

Machine Learning Model For Sepsis Prediction

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I. Introduction

Sepsis is a life-threatening infection that develops from staying in the Intensive Care Units (ICU), which happens when the infection-fighting processes damage its own organs. During this COVID-19 pandemic, the ICUs needs to focuses on this problems more than ever, therefore, the need to monitor patients status regarding their infection possibility considerably increases. With that in mind, this notebook goal is to build a machine learning model that can predict the infection propability of a patient based on a provided dataset.

Many libraries are used in this notebook including analytical and visualizing libraries such as *numpy*, *pandas*, *matplotlib* and *seaborn* and scikit-learn machine learning models. Since our object is predicting the Sepsis result, the models I use are **binary classifiers**, certainly, *LogisticRegression*, *RandomForest*.

II. Exploratory Data Analysis (EDA)

1. Import Necessary Libraries

- In this notebook, multiple libraries are used to do exploratory data analysis and visualize data.

```
In [1]: #import libraries
import warnings
import warnings
warnings.filterwarnings("ignore")

#measure running time
from time import time

#for analytics and visualization
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns

#data processing and machine learning algorithms
from sklearn.preprocessing import MinMaxScaler, StandardScaler, PolynomialFeatures
from sklearn.compose import ColumnTransformer
from sklearn.model_selection import train_test_split, KFold, cross_val_score, GridSearchCV
from sklearn.ensemble import RandomForestClassifier
from sklearn.linear_model import LogisticRegression
from sklearn.metrics import f1_score, classification_report, plot_confusion_matrix
```

2. Load dataset

Load the csv file to do some analysis prior to training the model.

```
In [2]: #train set
patientsFrame_Train = pd.read_csv('Patients_Files_Train.csv')
#test set
patientsFrame_Test = pd.read_csv('Patients_Files_Test.csv')

s = patientsFrame_Train.shape
print('The data has %d rows and %d columns' % (s[0], s[1]))

patientsFrame_Train.head(10)
```

The data has 599 rows and 11 columns

```
Out[2]:
```

	ID	PRG	PL	PR	SK	TS	M11	BD2	Age	Insurance	Sepsis
0	ICU200010	1	148	72	35	0	33.6	0.627	50	0	Positive
1	ICU200011	8	85	66	29	0	26.6	0.351	31	0	Negative
2	ICU200012	8	183	64	0	0	23.3	0.672	32	1	Positive
3	ICU200013	1	89	66	23	94	28.1	0.167	21	1	Negative
4	ICU200014	0	137	40	35	168	43.1	2.288	33	1	Positive
5	ICU200015	5	116	74	0	0	25.6	0.201	30	1	Negative
6	ICU200016	3	78	50	32	88	31.0	0.248	26	0	Positive
7	ICU200017	10	115	0	0	0	35.3	0.134	29	1	Negative
8	ICU200018	2	197	70	45	543	30.5	0.158	53	1	Positive
9	ICU200019	8	125	96	0	0	0.0	0.232	54	1	Positive

- The data has 599 entries and 11 columns for 11 different features with the last one is the result of sepsis.

Check for null/ missing value in each columns using the **isnull()**.

```
In [3]: patientsFrame_Train.isnull().sum()
```

```
Out[3]:
```

ID	0
PRG	0
PL	0
PR	0
SK	0
TS	0
M11	0
BD2	0
Age	0
Insurance	0
Sepsis	0
dtype:	int64

- As we can see, there are no null value found in any columns. Next, we check through the **info()** the data types of each feature to see whether the missing value is recorded as another format.

```
In [4]: patientsFrame_Train.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 599 entries, 0 to 598
Data columns (total 11 columns):
#  Column  Non-Null Count  Dtype
---  --
0  ID      599 non-null    object
1  PRG     599 non-null    int64
2  PL      599 non-null    int64
3  PR      599 non-null    int64
4  SK      599 non-null    int64
5  TS      599 non-null    int64
6  M11     599 non-null    float64
7  BD2     599 non-null    float64
8  Age     599 non-null    int64
9  Insurance 599 non-null    int64
10 Sepsis  599 non-null    object
dtypes: float64(2), int64(7), object(2)
memory usage: 51.6+ KB
```

- With these simple examination through the dataset, there are no missing values and we can assume that the data set is cleaned and we can proceed to do the analytics.

