



fundamental data structure report1

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1 Chapter 1:Introduction

There are at least two different algorithms can calculate X^N . For a positive integer N, algorithm uses N-1 multiplication. Algorithm 2 works as follows:

```
if N is an even number :
 \!X^N=X^{N/2}*X^{N/2} if N is an odd number :
 \!\!X^N=X^{(N-1)/2}*X^{(N-1)/2}*X
```

1.1 algorithm 1

To implement algorithm 1, we only need to multiply n numbers.

The pseudo code is as follows:

```
Algorithm 1 Calculate X^N

Require: N \ge 0 \lor x \ge 0
i \leftarrow 0
if i < N then
res \leftarrow res * X
i \leftarrow i + 1
end if
return res
```

1.2 algorithm 2

And there are at least ways to implement algorithm 2, one is iteration and the other is recursion.

Iterative version: The pseudo code is as follows

Algorithm 2 Calculate X^N , Iterative version

```
Require: N \ge 0 \lor x \ge 0
  temp = X
  i = 1
  if N \mod 2 == 0 then
     if i < N then
       temp1 \leftarrow temp * temp
       temp \leftarrow temp1
       i \leftarrow i * 2
     end if
  else
     if N \mod 2 == 0 then
       temp1 \leftarrow temp * temp
       temp \leftarrow temp1
       i \leftarrow i * 2
     end if
  end if
  return temp1
```

2 Chapter 2:Algorithm Specification

2.1 algorithm 1

The code of function function is as follows:

```
double function(double num,int N){
    double res = 1;
    if(N == 0)
        return 1;
    else{
        for(int i = 0;i<N;i++){
            res *= num;
        }
        return res;
    }
}</pre>
```

The time complexity of this algorithm is O(N), It uses a for loop that loops n times to get the nth power of X.

The spatial complexity of this algorithm is O(1).

2.2 algorithm 2

The function code of iterative version is as follows:

```
double function(double num, int N){
        double res;
2
        double temp = num;
3
        double temp1;//Return temp1 on return
        int i = 1;
5
        if(N == 0)
            return 1;
        else if (N == 1)
            return num;
        else if (N \% 2 == 0){
10
            for(;i<N;){</pre>
11
                 temp1 = temp * temp;
                 temp = temp1;
13
                 i *= 2;
14
            }
        }
16
        else{
17
            for(;i<N-1;){</pre>
18
                 temp1 = temp * temp;
19
                 temp = temp1;
20
                 i *= 2;
21
            }
22
            temp1 *= num;
23
        }
        res = temp1;
25
        return res;
26
   }
27
```

The time complexity of the code is O(log N). In this version of the function, n is continuously divided into two parts, and the temp variable is set to store the previous product. Each iteration, I is multiplied by 2, and temp is equivalent

to square once until I is equal to n.

The spatial complexity of this algorithm is O(1).

The function code of recursive version is as follows:

```
double function(double num,int N){
   if(N == 0)
      return 1;
   if(N == 1)
      return num;
   if(N % 2 == 0)
      return function(num*num,N/2);
   else
      return function(num * num,N/2) * num;
}
```

The time complexity of the code is $O(\log N)$, for example to caculate X^62 , We only used nine multiplication. Obviously, the maximum number of multiplications required is 2 log N. Because it takes up to two multiplications to divide the problem in half.

The spatial complexity of this algorithm is $O(\log N)$. Each recursive call to the function will declare a new variable, so the spatial complexity of the algorithm is $O(\log N)$.

