# NICE 2020 model — code documentation

# T. O. Da Costa Update by M Young-Brun 30/08/2024

# Contents

1	Model - Indexes				
2	Mod	del - Parameters	4		
3	Mod	del - Variables	6		
4	In t	heory	9		
5	<b>aba</b> r 5.1 5.2 5.3 5.4	tement.jl Indexes Parameters 5.2.1 Time-dependent 5.2.2 Time and country dependent 5.2.3 Independent Variables 5.3.1 Time and country dependent 5.3.2 Time-dependent Equations 5.4.1 Calculating $\theta 1$ for each country 5.4.2 Calculation of abatement cost, abatement rate and overall abatement rate in the case of full abatement	9 9 9 9 9 9 9 9 10 10 10		
e	dam		11		
6	6.1 6.2	Indexes	11 11 11 11 11 11		
	6.4	Variables	11 11 12		
7		ssions.jl Indexes Parameters 7.2.1 Country dependent 7.2.2 Time and country dependent Variables 7.3.1 Time-dependent 7.3.2 Time and country dependent 7.3.3 Time and WPP region dependent	12 12 12 12 12 12 12 12 12		
	7.4	Equations	12 12 13		

	7.4.3 $7.4.4$	Global emissions in Carbon Units (GtC)
$\operatorname{gro}$	ssecon	
8.1	Index	
8.2		neters
	8.2.1	Country dependent
	8.2.2	Time and country dependent
	8.2.3	Independent
8.3	Variab	oles
	8.3.1	Time-dependent
	8.3.2	Time and country dependent
8.4	Equat	ions
	8.4.1	Capital (K)
	8.4.2	Calculation of Gross Production by Country (YGROSS)
	8.4.3	Calculation of Global Gross Production (YGROSS_global)
net	econon	
9.1	Indexe	es
9.2	Param	neters
	9.2.1	Country dependent
	9.2.2	Time and country dependent
9.3	Variab	les
	9.3.1	Time and country dependent
	9.3.2	Time and WPP region dependent
9.4	Equat	ions
	9.4.1	Country loop
	9.4.2	Loop over WPP regions
) pat	${ m tern\_s}$	cale.jl
10.1	l Index	
10.2	2 Param	neters
10.3	3 Variab	les
10.4	4 Functi	on
10.5	5 Equat	ion
		recycle.jl
		S
11.2		neters
	11.2.1	Time and country dependent
	11.2.2	Other
11.3	3 Variab	les
	11.3.1	Time-dependent
	11.3.2	Time and country dependent
	11.3.3	Time, country and quantile dependent
		Time and regionwpp dependent
11.4	4 Equat	0 11 1
	-	Temporary variables for global population and by quantile (in thousands) .
		Income elasticity - CO2 price
		Distribution of Tax Burdens and Mitigation Costs
		Consumption per Quantile
		Calculation of per capita consumption
		Calculation of the Gini Index and the Poverty Rate

12.2.2 Country dependent 12.2.3 Independent 12.3 Variables 12.3.1 Time-dependent 12.3.2 Time and country dependent 12.4.2 Equation 12.4.1 Carbon tax revenue 12.4.2 Dividends according to Boolean values 12.4.3 Total dividends 13 welfare.jl 13.1 Indexes 13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale_jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle_jl 15.11Quanties: quantile_distribution.jl 15.11Quanties: quantile_distribution.jl 15.11Quanties: quantile_distribution.jl 15.11Quanties: quantile_distribution.jl 15.11Quanties: quantile_distribution.jl 15.12Welfare: welfare.jl		12.2	Parameters	1
12.2.3 Independent  12.3 Variables  12.3.1 Time-dependent  12.3.2 Time and country dependent  12.4 Equation  12.4.1 Carbon tax revenue  12.4.2 Dividends according to Boolean values  12.4.3 Total dividends  13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5 Damages: damages.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.10Ioncome recycling: revenue_recycle.jl  15.10Uncomire everlare: jl  15.10Uncomire everlare: jl  15.10Uncome recycling: revenue_recycle.jl  15.10Uncome recycling: revenue_recycle.jl			12.2.1 Time and country dependent	1
12.3 Variables.  12.3.1 Time-dependent  12.3.2 Time and country dependent  12.4 Equation  12.4.1 Carbon tax revenue  12.4.2 Dividends according to Boolean values  12.4.3 Total dividends  13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4.1 The update_paran! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl			12.2.2 Country dependent	1
12.3 Variables.  12.3.1 Time-dependent  12.3.2 Time and country dependent  12.4 Equation  12.4.1 Carbon tax revenue  12.4.2 Dividends according to Boolean values  12.4.3 Total dividends  13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4.1 The update_paran! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl			12.2.3 Independent	1
12.3.1 Time-dependent 12.3.2 Time and country dependent 12.4 Equation 12.4.1 Carbon tax revenue 12.4.2 Dividends according to Boolean values 12.4.3 Total dividends  13 welfare.jl 13.1 Indexes 13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: velfare.jl		12.3		1
12.3.2 Time and country dependent  12.4 Equation  12.4.1 Carbon tax revenue  12.4.2 Dividends according to Boolean values  12.4.3 Total dividends  13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Vevelfare: velfare.jl				1
12.4.1 Carbon tax revenue 12.4.2 Dividends according to Boolean values 12.4.3 Total dividends  13 welfare.jl 13.1 Indexes 13.2 Parameters 13.3 Variables 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.4.3 Greeate_nice2020(f) function 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				1
12.4.1 Carbon tax revenue 12.4.2 Dividends according to Boolean values 12.4.3 Total dividends  13. welfare.jl 13.1 Indexes 13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement : abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions : emissions.jl 15.7 Temperature : pattern_scale.jl 15.8 Damages : damages.jl 15.9 Net economy : net_economy.jl 15.10Income recycling : revenue_recycle.jl 15.11Quantiles : quantile_distribution.jl 15.12Welfare : welfare.jl		12.4		2
12.4.2 Dividends according to Boolean values 12.4.3 Total dividends  13 welfare.jl 13.1 Indexes 13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4.1 The update_param! function 15.4.2 Acrosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement : abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions : emissions.jl 15.7 Temperature : pattern_scale.jl 15.8 Damages : damages.jl 15.9 Net economy : net_economy.jl 15.10Income recycling : revenue_recycle.jl 15.11Quantiles : quantile_distribution.jl 15.12Welfare : welfare.jl				
13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Ountiles: quantile_distribution.jl  15.12Welfare: welfare.jl				
13 welfare.jl  13.1 Indexes  13.2 Parameters  13.3 Variables  13.4 Equations  13.4.1 Case where η ≠ 1  13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Ountiles: quantile_distribution.jl  15.12Welfare: welfare.jl				
13.1 Indexes 13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl 14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				_
13.2 Parameters 13.3 Variables 13.4 Equations 13.4.1 Case where η ≠ 1 13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions 14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4.1 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl	<b>13</b>	welf	fare.jl 23	3
13.3 Variables  13.4 Equations  13.4.1 Case where $\eta \neq 1$ 13.4.2 Case where $\eta \neq 1$ 13.4.2 Case where $\eta = 1$ 14 helper_functions.jl  21  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4 Initial conditions  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl		13.1	Indexes	3
$13.4.1 \text{ Case where } \eta \neq 1$ $13.4.2 \text{ Case where } \eta = 1$ $14 \text{ helper_functions.jl}$ $14.1 \text{ Functions}$ $14.1.1 \text{ country_quantile_distribution}$ $14.1.2 \text{ linear_tax_trajectory}$ $14.1.3 \text{ save_nice2020_results}$ $14.1.4 \text{ get_global_mitigation}$ $15 \text{ nice2020\_module.jl}$ $15.1 \text{ Loading packages and data}$ $15.2 \text{ Mimi Model Auxiliary Functions and Components}$ $15.3 \text{ create_nice2020() function}$ $15.4 \text{ Initial conditions}$ $15.4.1 \text{ The update_param! function}$ $15.4.2 \text{ Aerosol cycle and temperature}$ $15.4.3 \text{ Gross economy}$ $15.5 \text{ Abatement: abatement.jl}$ $15.5.1 \text{ set_param! function}$ $15.6 \text{ CO2 emissions: emissions.jl}$ $15.7 \text{ Temperature: pattern_scale.jl}$ $15.8 \text{ Damages: damages.jl}$ $15.9 \text{ Net economy: net_economy.jl}$ $15.10 \text{Income recycling: revenue_recycle.jl}$ $15.11 \text{ Quantiles: quantile_distribution.jl}$ $15.12 \text{ Welfare: welfare.jl}$		13.2	Parameters	3
$13.4.1 \text{ Case where } \eta \neq 1$ $13.4.2 \text{ Case where } \eta = 1$ $14 \text{ helper_functions.jl}$ $14.1 \text{ Functions}$ $14.1.1 \text{ country_quantile_distribution}$ $14.1.2 \text{ linear_tax_trajectory}$ $14.1.3 \text{ save_nice2020_results}$ $14.1.4 \text{ get_global_mitigation}$ $15 \text{ nice2020_module.jl}$ $15.1 \text{ Loading packages and data}$ $15.2 \text{ Mimi Model Auxiliary Functions and Components}$ $15.3 \text{ create_nice2020() function}$ $15.4 \text{ Initial conditions}$ $15.4.1 \text{ The update_param! function}$ $15.4.2 \text{ Aerosol cycle and temperature}$ $15.4.3 \text{ Gross economy}$ $15.5 \text{ Abatement: abatement.jl}$ $15.5.1 \text{ set_param! function}$ $15.6 \text{ CO2 emissions: emissions.jl}$ $15.7 \text{ Temperature: pattern_scale.jl}$ $15.8 \text{ Damages: damages.jl}$ $15.9 \text{ Net economy: net_economy.jl}$ $15.10 \text{Income recycling: revenue_recycle.jl}$ $15.11 \text{ Quantiles: quantile_distribution.jl}$ $15.12 \text{ Welfare: welfare.jl}$		13.3	Variables	3
$13.4.1 \text{ Case where } \eta \neq 1$ $13.4.2 \text{ Case where } \eta = 1$ $14 \text{ helper_functions.jl}$ $14.1 \text{ Functions}$ $14.1.1 \text{ country_quantile_distribution}$ $14.1.2 \text{ linear_tax_trajectory}$ $14.1.3 \text{ save_nice2020_results}$ $14.1.4 \text{ get_global_mitigation}$ $15 \text{ nice2020_module.jl}$ $15.1 \text{ Loading packages and data}$ $15.2 \text{ Mimi Model Auxiliary Functions and Components}$ $15.3 \text{ create_nice2020() function}$ $15.4 \text{ Initial conditions}$ $15.4.1 \text{ The update_param! function}$ $15.4.2 \text{ Aerosol cycle and temperature}$ $15.4.3 \text{ Gross economy}$ $15.5 \text{ Abatement: abatement.jl}$ $15.5.1 \text{ set_param! function}$ $15.6 \text{ CO2 emissions: emissions.jl}$ $15.7 \text{ Temperature: pattern_scale.jl}$ $15.8 \text{ Damages: damages.jl}$ $15.9 \text{ Net economy: net_economy.jl}$ $15.10 \text{Income recycling: revenue_recycle.jl}$ $15.11 \text{ Quantiles: quantile_distribution.jl}$ $15.12 \text{ Welfare: welfare.jl}$				4
13.4.2 Case where η = 1  14 helper_functions.jl  14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4 Initial conditions  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement : abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions : emissions.jl  15.7 Temperature : pattern_scale.jl  15.8 Damages : damages.jl  15.9 Net economy : net_economy.jl  15.10Income recycling : revenue_recycle.jl  15.11Quantiles : quantile_distribution.jl  15.12Welfare : welfare.jl				4
14 helper_functions.jl       2         14.1 Functions       14.1.1 country_quantile_distribution         14.1.2 linear_tax_trajectory       14.1.3 save_nice2020_results         14.1.4 get_global_mitigation       2         15 nice2020_module.jl       2         15.1 Loading packages and data       5.2 Mimi Model Auxiliary Functions and Components         15.3 create_nice2020() function       5.4 Initial conditions         15.4.1 The update_param! function       5.4.2 Aerosol cycle and temperature         15.4.3 Gross economy       5.4 Abatement: abatement.jl         15.5 Abatement: abatement.jl       5.5 Abatement: abatement.jl         15.7 Temperature: pattern_scale.jl       5.7 Temperature: pattern_scale.jl         15.8 Damages: damages.jl       5.8 Damages: damages.jl         15.10Income recycling: revenue_recycle.jl       5.11Quantiles: quantile_distribution.jl         15.12Welfare: welfare.jl       5.12Welfare: welfare.jl			1 /	
14.1 Functions  14.1.1 country_quantile_distribution  14.1.2 linear_tax_trajectory  14.1.3 save_nice2020_results  14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4 Initial conditions  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl				
14.1.1 country_quantile_distribution 14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 2	<b>14</b>	help	per_functions.jl 25	5
14.1.2 linear_tax_trajectory 14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl 15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl		14.1	Functions	5
14.1.3 save_nice2020_results 14.1.4 get_global_mitigation  15 nice2020_module.jl  2			14.1.1 country_quantile_distribution	5
14.1.4 get_global_mitigation  15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4 Initial conditions  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl			14.1.2 linear_tax_trajectory	5
15 nice2020_module.jl  15.1 Loading packages and data  15.2 Mimi Model Auxiliary Functions and Components  15.3 create_nice2020() function  15.4 Initial conditions  15.4.1 The update_param! function  15.4.2 Aerosol cycle and temperature  15.4.3 Gross economy  15.5 Abatement: abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl			14.1.3 save_nice2020_results	6
15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl			14.1.4 get_global_mitigation	7
15.1 Loading packages and data 15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				
15.2 Mimi Model Auxiliary Functions and Components 15.3 create_nice2020() function 15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl	<b>15</b>			
15.3 create_nice2020() function 15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				
15.4 Initial conditions 15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				
15.4.1 The update_param! function 15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy 15.5 Abatement: abatement.jl 15.5.1 set_param! function 15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl				
15.4.2 Aerosol cycle and temperature 15.4.3 Gross economy  15.5 Abatement: abatement.jl 15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl 15.7 Temperature: pattern_scale.jl 15.8 Damages: damages.jl 15.9 Net economy: net_economy.jl 15.10Income recycling: revenue_recycle.jl 15.11Quantiles: quantile_distribution.jl 15.12Welfare: welfare.jl		15.4		
15.4.3 Gross economy  15.5 Abatement : abatement.jl  15.5.1 set_param! function  15.6 CO2 emissions : emissions.jl  15.7 Temperature : pattern_scale.jl  15.8 Damages : damages.jl  15.9 Net economy : net_economy.jl  15.10Income recycling : revenue_recycle.jl  15.11Quantiles : quantile_distribution.jl  15.12Welfare : welfare.jl			15.4.1 The update_param! function	
15.5 Abatement : abatement.jl       15.5.1 set_param! function         15.6 CO2 emissions : emissions.jl       15.7 Temperature : pattern_scale.jl         15.8 Damages : damages.jl       15.9 Net economy : net_economy.jl         15.10Income recycling : revenue_recycle.jl       15.11Quantiles : quantile_distribution.jl         15.12Welfare : welfare.jl       5.12Welfare : welfare.jl				
15.5.1 set_param! function  15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl				9
15.6 CO2 emissions: emissions.jl  15.7 Temperature: pattern_scale.jl  15.8 Damages: damages.jl  15.9 Net economy: net_economy.jl  15.10Income recycling: revenue_recycle.jl  15.11Quantiles: quantile_distribution.jl  15.12Welfare: welfare.jl		15.5		9
15.7 Temperature: pattern_scale.jl				9
15.8 Damages: damages.jl          15.9 Net economy: net_economy.jl          15.10Income recycling: revenue_recycle.jl          15.11Quantiles: quantile_distribution.jl          15.12Welfare: welfare.jl		15.6	CO2 emissions: emissions.jl	0
15.9 Net economy: net_economy.jl		15.7	Temperature: pattern_scale.jl 30	0
15.9 Net economy: net_economy.jl		15.8	Damages: damages.jl 30	0
15.10Income recycling : revenue_recycle.jl				0
15.11Quantiles: quantile_distribution.jl				0
15.12Welfare: welfare.jl				0
				0
				0