Drop column ID and Insurance as they are unnecessary for the analysis.

```
In [5]: patientsFrame_Train = patientsFrame_Train.drop(columns=['ID', 'Insurance'])
patientsFrame_Test = patientsFrame_Test.drop(columns=['ID', 'Insurance'])
```

We can see that Sepsis value is binary (positive and negative), hence, for convenience upon further analysis, we convert Sepsis value to 0 for 'negative' and 1 for 'positive'

```
In [6]: seps = {'Negative': 0, 'Positive': 1}
patientsFrame_Train['Sepsis'] = patientsFrame_Train['Sepsis'].map(seps)
#check the dataframe again
patientsFrame_Train.head()
```

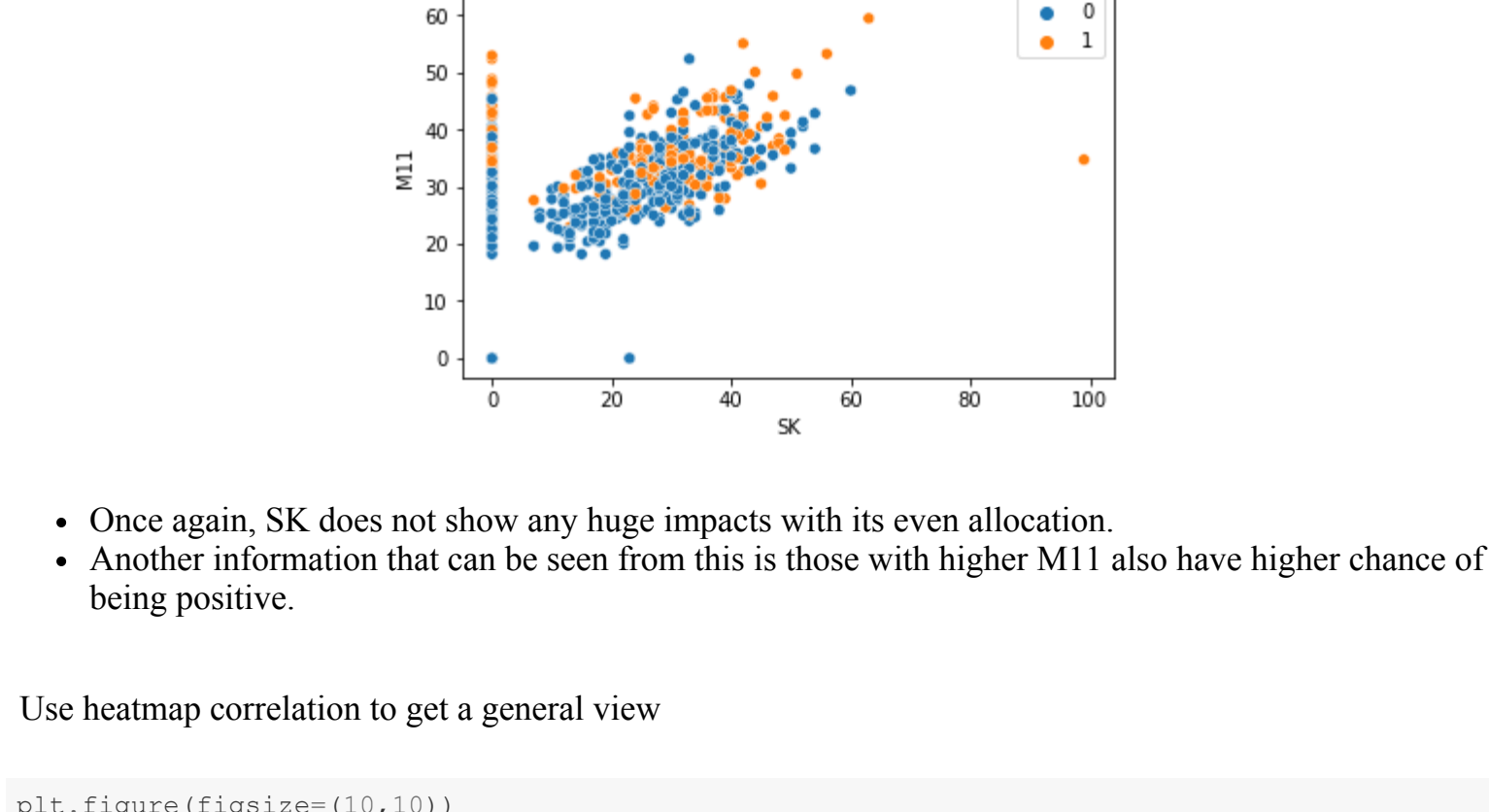
```
Out[6]:
```

	PRG	PL	PR	SK	TS	M11	BD2	Age	Sepsis
