

Birla Institute of Technology and Science, Pilani

Semester-I, 2013-14

Comprehensive Examination (Close Book)

Course No. : EEE C371 (Electro Mechanical Energy Conversion)

Date: 11-12-2013

Max. Time - 180 Min.

Marks -120

Name

ID. No.

Instructions: Question Paper is in 2-Parts **A & B**. Part **A**, has to be answered in Question paper itself.

PART – A

Marks – 4x10 = 40

Max. Time - 60 Min.

- Q.1.** A 50 hp, 3-phase, star connected Induction motor operates at an efficiency of 85% and 0.8 lagging power factor when connected to 3-phase, 500V mains. The per phase current and reactive power drawn by the motor is _____ and _____ respectively.
- Q.2.** A 200/100 V, 50 Hz, single phase transformer has primary leakage impedance $0.15 + j 0.76 \Omega$ and secondary leakage impedance $0.04 + j 0.19 \Omega$. The transformer supplies a load of impedance $3.92 + j 2.62 \Omega$. The voltage regulation and efficiency of the transformer, if the primary is supplied at rated voltage are _____ and _____ respectively.
- Q.3.** Two single-phase transformers operate in parallel to supply a load of $44 + j 18.6 \Omega$. The transformer-A has a secondary emf. of 400 V on open circuit with an internal impedance of $1.8 + j 5.6 \Omega$ referred to the secondary. The corresponding figures for transformer-B are 410 V and $1.8 + j 7.4 \Omega$. The current supplied by each transformer is _____ and _____ respectively.
- Q.4.** A 20 hp, 60 Hz, three phase induction motor has a rated speed of 1723 rpm. If the friction and windage losses amount to 5% of the output power. The rotor copper losses and air gap power is _____ and _____ respectively.
- Q.5.** The supply connected to the stator of a three phase induction motor feeds 29kW at 50 Hz, of which 25kW is transferred to the rotor, the rotor copper loss amounts to 2.9kW, and 21kW is obtained as output power. The stator iron loss for this machine can be assumed to remain constant at 1.3kW. The frequency of the rotor circuit and motor slip is _____ and _____ respectively.

- Q.6.** A 200V, 7.5 kW, separately excited dc motor has an armature resistance of $0.25\ \Omega$ and a field resistance of $200\ \Omega$. The machine runs at 1800 rpm to supply full load at 90 % efficiency. The no load current and speed is _____ and _____ respectively.
- Q.7.** A 115 V, 4-pole, 60 Hz, single phase Induction Motor is rotating clockwise at a speed of 1710 rpm. Its perunit slip in forward and back word direction is _____ and _____ respectively.
- Q.8.** A 6.6 kV, 50Hz star connected 3 phase synchronous generator, having a per-phase synchronous reactance of $9.5\ \Omega$, operates on 6.6kV infinite bus bars with the field current set to produce excitation emf. of 1.1 pu. The maximum power that this generator can feed to the bus bars, and the power factor at which it will do so are _____ and _____ respectively.
- Q.9.** A 3-phase, star connected alternator rated for 230V operation, the per phase resistance and synchronous reactance are $0.15\ \Omega$ and $9\ \Omega$, respectively. The excitation emf, and load angle for the alternator when alternator is delivering 9 A at UPF are _____ and _____ respectively.
- Q.10.** A 3-phase star connected alternator has 81 slots, 6-poles, and a double layer winding having a coil span of 13 slots. The breadth and pitch factor for the fundamental component of voltage are _____ and _____ respectively.

Instruction: Attempt all the parts of a question in sequence.
Solution must be neat and clean, showing all major steps for full credit.

Q.1. a. Show that kVA rating of an Auto-transformer is greater than a two winding transformer when it is configured as an Auto-transformer. Also discuss the advantages & disadvantages of an Auto-transformer.

Q.1.b. For a 6600/384V, 200kVA, single phase transformer, the efficiency at half and full load is 98% when operating at upf. The no load pf is 0.2 lagging, and the full load voltage regulation at 0.8 lagging pf is 4%. Draw the approximate equivalent circuit referred to low voltage side and insert all the impedance value.

[10+10]

Q.2. a. Show that in a 3-phase Induction Motor, torque at any slip is (assume stator impedance is zero)

$$T = 2 T_{\text{Max}} / (S / S_{\text{Max}} + S_{\text{Max}} / S)$$

Q.2.b. Explain with the help of two field reaction theory that the starting torque of Single phase Induction Motor is zero.

The 3-phase squirrel cage Induction Motor, with negligible core and mechanical losses and magnetizing current under all operating conditions is fed from a variable voltage & variable frequency source. If the motor is always made to operate at the same slip, how does the efficiency vary with operating condition? Justify with the relevance derivation only.

[10+15]

Q.3.a. A 2.3kV, 3-phase synchronous motor, driving a pump, is provided with an arrangement to vary the field excitation. Neglecting the losses, what is the power delivered to the pump when the excitation is set corresponding to a minimum AC line current of 8.8 A? What will be the current drawn and reactive power supplied by the motor system, if the excitation is set so as to make the motor power factor 0.8 leading.

