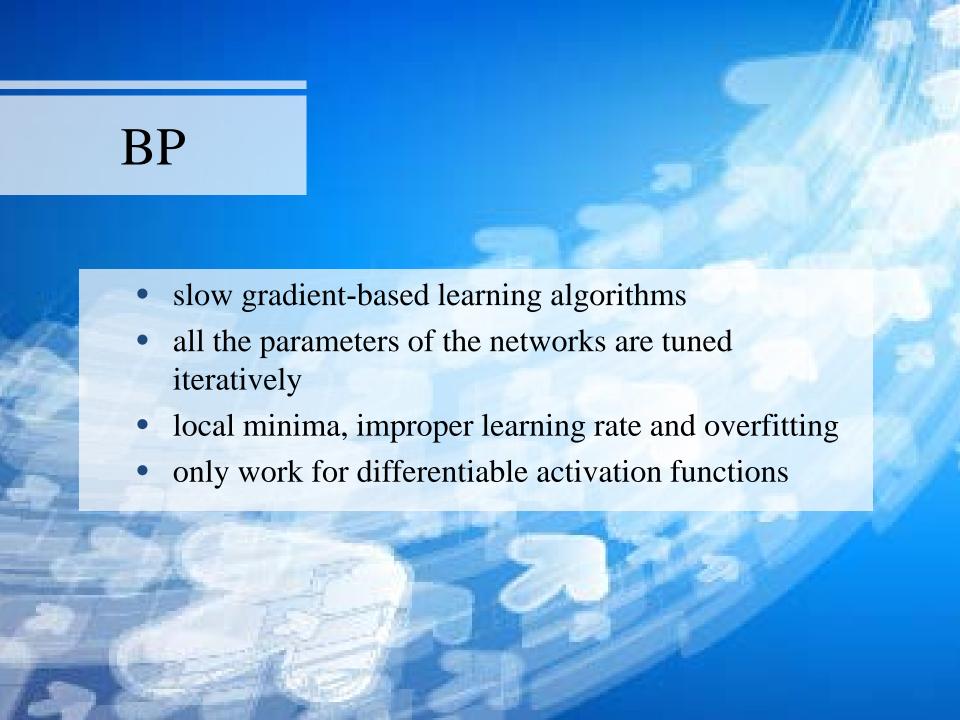
$$E = \frac{1}{2} [d_i - f(W_i^T X)]^2$$

$$\frac{\partial E}{\partial w_{ii}} = -(d_i - y_i) f'(W_i^T X) x_j$$
 j=1,2,...,n

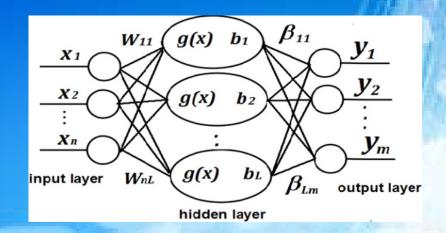
$$\Delta W_{i} = -\eta \frac{\partial E}{\partial w_{ij}}$$

$$\Delta W_i = \eta(d_i - y_i) f'(net_i) X$$

$$\Delta w_{ij} = \eta(d_i - y_i) f'(net_i) x_j$$



ELM



For Training Set: $(x_j, y_j), j = 1, 2, 3 \cdots N$

activation functions: $g(x) = \text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$

ELM Model is as follows

$$\sum_{i=1}^{L} \beta_i g_i(x_j) = \sum_{i=1}^{L} \beta_i g_i(w_i \bullet x_j + b_i) = y_j, j = 1, 2, 3, \dots N$$

input layer weight: W_i output layer weight: β_i

Number of the hidden layer nodes: L

$$\sum_{i=1}^{L} \beta_i g_i(x_j) = \sum_{i=1}^{L} \beta_i g_i(w_i \bullet x_j + b_i) = y_j, j = 1, 2, 3, \dots N$$

$$H\beta = Y$$

where
$$H(w_1, w_2, \dots, w_L; b_1, b_2, \dots, b_L; x_1, x_2, \dots, x_N) =$$

$$\begin{vmatrix} g(w_1x_1 + b_1) & g(w_2x_1 + b_2) & \cdots & g(w_Lx_1 + b_L) \\ g(w_1x_2 + b_1) & g(w_2x_2 + b_2) & \cdots & g(w_Lx_2 + b_L) \\ \vdots & \vdots & \ddots & \vdots \\ g(w_1x_N + b_1) & g(w_2x_N + b_2) & \cdots & g(w_Lx_N + b_L) \\ \beta = \begin{bmatrix} \beta_1^T, \beta_2^T, \dots, \beta_L^T \end{bmatrix}_{M \times L}^T \\ Y = \begin{bmatrix} y_1^T, y_2^T, \dots, y_N^T \end{bmatrix}_{M \times N}^T \end{vmatrix}$$