0	1	148	72	35	0	33.6	0.627	50	1
1	8	85	66	29	0	26.6	0.351	31	0
2	8	183	64	0	0	23.3	0.672	32	1
3	1	89	66	23	94	28.1	0.167	21	0
4	0	137	40	35	168	43.1	2.288	33	1

3. Plotting and Analysing

Start with plotting the histogram of every features to examine their distribution.

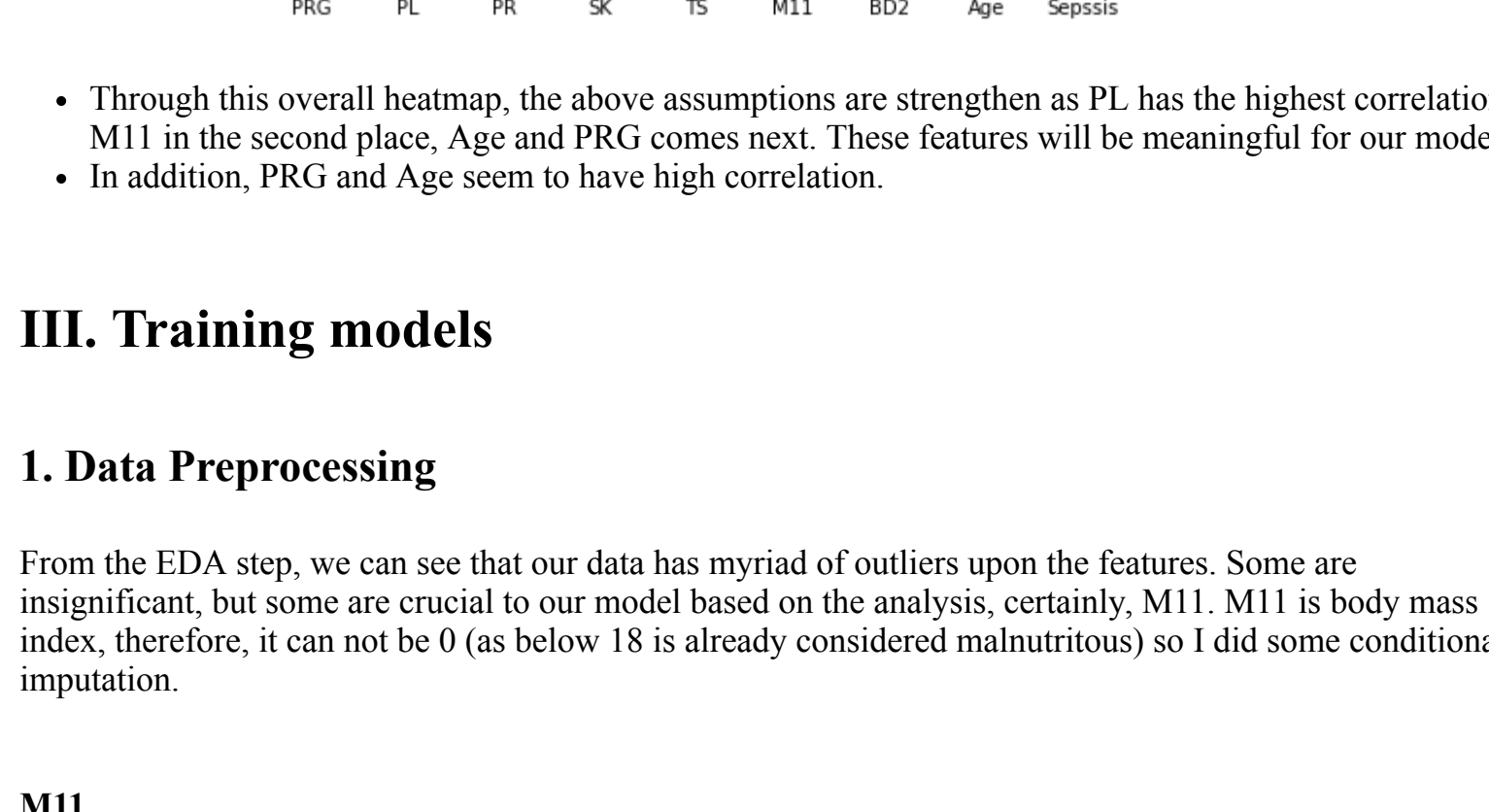
```
In [7]: #create a dataframe that dropped Sepsis
patientsFrame_dropSep = patientsFrame_Train.drop(columns=['Sepsis'])
plt.figure(figsize = (20,20))
for i, col in enumerate(patientsFrame_dropSep.columns):
    plt.subplot(4,3,i+1)
    plt.hist(patientsFrame_dropSep[col], alpha =0.5, color = 'b', density =True)
    plt.title(col)
    plt.style['mathticks']='vertical')
```



