

- Questions are printed on BOTH sides (total 15 questions). Symbols have their usual meanings.
- Answers should be CLEAR, CONCISE AND LEGIBLE. Specify your assumptions clearly.
- YOUR ANSWERS MUST BE JUSTIFIED. Simply writing yes/ no will not fetch you any marks.
- All parts of a question must be answered together and in the same sequence as given in question paper. ELSE QUESTION SHALL NOT BE EVALUATED.
- NO MARKS will be awarded for plots without proper labeling of axes.

Q1. The sequence $\{0, -\sqrt{2}, -2, 0, \sqrt{2}, 2, \sqrt{2}\}$ represents a periodic sinusoidal sequence $x[n] = A \sin(\omega_0 n + \phi)$. Determine the values of the parameters A and ω_0 . [1]

Q2. Determine and justify whether the following system is linear and time-invariant or not?

$$y(t) = \int_{-\infty}^{2t} x(\tau) d\tau \quad [1]$$

Q3. The non-zero Fourier series coefficients in exponential form of a continuous-time periodic signal $f(t)$ with fundamental time period $T = 8$, are expressed as, $F_1 = F^*_{-1} = 2$; $F_3 = F^*_{-3} = 4j$. Determine the signal $f(t)$ in its sinusoidal form. [2]

Q4. For an LCR circuit the transfer function is, $H(s) = \frac{RCs}{LCs^2 + RCs + 1}$, with the following component values

as, $R = 10\Omega$, $C = 10\mu F$ and $L = 10mH$. Determine what kind of filter this LCR circuit encompasses, by sketching the pole-zero positions in the complex frequency plane. [3]

Q5. Transfer function of a first order low pass filter (LPF) with 3dB cutoff frequency f_c , is given by,

$H(f) = \frac{1}{1 + j(f/f_c)}$. This LPF is used as an anti-aliasing filter, when an analog signal $x(t)$ is sampled at a rate f_s . What is the minimum value for f_s , if the amplitude response to the aliased component at the edge of the pass band i.e. $f_s - f_c$, is to be at least 30dB below the amplitude response at f_c ? [3]

Q6. Realize the following system transfer function into cascade and parallel forms. [3]

$$H(s) = \frac{s(s+2)}{(s+1)(s+3)(s+4)}$$

Q7. A signal has Laplace transform of the form

$$X(s) = \frac{s+1}{s^2 + 3s + 4}$$

Find the Laplace transform $Y(s)$ of the following signals using Laplace transform properties only.

- (a) $y(t) = e^{-2t} x(t)$
- (b) $y(t) = x(t) * x(t)$

Q8. Determine whether the following system is linear or non linear.

$$y[n] = n^2 x[n-1]$$

Q9. What is the importance of impulse response? Does the impulse response of a nonlinear characterize the system? Determine whether the following system is causal or non causal.

$$y(t) = x(t) \cos(t+1)$$

Q10. Find the Nyquist rate & the Nyquist interval for the following signal.

$$x(t) = -10 \sin(40\pi t) \cos(300\pi t)$$

Q11. State Parseval's theorem for energy signals. When the z-transform & discrete-time Fourier transform same?

Q12. Sketch the following signals & determine whether they are energy signals or power signals.

Calculate the respective energy or power values. (a) $u(t) - u(t-3)$ (b) $\left(2 + e^{-6t}\right)u(t)$

Q13. Consider a sinusoidal signal $x(t) = \cos 15t$

(a) Find the expression for the sampling interval (T_s) such that $x[n] = x(nT_s)$ is periodic.

(b) Find the fundamental period for $x[n]$ if the folding frequency for sampling is $5/\pi$ Hz. Comment on the periodicity of $x[n]$.

Q14. Consider a sequence $x[n] = \sum_{k=-\infty}^{\infty} \delta[n-4k]$. (a) Sketch $x[n]$. (b) Find the Fourier series coefficient for $x[n]$.

Q15. Let $x(t)$ be a real valued band limited signal. If it is sampled at a rate T_s , then find the Fourier transform of the sampled signal.