3 Chapter 3: Testing Results

We take x=1.0001 and N as 1000, 5000, 10000, 20000, 40000, 60000, 80000 and 100000 respectively. Because the time of one test is too short, I repeat 1000000000 cycles to obtain large enough ticks. The test data results of the three algorithms are as follows:

N iterations(K) ticks	1000 1000000 2657	5000 1000000	10000 1000000	20000 1000000	40000	60000	80000	100000
ticks			1000000	1000000				
	2657				1000000	1000000	1000000	1000000
		13270	26423	53469	107586	156000	214099	267605
otal time(sec)	2.6	13	26	53	107	156	210	267
thm1 duration(sec)	0.000002	0.000013	0.000026	0.000053	0.000107	0.000156	0.00021	0.000267
iterations(K)	1000000000	100000000	1000000000	1000000000	100000000	1000000000	1000000000	1000000000
ticks	22430	29658	32016	34199	38103	38069	41162	40000
otal time(sec)	22	29	32	34	38	38	41	40
version duration(sec	0.000000022	0.000000029	0.000000032	0.000000034	0.000000038	3.8E-08	0.000000041	0.00000004
iterations(K)	1000000000	1000000000	1000000000	1000000000	1000000000	1000000000	1000000000	1000000000
ticks	28752	36694	40308	44313	47784	47096	49431	49671
otal time(sec)	28	36	40	44	47	47	49	49
version duration(sec	0.000000028	0.000000036	0.00000004	0.000000044	0.000000047	4.7E-08	0.000000049	0.000000049
	hm1 duration(sec) iterations(K) ticks otal time(sec) version duration(sec) iterations(K) ticks otal time(sec)	hm1 duration(sec) 0.000002 iterations(K) 100000000 ticks 22430 tall time(sec) 22 version duration(sec) 0.00000002 iterations(K) 100000000 ticks 28752 tall time(sec) 28	hm1 duration(sec) 0.000002 0.000013 treations(K) 100000000 100000000 ticks 22430 29568 tal time(sec) 22 29 version duration(sec 0.000000022 0.0000000029 treations(K) 100000000 100000000000000000000000000	hm1 duration(sec) 0.000002 0.000013 0.000026 treatons(K) 100000000 100000000 100000000 ticks 22430 26568 30016 stal time(sec) 22 29 32 29 32 occession duration(sec) 0.000000002 0.00000000029 0.00000000000	hm1 duration(sec) 0.000002 0.000013 0.000026 0.000053 teterations(K) 100000000 1000000000 1000000000 1000000	hml duration(sec) 0.000002 0.000013 0.000026 0.000053 0.000107 treations(K) 1.000000000 1.000000000 1.000000000 1.000000000 1.00000000 <td>hml duration(sec)</td> <td>hml duration(sec) 0.000002 0.000013 0.000026 0.000053 0.000107 0.000156 0.00021 treaton(K) 100000000 100000000 100000000 100000000</td>	hml duration(sec)	hml duration(sec) 0.000002 0.000013 0.000026 0.000053 0.000107 0.000156 0.00021 treaton(K) 100000000 100000000 100000000 100000000

Figure 1: result

Since the running time of algorithm 1 is too large compared with that of algorithm 2, the n-runtime line graph of iterative version and recursive version of algorithm 2 is shown below

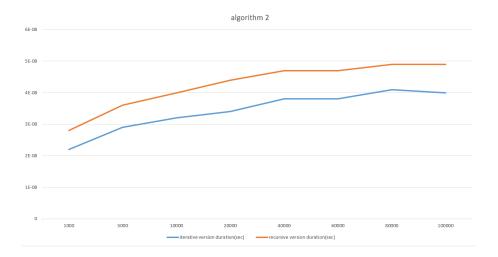


Figure 2: algorithm2 result

The following figure is the n-runtime diagram obtained by drawing the running time of two versions of algorithm 1 and algorithm 2 in the same line graph

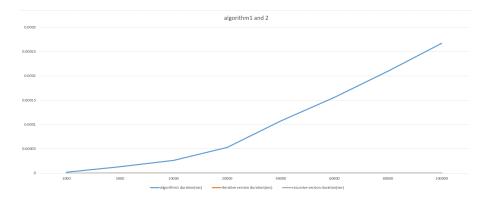


Figure 3: algorithm1 and 2 result

From the line graph, we can see that the running time of algorithm 1 is much longer than that of algorithm 2, and the running time of the two versions of algorithm 2 is almost the same

4 Declaration

I hereby declare that all the work done in this project titled "POW" is of my independent effort.