- Gaussian Distribution:** PL, PR, M11
- From observation, there seems to be outliers in PL, PR, and M11. These will be put into consideration.

Now, I use boxplots on the features with the division of Sepsis results to see the correlation between the caught rate and other attributes.

```
In [8]: plt.figure(figsize = (20,20))
for i, col in enumerate(patientsFrame_Train.columns):
    plt.subplot(4,3,i+1)
    sns.boxplot(data=patientsFrame_Train, x='Sepsis', y=patientsFrame_Train[col])
    plt.title(col)
```



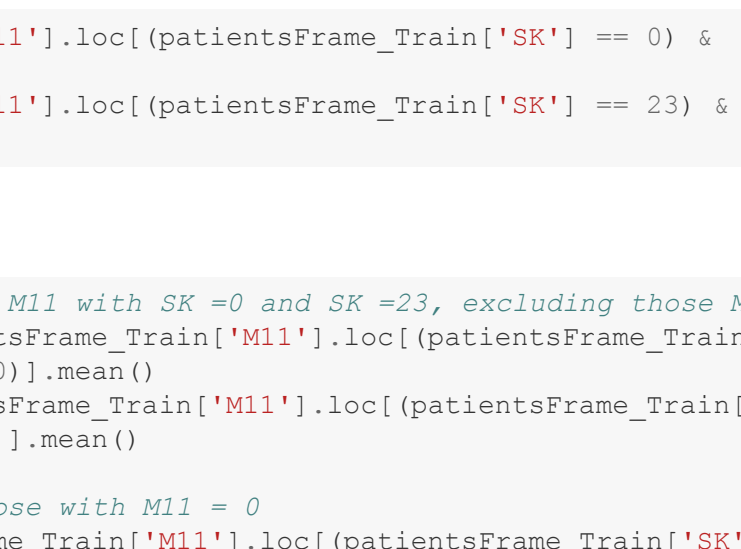
As shown in the graph, firstly, there are many outliers upon every divided features. These outliers are just outliers of the data as plotting out with two groups. However, there are some points that are considerable:

- For **SK**, the outliers are minor, which do not significantly affect our prediction later on. Moreover, the distribution of **negative** and **positive** results are equivalent, we can assume that **SK** feature is **not so important**.
- In **PL, PR and M11**, by comparing with the previous histogram, the under outliers may not have substantial impact on the prediction results as they are evenly scattered upon both groups.
- On the other hand, also from observation, PL and PRG are the most correlated features.

More visualization to examine more insight.

```
In [9]: age_group = pd.cut(patientsFrame_Train.Age, bins=[0,10,20,30,40,50,60,70,80],
                        labels = ['0-10','10-20','20-30','30-40','40-50','50-60','60-70','70-80'])
sns.countplot(patientsFrame_Train.Age, color = 'black')
sns.countplot(age_group(patientsFrame_Train.Sepsis == 0), color = 'b')
```

```
Out[9]: <AxesSubplot: xlabel='Age', ylabel='count'>
```



```
In [10]: sns.scatterplot(data=patientsFrame_Train, x='PL', y='Age', hue='Sepsis')
```