# 1 Model - Indexes

Symbol Name	Model Name	Short description
c	country	Countries included in the model
q	quantile	Index of income quantiles
rwpp	regionwpp	Regions defined from the World Population Prospects database (UN)
t	time	Time index

# 2 Model - Parameters

N.B.: \$ = 2017 US dollars. pers. = person. yr = year.

Name	Short description	Unit	Value
$\beta$ 1	Linear damage coefficient on temperature.  This parameter represents the direct impact of the temperature anomaly on the economy	$T^{-eta 2}$	0.0236
$\beta1\_KW[t,c]$	Linear damage coefficient on local temperature anomaly for Kalkuhl and Wenz based damage function	$T^{-1}$	
eta 2	Power damage coefficient on temperature. This parameter captures the non-linear effects of temperature anomalies on the economy	_	2
$\beta 2\_KW[t,c]$	Quadratic damage coefficient on local temperature anomaly for Kalkuhl and Wenz based damage function	$T^{-2}$	
$\beta\_temp[c]$	Temperature scaling coefficients, which translate global temperature anomalies into country-level temperature anomalies	_	
$\eta$	Inequality aversion.	_	1.5 (by default)
$\sigma[t,c]$	Emissions output ratio. This parameter is used for modelling emissions intensity as a function of economic activity	$GtCO_2/(10^6 \$)$	
$\theta 2$	Exponent of abatement cost function (DICE-2023 value)	_	2.6
$\mu\_input[t,c]$	Input mitigation rate, used with option 3 "country_abatement_rate"	%	_
control_regime	Switch for emissions control regime; 1 = "global_carbon_tax", 2 = "country_carbon_tax", 3 = "country_abatement_rate"	_	3 (by default)
damage_elasticity	Income elasticity of climate damages $(1 = proportional to income)$	_	0.85
depk[t,c]	Depreciation rate on capital	%	_

Name	Short description	Unit	Value
elasticity	Income elasticity with respect to climate damage, mitigation costs, etc. It can either be damage_elasticity or CO2_income_elasticity	_	_
$elasticity\_intercept[t]$	Intercept term for estimating income elasticity	_	$3.22^{1}$
$elasticity\_slope[t]$	Slope term for estimating income elasticity	_	$-0.2^{1}$
$global\_carbon\_tax[t]$	Global carbon tax	$fCO_2$	_
global_recycle_share[c]	Share of country revenues that are recycled globally in the form of international transfers $(1 = 100\%)$	%	1 (by default)
$\begin{array}{l} global\_temperature[t] = \\ temp\_anomaly[t] \end{array}$	Global average surface temperature excess (above pre-industrial [year 1750] level)	°C	_
$income\_shares[c,q]$	An array of income shares by quantile (where rows represent countries and columns represent quantiles)	_	_
increase_value	The annual tax increase value. By default, it is equal to tax_start_value, which means that the tax increases by its initial value each year	\$/tCO <sub>2</sub>	_
k0[c]	Initial level of capital. Determines the starting point for capital accumulation	$10^6 \ {\rm yr}$	_
l[t,c]	Labor/population. This parameter represents either the population or the available workforce for production of a given country	$10^3$ pers.	_
$local\_temp\_anomaly[t,\!c]$	Country-level average surface temperature anomaly (above pre-industrial [year 1750] level)	°C	
lost_revenue_share	Portion of carbon tax revenue that is lost and cannot be recycled $(1 = 100\%)$ of revenue lost, $0 = 100\%$ no revenue lost	%	0 (by default)
mapcrwpp[c]	Mapping from country index to UN WPP region index	_	183 countries to 20 regions
$max\_study\_gdp$	Maximum value of GDP per capita observed in elasticity studies	\$/pers.	48892
$min\_study\_gdp$	Minimum value of GDP per capita observed in elasticity studies	\$/pers.	647
nb_country	Number of countries	_	183
nb_quantile	Number of quantiles	_	10 (by default)
pbacktime[t]	Backstop price from DICE 2023	$ftCO_2$	_
$\begin{array}{c} \text{quantile\_income} \\ \text{\_shares[t,c,q]} \end{array}$	Income shares of quantile	_	_