ELM

ELM Model: $H\beta = Y$

$$H(w_1, w_2, \dots, w_L; b_1, b_2, \dots, b_L; x_1, x_2, \dots, x_N)$$

If w and b are given <u>randomly</u>,

the output weights can be <u>analytically</u> determined, namely

$$\beta = H^{-1}Y \quad \blacksquare \quad \beta = H^{+}Y$$

The only one artificial setting is number of the hidden layer nodes, L

ELM

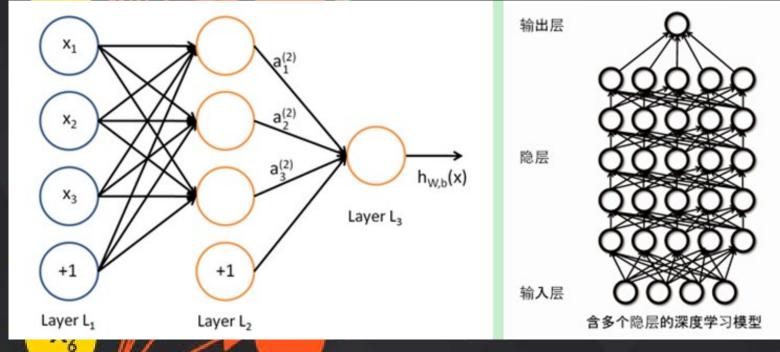
- ELM advantages
 - Batch training, extremely fast learning speed
 - better generalization performance
 - adopt the simplest method to overcome local minima, improper learning rate and overfitting
 - work for differentiable and nondifferentiable activation functions
 - mathematical foundation
- ELM disadvantages
 - The number of the hidden layer nodes is artificially given.
 - H is generally a non-square matrix

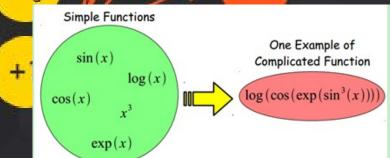


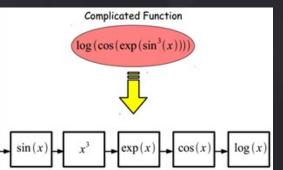


Hidden II

Outputs







Deep Learning Hidden I

Hidden II

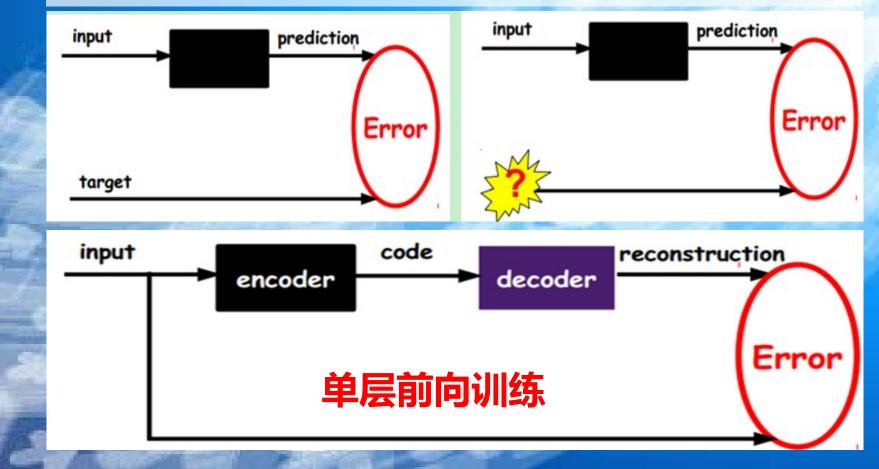
Outputs

BP算法存在的问题:

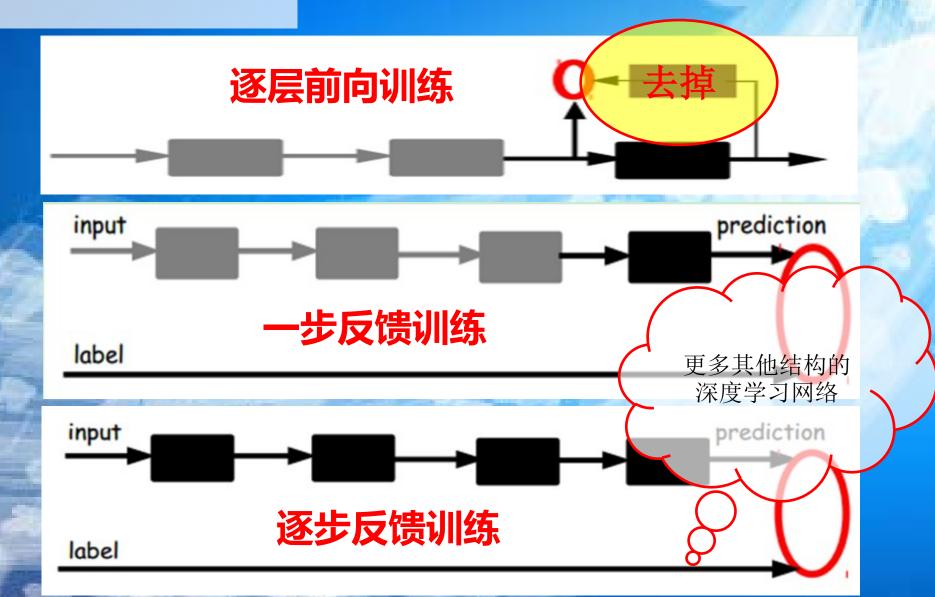
- (1) 梯度越来越稀疏: 从顶层越往下, 误差校正信号越来越小;
- (2) 收敛到局部最小值:尤其是从远离最优区域开始的时候
- (随机值初始化会导致这种情况的发生);
- (3)一般,我们只能用有标签的数据来训练:但大部分的数据
- 是没标签的,而大脑可以从没有标签的的数据中学习;

Auto Encoder

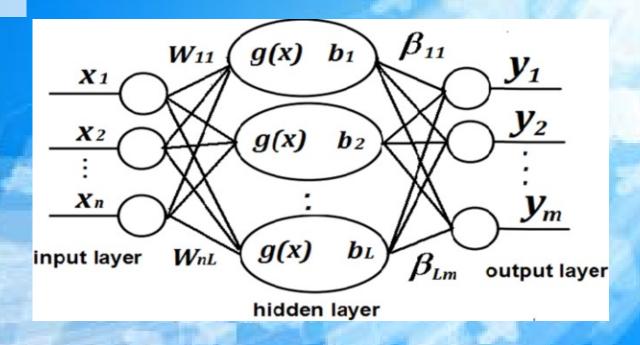
自动编码器就是一种尽可能复现输入信号的神经网络.



Auto Encoder



ELM-AE



- \blacksquare target output is the same as input x: x = y
- the hidden node parameters are made orthogonal after being randomly generated: $w_i^T w_i = I, b^T b = 1$