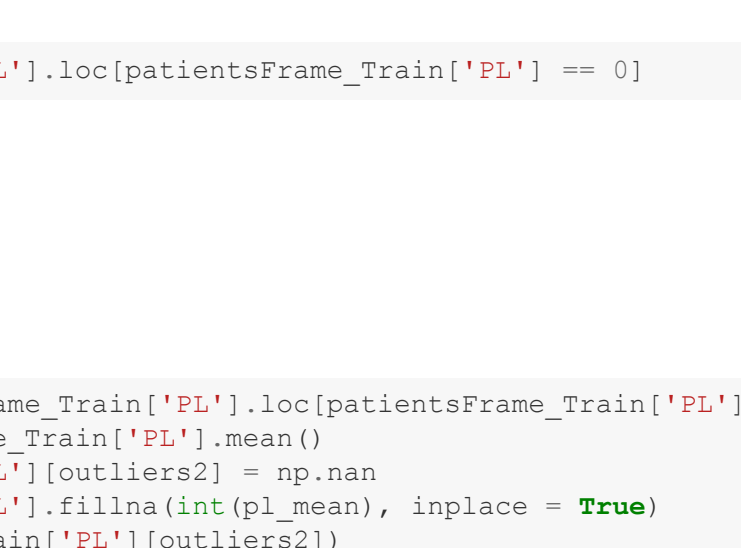
```
Out[10]: <AxesSubplot: xlabel='PL', ylabel='Age'>
```



- From the two above graphs, older patients have higher rate of getting the disease but this only happens in groups, that means in a group of older people, the positive percentage is higher compared to younger groups. Additionally, the higher the PL value is the more chance that patient is positive.

```
In [11]: sns.scatterplot(data=patientsFrame_Train, x='SK', y='M11', hue='Sepsis')
```

```
Out[11]: <AxesSubplot: xlabel='SK', ylabel='M11'>
```



- Once again, SK does not show any huge impacts with its even allocation.
- Another information that can be seen from this is those with higher M11 also have higher chance of being positive.

Use heatmap correlation to get a general view

```
In [12]: plt.figure(figsize=(10,10))
plt.title('Correlation of Features')
sns.heatmap(patientsFrame_Train.corr(), cbar=True, annot=True, cmap='Reds')
```

```
Out[12]: <AxesSubplot:title='center': 'Correlation of Features'>
```



- Through this overall heatmap, the above assumptions are strengthen as PL has the highest correlation, M11 in the second place, Age and PRG comes next. These features will be meaningful for our model.
- In addition, PRG and Age seem to have high correlation.

III. Training models

1. Data Preprocessing

From the EDA step, we can see that our data has myriad of outliers upon the features. Some are insignificant, but some are crucial to our model based on the analysis, certainly, M11. M11 is body mass index, therefore, it can not be 0 (as below 18 is already considered malnourished) so I did some conditional imputation.

M11

```
In [13]: patientsFrame_Train['M11'].describe()
```

```
count      599.000000
mean       31.920033
std        8.008227
min        0.000000
25%       27.100000
50%       32.000000
75%       36.550000
max        67.100000
Name: M11, dtype: float64
```

From the heatmap from EDA process, we can see that **M11** is highly correlate to **SK**, so I will examine the SK value of those outliers.

```
In [14]: patientsFrame_Train[['M11', 'SK']].loc[patientsFrame_Train['M11'] == 0]
```

```
Out[14]:
```