Name	Short description	Unit	Value
recycle_share[c,q]	Share of carbon tax revenues recycled to each quantile	_	nb_quantile (by default)
reference_carbon_tax[t]	Reference carbon tax	$fCO_2$	_
reference_country_index	Reference country index	_	USA
s[t,c]	Savings rate	%	_
share	Capital's share of production. This parameter is global and affects the distribution of income between capital and labor	%	0.3
switch_global _pc_recycle	Boolean, carbon tax revenues are recycled globally on an equal per capita basis	_	0 or 1
switch_recycle	Boolean for recycling carbon tax revenue	_	0 or 1
switch_scope_recycle	Boolean, carbon tax revenues are recycled at national (0) or global (1) level	_	0 or 1
tax_start_value	The initial value of the carbon tax	\$/tCO <sub>2</sub>	Depends on the chosen carbon tax pathway
temp_anomaly[t] = global_temperature[t]	Global average surface temperature excess (above pre-industrial [year 1750] level)	$^{\circ}\mathrm{C}$	_
tfp[t,c]	Total factor productivity	_	_
year_model_end	The end of the model. If it is less than year_tax_end, the last tax value is repeated up to this year	yr	2300 (by default)
year_step	The step in years between two tax values	yr	1 (by default)
year_tax_end	The last year for which to calculate the tax	yr	2200 (by default)
year_tax_start	The first year of the tax increase	yr	2020 (by default)

# 3 Model - Variables

Name	Short description	Unit
$\mu[t,c]$	GHG emissions mitigation rate	%
$\theta 1[t,c]$	Multiplicative parameter of abatement cost function. Equal to ABATEFRAC at 100% mitigation	_
ABATECOST[t,c]	Cost of emission reductions	$10^6  \text{\$/yr}$
ABATEFRAC[t,c]	Cost of emission reductions as a share of gross economic output	%
	Share of the distribution of abatement costs per quantile	_

 $<sup>^{1}</sup>$ Results from the meta-regression based on study results to calculate elasticity vs. ln gdp per capita relationship.

Name	Short description	Unit
C[t,c]	Country consumption	$10^6  \text{\$/yr}$
$carbon\_tax\_dist[t,c,q]$	Shares of the distribution of CO2 tax burden per quantile	_
$cons\_EDE\_country[t,c]$	Consumption equivalent to equitably distributed well-being in a given country	$10^3  \text{\$/pers}$
$cons\_EDE\_global[t]$	Global consumption equivalent to equitably distributed well-being	$10^3  \text{\$/pers}$
$cons\_EDE\_rwpp[t,rwpp]$	Consumption equivalent to equitably distributed well-being for WPP regions	$10^3  \text{\$/pers}$
$country\_carbon\_tax[t,c]$	CO2 tax rate	$tCO_2$
$country\_pc\_dividend[t,\!c]$	Total fiscal dividends per person, including all international monetary transfers	$10^3  \text{\$/pers}$
$\begin{array}{c} country\_pc\_dividend \\ \_domestic\_transfers[t,c] \end{array}$	Fiscal dividends per person from domestic redistribution, i.e., within a country	$10^3  \text{\$/pers}$
$\begin{array}{c} country\_pc\_dividend \\ \_global\_transfers[t,c] \end{array}$	Tax dividends per person from international transfers	$10^3  \text{\$/pers}$
CPC[t,c]	Country level consumption per capita	$10^3$ \$/pers
$CPC\_post[t,c]$	Country level consumption per capita after recycling	$10^3  \text{\$/pers}$
$CPC\_post\_global[t]$	World consumption per capita after recycling	$10^3  \text{\$/pers}$
$CPC\_post\_rwpp[t,rwpp]$	Regional per capita consumption after recycling	$10^{3} \ \text{\$/pers}$
$CPC\_rwp[t,rwpp]$	Regional level consumption per capita	$10^3$ \$/pers
$\mathrm{DAMFRAC}[\mathrm{t,c}]$	Country-level damages as a share of net GDP based on global temperatures	%
$damage\_dist[t,c,q]$	Share of the distribution of climate damage per quantile	_
$E\_gtco2[t,c]$	Country-level total GHG emissions	$10^9 \text{ tCO2}/$
$E\_Global\_gtco2[t]$	Global emissions (sum of all country emissions)	$10^9 \text{ tCO2}$
$E\_Global\_gtc[t]$	Global emissions in units of gigatonnes of carbon, giving compatible units with FAIR	$10^9 \text{ tC/yr}$
$\begin{array}{c} {\rm GLOBAL\_ABATEFRAC} \\ {\rm \_full\_abatement[t]} \end{array}$	Global ABATEFRAC[t] in case of full mitigation	%
$global\_gini\_cons[t]$	Gini index of world consumption	_
$global\_revenue[t]$	Carbon tax revenue, derived from the total recycled revenue of all countries $$	\$/yr
$global\_pc\_revenue[t]$	Carbon tax revenue per person, derived from the total recycled revenue of all countries	$10^3  \text{\$/pers}$
$gini\_cons[t,c]$	Gini index of country consumption	_
gini_cons_rwpp[t,rwpp]	Gini index of regional consumption	_
I[t,c]	Investment	$10^6  \text{\$/yr}$
K[t,c]	Capital	$10^6  \text{\$/yr}$

Name	Short description	Unit
l_rwpp[t,rwpp]	Regional population	$10^3$ pers.
$\begin{array}{c} LOCAL\_\\ DAMFRAC\_KW[t,c] \end{array}$	Country-level damages as a share of net GDP based on local temperatures and on Kalkuhl & Wenz	%
$local\_temperature[t,c]$	Excess temperature at country level (above preindustrial [year 1750] level)	$^{\circ}\mathrm{C}$
$qcpc\_base[t,c,q]$	Consumption per quantile per capita before damage, before abatement cost, before tax	$10^3 \text{ $pers/yr}$
qcpc_post _damage_abatement[t,c,q	Consumption per quantile per capita after damage, ] after abatement	$10^3$ \$/pers/yr
$qc\_post\_recycle[t,c,q]$	Consumption per quantile per capita after recycling the carbon tax to each quantile	$10^3$ \$/pers/yr
$qcpc\_post\_tax[t,c,q]$	Consumption per quantile per capita after subtraction of the carbon tax $$	$10^3$ \$/pers/yr
$qcpc\_share[t,c,q]$	Proportion of consumption per quantile per capita	%
revenue_recycled _global_level[t]	Recycle a share global_recycle_share of tax_revenue at global level	$10^3 \ \text{\$/yr}$
tax_pc_revenue[t,c]	Carbon tax revenue per capita from country emissions	$10^3$ \$/pers/yr
$tax\_revenue[t,c]$	Carbon tax revenue for a given country	\$/yr
tax_values[t]	Array containing the carbon tax values over time, until the last year of tax defined	_
sum_qcpc_ post_recycle[t,c]	Sum of quantiles post consumption per capita	$10^3$ \$ / (pers per quant) / yr
total_tax_pc_revenue[t]	Total carbon tax revenue per person, sum of tax revenues in all countries per person	$10^3$ \$/pers/yr
total_tax_revenue[t]	Total carbon tax revenue, sum of tax revenues in all countries	$10^3 \ \text{\$/yr}$
$\begin{array}{c} \operatorname{updated\_quantile} \\ \operatorname{\_distribution[t,c,q]} \end{array}$	An array which contains the updated quantile share distribution for each country, considering the given income elasticity	_
$welfare\_country[t,c]$	Welfare for countries	
welfare_global[t]	Global welfare	_
$welfare\_rwpp[t,rwpp]$	Welfare in a given WPP region	
YGROSS[t,c]	Gross output	$10^6$ $$/yr$
YGROSS_global[t]	Global gross output, represents the sum of all countries' gross production	$10^{12} \ \$/\mathrm{yr}$
Y[t,c]	Output net of damages and abatement costs	$10^6 \ \text{\$/yr}$
$Y_{pc}[t,c]$	Net GDP per capita after damages and mitigation costs	\$/pers/yr
Y_pc_rwpp[t,rwpp]	Regional per capita output net of abatement and damages	\$/pers/yr

# 4 In theory

The goal is to maximize the following Social Welfare function:

$$W(\cos(c, q, t)) = \sum_{cqt} \frac{l(c, q, t)}{(1 + \rho)^t} \frac{\cos(c, q, t)^{1 - \eta}}{1 - \eta}$$
(1)

- $\bullet$  W: social welfare
- cons : per capita consumption
- l: population
- $\eta$ : inequality aversion (marginal utility elasticity)
- $\rho$ : rate of pure time preference
- c: country
- q: quantile
- t: time

# 5 abatement.jl

This file defines the components needed to calculate the cost of mitigation.

#### 5.1 Indexes

• country: Countries included in the model.

#### 5.2 Parameters

#### 5.2.1 Time-dependent

- pbacktime: backstop price from DICE 2023, in USD2017 per tCO2.
- global\_carbon\_tax: Global carbon tax (USD2017 per tCO2).
- reference\_carbon\_tax: Reference carbon tax (USD2017 per tCO2).

# 5.2.2 Time and country dependent

- $\sigma$ : Emissions output ratio, GtCO2 per million of 2017 US dollars .
- YGROSS: Gross output, measured in millions of 2017 US dollars per year.
- s: Savings rate (%).
- 1: Labor/population (thousands).
- $\mu$ \_input : Input mitigation rate, used with option 3 "country\_abatement\_rate".