Q.3.b. Explain significance of term SCR (Short Circuit Ratio).

A 2 MVA, 50 Hz, 3-phase, 3.3 kV star connected synchronous generator has a per phase synchronous impedance of $j5.5 \Omega$. Under normal operating conditions, the generator delivers 1.5MW at lagging power factor of 0.8 to infinite bus bars at rated voltage. Keeping the excitation constant, find the current and power factor at the stability limit for the machine.

Q.3.c. A 240 V DC series motor has an armature + field resistance of 0.2Ω . When operating at 1800 rpm, the motor takes a current of 40A. Find the external resistance to be added in series so as to limit the current at 10 A when operating at 3600 rpm. Assume the mechanical losses to be negligible, the field flux to be proportionate to current when operating in the 10-40 A range.

[10+15+10]

GOOD LUCK

Mid- Sem Test Solution- EEE C371_2013

Sol.1- Given Transf. 16.67 kVA , 7200/120V; approximate equivalent ckt. referred to HV side.

$X_{eq} = X_1 + 60^2 X_2$; (where X_1 & X_2 are the leakage reactances of primary & secondary side)

Taking load side terminal voltage as reference.

$V_L' = 7200 \angle 0^\circ$; since load is resistive

$I_2 = (16.67 \times 1000) / 120 = 139 \angle 0^\circ$ amp. -LV side

$I_2' = 139 / 60 = 2.32 \angle 0^\circ$ Amp. —HV side -----(2)

$E = V_2' + I_2' (R_{eq} + jX_{eq})$; $= 7200 \angle 0^\circ + 2.32 \angle 0^\circ (37.38 + j155.56)$

$E = 7286.56 + j360.13$ V; $E = V_1 = 7296 \angle 3^\circ$ V-----
-(2)

Primary Current $I_1 = I_o + I_2'$

$I_o = I_i + I_m$; Core loss component Current $I_i = (V_1 / R_c)$
 $= 7295 / (311 \times 10^3) = 0.0234 \angle 3^\circ$ Amp. -----(2)

$I_m = V_1 / (jX_m) = 7296 \angle 3^\circ / (58 \times 10^3 \angle 90^\circ) = 0.1257 \angle -87^\circ$

$I_1 = I_o + I_2' = 2.32 \angle 0^\circ + 0.127 \angle -77^\circ = 2.34 \angle -3^\circ$ Amp.

Copper Loss $= I_2'^2 \times R_{eq} = 2.32^2 \times 37.38 = 201$ Watt

Core Loss $= (V_1^2 / R_c)$

$= (7295)^2 / (311 \times 10^3) = 170$ Watt------(2)

Efficiency (η) = Out Put Power / Input Put Power

$= (16.67 \times 10^3 \times 1) / ((16.67 \times 10^3) + 201 + 170)$

$= (16670 / 17045) \times 100\% = 97.82\%$ -----(2)

Sol. 1(b) :

25 kVA, 660/220 V, Auto. Transformer.

$P_{cu}(\text{full L load}) = 320$ Watt ; $P_i = 360$ Watt

Efficiency (η) = Out Put Power / Input Put Power

$= (0.9 \times 25 \times 10^3) / ((0.9 \times 25 \times 10^3) + 680) = 97\%$ -----

(2)

For % vol. regulation. The step up Auto transformer is assumed to be made out of 440/220 V; 16.67 KVA two winding transformer.

$25 \times 10^3 = V_1 \times I_1 = 660 \times I_1$; i.e $I_1 = 37.82$ Amp

$220 \times I_2 = 25 \times 10^3$; So $I_2 = 113.63$ Amp.

VA rating of two winding transf. is

$V_2 \times (I_2 - I_1) = 16.67$ kVA------(2)

$I_2^2 \times R_{eq} = 320$

$\rightarrow R_{eq} = 320 / 37.86^2 = 0.223 \Omega$ ------(2)

$Z_{eq} = 27.6 / 37.86 = 0.73 \Omega$. $X_{eq} = \sqrt{Z_{eq}^2 - R_{eq}^2} = 0.48 \Omega$

%V.R $= (I_{rated} \times (R_{eq} \cos \phi + X_{eq} \sin \phi)) / V_{rated}$.

$$= (37.86 \times (0.223 \times 0.9) + (0.48 \times 0.435)) / 440 = \mathbf{3.5\%}$$

---(2)

Sol 2(b):

Given $Z_L = 44 + j18.6 \Omega$,

$E_A = 400 \text{ V}$, $Z_A = 1.8 + j5.6 \Omega$,

$E_B = 410 \text{ V}$, $Z_B = 1.8 + j7.4 \Omega$;

Current through the transf.

$$I_A = ((E_A Z_B) + (E_A - E_B) Z_L) / ((Z_A Z_B) + (Z_A + Z_B) Z_L) \quad \&$$

$$I_B = ((E_B Z_A) - (E_A - E_B) Z_L) / ((Z_A Z_B) + (Z_A + Z_B) Z_L)$$

Circulating current I_C (current flow through the windings when load is not connected).