	M11	SK
9	0.0	0
49	0.0	0
60	0.0	0
81	0.0	0
145	0.0	23
371	0.0	23
426	0.0	0
494	0.0	0
522	0.0	0

Most of the outliers has the SK values of 0 and some is 23. Therefore, I will impute those with the average M11 that has SK equal to 0, the same for 23. The technique that is used is initially replace the outliers with *nan* and use *fillna* to fill those spots with the calculated value.

```
In [15]: patientsFrame_Train['M11'].loc[(patientsFrame_Train['SK'] == 0) & (patientsFrame_Train['M11'] != 0)].mean()
```

```
Out[15]: 31.686666666666664
```

```
In [16]: #calculate the mean of M11 with SK =0 and SK =23, excluding those M11 = 0
m11_mean_sk23 = patientsFrame_Train['M11'].loc[(patientsFrame_Train['SK'] == 23) & (patientsFrame_Train['M11'] != 0)].mean()
m11_mean_sk0 = patientsFrame_Train['M11'].loc[(patientsFrame_Train['SK'] == 0) & (patientsFrame_Train['M11'] != 0)].mean()
```

```
#get the indices of those with M11 = 0
outliers = patientsFrame_Train['M11'].loc[(patientsFrame_Train['SK'] == 0) & (patientsFrame_Train['M11'] == 0)].index
outliers1 = patientsFrame_Train['M11'].loc[(patientsFrame_Train['SK'] == 23) & (patientsFrame_Train['M11'] == 0)].index

#impute
print(patientsFrame_Train['M11'][outliers])
print(patientsFrame_Train['M11'][outliers1])
patientsFrame_Train['M11'].loc[outliers] = np.nan
patientsFrame_Train['M11'].fillna(round(m11_mean_sk0, 2), inplace = True)
print(patientsFrame_Train['M11'].loc[outliers])
print(patientsFrame_Train['M11'].loc[outliers1])
print(patientsFrame_Train['M11'].loc[outliers])
print(patientsFrame_Train['M11'].loc[outliers1])
```

```
9      0.0
49     0.0
60     0.0
81     0.0
426    0.0
494    0.0
522    0.0
Name: M11, dtype: float64
145    31.69
371    0.0
Name: M11, dtype: float64
49      31.59
60      31.59
81      31.59
426    31.59
494    31.59
522    31.59
Name: M11, dtype: float64
145    31.69
371    31.69
Name: M11, dtype: float64
```

PL

Although, as analysed above, the Sepsis result distribution in PL outliers are even, but they are still outliers and PL is a significant figure, it is a good idea to handle the outliers carefully so that the values are sufficiently standardized to train.

Imply the same technique to PL, the general mean is decent enough for this case as the Sepsis status of these outliers are balanced.

The value that is imputed to the outliers must be integer following the initial format of the dataset.

```
In [17]: patientsFrame_Train['PL'].describe()
```

```
Out[17]:
```

count	599.000000
mean	120.153589
std	32.682364
min	0.000000
25%	99.000000
50%	116.000000
75%	140.000000
max	198.000000
Name: PL, dtype: float64	

```
In [18]: patientsFrame_Train['PL'].loc[patientsFrame_Train['PL'] == 0]
```

```
Out[18]:
```

75	0
182	0
342	0
349	0
Name: PL, dtype: int64	

```
In [19]: outliers2 = patientsFrame_Train['PL'].loc[patientsFrame_Train['PL'] == 0].index
pl_mean_sk23 = patientsFrame_Train['PL'].loc[(patientsFrame_Train['SK'] == 23) & (patientsFrame_Train['PL'] != 0)].mean()
outliers1 = patientsFrame_Train['PL'].loc[(patientsFrame_Train['SK'] == 23) & (patientsFrame_Train['PL'] == 0)].index
patientsFrame_Train['PL'].fillna(int(pl_mean), inplace = True)
print(patientsFrame_Train['PL'][outliers2])
```

```
75      120.0
182     120.0
342     120.0
349     120.0
502     120.0
Name: PL, dtype: float64
```

Set Up Training And Testing Data

In this notebook, I will use both univariate model and multivariate model so I will set up the data frame for both models. The picked split ratio is 7:3, this feeds more data to train the model which results in better accuracy.

Dependent Variable

```
In [20]: patientsFrame_Train_Y = patientsFrame_Train['Sepsis']
```

Univariate Model

Undoubtedly, the independent variable is **PL** with the highest correlation with our prediction target.

```
In [21]: patientsFrame_Test_X_U = patientsFrame_Test[['PL']]
patientsFrame_Train_X_U = patientsFrame_Train[['PL']]

train_X_U, val_X_U, train_Y_U, val_Y_U = train_test_split(patientsFrame_Train_X_U, patientsFrame_Train_Y, test_size=0.3, shuffle=True)
#examine the split
print(train_X_U.shape)
print(val_X_U.shape)
print(train_Y_U.shape)
print(val_Y_U.shape)
```

```
(479, 1)
(120, 1)
(479, 1)
(120, 1)
```