# 5.2.3 Independent

- $\eta$ : Inequality a version.
- $\theta 2$ : Exponent of abatement cost function (DICE-2023 value).
- reference\_country\_index: Reference country index.
- control\_regime: Switch for emissions control regime; 1 = "global\_carbon\_tax", 2 = "country\_carbon\_tax", 3 = "country\_abatement\_rate".

#### 5.3 Variables

#### 5.3.1 Time and country dependent

- $\theta 1$ : Multiplicative parameter of a batement cost function. Equal to ABATEFRAC at 100% mitigation
- country\_carbon\_tax: CO2 tax rate (2017 USD per tCO2)

- $\mu$ : GHG emissions mitigation rate ( $\mu \in [0; 1]$ ).
- ABATEFRAC: Cost of emission reductions in share of gross output.
- ABATECOST: Cost of emission reductions, in millions USD2017 per year.

# 5.3.2 Time-dependent

• GLOBAL\_ABATEFRAC\_full\_abatement: global ABATEFRAC in case of full mitigation (i.e.  $\mu = 1$ ).

# 5.4 Equations

#### 5.4.1 Calculating $\theta 1$ for each country

For each country c in the country set,  $\theta 1$  is calculated as follows:

$$\theta 1[t,c] = pbacktime[t] \times \frac{\sigma[t,c] \times 10^3}{\theta 2}$$
 (2)

The  $10^3$  factor is used for converting  $\sigma$  into tCO2/USD2017.

Then, depending on the emission control regime specified by p.control\_regime, different methods are used to calculate the abatement rate  $\mu$  and the country-specific carbon tax country\_carbon\_tax.

a. Global carbon tax, control\_regime == 1 A global carbon tax is applied to all countries:

$$country\_carbon\_tax[t,c] = global\_carbon\_tax[t]$$
(3)

$$\mu[t,c] = \min\left(\max(0, (\frac{country\_carbon\_tax[t,c] \times \sigma[t,c] \times 10^3}{\theta 1[t,c] \times \theta 2})^{\frac{1}{\theta 2-1}}), 1\right) \tag{4}$$

**b.** Carbon tax by country, control\_regime == 2 Each country's carbon tax is calculated from the reference carbon tax, adjusted according to the country's economic and demographic parameters.

$$country\_carbon\_tax[t,c] = reference\_carbon\_tax[t] \times \frac{1 - s[t, reference\_country\_index]}{1 - s[t,c]} \times \left(\frac{YGROSS[t,c]l[t,c]}{YGROSS[t, reference\_country\_index]l[t, reference\_country\_index]}\right)^{\eta}$$
 (5)

$$\mu[t,c] = min\left(max(0, (\frac{country\_carbon\_tax[t,c] \times \sigma[t,c] \times 10^3}{\theta 1[t,c] \times \theta 2})^{\frac{1}{\theta 2-1}}), 1\right)$$
(6)

c. Abatement rate by country, control\_regime == 3 The abatement rate  $\mu$  is supplied directly by the user  $(\mu[t,c] = \mu\_input[t,c])$  and the country's carbon tax is calculated according to this rate.

$$country\_carbon\_tax[t,c] = \frac{\theta 1[t,c] \times \theta 2}{\sigma[t,c] \times 10^3} * \mu^{\theta 2 - 1}[t,c]$$
 (7)

# 5.4.2 Calculation of abatement cost, abatement rate and overall abatement rate in the case of full abatement

For each country, the abatement rate  $\verb|ABATEFRAC|$  and the abatement cost  $\verb|ABATECOST|$  are calculated as follows:

$$ABATEFRAC[t,c] = \theta 1[t,c] \times \mu^{\theta 2}[t,c]$$
(8)

$$ABATECOST[t, c] = YGROSS[t, c] \times ABATEFRAC[t, c]$$

$$(9)$$

$$GLOBAL\_ABATEFRAC\_full\_abatement[t] = \frac{\sum_{c} (\theta 1[t, c] \times YGROSS[t, c])}{\sum_{c} YGROSS[t, c]}$$
(10)

# 6 damages.jl

This file calculates the economic damage linked to temperature anomalies, as a share of GDP.

#### 6.1 Indexes

- country: Countries included in the model.
- regionwpp: Regions WPP.

#### 6.2 Parameters

#### 6.2.1 Independent

- $\beta 1$ : Linear damage coefficient on temperature. This parameter represents the direct impact of the temperature anomaly on the economy.
- $\beta 2$ : Power damage coefficient on temperature. This parameter captures the non-linear effects of temperature anomalies on the economy.

# 6.2.2 Time-dependent

• temp\_anomaly: Global average surface temperature anomaly (°C above pre-industrial [year 1750]).

# 6.2.3 Time and country dependent

- local\_temp\_anomaly: Country-level average surface temperature anomaly (°C above pre-industrial [year 1750]).
- $\beta1\_KW$ : Linear damage coefficient on local temperature anomaly for Kalkuhl and Wenz based damage function.
- $\beta 2\_KW$ : Quadratic damage coefficient on local temperature anomaly for Kalkuhl and Wenz based damage function.

#### 6.3 Variables

# 6.3.1 Time and country dependent

- LOCAL\_DAMFRAC\_KW: Country-level damages as a share of net GDP based on local temperatures and on Kalkuhl & Wenz.
- DAMFRAC: Country-level damages as a share of net GDP based on global temperatures.

# 6.4 Equations

$$DAMFRAC[t,c] = \beta 1 \times temp\_anomaly^{\beta 2}[t]$$
(11)

$$LOCAL\_DAMFRAC\_KW[t,c] = \beta 1\_KW[c] \times local\_temp\_anomaly[t,c] \\ + \beta 2\_KW[c] \times local\_temp\_anomaly^2[t,c] \quad (12)$$

# 7 emissions.jl

This file allows to calculate greenhouse gas (GHG) emissions at global and national level.

#### 7.1 Indexes

- country: Countries included in the model.
- regionwpp: WPP regions.

# 7.2 Parameters

# 7.2.1 Country dependent

• mapcrwpp: Mapping from country index to WPP region index. This parameter is indexed by country, linking country data to specific WPP regions.

#### 7.2.2 Time and country dependent

- $\sigma$ : Emissions output ratio, GtCO2 per million USD2017. This parameter is used for modelling emissions intensity as a function of economic activity.
- YGROSS: Gross output, in million USD2017 per year. This parameter represents the economic activity of each country.
- $\mu$ : GHG emissions control rate.

# 7.3 Variables

#### 7.3.1 Time-dependent

- E\_Global\_gtco2: Global emissions (sum of all country emissions), in GtCO2 per year.
- E\_Global\_gtc: Global emissions in units of gigatonnes of carbon (GtC per year), giving compatible units with FAIR.

# 7.3.2 Time and country dependent

• E\_gtco2: Country level total greenhouse gas emissions, in GtCO2 per year.

# 7.3.3 Time and WPP region dependent

• E\_gtco2\_rwpp: Regional GHG emissions for the WPP regions, measured in GtCO2 per year.

# 7.4 Equations

#### 7.4.1 Emissions by country

For each country c in the country set, CO2 emissions are calculated using the following equation:

$$E_{\text{gtco2}}[t,c] = YGROSS[t,c] \cdot \sigma[t,c] \cdot (1 - \mu[t,c])$$
(13)

#### 7.4.2 Global emissions

Global CO2 emissions in year t are calculated as the sum of all countries' emissions:

$$E_{\text{Global\_gtco2}}[t] = \sum_{c} E_{\text{gtco2}}[t, c]$$
(14)

# 7.4.3 Global emissions in Carbon Units (GtC)

Global emissions are then converted into gigatons of carbon (GtC) using the molecular conversion factor :

$$E_{\text{Global\_gtc}}[t] = E_{\text{Global\_gtco2}}[t] \cdot \frac{12.01}{44.01}$$
(15)

This conversion is necessary for integration with the FAIR model, which uses emissions in GtC.

#### 7.4.4 Regional emissions for WPP regions

For each rwpp WPP region in the set of regionwpp regions, regional CO2 emissions are calculated as the sum of the emissions of the countries belonging to that region:

$$E_{\text{gtco2\_rwpp}}[t, rwpp] = \sum_{c \in \text{rwpp}} E_{\text{gtco2}}[t, c]$$
 (16)

This process makes it possible to aggregate CO2 emissions at different levels of granularity.

# 8 grosseconomy.jl

#### 8.1 Index

• country: Countries in the model.

# 8.2 Parameters

#### 8.2.1 Country dependent

• k0: Initial level of capital. Determines the starting point for capital accumulation.

### 8.2.2 Time and country dependent

- I: Investment, in millions of 2017 US dollars per year (1e6 USD2017/year).
- 1: Labor/population (workforce available for production).
- tfp: Total factor productivity.
- depk: Depreciation rate on capital. Represents the loss of capital value due to wear and tear and obsolescence.

#### 8.2.3 Independent

• share: Capital's share of production. This parameter is global and affects the distribution of income between capital and labor.

# 8.3 Variables

#### 8.3.1 Time-dependent

• YGROSS\_global: Global gross output, measured in trillions of 2017 US dollars per year (1e12 USD2017/year). Represents the sum of all countries' gross production.

#### 8.3.2 Time and country dependent

- YGROSS: Gross output in each country, measured in millions of 2017 US dollars per year.
- K: Capital, in millions of USD2017 per year.

# 8.4 Equations

# 8.4.1 Capital (K)

The capital in each country is calculated for each period  ${\tt t}$  and for each country  ${\tt c}.$ 

• For the first period (t is the first period), capital is initialized to the value k0 for country c:

$$K[t,c] = k0[c] \tag{17}$$

• For subsequent periods, capital is calculated by taking into account the previous year's capital depreciation and the previous year's investment:

$$K[t,c] = (1 - depk[t,c]) \cdot K[t-1,c] + I[t-1,c]$$
(18)

# 8.4.2 Calculation of Gross Production by Country (YGROSS)

Gross output by country is calculated for each period t and for each country c using the Cobb-Douglas production function equation:

$$YGROSS[t,c] = tfp[t,c] \cdot K[t,c]^{share} \cdot l[t,c]^{(1-share)}$$
(19)

# 8.4.3 Calculation of Global Gross Production (YGROSS\_global)

Global gross output is calculated for each period  ${\tt t}$  by aggregating the gross output of all countries and converting the result into trillions of USD2017 :

$$YGROSS\_global[t] = \frac{\sum_{c} YGROSS[t, c]}{10^{6}}$$
 (20)

# 9 neteconomy.jl

This file calculates the net savings by taking into account the mitigation costs and damages associated with climate change.