ELM-AE

$$\beta = H^{-1}Y$$

$$\beta = \left(\frac{1}{C} + H^T H\right)^{-1} H^T Y$$

$$X = Y$$

$$H\beta = X$$

$$\beta^T \beta = I \qquad H = X \beta^T$$

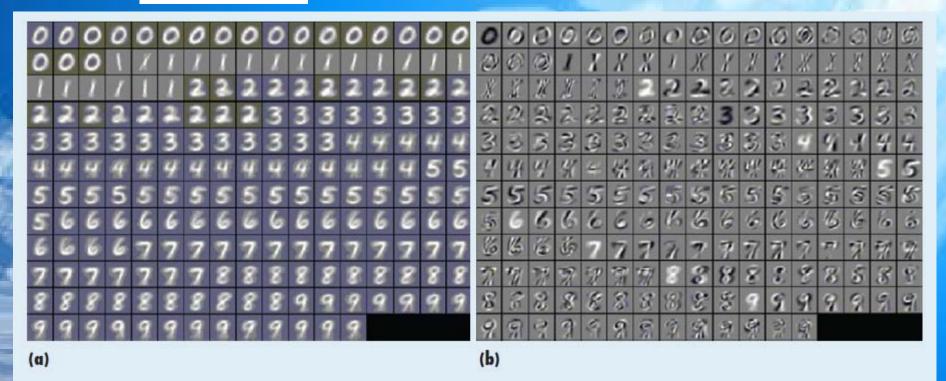
PCA

$$TP^T = X$$

Deep Learning

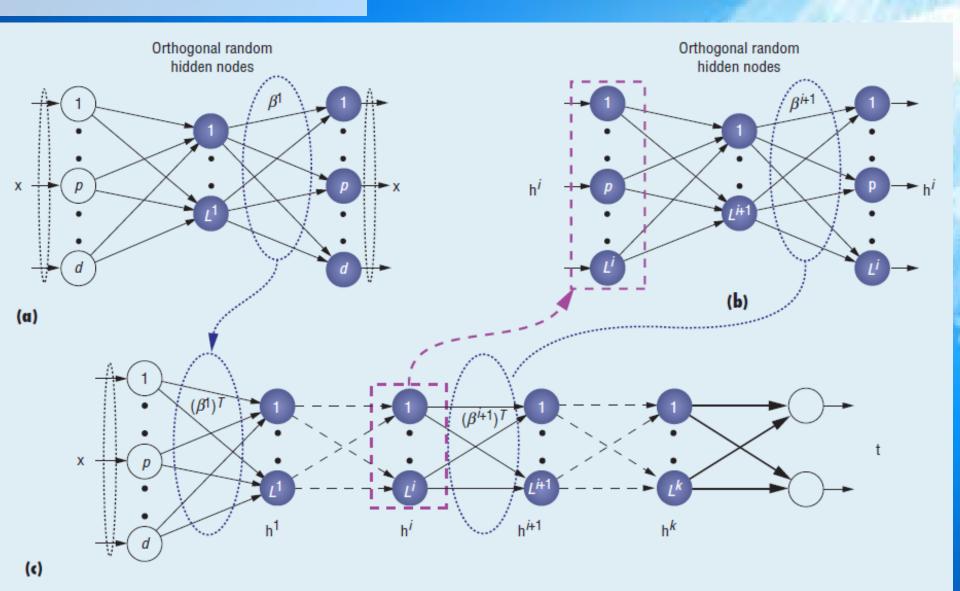
$$\beta = H^{-1}Y$$

PCA



 $784 \times 20 \times 784$

Deep Learning

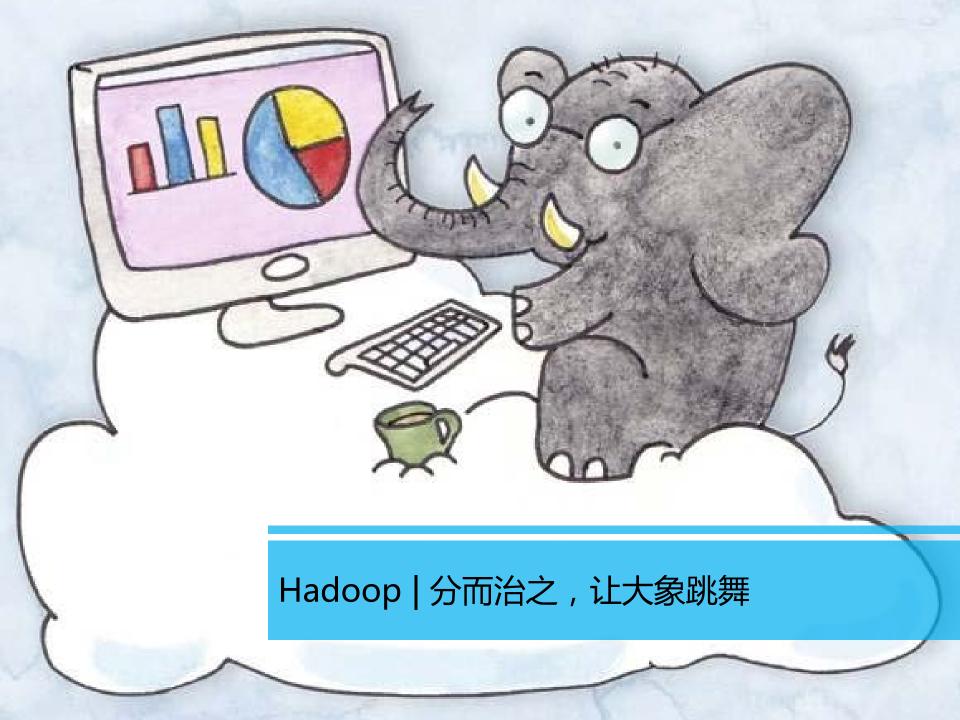


Deep Learning

Table 1. Performance comparison of ML-ELM with state-of-the-art deep networks.

Algorithms	Testing accuracy % (standard deviation %)	Training time
Multi-layer extreme learning machine (ML-ELM)	99.03 (±0.04)	444.655 s
Extreme learning machine (ELM random features)	97.39 (±0.1)	545.95 s
ELM (ELM Gaussian kernel); run on a faster machine	98.75	790.96 s
Deep belief network (DBN)	98.87	20,580 s
Deep Boltzmann machine (DBM)	99.05	68,246 s
Stacked auto-encoder (SAE)	98.6	_
Stacked eenoising auto-encoder (SDAE)	98.72	_







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