Feature Selection For Multivariate Model

With the EDA process output, the dataframe that is put into model will have selective features, so that the model will be less resources-consuming, more efficient regarding accuracy and more comprehensible. In this case, I only keep **PL**, **M11**, **Age** and **PRG**.

```
In [22]: patientsFrame_Train_X_M = patientsFrame_Train[['PL', 'M11', 'Age', 'PRG']]
patientsFrame_Test_X_M = patientsFrame_Test[['PL', 'M11', 'Age', 'PRG']]
train_X_M, val_X_M, train_Y_M, val_Y_M = train_test_split(patientsFrame_Train_X_M, patientsFrame_Train_Y, test_size=0.3, shuffle=True)
#examine the split
print(train_X_M.shape)
print(val_X_M.shape)
print(train_Y_M.shape)
print(val_Y_M.shape)
```

```
(419, 4)
(180, 4)
(419, 4)
(180, 4)
```

Regarding the value distribution and range of the selected features of the processing data, the difference between features's range is significant and with the inclusion of later-used technique (Polynomial Features), it is necessary to perform data scaling. Moreover, this action can save computational resources and enhance accuracy due to the facts that LogisticRegression is sensitive to the range of data points.

In this notebook, both Logistic Regression and tree-based algorithms are used. The scaling step is helpful for the performance of LogisticRegression but is not effective for the tree-based. Furthermore, for classification tasks, the results of tree-based algorithms is class selected, no calculation involved, consequently, data scaling does not affect the output of tree-based classifier.