# 9.1 Indexes

- country: Countries included in the model.
- regionwpp: Regions defined from the World Population Prospects database (UN).

# 9.2 Parameters

#### 9.2.1 Country dependent

• mapcrwpp: Mapping from country index to WPP region index. This parameter is indexed by country, linking country data to specific regions defined by the UN WPP.

### 9.2.2 Time and country dependent

- YGROSS: Gross output in each country, measured in millions of 2017 US dollars per year.
- ABATEFRAC: Cost of emission reductions in share of gross output.

- LOCAL\_DAMFRAC\_KW: Country-level damages as a share of net GDP based on local temperatures and on Kalkuhl & Wenz.
- s: Savings rate (%).
- 1: Labor/population (in thousands).

#### 9.3 Variables

#### 9.3.1 Time and country dependent

- Y: Output net of damages and abatement costs, in millions USD2017 per year.
- C: Country consumption, in millions USD2017 per year.
- CPC: Country level consumption per capita, in thousands USD2017 per person per year.
- Y\_pc: Per capita output net of abatement and damages, in USD2017 per person per year.
- I: Investment, in millions of USD2017 per year.

# 9.3.2 Time and WPP region dependent

- C rwpp: Regional consumption, in millions USD2017 per year.
- 1\_rwpp: Regional population (in thousands).
- CPC\_rwpp: Regional level consumption per capita, in thousand USD2017 per person per year.
- Y\_pc\_rwpp: Regional per capita output net of abatement and damages, in USD2017 per person per year.

# 9.4 Equations

• Regional consumption C\_rwpp is initialized to zero for the current time step.

#### 9.4.1 Country loop

For each country c in the country set:

1. **Net Output** calculation: Net output Y is calculated by adjusting gross output YGROSS for mitigation costs ABATEFRAC and damages LOCAL\_DAMFRAC\_KW according to equation:

$$Y[t,c] = \frac{(1 - ABATEFRAC[t,c])}{(1 + LOCAL\_DAMFRAC\_KW[t,c])} \cdot YGROSS[t,c]$$
 (21)

2. Investment: Investment I is determined as a fraction s of net output Y:

$$I[t,c] = s[t,c] \cdot Y[t,c] \tag{22}$$

3. Consumption by country: Consumption C is calculated as net output Y minus investment I, except for the last period where it is equal to consumption in the previous period.

$$C[t,c] = \begin{cases} Y[t,c] - I[t,c] & \text{if } t \text{ is not the last period} \\ C[t-1,c] & \text{otherwise} \end{cases}$$
 (23)

4. **Consumption per capita**: Per capita consumption CPC is calculated by dividing consumption C by population 1.

$$CPC[t,c] = \frac{C[t,c]}{l[t,c]}$$
(24)

Net output per head: Net output per capita Y\_pc is calculated by adjusting net output Y
for population 1, with scaling to convert units.

$$Y_{pc}[t,c] = \frac{Y[t,c]}{l[t,c]} \times 10^{3}$$
(25)

# 9.4.2 Loop over WPP regions

For each region rwpp in the set of regions regionwpp:

- 1. Country indices: The indices of the c countries belonging to the rwpp region are identified.
- 2. Regional Consumption:

$$C\_rwpp[t, rwpp] = \sum_{c \in rwpp} C[t, c]$$
 (26)

3. Regional population:

$$l\_rwpp[t, rwpp] = \sum_{c \in rwpp} l[t, c]$$
 (27)

4. Regional per capita consumption:

$$CPC\_rwpp[t, rwpp] = \frac{C[t, rwpp]}{l[t, rwpp]}$$
(28)

5. Regional net output per capita:

$$Y\_pc\_rwpp[t,c] = \frac{\sum_{c \in rwpp} Y[t,c]}{\sum_{c \in rwpp} l[t,c]} \times 10^3$$
(29)

# 10 pattern\_scale.jl

File designed to calculate local temperature changes from global mean temperature variations, using country-specific scaling coefficients.

#### 10.1 Index

• country = Index(): defines a country index for the modelled regions. This index is used for iterating over the different countries in the model.

# 10.2 Parameters

- $\beta\_temp$ = Parameter(index=[country]): declares a  $\beta\_temp$  parameter which represents temperature scaling coefficients. These coefficients translate global temperature anomalies into country-level temperature anomalies. They are indexed by country.
- global\_temperature = Parameter(index=[time]): declares a global\_temperature parameter which represents the time-dependent global average temperature excess (in °C).

#### 10.3 Variables

• local\_temperature = Variable(index=[time, country]): declares a local\_temperature variable which represents the excess temperature at country level (in °C) according to country and year (time-dependent).

#### 10.4 Function

• function run\_timestep(p, v, d, t): Defines the run\_timestep function which is called at each time step of the model. It takes as parameters the parameters (p), the variables (v), the dimensions (d), and the current time step (t).

# 10.5 Equation

For all countries, the local temperature is estimated as the product of the scaling coefficient  $\beta\_temp$  and the global mean temperature anomaly at time t.

$$local\_temperature[t, c] = \beta\_temp[c] \cdot global\_temperature[t]$$
(30)

# 11 quantile\_recycle.jl

This file calculates many variables (see *infra*), including per capita consumption, the poverty rate or the Gini index.

#### 11.1 Indices

- country: Countries included in the model.
- regionwpp: Regions defined from the World Population Prospects database (UN).
- quantile: Index of income quantiles

#### 11.2 Parameters

#### 11.2.1 Time and country dependent

- ABATEFRAC: Cost of CO2 emission reductions as share of gross economic output.
- LOCAL\_DAMFRAC\_KW: National damages as a share of net GDP calculated from national temperatures.
- CPC: Country level consumption per capita, in thousands of USD2017 per person per year.
- 1: Population of the country (in thousands).
- Y: Net production after damage and mitigation costs, in millions USD2017 per year.
- Y\_pc: Net production per capita after damage and mitigation costs, in USD2017 pers person per year.
- country\_pc\_dividend: Total per capita revenue from the carbon tax, including any international transfers, in thousands of USD2017 per person per year.
- tax\_pc\_revenue: Carbon tax revenue per capita from country emissions, in thousands of USD2017 per person per year.

#### 11.2.2 Other

- switch\_recycle: Recycling of carbon tax revenues.
- nb quantile: Number of quantiles (10 by default).
- min\_study\_gdp, max\_study\_gdp: Minimum and maximum values of GDP per capita observed in elasticity studies (in dollars per person).
- elasticity\_intercept, elasticity\_slope: Intercept and slope terms for estimating income elasticity (time-dependent).
- damage\_elasticity: Elasticity of income in relation to climate damage (1 = proportional to income).
- quantile\_income\_shares: Income shares of deciles, depending on time, country and quantiles
- recycle\_share: Share of carbon tax revenues recycled to each quantile, depending on country and quantiles.
- mapcrwpp: Mapping from country index to WPP region index.

#### 11.3 Variables

#### 11.3.1 Time-dependent

- CPC\_post\_global: World consumption per capita after recycling, in thousands of USD2017 per person per year.
- global\_gini\_cons: Gini index of world consumption.

#### 11.3.2 Time and country dependent

- CO2\_income\_elasticity: Income elasticity price of CO2.
- sum\_qcpc\_post\_recycle: Sum of quantiles consumption per capita after abatement, damages and revenue recycling (thousand USD2017 per (capita per quantile) per year).
- CPC\_post: National consumption per capita after recycling, in thousands of USD2017 per person per year.
- gini\_cons: Gini index of country consumption (%).

### 11.3.3 Time, country and quantile dependent

- abatement\_cost\_dist, carbon\_tax\_dist, damage\_dist: Shares of the distribution of abatement costs, CO2 tax burden and climate damage per quantile.
- qcpc\_base: Consumption per quantile per capita before damage, before abatement cost, before tax (thousands of USD2017 per person per year).
- qcpc\_post\_damage\_abatement: Consumption per quantile per capita after damage, after abatement (thousands of USD2017 per person per year).
- qcpc\_post\_tax: Consumption per quantile per capita after subtraction of the carbon tax (thousands USD2017 per person per year).
- qcpc\_post\_recycle: Consumption per quantile per capita after recycling the carbon tax to each quantile (thousands USD2017 per person per year).
- qc\_share: Proportion of consumption per quantile per capita (%).

#### 11.3.4 Time and regionwpp dependent

- CPC\_post\_rwpp: Regional per capita consumption after recycling, in thousands of USD2017 per person per year.
- gini\_cons\_rwpp: Gini index of regional consumption (%).

#### 11.4 Equation

The run\_timestep function calculates various economic indicators for each time step, country and income quantile.

# 11.4.1 Temporary variables for global population and by quantile (in thousands)

# 11.4.2 Income elasticity - CO2 price

$$CO2\_income\_elasticity[t, c] = elasticity\_intercept + elasticity\_slope \times log(GDP)$$
 (31)

where:

$$GDP = \begin{cases} pc\_gdp[t,c] & \text{if pc\_gdp[t,c]} \in [\text{min\_study\_gdp, max\_study\_gdp}] \\ min\_study\_gdp & \text{if pc\_gdp[t,c]} < \text{min\_study\_gdp} \\ max\_study\_gdp & \text{if pc\_gdp[t,c]} > \text{max\_study\_gdp} \end{cases}$$
(32)

# 11.4.3 Distribution of Tax Burdens and Mitigation Costs

The distributions of the shares of the carbon tax burden (carbon\_tax\_dist), mitigation costs (abatement\_cost\_dist), and climate damages (damage\_dist) per quantile are calculated using the country\_quantile\_distribution function.