$$I_C = (E_A - E_B) / (Z_A + Z_B)$$

$$I_C = 10 / (3.6 + j13) = 10 / (13.5 \angle -74.5^\circ) \text{ amp} \text{-----(2)}$$

Putting the values and simplifying then.

$$I_A = 4.1 \angle -16^\circ, \text{-----(2)} \quad I_B = 4.08 \angle -36^\circ, \text{-----(2)}$$

$$V_L = E_A - (I_A Z_A) = 400 \angle 0^\circ - (4.1 \angle -16^\circ \times (1.8 + j5.6))$$

$$= 387 \angle -3^\circ \text{ V} \text{-----(2)}$$

$$PF_a = \cos(12^\circ) = 0.96 \text{ lag}; \quad PF_b = \cos(33^\circ) = 0.8 \text{ lag} \text{---(2)}$$

Sol. 3(a) :

The 3 single phase transf. of 11kV/230V ; 110kVA

$$Z_{\text{base(LV)}} = 230^2 / (110 \times 10^3) = 0.48 \Omega$$

$$Z_a = 0.1 \text{ pu}, \quad Z_b = 0.12 \text{ pu}, \quad Z_c = 0.15 \text{ pu}$$

$$Y_{\text{net}} = Y_A + Y_B + Y_C = (1/0.1) + (1/0.12) + (1/0.15) = 25 \text{ pu.} \text{-----(2)}$$

From current division method

$$I_A = I_L \times (Y_A / Y_{\text{net}}) = 0.4 I_L$$

$$I_L = 1200 \angle -26^\circ = 2.5 \angle -26^\circ, \text{-----(2)}$$

$$I_{\text{Base}} = (110 \times 10^3) / 230 = 478 \text{ Amp}$$

$$\rightarrow I_A = 2.5 \times 0.4 \angle -26^\circ \text{ pu} = 1 \angle -26^\circ \text{ pu} = 480 \text{ Amp.} \text{---(2)}$$

$$\text{Similarly } I_B = (Y_B / Y_{\text{net}}) \times I_L = 400 \angle -26^\circ \text{ Amp.}$$

$$I_C = (Y_C / Y_{\text{net}}) \times I_L = 320 \angle -26^\circ \text{ Amp;}$$

$$\text{terminal voltage } V_L = |V| \angle 0^\circ = E_A - I_A Z_A$$

$$= 1 \angle 0^\circ - (1 \angle -26^\circ \times 0.1 \angle -90^\circ) = (\cos \phi + j \sin \phi) - 0.1(\cos 64^\circ + j \sin 64^\circ) \rightarrow \phi = 5^\circ,$$

$$E = 230 \angle 5^\circ \text{ V,} \text{-----(2)} \quad V_t = 220 \angle 0^\circ \text{ V}$$

Load shared by each transformer.

$$\mathbf{S_A = V_L \cdot I_A = 105 \text{ kVA.} \quad S_B = 87.52 \text{ KVA,} \quad S_C = 63.0 \text{ kVA} \text{-----(2)}}$$

Sol. 3(b):

Since 2-phase load is 50 kVA at 0.8pf; each phase load current

$$25 \times 10^3 = 220 \times |I_a| = |I_b| \rightarrow |I_a| = 113.63 \text{ amp} = |I_b|$$

$$V_b = 220 \angle 0^\circ; \quad V_a = 220 \angle 90^\circ; \quad I_b = 11.63 \angle -37^\circ;$$

$$I_a = 113.63 \angle 53^\circ \text{ Amp.} \text{-----(2)}$$

Line Currents are

$$I_B = I_{BC} - I_{A/2}; \quad I_C = -(I_{BC} + I_{A/2})$$

$$(3^{1/2}/2) N_1 I_A = N_2 I_a$$

$$\rightarrow I_A = (2/3^{1/2}) (N_2 / N_1) I_a$$

$$= (113.63 \angle 53^\circ) / 3 = 65.6 \angle 53^\circ \text{ Amp.} \text{----(2)}$$

$$\mathbf{I_A = 65.6 \angle 53^\circ \text{ Amp.}}$$

$$I_{BC} = (N_2 / N_1) \times I_b = I_b / 2;$$

$$= (113.63 \angle -37^\circ) / 2 = 56.8 \angle -37^\circ \text{ amp} \text{-----(2)}$$

$$I_B = I_{BC} - I_{A/2} = (56.8 \angle -37^\circ) - (65.6 \angle 53^\circ) = (45.36 - j34.18) - (19.74 + j26.2) = (25.62 - j60.5) = 65.63 \angle -67^\circ \text{ Amp}$$

$$\mathbf{I_B = 65.63 \angle -67^\circ \text{ Amp.}}$$

$$\mathbf{I_C = -65.68 \angle -70^\circ = 65.68 \angle 173^\circ \text{ Amp.} \text{-----(2)}}$$