

HW 6

Problem 1

对于 *ordinary wave*, $\theta_1 = \theta_2$
对于 *extraordinary wave*, $\theta_2 > \theta_1$

Problem 2

(a)

由于 $\sigma_z = 0.2\epsilon_0 > 0$ 且足够厚
把 z 变换到 u 或 v 都能满足条件

(b)

等价于求 d_p

$$K_I = w\sqrt{u\epsilon} \left[\frac{1}{2} \left(\sqrt{1 + \frac{\sigma^2}{\epsilon^2 w^2}} - 1 \right) \right]^{0.5}$$
$$d_p = \frac{1}{K_I} = 3.18\lambda$$

(c)

$$z- > w, x- > u, y- > v$$
$$E_{inc} = \frac{E_o}{\sqrt{2}} (x - y) \cos(k_0 z - wt)$$

$z = d$ 时, 由于是 *circularly polarized*

$$(2\sqrt{3} - 1)k_0 d = \frac{\pi}{2}$$
$$d = \frac{\lambda}{4(2\sqrt{3} - 1)}; \text{此时是右旋的}$$

Problem 3

(a)

$$\bar{\bar{z}} = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

(b)

$$\frac{dM}{dt} = gu_0 M \times H = gu_0 [(\vec{z}M_0 + M_1) \times (\vec{z}H_0 + H_1)]$$

由于 $M_1 \times H_1$ 可忽略

$$\text{上式等于 } gu_0 (M_0 \vec{z} \times H_1 - H_0 \vec{z} \times M_1)$$

$$= gu_0 (M_0 \vec{\bar{z}} \cdot H_1 - H_0 \vec{\bar{z}} \cdot M_1)$$

$$B = u_0 (H + M)$$

$$B_1 = u_0 (H_1 + M_1) = \vec{\bar{u}} \cdot H_1$$

$$\text{可以得到 } \vec{\bar{u}} = \begin{bmatrix} u & iu_g & 0 \\ -iu_g & u & 0 \\ 0 & 0 & u_z \end{bmatrix}$$

(c)

$$\vec{\bar{v}} = \begin{bmatrix} v & iv_g & 0 \\ -iv_g & u & 0 \\ 0 & 0 & v_z \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u^2 - kv & -ikv_g \cos \theta \\ ikv_g \cos \theta & u^2 - k(v \cos^2 \theta + v_z \sin^2 \theta) \end{bmatrix} \cdot \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} = 0$$

$$\frac{D_2}{D_1} = -\frac{B_1}{B_2} = \frac{(v - nu_0) \sin^2 \theta_0 \pm \sqrt{(v - v_0)^2 \sin^4 \theta + 4v_g^2 \cos^2 \theta}}{2iv_g \cos \theta}$$

(d)

$$\text{定义 } \cos 2\phi = \frac{2v_g \cos \theta}{(v - v_z) \sin^2 \theta}$$

$$\frac{D_2}{D_1} = i \tan \phi \text{ 或 } i \cot \phi, \text{ 是椭圆极化波}$$

$\Rightarrow \text{Faraday rotation exists}$