• The carbon tax burden and mitigation costs are equal, calculated with the function country\_quantile\_distribution (see 14.1.1 for more details).

• Climate damages are calculated by replacing the income-price elasticity of CO2 by the damage-income elasticity damage\_elasticity in the above function.

# 11.4.4 Consumption per Quantile

$$\begin{split} \text{qcpc\_base}[t,c,q] &= \text{nb\_quantile} \times \text{CPC}[t,c] \times \text{quantile\_income\_shares}[t,c,q] \\ &\times \frac{1 + \text{LOCAL\_DAMFRAC\_KW}[t,c]}{1 - \text{ABATEFRAC}[t,c]} \quad (35) \end{split}$$

$$\begin{aligned} \text{qcpc\_post\_damage\_abatement}[t,c,q] &= max \bigg[ \text{qcpc\_base}[t,c,q] - \text{nb\_quantile} \times \text{CPC}[t,c] \\ &\quad \times \bigg( \text{LOCAL\_DAMFRAC\_KW}[t,c] \times \text{damage\_dist}[t,c,q] \\ -\frac{1 + \text{LOCAL\_DAMFRAC\_KW}[t,c]}{1 - \text{ABATEFRAC}[t,c]} \times \text{ABATEFRAC}[t,c] \times \text{abatement\_cost\_dist}[t,c,q] \bigg), 10^{-8} \bigg] \end{aligned}$$

$$\begin{split} \operatorname{qcpc\_post\_tax}[t,c,q] &= \operatorname{qcpc\_post\_damage\_abatement}[t,c,q] \\ &- (\operatorname{nb\_quantile} \times \operatorname{tax\_pc\_revenue}[t,c] \times \operatorname{carbon\_tax\_dist}[t,c,q]) \end{split} \tag{37}$$

• If the revenues are recycled, then consumption per post-tax quantile is increased by the product of the total per capita revenue from the carbon tax and the share of its recycling to each quantile:

• If revenues are not recycled, then consumption per post-tax quantile is increased by the product of the carbon tax revenue per capita from each country's emissions and its initial tax burden:

$$\begin{split} \operatorname{qcpc\_post\_recycle}[t,c,q] &= \operatorname{qcpc\_post\_tax}[t,c,q] \\ &+ (\operatorname{nb\_quantile} \times \operatorname{tax\_pc\_revenue}[t,c] \times \operatorname{carbon\_tax\_dist}[t,c,q]) \end{split} \tag{39}$$

# 11.4.5 Calculation of per capita consumption

• Sum of country quantiles' consumption per capita after abatement, damages and revenue recycling (thousand USD2017 per (capita per quantile) per year)

$$\operatorname{sum\_qcpc\_post\_recycle}[t,c] = \sum_{q} \operatorname{qcpc\_post\_recycle}[t,c,q] \tag{40}$$

• Per capita consumption after recycling:

$$CPC\_post[t, c] = \frac{sum\_qcpc\_post\_recycle[t, c]}{nb\_quantile}$$
(41)

• Share of country consumption by quantile (%):

$$qc\_share[t, c, q] = \frac{qcpc\_post\_recycle[t, c, q]}{sum \ qcpc \ post \ recycle[t, c]} \times 100$$
(42)

#### 11.4.6 Calculation of the Gini Index and the Poverty Rate

The Gini index (gini\_cons) and the poverty rate (poverty\_rate\_cons) are calculated using the quantile distribution of consumption.

• The **Gini Index** is calculated using the Gini function in Julia :

$$gini\_cons[t,c] = gini(convert(Vector{Real},qc\_share[t,c,:])) \times 100$$
 (43)

### 11.4.7 Regional and global calculations

Country indices c and regional indices rwpp are mapped using mapcrwpp.

• Regional per capita consumption after recycling:

$$CPC\_post\_rwpp[t, rwpp] = \frac{\sum_{c \in rwpp} (l[t, c] \cdot CPC\_post[t, c])}{\sum_{c \in rwpp} l[t, c]}$$
(44)

• CPC\_post\_global is calculated as the weighted sum of countries' total consumption after recycling, divided by the world population:

$$CPC\_post\_global[t] = \frac{\sum_{c}(total\_c\_post\_recycle[t,c] \cdot l[t,c]/nb\_quantile)}{\sum_{c} l[t,c]} \tag{45}$$

• Regional Gini index:

• Global Gini index:

$$\begin{split} \texttt{global\_gini\_cons[t]} = & \texttt{gini} \bigg( \texttt{convert} \Big( \texttt{Vector\{Real\}, vec(qc\_post\_recycle[t, :, :])} \Big), \\ & \texttt{convert} \Big( \texttt{Vector\{Real\}, vec(qpop[t, :, :])} \Big) \\ & \times 100 \quad (47) \end{split}$$

# 12 revenue recycle.jl

This component models the recycling of carbon tax revenues across different countries and quantiles. It is essential for studying mitigation policies and their impact on reducing poverty and inequality. revenue\_recycle.jl is used by nice\_v2\_module.jl and interacts with quantile\_distribution.jl and welfare.jl.

### 12.1 Index

• country: Countries included in the model.

# 12.2 Parameters

#### 12.2.1 Time and country dependent

- Y: Net production, in millions of USD2017 per year.
- country\_carbon\_tax: Carbon tax by country (\$/tCO2).
- LOCAL\_DAMFRAC\_KW: National damage as a percentage of net GDP calculated from national temperatures.
- E\_gtco2: Industrial carbon emissions (GtCO2 per year).
- 1: Country population (in thousands).
- tax\_pc\_revenue: Carbon tax revenue per capita from the country's emissions, in thousands of USD2017 per person per year.

#### 12.2.2 Country dependent

• global\_recycle\_share: Share of country revenues that are recycled globally in the form of international transfers (1 = 100%).

#### 12.2.3 Independent

- switch\_recycle: Recycling of carbon tax revenues.
- lost\_revenue\_share: Portion of carbon tax revenue that is lost and cannot be recycled (1 = 100% of revenue lost, 0 = no revenue lost).
- switch\_recycle: Boolean for recycling carbon tax revenue.
- switch\_scope\_recycle: Boolean, carbon tax revenues are recycled at national (0) or global (1) level.
- switch\_global\_pc\_recycle: Boolean, carbon tax revenues are recycled globally on an equal per capita basis (1).

#### 12.3 Variables

# 12.3.1 Time-dependent

- total\_tax\_revenue: Total carbon tax revenue (USD2017/year), sum of tax revenues in all countries.
- total\_tax\_pc\_revenue: Total carbon tax revenue per person per year (in thousands of dollars per person per year), sum of tax revenues in all countries per person per year.
- global\_revenue: Carbon tax revenue, derived from the total recycled revenue of all countries (in thousand USD2017 per year).
- revenue\_recycled\_global\_level: Sum for all countries of tax\_revenue recycled at a global\_recycle\_share. Mesured in thousands of USD2017 per year.

#### 12.3.2 Time and country dependent

- tax\_revenue: Carbon tax revenue for a given country, in USD2017 per year.
- tax\_pc\_revenue: Carbon tax revenue per person for a given country, in thousands of USD2017 per person per year.

- country\_pc\_dividend: Total fiscal dividends per person, including all international monetary transfers, in thousands of USD2017 per person per year.
- country\_pc\_dividend\_domestic\_transfers: Fiscal dividends per person from domestic redistribution, i.e. within a country, in thousands of USD2017 per person per year.
- country\_pc\_dividend\_global\_transfers: Tax dividends per person from international transfers, in thousands of USD2017 per person per year.

# 12.4 Equation

# 12.4.1 Carbon tax revenue

$$\label{eq:tax_revenue} \begin{split} \text{tax\_revenue}[t,c] &= \left(E\_gtco2[t,c] \times \text{country\_carbon\_tax}[t,c] \times 10^9\right) \\ &\qquad \qquad \times \left(1 - \text{lost\_revenue\_share}\right) \end{split} \tag{48}$$

Emissions are in GtCO2 and country\_carbon\_tax in USD2017/tCO2, hence the normalisation by  $10^9$ .

$$tax\_pc\_revenue[t,c] = \frac{tax\_revenue[t,c]}{l[t,c] \times 10^6}$$
 (49)

tax\_revenue is in USD2017/year and population in thousands of inhabitants, hence the normalisation by  $10^{-6}$ .

$$total\_tax\_revenue[t] = \sum_{c} tax\_revenue[t, c]$$
 (50)

$$total\_tax\_pc\_revenue[t] = \frac{total\_tax\_revenue[t]}{\sum_{c} l[t, c] \times 10^{6}}$$
 (51)

$${\rm global\_revenue}[t] = \sum_{c} \Big( {\rm tax\_revenue}[t,c] \times {\rm global\_recycle\_share}[c] \times {\rm switch\_scope\_recycle} \Big)$$
 (52)

$$global\_pc\_revenue[t] = \frac{global\_revenue[t]}{\sum_{c} (l[t, c]) \times 10^{6}}$$
(53)

### 12.4.2 Dividends according to Boolean values

switch\_recycle = 1 No income recycling implies no dividends.

$$\begin{array}{c} \text{country\_pc\_dividend\_domestic\_transfers}[t,c] \\ \text{country\_pc\_dividend\_global\_transfers}[t,c] \end{array} \right\} = 0$$

switch\_recycle==1, switch\_scope\_recycle==0 Revenues from the carbon tax are recycled at
a national level:

$$country\_pc\_dividend\_domestic\_transfers[t, c] = \frac{tax\_revenue[t, c]}{l[t, c] \times 10^6}$$
(55)

$$country_pc_dividend_global_transfers[t, c] = 0$$
 (56)

$$\label{eq:country_pc_dividend_domestic_transfers} \\ [t,c] = (1 - \text{global\_recycle\_share}[c]) \\ \times \frac{tax\_revenue[t,c]}{l[t,c] \times 10^6} \\ (57)$$

$$revenue\_recycled\_global\_level[t] = \sum_{c} (tax\_revenue[t, c] \times global\_recycle\_share[c]) \times 10^{-3} (58)$$

## Booleans change the way dividends are calculated.

• switch\_pc\_global\_recycle = 1; Carbon tax revenues are recycled globally on an equal per capita basis.

$$country\_pc\_dividend\_global\_transfers[t, c] = \frac{revenue\_recycled\_global\_level[t]}{\sum_{c}(l[t, c]) \times 10^{3}}$$
(59)

Otherwise:

country pc dividend global transfers
$$[t, c] = 0$$
 (60)

### 12.4.3 Total dividends

Total dividends per person are written as:

$$country\_pc\_dividend[t, c] = country\_pc\_dividend\_domestic\_transfers[t, c] + country\_pc\_dividend\_global\_transfers[t, c]$$
 (61)

# 13 welfare.jl

This file calculates economic welfare and consumption equivalent to equitably distributed welfare (EDE) as a function of inequality aversion  $(\eta)$ . welfare.jl is loaded by nice\_v2\_module.jl and uses data provided by revenue\_recycle.jl and quantile\_distribution.jl.