Throughout the 4 features we selected, there are two that have Gaussian Distribution and the other two are skewed. Thus, I will mix the scaling techniques to suit the distribution of each. **Normalization** to the skewed features and **Standardization** to the normal distribution.


```
In [23]: #Scale the features using ColumnTransformer, conditionally transform the data
scaler = ColumnTransformer([('standard', StandardScaler()), ('PL', 'ML', 'I'), ('norm', MinMaxScaler()), ('Age', 'FRG')])

#Fit the data with the scaler
print(trainX_M)
print(valX_M)

scaler.fit(trainX_M)
trainX_M = scaler.transform(trainX_M)
valX_M = scaler.transform(valX_M)

print(trainX_M)
print(valX_M)

PL    M11    Age    PRG
156  99.0  24.6    21    2
179  120.0 39.1    37    1
380  107.0 30.8    24    1
16  118.0 45.8    31    0
304 150.0 21.0    37    3
...
161 102.0 37.2    45    7
7  115.0 35.3    29    10
206 180.0 36.5    35    0
108  83.0 34.3    25    3
389 100.0 31.6    28    3

[419 rows x 4 columns]

PL    M11    Age    PRG
582 121.0 26.5    62    12
99  122.0 49.7    31    1
65  99.0 29.0    32    5
381 105.0 20.0    22    0
43  171.0 45.4    54    9
...
476 105.0 33.7    29    2
583 100.0 38.7    42    8
328 102.0 45.5    31    2
253  86.0 35.8    25    0
28  145.0 22.2    57    13

[180 rows x 4 columns]

[[0.71722982 -1.10374295  0.         0.         0.16764706]
 [0.13785848  0.58806021  0.26666667  0.66666667  0.29417651]
 [-0.45284951 -0.1763504  0.         0.         0.05882353]
 ...
 [1.95860429  0.59701256  0.23333333  0.         0.         ]
 [-1.24578965  0.28288717  0.06666667  0.17647059  0.         ]
 [-0.68419483 -0.10329853  0.16666667  0.16666667  0.17647059]
 [[ 0.00953994 -0.83219375  0.68333333  0.70588235]
 [ 0.04257493  2.4035649  0.66666667  0.05882353]
 [ 0.71722982 -0.4749217  0.18333333  0.29417651]
 [-0.51901989 -1.76117785  0.01666667  0.         0.         ]
 [ 1.61218939  1.86900618  0.55         0.52941761]
 [-1.21275466 -1.02577446  0.66666667  0.35294181]
 [-1.11364969 -1.30833183  0.18333333  0.35294181]
 [-1.31185963 -0.6608899  0.06666667  0.17647059]
 [-0.28777496 -0.10329853  0.06666667  0.17647059]
 [-0.55205488 -1.98985086  0.1         0.         0.         ]
 [ 0.7363097  1.81183793  0.43333333  0.29417651]
 [ 2.52019911 -0.1794613  0.06666667  0.17647059]
 [ 0.38508887 -1.18949533  0.2         0.23529412]
 [-0.91543976  1.58316492  0.23333333  0.         0.         ]
 [-1.54310455 -0.10472774  0.01666667  0.17647059]
 [ 0.7172936  -0.9840644  0.16666667  0.05882353]
 [-1.21275466  0.49696812  0.         0.         0.         ]
 [-1.04757971 -0.60352074  0.         0.05882353]
 [ 2.52019911  0.28288717  0.33333333  0.         0.         ]
 [-0.45294991  0.61130463  0.06666667  0.         0.         ]
 [ 1.72735937  0.86856176  0.06666667  0.17647059]
 [-0.72777496  0.11418284  0.05         0.17647059]
 [-1.1364969  0.49705702  0.01666667  0.05882353]
 [-0.84936978 -0.889362  0.01666667  0.17647059]
 [-0.12260002  0.25400305  0.28333333  0.29417651]
 [-1.0460936  0.60820523  0.33333333  0.52941761]
 [-1.0806147  -1.13232708  0.15         0.29417651]
 [ 0.1086449  -0.51776836  0.01666667  0.47058824]
 [ 0.42259192  0.78930961  0.01666667  0.17647059]
 [ 1.13272957 -0.81790169  0.1         0.17647059]
 [-1.3729296  -0.04613028  0.01666667  0.05882353]
 [ 0.60416974 -0.52026042  0.08333333  0.29417651]
 [-1.1364969  0.49280388  0.01666667  0.17647059]
 [-0.61812486  0.48267606  0.01666667  0.05882353]
 [-0.91543976 -1.40387628  0.01666667  0.05882353]
 [-0.28777496 -0.10329853  0.06666667  0.17647059]
 [ 0.7363097  1.44024429  0.01666667  0.05882353]
 [ 0.76203972 -0.67498106  0.31666667  0.35294181]
 [ 2.58053004  0.45491903  0.06666667  0.05882353]
 [ 2.18984922  0.76851732  0.33333333  0.41176471]
 [ 1.23183453 -0.10329853  0.75         0.17647059]
 [ 2.52019911  0.28288717  0.33333333  0.41176471]
 [-0.88240477 -0.10472774  0.06666667  0.         0.         ]
 [-1.0806147  -0.3462636  0.03333333  0.05882353]
 [-1.46220959 -0.17047059  0.01666667  0.05882353]
 [ 0.57113475  0.12537448  0.33333333  0.64705882]
 [ 2.52019911  0.33975543  0.68333333  0.17647059]
 [ 0.24018488  1.07973487  0.05         0.17647059]
 [ 0.7172936  -0.9840644  0.01666667  0.05882353]
 [-0.68419483 -0.04613028  0.35         0.05882353]
 [ 0.14167989 -0.48918423  0.4         0.35294181]
 [ 0.8541466  0.79710145  0.16666667  0.         0.         ]
 [-0.68419483 -0.21763504  0.         0.         0.         ]
 [ 0.40595981  0.06820623  0.4         0.05882353]
 [-0.94847475 -1.75196992  0.16666667  0.35294181]
 [ 1.31185963 -0.68927312  0.01666667  0.17647059]
 [-1.17971967 -0.64639693  0.16666667  0.23529412]
 [ 1.82046434  0.1968348  0.01666667  0.07588241]
 [ 0.69314469  0.48280388  0.06666667  0.17647059]
 [ 1.9255693  0.39692368  0.26666667  0.88235291]
 [-0.98130974  1.082894271  0.06666667  0.         0.         ]
 [ 2.53231941  1.28303159  0.16666667  0.         0.         ]
 [-0.05653004  0.36833955  0.03333333  0.         0.         ]
 [ 0.76203972 -0.67498106  0.31666667  0.35294181]
 [ 2.58053004  0.45491903  0.06666667  0.05882353]
 [ 2.18984922  0.76851732  0.33333333  0.41176471]
 [ 1.23183453 -0.10329853  0.75         0.17647059]
 [ 2.52019911  0.33975543  0.68333333  0.17647059]
 [ 0.24018488  1.07973487  0.05         0.17647059]
 [ 0.7172936  -0.9840644  0.01666667  0.05882353]
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