#### 13.1 Indexes

 country, regionwpp, quantile: Indexes representing countries, regions and income quantiles respectively.

#### 13.2 Parameters

- qcpc\_post\_recycle: Per capita quantile consumption after redistribution of the recycling tax (in thousands of USD2017 per person per year). It depends on time, country and quantile.
- $\eta$ : Inequality aversion.
- nb\_quantile: Number of quantiles.
- 1: Population (in thousands). This parameter is time and country dependent.
- mapcrwpp: Correspondence of the country index with the WPP regions index (country dependent).

#### 13.3 Variables

- cons\_EDE\_country, cons\_EDE\_rwpp, cons\_EDE\_global: Consumption equivalent to equitably distributed well-being (in thousands of USD2017 per person per year) for countries, regions and globally.
- welfare\_country, welfare\_rwpp, welfare\_global: Welfare for countries, regions and globally.

# 13.4 Equations

#### 13.4.1 Case where $\eta \neq 1$

For each country (c), EDE consumption and welfare are calculated as follows:

# EDE consumption by country

$$cons\_EDE\_country[t,c] = \left(\frac{1}{nb\_quantile} \sum_{q} (qcpc\_post\_recycle[t,c,q]^{(1-\eta)})\right)^{\frac{1}{(1-\eta)}}$$
(62)

**EDE consumption by region** For each region, the country indices c are mapped using mapcrwpp.

$$cons\_EDE\_rwpp[t, rwpp] = \left(\frac{\sum_{c \in rwpp} (l[t, c] \cdot cons\_EDE\_country[t, c]^{(1-\eta)})}{\sum_{c \in rwpp} l[t, c]}\right)^{\frac{1}{(1-\eta)}}$$
(63)

# Overall EDE consumption

$$cons\_EDE\_global[t] = \left(\frac{\sum_{c} (l[t, c] \cdot cons\_EDE\_country[t, c]^{(1-\eta)})}{\sum_{c} l[t, c]}\right)^{\frac{1}{(1-\eta)}}$$
(64)

# Welfare by country

$$welfare\_country[t,c] = \left(\frac{l[t,c]}{nb\_quantile}\right) \sum_{q} \left(\frac{qcpc\_post\_recycle[t,c,q]^{(1-\eta)}}{(1-\eta)}\right)$$
(65)

# Welfare by region

$$welfare\_rwpp[t, rwpp] = \sum_{c \in rwpp} welfare\_country[t, c]$$
 (66)

# Global welfare

$$welfare\_global[t] = \sum_{c} (welfare\_country[t, c])$$
 (67)

#### **13.4.2** Case where $\eta = 1$

For each country (c), EDE consumption and welfare are calculated using the logarithm :

#### EDE consumption by country

$$cons\_EDE\_country[t, c] = \exp\left(\frac{1}{nb\_quantile} \sum_{q} \log(qcpc\_post\_recycle[t, c, q])\right)$$
(68)

#### EDE consumption by region

$$cons\_EDE\_rwpp[t, rwpp] = \exp\left(\frac{\sum_{c \in rwpp} l[t, c] \cdot \log(cons\_EDE\_country[t, c])}{\sum_{c \in rwpp} l[t, c]}\right)$$
(69)

#### Total EDE consumption

$$cons\_EDE\_country[t] = \exp\left(\frac{\sum_{c} l[t, c] \cdot \log(cons\_ED\_country[t, c])}{\sum_{c} l[t, c]}\right)$$
(70)

#### Welfare by country

$$welfare\_country[t,c] = \left(\frac{l[t,c]}{nb\_quantile}\right) \sum_{q} \log(qcpc\_post\_recycle[t,c,q]) \tag{71}$$

Welfare by region

$$welfare\_rwpp[t, rwpp] = \sum_{c \in rwpp} welfare\_country[t, c] \tag{72}$$

Global welfare

$$welfare\_global[t] = \sum_{c} (welfare\_country[t, c])$$
 (73)

# 14 helper\_functions.jl

# 14.1 Functions

### 14.1.1 country\_quantile\_distribution

**Objective** The country\_quantile\_distribution function calculates the distribution of quantile shares for a given country, based on a given income elasticity. This function is useful for analysing the impact of climate damage,  $CO_2$  mitigation costs, or  $CO_2$  related tax burdens on different segments of the population within a country.

#### Arguments of the function

- elasticity: Income elasticity with respect to climate damage,  $CO_2$  mitigation costs,  $CO_2$  tax burdens, etc. This must be a real number.
- income\_shares: An array of income shares by quantile (where the rows represent the countries and the columns the quantiles)
- nb\_quantile: Number of quantiles, specified as an integer.

#### **Process**

1. **Application of elasticity**: For a given country, income elasticity is applied to income shares per quantile by raising each income share to the power of the elasticity.

$$scaled\_shares[t, c, q] = income\_shares^{elasticity}[t, c, q]$$
 (74)

- 2. Allocate an empty array: An empty array updated\_quantile\_distribution is allocated to store the distribution across quantiles resulting from the application of the elasticity.
- 3. Calculation of updated distributions: The function iterates over each quantile to calculate the updated distribution. For each quantile, the updated share is calculated by dividing the scaled income share for that quantile by the total sum of scaled income shares for all quantiles.

**Return** The function returns the array updated\_quantile\_distribution, which contains the updated quantile share distribution for each country, reflecting the impact of income elasticity on the distribution of economic costs or damages.

#### 14.1.2 linear\_tax\_trajectory

This function calculates a linear carbon tax trajectory. It assumes that a carbon tax is \$0 in the first period and increases linearly until the end of the specified period.

#### **Function arguments**

- tax\_start\_value (Real): The initial value of the carbon tax (in 2017 US dollars per tonne of CO2).
- increase\_value (Real): The annual tax increase value. By default, it is equal to tax\_start\_value, which means that the tax increases by its initial value each year.
- year\_tax\_start (Int64): The first year of the tax trajectory. The tax starts at 0 in this year and increases to tax\_start\_value the following year.
- year\_tax\_end (Int64): The last year for which to calculate the tax.
- year\_step (Int64): The step in years between two tax values. The default is 1, indicating an annual increase.
- year\_model\_end (Int64): The end of the model. If it is less than year\_tax\_end, the last tax value is repeated up to this year. By default, it is set to 2300.

**Description** The linear\_tax\_trajectory function generates a carbon tax trajectory which starts at \$0 and increases linearly each year according to the increase\_value specified, from year year\_tax\_start + 1 to year year\_tax\_end. After year\_tax\_end, the tax value remains constant until year\_model\_end if specified.

```
function linear_tax_trajectory(;tax_start_value::Real, increase_value::Real=tax_start_value,
    year_tax_start::Int64, year_tax_end::Int64, year_step::Int64=1, year_model_end::Int64=2300)

for t in [year_tax_start+1:year_step:year_tax_end]
    tax_values = tax_start_value + increase_value * (t-(year_tax_start+1))

full_tax_path = [0; tax_values; fill(tax_values[end], year_model_end - year_tax_end)]
    return full_tax_path
end
```

```
For t \in [\text{year\_tax\_start} + 1 : \text{year\_step} : \text{year\_tax\_end}]:
\text{tax\_values}[t] = [\text{tax\_start\_value} + \text{increase\_value} \times (t - (\text{year\_tax\_start} + 1)) (76)
```

```
full\_tax\_path = [0; tax\_values; fill(tax\_values[end], year\_model\_end - year\_tax\_end)]  (77)
```

**Return** The function returns a vector containing the complete trajectory of the carbon tax, from the start year to the end year of the model.

#### Example of use

```
linear_tax_path = linear_tax_trajectory(tax_start_value=10, increase_value=5,
year_tax_start=2020, year_tax_end=2050, year_step=1, year_model_end=2100)
```

#### 14.1.3 save\_nice2020\_results

**Description** This function creates a directory of files to store the results of a model, dividing the model output by global, regional and quantile levels. A different sub-folder name is used for each type of revenue recycle (careful: revenue recycling type must be set with the use of the parameter switches).

#### Arguments

- m::Model: A version of the NICE model.
- output\_directory::String: The path to the directory where the model results will be saved.
- recycling\_revenue::Bool=true: Indicates whether CO2 tax revenues are recycled (true) or not (false).
- recycling\_type::Int64=0: The type of revenue recycling.
- result\_year\_end::Int64=2100: The end year for the results.

**Process** The function begins by creating sub-directories to store the results, with and without revenue recycling. The type of revenue recycling is determined by the recycling\_type argument, which influences the name of the sub-folder.

The function then saves different types of results in the appropriate directories:

- Global Output: Includes files such as global temperature, global gross GDP, CO2 emissions, etc.
- **Regional Output**: Includes files such as consumption per capita per region, net GDP per capita per region, etc.
- Output by Country: Includes files such as gross GDP per country, consumption per country, population per country, etc.
- Output by Quantile: Includes files such as CO2 tax distribution, per capita consumption, consumption after damage and abatement, etc.

# Example of use

```
m = load_modele_nice() # Hypothetical function to load a NICE model
output_directory = "path/to/folder/results"
save_nicev2_results(m, output_directory, revenue_recycling=true, recycling_type=1)
```

# 14.1.4 get\_global\_mitigation

This function calculates the global CO2 mitigation rate for a given model with a specific mitigation policy, compared with a reference scenario with no CO2 policy (business as usual, BAU).

#### Arguments

- m\_policy (Model): A model representing the economy or environmental system with a CO2 mitigation policy applied.
- m\_bau (Model): A model representing the reference scenario (business as usual) without a CO2 mitigation policy.

**Description** The function performs the following operations:

 Calculates the global industrial CO2 emissions for the m\_policy model which includes a specific mitigation policy.

$$global\_emissions\_policy = \sum (m\_policy[: emissions, : E\_Global\_gtco2], dims = 2) \quad (78)$$

2. Calculation of global CO2 emissions without policy (BAU): Calculates global industrial CO2 emissions for the m\_bau model, which represents a scenario without a CO2 emissions mitigation policy.

$$global\_emissions\_base = \sum (m\_bau[: emissions, : E\_Global\_gtco2], dims = 2) \qquad (79)$$

3. Calculation of the mitigation rate: Determines the global mitigation rate by comparing the emissions with mitigation policy to the emissions of the BAU scenario.

$$global\_mitigation\_rates = \frac{global\_emissions\_base - global\_emissions\_policy}{global\_emissions\_base}$$
(80)

# Return

• global\_mitigation\_rates: A vector containing global CO2 mitigation rates, calculated as the relative reduction in emissions compared with the BAU scenario.

#### Example of use

```
# Creating the m_policy and m_bau models
m_policy = Model(...) # Model with mitigation policy
m_bau = Model(...) # BAU model

# Calculation of global mitigation rate
mitigation_rates = get_global_mitigation(m_policy, m_bau)
```

# 15 nice2020\_module.jl

This file defines the create\_nice2020 function, which creates a versison of the NICE 2020 simulated model by coupling the FAIRv2.0 model to a simple damage function.

# 15.1 Loading packages and data

The module uses several Julia packages for its operations:

- Mimi: A framework for developing and analysing AMIs.
- MimiFAIRv2: A specific implementation of the FAIR model within the Mimi framework.
- Statistics: Provides basic statistical functions.
- Random: Functions for generating random numbers.
- Distributions: A package for defining and working with probabilistic distributions.
- Inequality: Used to analyse inequalities in data or model results.

Economic data is loaded from an external parameters.jl file, located in the data folder relative to the module.

# 15.2 Mimi Model Auxiliary Functions and Components

The module includes auxiliary functions from the helper\_functions.jl file. The following model components are loaded from the components folder:

- gross\_economy.jl: Defines how the gross economy works before abatement costs or damages are taken into account.
- abatement.jl: Manages emission abatement costs and strategies.
- emissions.jl: Calculates emissions based on various economic and abatement factors.
- pattern\_scale.jl: Compute local temperature values.
- damages.jl: Estimates the economic damage caused by climate change.
- net\_economy.jl: Calculates the net savings after taking into account damage and abatement costs.
- revenue\_recycle.jl: Processes the recycling of revenues generated by taxes or emission permits.
- quantile\_reycle.jl: Analyses the distribution of impacts or costs across different quantiles of the population.
- welfare.jl: Evaluates general welfare, taking into account economic and environmental aspects.

# 15.3 create\_nice2020() function

The function is based on the Mimi-FAIRv2 model with an emissions and radiative forcing scenario defined according to SSP2-45, between 2020 and 2300. 20 World Population Prospects and 10 quantiles are created, **c** is defined as the symbol representing the countries (countries).

The emissions, abatement and gross economy components are added before the FAIR carbon cycle, and this model (FAIR) is coupled with scaling, regional damages, net production, income recycling, quantile recycling and welfare valuation components, in that order.

By default, tax revenues are not recycled (i.e., they are returned to each quantile). We define the mapping of countries to the WPP regions and the number of quantiles that will be used.

# 15.4 Initial conditions

Initial conditions are updated for different environmental cycles in the FAIR model. Each block of code relates to a specific cycle and updates the parameters associated with that cycle.

# 15.4.1 The update\_param! function

An explainer for the Mimi framework syntax for setting and updating parameters can be found at https://www.mimiframework.org/Mimi.jl/stable/howto/howto\_5/.

The update\_param! function is used for setting unshared model parameters. It generally takes four arguments:

- 1. m: The model to which the parameter belongs.
- 2. The name of the cycle for which the parameter is being updated.
- 3. The name of the parameter to be updated.
- 4. The new parameter value.

#### 15.4.2 Aerosol cycle and temperature

Initial concentration (aerosol\_plus\_0), radiative response (RO\_aerosol\_plus), and radiative forcing (GU\_aerosol\_plus\_0) of aerosols are updated. The same is done for methane (CH4), carbon dioxide (CO2), fluorinated gases, substances controlled by the Montreal Protocol, and nitrous oxide (N2O). Finally, the initial temperature is defined.

### 15.4.3 Gross economy

We connect the population parameter 1 to the gross economy, and do the same with total factor productivity, the rate of capital depreciation, initial capital kO and the share of income allocated to capital (here share is set to 0.3).

# 15.5 Abatement: abatement.jl

#### 15.5.1 set\_param! function

The **set\_param!** function is used for defining or modifying the value of a specific parameter for a given component of the model.

- The mitigation control regime is defined (1: Global carbon tax, 2: Carbon tax per country, 3: Mitigation rate per country), which is set to 3 by default.
- Set the global carbon tax (global\_carbon\_tax) and the reference carbon tax (reference\_carbon\_tax) to zero for each time period.
- The USA is defined as the reference country.
- Initialise  $\mu$  to 0 in order to prepare the model to receive specific mitigation rate values for each country and time period.
- Set  $\theta_2 = 2.6$  and  $\eta = 1.5$ .
- The cost of the CO2 removal technology over time is specified with full\_pbacktime.

- The values of the emission rate  $\sigma$  and the savings rate s are set.
- The population parameter 1 is connected to the mitigation component, so that the value of 1 is the same throughout the model.

# 15.6 CO2 emissions: emissions.jl

We map countries to WPP regions with mapcrupp, and update the emission rate  $\sigma$ .

# 15.7 Temperature: pattern\_scale.jl

Update the  $\beta$  temperature dimensioning parameter according to CMIP projections.

# 15.8 Damages: damages.jl

The damage coefficients  $\beta 1$  (= 0.0236),  $\beta 2$  (= 2),  $\beta 1 KW$ , and  $\beta 2 KW$  are defined.

# 15.9 Net economy: net\_economy.jl

We map countries to WPP regions with mapcrwpp, update the savings rate s, and connect the population parameter 1.

# 15.10 Income recycling: revenue\_recycle.jl

- Assume a damage-income elasticity of 0.85 (damage\_elasticity\_data = 0.85)
- By default, the proportion of countries' revenues that are recycled globally in the form of international transfers is set at 100% for all countries.
- By default, carbon tax revenues are recycled globally (switch\_scope\_recycle = 1), and all other Booleans are disabled. The share of revenue lost (lost\_revenue\_share) is set to 0.

# 15.11 Quantiles: quantile\_distribution.jl

- The minimum (647 USD2017 per capita) and maximum (48892 USD2017 per capita) GDP per capita used in elasticity studies are defined.
- Update the intercept and slope parameters for elasticity, which define the relationship between GDP per capita and demand elasticity, essential for modelling how economic changes affect consumption.
- The elasticity of damage and income distribution is configured.
- The share of income recycling for a quantile is uniformly defined as the inverse of the total number of quantiles.
- The demographic parameters of population and correspondence between countries and WPP regions are connected. The Boolean for activating income recycling (switch\_recycle) is also connected.

# 15.12 Welfare: welfare.jl

Similarly, we set certain values (number of quantiles and inequality aversion  $\eta = 1.5$ ) and connect the demographic parameters.

# 15.13 Connection between components

The general syntax for creating a connection is :

connect\_param!(model\_name, :component\_requiring\_value => :name\_of\_required\_value,
:component\_calculating\_value => :name\_of\_calculated\_value)

- model\_name: The name of the model, in this case m.
- :component\_requiring\_value : The component which requires a value from another component.
- :name\_of\_required\_value : The name of the value required by the component.

- :component\_calculating\_value : The component which calculates the required value.
- name\_of\_calculated\_value': The name of the value calculated by the component.

# Component connections are:

- I is calculated by neteconomy and is used by grosseconomy.
- YGROSS is calculated by grosseconomy and is used for abatement, emissions and neteconomy.
- $\mu$  is calculated by abatement and used for emissions.
- E\_Global\_gtc is calculated by emissions, is required under the name E\_co2 and is used for co2 cycle.
- T is calculated by temperature, is required under the name global\_temperature and is used for pattern\_scale.
- T is calculated by temperature, is required under the name temp\_anomaly and is used for damages.
- local\_temperature is calculated by pattern\_scale, is required under the name local\_temp\_anomaly and is used for damages.
- ABATEFRAC is calculated by abatement and is used for neteconomy.
- LOCAL\_DAMFRAC\_KW is calculated by damages and is used for neteconomy, revenue\_recycle, and quantile\_recycle.
- E\_gtco2 is calculated by emissions and is used for revenue\_recycle.
- country\_carbon\_tax is calculated by abatement and is used for revenue\_cycle.
- Y is calculated by neteconomy and used for revenue recycle and quantile recycle.
- CPC is calculated by neteconomy and used for quantile\_recycle.
- Y\_pc is calculated by neteconomy and used for quantile\_recycle.
- country\_pc\_dividend is calculated by revenue\_recycle and is used for quantile\_recycle.
- tax\_pc\_revenue is calculated by revenue\_recycle and is used for quantile\_recycle.
- qcpc\_post\_recycle is calculated by quantile\_recycle and is used for welfare.